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° AN

ADVANCED ARITHMETIC

FOR

HIGH SCHOOLS, NORMAL SCHOOLS AND ACADEMIES

BY

G. A. WENTWORTH, A.M.
AUTHOR OF A SERIES OF TEXT-BOOKS IN MATHEMATICS

TEACHERS' EDITION

BOSTON, U.S.A.
GINN & COMPANY, PUBLISHERS
The Athensum Press
1898

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PREFACE.

This edition is intended for teachers, and for them only. The publishers will make every effort to keep the book from pupils; and teachers are urged to exercise the utmost care not to lose their copies, or to leave them where pupils can have access to them.

It is hoped that young teachers will derive great advantage from studying the systematic arrangement of the algebraic work, for such attention has been paid to this as the limitation of the page would allow.

It is also expected that many teachers, who are pressed for time, will find great relief by not being obliged to work out every problem in the Algebra.

G. A. WENTWORTH.

EXETER, N.H., September, 1898.



ADVANCED ARITHMETIC.

TEACHERS' EDITION.

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Exercise 1. Page 5.

Write in periods, and read:

- 1. 7000; seven thousand.
- 2. 7842; seven thousand, eight hundred forty-two.
- 3. 5043; five thousand, forty-three.
- 4. 8375; eighty-three hundred seventy-five.
- 5. 2020; two thousand, twenty.
- 6. 1753; seventeen hundred fifty-three.
- 7. 18,757; eighteen thousand, seven hundred fifty-seven.
- 8. 75,764; seventy-five thousand, seven hundred sixty-four.
- 9. 22,003; twenty-two thousand, three.
- 10. 70,856; seventy thousand, eight hundred fifty-six.
- 11. 234,567; two hundred thirty-four thousand, five hundred sixty-seven.
 - 12. 34,561; thirty-four thousand, five hundred sixty-one.
- 13. 123,456; one hundred twenty-three thousand, four hundred fifty-six.
 - 14. 654,089; six hundred fifty-four thousand, eighty-nine.
 - 15. 600,897; six hundred thousand, eight hundred ninety-seven.
 - 16. 704,608; seven hundred four thousand, six hundred eight.
 - 17. 350,709; three hundred fifty thousand, seven hundred nine.
 - 18. 240,682; two hundred forty thousand, six hundred eighty-two.
 - 19. 682,000; six hundred eighty-two thousand.
 - 20. 753,110; seven hundred fifty-three thousand, one hundred ten.
 - 21. 703,101; seven hundred three thousand, one hundred one.
- 22. 870,890; eight hundred seventy thousand, eight hundred ninety.
- 23. 21,978,564; twenty-one million, nine hundred seventy-eight thousand, five hundred sixty-four.

- 24. 17,756,423; seventeen million, seven hundred fifty-six thousand, four hundred twenty-three.
- 25. 300,200,100; three hundred million, two hundred thousand, one hundred.
- 26. 707,303,202; seven hundred seven million, three hundred three thousand, two hundred two.
- 27. 3,125,476,890; three billion, one hundred twenty-five million, four hundred seventy-six thousand, eight hundred ninety.
- 28. 79,501,346,081; seventy-nine billion, five hundred one million, three hundred forty-six thousand, eighty-one.
- 29. 3,000,872,696; three billion, eight hundred seventy-two thousand, six hundred ninety-six.
- 30. 72,727,000,000; seventy-two billion, seven hundred twenty-seven million.

Exercise 2. Page 6.

Write in figures, arranged in periods:

7	an	Λ	α
	υU	v,	006.

2. 713,329.

3. 7854.

4. 4,003,330.

5. 110,000,279.

6. 19,000,004,000,309.

7. 7,676,466.

8. 347,651,785.

9. 200,000,207.

10. 400,000,400,004.

Exercise 3. Page 9.

Read:

- 1. Six million, seven hundred twenty-eight thousand, six hundred forty-two.
- 2. Three and twenty-four thousand, six hundred fifty-eight hundred-thousandths.
- 3. Forty-nine thousand, five hundred sixty-eight and four thousand, seven hundred eighty-two ten-thousandths.
- 4. Thirty-four billion, five hundred ninety-eight million, four hundred ninety-two thousand, two hundred twelve.
 - 5. Four million, two thousand and two hundredths.
 - 6. Eighteen hundred seventy-two and seventeen hundredths.
- 7. Ninety-four and six hundred fifty-eight thousand, two hundred sixty-five millionths.
 - 8. Three hundred seven ten-thousandths.
 - 9. One hundred and one hundredth.

- 10. One million, eight hundred seventy-two thousand, five hundred sixty-three and three hundred seventy-two thousandths.
 - 11. Seventeen and eight thousandths.
- 12. One hundred forty-three and one hundred forty-three hundred-thousandths.
 - 13. Twenty-nine and eighty-one hundred-thousandths.
- 14. Five million, two hundred sixty-two thousand, eight hundred seventy-three.
 - 15. Eight and seventy-eight hundred fifty-four ten-thousandths.
- 16. One hundred eighty-two dollars, and twenty-seven cents, five mills.
 - 17. Eight cents, six mills.
 - 18. Seven cents, five mills.
 - 19. Four hundred sixty-three dollars and eighty-seven cents.
- 20. Twenty thousand, five hundred forty-two dollars and two cents.
 - 21. Seventy-five cents.
- 22. Four hundred twenty-eight thousand, four hundred twenty-eight and four hundred twenty-eight thousandths.
 - 23. Fifteen hundred forty-two and eighty-seven thousandths.
- 24. Six hundred forty-two and eight hundred seventy-three thousand, six hundred fifty-four millionths.
 - 25. Four hundred and four hundred-thousandths.
- 26. Three billion, five hundred forty-three million, three hundred sixty-two thousand, three hundred thirty-eight.
 - 27. Nine ten-millionths.
 - 28. Fifty-two and two hundredths.
- 29. Fifty-six thousand, four hundred eighty-two and fifty-six hundredths.
- 30. Eighty-seven million, eight hundred sixty-five thousand, eight hundred forty-two and eighty-seven thousand, eight hundred sixty-six hundred-thousandths.

Exercise 4. Page 9.

Write in figures:

- 1. 81,000.345.
- 2. 3741.675.
- **3.** 413.08.
- 4. 96.096.
- **5.** 9.000043,

- **6.** 154.0032.
- **7.** 0,075.
- 8. 0.3.
- 9. 44,044,044.044.
- **10.** 100.000043.

ADVANCED ARITHMETIC.

11. 0.000143.

12. 140.000003.

13. 943,000.943.

14. 0.0000722.

15. 13.01468.

16. 4.1009.

17. 101.0101.

18. 17,649,000.

19. 12,000,012,000.

20. 12,000,000,000.012.

21. \$8.12.

22. \$127.01.

23. \$14,278.275.

24. \$1000.011.

25. \$234.55.

26. \$0.25; \$0.034.

27. 1,489,590.590.

28. 43,677.04006.

29. 3069.0078416.

Exercise 5. Page 11.

Read:

Chirty-six; forty; forty-six; fifty-eight; fifty-nine; eighty-one; ety-one; ninety-three; one hundred nine; two hundred nine; hundred twenty; one hundred fifty-nine; eighteen hundred hty-six; sixteen hundred sixty-six; seventeen hundred seventy; fourteen hundred fifty-nine; fifteen hundred eighty-nine.

Express in the Roman system:

⟨LIII; LV; LXXXI; LXXVII; XCIX; CXIII; CXXVIII;

⟨IV; DCCXXIV; DCXXX; MXX; MXL; MLXXXVIII;

⟨XXXI; MCCXVIII; MCDXCII; MDCCLXXVI; MDCCCXCIX;

⟨CCXIX; MDLVI; MDCCCXCVII; MDCXX; MDCCLXXXIII;

⟩CCCXII; MDCCCLXI; MDCCCLXXII.

Exercise 6. Page 12.

- L. Count to 100 or more by 2's.
- 1, 2, 4, 6, 8, 10, 12, 14, 16, 18, 20, 22, 24, 26, 28, 30, 32, 34, 36, 38,
- 42, 44, 46, 48, 50, 52, 54, 56, 58, 60, 62, 64, 66, 68, 70, 72, 74, 76,
- 80, 82, 84, 86, 88, 90, 92, 94, 96, 98, 100.
- ., 3, 5, 7, 9, 11, 13, 15, 17, 19, 21, 23, 25, 27, 29, 31, 33, 35, 37, 39,
- 43, 45, 47, 49, 51, 53, 55, 57, 59, 61, 63, 65, 67, 69, 71, 73, 75, 77,
- 81, 83, 85, 87, 89, 91, 93, 95, 97, 99, 101.
- 2. Count to 100 or more by 3's.
-), 3, 6, 9, 12, 15, 18, 21, 24, 27, 30, 33, 36, 39, 42, 45, 48, 51, 54, 57, 63, 66, 69, 72, 75, 78, 81, 84, 87, 90, 93, 96, 99, 102.

- 1, 4, 7, 10, 13, 16, 19, 22, 25, 28, 31, 34, 37, 40, 43, 46, 49, 52, 55, 58, 61, 64, 67, 70, 73, 76, 79, 82, 85, 88, 91, 94, 97, 100.
- 2, 5, 8, 11, 14, 17, 20, 23, 26, 29, 32, 35, 38, 41, 44, 47, 50, 53, 56, 59, 62, 65, 68, 71, 74, 77, 80, 83, 86, 89, 92, 95, 98, 101.
 - 3. Count to 100 or more by 4's.
- 0, 4, 8, 12, 16, 20, 24, 28, 32, 36, 40, 44, 48, 52, 56, 60, 64, 68, 72, 76, 80, 84, 88, 92, 96, 100.
- 1, 5, 9, 13, 17, 21, 25, 29, 33, 37, 41, 45, 49, 53, 57, 61, 65, 69, 73, 77, 81, 85, 89, 93, 97, 101.
- 2, 6, 10, 14, 18, 22, 26, 30, 34, 38, 42, 46, 50, 54, 58, 62, 66, 70, 74, 78, 82, 86, 90, 94, 98, 102.
- 3, 7, 11, 15, 19, 23, 27, 31, 35, 39, 43, 47, 51, 55, 59, 63, 67, 71, 75, 79, 83, 87, 91, 95, 99, 103.
 - 4. Count to 100 or more by 5's.
- 0, 5, 10, 15, 20, 25, 30, 35, 40, 45, 50, 55, 60, 65, 70, 75, 80, 85, \$0, 95, 100.
- 1, 6, 11, 16, 21, 26, 31, 36, 41, 46, 51, 56, 61, 66, 71, 76, 81, 86, 91, 96, 101.
- 2, 7, 12, 17, 22, 27, 32, 37, 42, 47, 52, 57, 62, 67, 72, 77, 82, 87, 92, 97, 102.
- 8, 8, 13, 18, 23, 28, 33, 38, 43, 48, 53, 58, 63, 68, 73, 78, 83, 88, 93, 98, 103.
- 4, 9, 14, 19, 24, 29, 34, 39, 44, 49, 54, 59, 64, 69, 74, 79, 84, 89, 94, 99, 104.
 - 5. Count to 100 or more by 6's.
 - 0, 6, 12, 18, 24, 30, 36, 42, 48, 54, 60, 66, 72, 78, 84, 90, 96, 102.
 - 1, 7, 13, 19, 25, 31, 37, 43, 49, 55, 61, 67, 73, 79, 85, 91, 97, 103.
 - 2, 8, 14, 20, 26, 32, 38, 44, 50, 56, 62, 68, 74, 80, 86, 92, 98, 104.
 - 3, 9, 15, 21, 27, 33, 39, 45, 51, 57, 63, 69, 75, 81, 87, 93, 99, 105.
 - 4, 10, 16, 22, 28, 34, 40, 46, 52, 58, 64, 70, 76, 82, 88, 94, 100.
 - 5, 11, 17, 23, 29, 35, 41, 47, 53, 59, 65, 71, 77, 83, 89, 95, 101.
 - 6. Count to 100 or more by 7's.
 - 0, 7, 14, 21, 28, 35, 42, 49, 56, 63, 70, 77, 84, 91, 98, 105.
 - 1, 8, 15, 22, 29, 36, 43, 50, 57, 64, 71, 78, 85, 92, 99, 106.
 - 2, 9, 16, 23, 30, 37, 44, 51, 58, 65, 72, 79, 86, 93, 100.
 - 3, 10, 17, 24, 81, 38, 45, 52, 59, 66, 73, 80, 87, 94, 101.

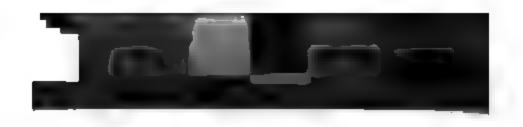
- 4, 11, 18, 25, 32, 39, 46, 53, 60, 67, 74, 81, 88, 95, 102.
- 5, 12, 19, 26, 33, 40, 47, 54, 61, 68, 75, 82, 89, 96, 103.
- 6, 13, 20, 27, 34, 41, 48, 55, 62, 69, 76, 83, 90, 97, 104.
- 7. Count to 100 or more by 8's.
- 0, 8, 16, 24, 32, 40, 48, 56, 64, 72, 80, 88, 96, 104.
- 1, 9, 17, 25, 33, 41, 49, 57, 65, 73, 81, 89, 97, 105.
- 2, 10, 18, 26, 34, 42, 50, 58, 66, 74, 82, 90, 98, 106.
- 3, 11, 19, 27, 35, 43, 51, 59, 67, 75, 83, 91, 99, 107.
- 4, 12, 20, 28, 36, 44, 52, 60, 68, 76, 84, 92, 100.
- 5, 13, 21, 29, 37, 45, 53, 61, 69, 77, 85, 93, 101.
- 6, 14, 22, 30, 38, 46, 54, 62, 70, 78, 86, 94, 102.
- 7, 15, 23, 31, 39, 47, 55, 63, 71, 79, 87, 95, 103.
- 8. Count to 100 or more by 9's.
- 0, 9, 18, 27, 36, 45, 54, 63, 72, 81, 90, 99, 108.
- 1, 10, 19, 28, 37, 46, 55, 64, 73, 82, 91, 100.
- 2, 11, 20, 29, 38, 47, 56, 65, 74, 83, 92, 101.
- 3, 12, 21, 30, 39, 48, 57, 66, 75, 84, 93, 102.
- 4, 13, 22, 31, 40, 49, 58, 67, 76, 85, 94, 103.
- 5, 14, 23, 32, 41, 50, 59, 68, 77, 86, 95, 104.
- 6, 15, 24, 33, 42, 51, 60, 69, 78, 87, 96, 105.
- 7, 16, 25, 34, 43, 52, 61, 70, 79, 88, 97, 106.
- 8, 17, 26, 35, 44, 53, 62, 71, 80, 89, 98, 107.

Find the sum of:

9.	10.	11.	12 .	13.	14.	15.	16.	17 .	18.	19.	20 .
3	2	3	5	3	2	5	5	4	5	3	1
5	1	6	6	3	7	3	6	8	5	6	8
7	9	7	7	4	7	2	4	7	3	7	8
6	8	8	8	5	3	1	7	3	6	3	7
21	20	24	26	15	19 .	11	22	22	19	19	24

Exercise 7. Page 15.

Rind the	sum of:		_	15.	
		•	•	_	
1.	2.	3.	4.	5.	6.
231	341.	430.31	512.87	12.78	1543.1
764	<u>57.8</u>	58.61	36.84	711.58	164.7
995	398.8	488.92	549.71	415.86	1707.8
				1140.20	
7 .	8.	9.		10.	11.
1728.	1897.3	475	.34	402.56	0.7854
402.56	675.34	6897.	.65	164.7	3.1416
2130.56	6897.65	1728.	•	0.5236	2.71828
	9470.29	9100	.99	567.7836	6.64528
12.	13	3.	14.	15.	16.
2.71828	0.7	7854	2.7113	230.8	32.358
402.56	4.1	2	27.53	223.	821.9
1897.3	30. 1	03 3	41.586	2.63	23.04
2302.57828	35.0	0084 3	71.8273	373.8	73.7
				830.23	950.998
17.		18.	1	9.	20.
202.30	031	0.0078	653.	03	939.303
				•	
71.57		7.377		303	65.746
71.57 65.81	75		65.		
	75 1 <u>3</u>	7.377	65. 6.	303	65.746
65.81	75 1 <u>3</u>	7.377 853.03 860.4148	65. 6.	303 5033	65.746 8.2794 1013.3284
65.81 339.69	75 1 <u>3</u> 911	7.377 853.03 860.4148	65. 6. 724.	303 5033 8363	65.746 8.2794 1013.3284
65.81 339.69	75 1 <u>3</u> 911	7.377 853.03 860.4148 2 0.43	65. 6. 724. 2 .	303 <u>5033</u> 8363	65.746 8.2794 1013.3284 3295
65.81 339.69 2	75 1 <u>3</u> 2 1. .7182818	7.377 853.03 860.4148 2 0.43 0.20	65. 6. 724. 2 . 42945	303 5033 8363 23 1.609	65.746 8.2794 1013.3284 3. 3295 3487
65.81 339.69 2 3. 0	75 13 911 21. .7182818 .1415927	7.377 853.03 860.4148 2 0.43 0.20 4.81	65. 6. 724. 2. 42945 98882	303 5033 8363 23 1.609 15.432	65.746 8.2794 1013.3284 3. 3295 3487
65.81 339.69 2 3. 0	75 13 911 21. .7182818 .1415927 .7853982	7.377 653.03 660.4148 2 0.43 0.20 4.81 $\overline{5.45}$	65. 6. 724. 2 . 42945 98882 04774	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487
65.81 339.69 2. 3. 0. 6.	75 13 911 21. .7182818 .1415927 .7853982	7.377 853.03 860.4148 2 0.43 0.20 4.810 5.45	65. 6. 724. 2. 42945 98882 04774 46601	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487 6782
65.81 339.69 24.	75 13 911 21. .7182818 .1415927 .7853982	7.377 853.03 860.4148 2 0.43 0.20 4.810 5.45	65. 6. 724. 2. 42945 98882 04774 46601	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487 6782
65.81 339.69 24. 0.4771213	75 13 911 21. .7182818 .1415927 .7853982	7.377 853.03 860.4148 2 0.43 0.20 4.810 5.45	65. 6. 724. 2. 42945 98882 04774 46601 25.	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487 6782 26. 0.6213768
65.81 339.69 24. 0.4771213 0.2908882	75 13 911 21. .7182818 .1415927 .7853982	7.377 653.03 660.4148 2 0.43 0.20 4.81 $\overline{5.45}$ 1.60 3.28 0.39	65. 6. 724. 2. 42945 98882 04774 46601 25. 93295 08693	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487 6782 26. 0.6213768 3.785
65.81 339.69 24. 0.4771213 0.2908882 4.8104774	75 13 911 21. .7182818 .1415927 .7853982	7.377 653.03 660.4148 2 0.43 0.20 4.81 $\overline{5.45}$ 1.60 3.28 0.39 0.52	65. 6. 724. 2. 42945 98882 04774 46601 25. 93295 08693 37043	303 5033 8363 23 1.609 15.432 3.785	65.746 8.2794 1013.3284 3. 3295 3487 6782 26. 0.6213768 3.785 0.264



29,

8	ADVANCED	ARITHMETIC.
•	20121000	25-071 1 24 24 27 1 1 VI

27.

47.	40.	49.
0.6213768	0.8937043	1.4142186
1.4142138	0.8047978	1.0000000
3.2808693	1.7320508	0.30103
0.3047973	2.236068	0.381966
4.8104774	0.381966	8.2808693
10.4817844	5.0485864	6.9874084
	Exercise 8. Page 17.	
Find the sum of:	•	
2.	E.	3.
\$45.68	\$ 154.31	\$73.86
73.91	296.85	458.71
78.54	736,48	137.64
534,69	345.19	98.87
184.70	782.34	643.48
581,43	78.43	462.71
\$1448.95	\$2393.60	\$1870.27
4.	5.	6.
\$4 98,50	\$ 65.42	\$ 621.65
17.37	638.34	107.32
684.29	763.48	856.96
2 31. 56	800.31	718.83
210.10	798.83	501.49
671.5 <u>4</u>	835.78	315.72
643.58	856.47	768.44
\$2956.89	\$4267.58	\$3950.41
7.	8.	9 .
\$ 791.52	\$ 32.54	\$ 763.89
504 83	254.63	78.23
879.26	63.27	345.61
243.97	131.66	26.73
732.86	506.72	489.56
47.95	283.54	812.35
856.43	345.83	607.28
497.65	643.46	219.07
541,26	708.91	68.72
616.72	463.73	216.78
857.94	67.74	436.74
\$ 6570.39	\$3501.93	\$4064.96

28.

10.	11.	12.
\$8400.07	\$ 1873 .33 .	\$2336.29
3212.17	6170.24	336.00
1716.41	4813.25	2456.25
1020.08	662.25	641.25
1452.44	622.64	1174.50
1829.51	692.82	326.03
1929.96	24 57.75	1219.87
114.78	2126.76	226.7 8
89.75	5391.25	276.75
173.67	7349.86	5936.40
17.45	1422.75	1914.78
112.44	9667.50	311.87
1098.75	6000.00	7958.00
6170.24	572.80	1919.66
\$ 27337.72	\$ 49823.20	\$27032.43
30	7.4	16
13.	14.	15.
\$1482.40	\$773.72	\$2406.08
\$1482.40	\$ 773. 72	\$2406.08
\$1482.40 2575.71	\$ 773. 72 442. 37	\$2406.08 3101.24
\$1482.40 2575.71 3364.27	\$773.72 442.37 454.86	\$2406.08 3101.24 1452.09
\$1482.40 2575.71 3364.27 689.81	\$773.72 442.37 454.86 358.61	\$2406.08 3101.24 1452.09 3693.91
\$1482.40 2575.71 3364.27 689.81 1533.61	\$773.72 442.37 454.86 358.61 2003.17	\$2406.08 3101.24 1452.09 3693.91 2054.76
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58	\$773.72 442.37 454.86 358.61 2003.17 179.56	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69 261.64	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75 4179.54	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35 1562.50
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69 261.64 1516.56	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75 4179.54 3493.54	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35 1562.50 6937.50
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69 261.64 1516.56 2197.23	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75 4179.54 3493.54 178.17	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35 1562.50 6937.50 1987.57
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69 261.64 1516.56 2197.23 1317.71	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75 4179.54 3493.54 178.17 727.53	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35 1562.50 6937.50 1987.57 943.27
\$1482.40 2575.71 3364.27 689.81 1533.61 735.58 105.69 261.64 1516.56 2197.23 1317.71 408.30	\$773.72 442.37 454.86 358.61 2003.17 179.56 8493.75 4179.54 3493.54 178.17 727.53 2889.42	\$2406.08 3101.24 1452.09 3693.91 2054.76 1231.25 1828.35 1562.50 6937.50 1987.57 943.27 2312.11

Exercise 9. Page 19.

- 1. Subtract by 2's from 20 to 0; from 21 to 1.
 20, 18, 16, 14, 12, 10, 8, 6, 4, 2, 0.
 21, 19, 17, 15, 13, 11, 9, 7, 5, 3, 1.
- 2. Subtract by 3's from 20 to 2; from 21 to 0. 20, 17, 14, 11, 8, 5, 2.

21, 18, 15, 12, 9, 6, 3, 0.

3. Subtract by 4's from 30 to 2; from 31 to 3; from 32 to 0; from 33 to 1.

30, 26, 22, 18, 14, 10, 6, 2. 31, 27, 23, 19, 15, 11, 7, 3. 32, 28, 24, 20, 16, 12, 8, 4, 0. 33, 29, 25, 21, 17, 13, 9, 5, 1.

4. Subtract by 5's from 32 to 2; from 33 to 3; from 34 to 4; from 35 to 0; from 36 to 1.

32, 27, 22, 17, 12, 7, 2. 33, 28, 23, 18, 13, 8, 3. 34, 29, 24, 19, 14, 9, 4. 35, 30, 25, 20, 15, 10, 5, 0. 36, 31, 26, 21, 16, 11, 6, 1.

5. Subtract by 6's from 33 to 3; from 34 to 4; from 35 to 5; from 36 to 0; from 37 to 1; from 38 to 2.

33, 27, 21, 15, 9, 3. 34, 28, 22, 16, 10, 4. 35, 29, 23, 17, 11, 5. 36, 30, 24, 18, 12, 6, 0, 37, 31, 25, 19, 13, 7, 1. 38, 32, 26, 20, 14, 8, 2.

6. Subtract by 7's from 42 to 0; from 43 to 1; from 44 to 2; from 45 to 3; from 46 to 4; from 47 to 5.

42, 35, 28, 21, 14, 7, 0. 43, 36, 29, 22, 15, 8, 1. 44, 37, 30, 23, 16, 9, 2. 45, 38, 31, 24, 17, 10, 3. 46, 39, 32, 25, 18, 11, 4. 47, 40, 33, 26, 19, 12, 5.

7. Subtract by 8's from 42 to 2; from 43 to 3; from 44 to 4; from 45 to 5; from 46 to 6; from 47 to 7.

42, 34, 26, 18, 10, 2. 43, 35, 27, 19, 11, 3. 44, 36, 28, 20, 12, 4. 45, 37, 29, 21, 13, 5. 46, 38, 30, 22, 14, 6. 47, 39, 31, 23, 15, 7. 8. Subtract by 9's from 55 to 1; from 56 to 2; from 57 to 3; from 59 to 5; from 61 to 7; from 62 to 8.

55, 46, 37, 28, 19, 10, 1. 56, 47, 38, 29, 20, 11, 2. 57, 48, 39, 30, 21, 12, 3. 59, 50, 41, 32, 23, 14, 5. 61, 52, 43, 34, 25, 16, 7. 62, 53, 44, 35, 26, 17, 8.

Exercise 10. Page 21.

Find the remainder and prove:

1.	2.	3.	4.	5 .	6 .	7 .	8.
234	343	424	555	676	72 5	839	999
123	123	123	123	123	123	123	123
111	220	301	432	553	602	716	876
Proof.	Proof.	Proof.	Proof.	Proof.	Proof.	Proof.	Proof.
111	220	301	432	5 53	602	716	876
123	123	123	123	123	123	123	123
234	343	424	555	676	725	839	999
9.	10.	11.	12.	13.	14 .	15.	16 .
1000	5120	789	879	978	6378	6855	6853
123	123	456	456	456	456	456	456
877	4997	333	423	522	5922	6399	6397
Proof.	Proof.	Proof.	Proof.	Proof.	Proof.	Proof.	Proof.
877	4997	333	423	522	5922	6399	6397
123	123	456	456	456	456	456	456
1000	5120	789	879	978	6378	6855	6853
17.	18.	19	. 2	0.	21.	22.	23.
7797	7006	354	2 40	000	974	368	2301
456	456	45	6 4	156	779	249	479
7341	6550	308		<u></u> 544	195	119	1822
Proof.	Proof.	Pro	of. Pr	oof.	Proof.	Proof.	Proof.
7341	6550	308	6 35	544	195	119	1822
456	456	45	6 4	156	779	249	479
7797	7006	354	2 40	000	974	368	2301

ADVANCED ARITHMETIC.

24.	25 .	26 .	27.	28.	29.	30 .
2731	708	1123	891	8103	19,001	2180
929	394	1072	773	5621	3,456	792
1802	314	51	118	2482	15,545	1388
Proof.	Proof.	Proof.	Proof.	Proof.	Proof.	Proof.
1802	314	51	118	2482	15,545	1388
929	394	1072	773	5621	3,456	792
2731	708	1123	891	8103	19,001	2180 .
31.	32	2.	33 .	3	34.	35 .
\$ 183. 4 5	\$ 716.	43	\$64 7.51	\$27	0.04	\$ 125.
76.47	628.	74	549.64	12	28.31	101.50
\$106.98	\$87.	69	\$97.87	\$14	11.73	\$23.50
Proof.	Proc	of.	Proof.	P	roof.	Proof.
\$ 106.98	\$87.	69	\$ 97.87	\$ 14	1.73	\$23.5 0
76.47	628.	74	549.64	19	28.31	101.50
\$183.45	\$716.	43	\$647.51	\$27	70.04	\$125.00
36 .	37.		38 .	39).	4 0.
\$247.93	\$64 1.8	37	\$ 56.27	3.1415	927	0.7853982
129.47	333.8	95	29.89	2.7182	818	0.5235988
\$118.46	\$ 307.9	92	\$26.38	0.4233	109	0.2617994
Proof.	Proof	f.	Proof.	Proc	of.	Proof.
\$ 118.46	\$ 307.9	92	\$ 26.38	0.4233	109	0.2617994
129.47	333.9	95	29.89	2.7182	818	0.5235988
\$247.93	\$641.8	3 7	\$ 56.27	3.1415	927	0.7853982
41.	42	2.	4 3.	4	4.	45 .
4.8104774	2.539	9772	0.3937043	3.2 8	08693	3.2808693
0.4342945	0.393	7043	0.3047973	0.30	47973	1.6093295
4.3761829	2.146	2729	0.088907	2.97	6072	1.6715398
Proof.	Pro	oof.	Proof.	Pr	oof.	Proof.
4.3761829	2.146	2729	0.088907	2.97	6072	1.6715398
4.3761829 0.4342945	2.146 0.393		0.088907 0.3047973		76072 947973	1.6715398 1.6093295

46 .	47.	48 .	4 9.	50 .
3.785	15.4323487	1.7320508	2.236068	2.236068
0.6213768	0.264	1.4142136	1.7320508	0.618034
3.1636232	15.1683487	0.3178372	0.5040172	1.618034
Proof.	Proof.	Proof.	Proof.	Proof.
3.1636232	15.1683487	0.3178372	0.5040172	1.618034
0.6213768	0.264	1.4142136	1.7320508	0.618034
3.785	15.4323487	1.7320508	2.236068	2.236068
51 .	52 .	5	i3 .	54 .
0.381966	3.141592	27 2.38	661 94 5 1	.5707963
0.30103	0.785398	32 0.78	<u>853982</u> 0	.7853982
0.080936	2.356194	1.57	707963 0	.7853981
Proof.	Proof.	Pı	roof.	Proof.
0.080936	2.356194	1.57	07963 0	.7853981
0.30103	0.785398	32 0.78	353982 0	.7853982
0.381966	3.141592	2.35	661945 1	.5707963
55 .	56 .		57 .	58 .
3.141592	7 2.61799	39 2.09	943951 1	.5707963
0.523598	0.52359	88 0.55	235988 0	.5235988
2.617993	9 2.09439	51 1.57	707963	.0471975
Proof.	Proof.	. P	roof.	Proof.
2.617993	2.09439	51 1.57	707963 1	.0471975
0.523598	8 0.52359	88 0.59	235988 0	.5235988
3.141592	2.61799	39 2.09	043951 · 1	.5707963
59 .	60 .		51 .	62 .
1.047197	5 1.	1.4	142136 0	.618034
0.523598	0.38196	0.6	18034 0	.381966
0.523598	0.61803	0.79	961796 0	.236068
Proof.	Proof.	P	roof.	Proof.
0.523598	0.61803	0.79	9 61796 0	.236068
0.523598	0.38196	0.6	18034 0	.381966
1.047197	75 1.	1.4	142136	1.618034

63 .	64 .	65 .	66 .
9,873,210	8010.101	1,000,000	729,434
8,765,420	4187.94	817,259	613,488
1,107,790	3822.161	182,741	115,946
Proof.	Proof.	Proof.	Proof.
1,107,790	3822.161	182,741	115,946
8,765,420	4187.94	817,259	613,488
9,873,210	8010.101	1,000,000	729,434
67 .	68 .	69.	70 .
6532.18	1718.754	21,205.	42,786.95
1916.47	1389.328	1,787.563	4,278.695
4615.71	329.426	19,417.437	38,508.255
Proof.	Proof.	Proof.	Proof.
4615.71	329.426	19,417.437	38,508.255
1916.47	1389.328	1,787.563	4,278.695
6532.18	1718.754	21,205.	42,786.95

Exercise 11. Page 22.

1. In a till are \$391 in bills, \$67.50 in gold, \$39.75 in silver, and \$2.77 in copper and nickel. How much money is in the till?

2. Starting out with \$315.75 in one wallet and \$54.37 in another, I pay the grocer \$127.38; the butcher, \$64.17; the shoemaker, \$21.40; the landlord, \$50; the tailor, \$35. What ought I to have left?

\$ 315.75	\$127.38	\$ 370.12
54.37	64.17	297.95
\$ 370.12	21.40	\$72.17 Ans.
	50.00	
	35.00	
	• \$297.95	

3. On a bill of \$753.43 I pay \$517.87. How much do I still owe? If I owe \$817.87, and have but \$637.50, how much do I lack of being able to pay?

\$753.43 517.87 \$235.56 Ans. \$817.87 637.50 \$180.37 Ans.

4. If a man was born January 1, 1812, how old was he January 1, 1878.

1878 1812 66

66 years. Ans.

5. America was discovered in 1492. How many years after its discovery was each of the following events?

Settlement of Florida, 1565; of Virginia, 1607; of Massachusetts, 1620; of Quebec, 1608; French and Indian War, 1756; Declaration of Independence, 1776; Inauguration of Washington, 1789; War with England, 1812; Mexican War, 1846; Civil War, 1861.

1565	1607	1620	1608	1756
1492	1492	1492	1402	1492
73	115	128	116	264
1776	1789	1812	1846	1861
1492	1492	1492	1492	1492
284	297	320	354	369

73; 115; 128; 116; 264; 284; 297; 320; 354; 369. Ans.

6. The minuend is one hundred million, two hundred fifty-six thousand, three hundred seventy-two, and the subtrahend is nineteen million, nine hundred thousand, nine hundred ninety-nine. Find the remainder.

100,256,372 19,900,999 80,355,373 Ans.

7. If the minuend is 9874, and remainder 3185, what is the subtrahend? The subtrahend being 7659, and remainder 675.68, what is the minuend?

9874 675.68 3185 7659. 6689 Ans. 8334.68 Ans. 8. The smaller of two numbers is 7.95764328; their difference is 0.00087692. What is the larger number?

7.95764328 0.00087692 7.9585202 Ans.

9. The larger of two numbers is 7.95764328, and their difference is 7.153485. What is the smaller number?

10. If the subtrahend is 10,542, and the difference 544.2, what is the minuend?

10,542.

544.2

11,086.2 Ans.

11. A man pumps out of a cistern in one hour 243.75 gallons; in the next hour, 227.5 gallons; in 45 minutes more, 137.75 gallons; and the cistern is empty. How many gallons of water were in it?

243.75 227.5 137.75 609. Ans.

12. From what number must I subtract 5 to leave 7? 8 to leave 9? From what number must I subtract 5.1736 to leave 8.1964? 6.231 to leave 9.6648? 74.213 to leave 25.787?

7 9 8.1964 5 8 5.1736 12 Ans. 17 Ans. 13.37 Ans. 9.6648 25.787 6.231 74.213 15.8958 Ans. 100. Ans. 13. What must be subtracted from 1 to leave 0.5? to leave 0.53? to leave 0.532? to leave 0.5236? to leave 0.5235988?

1.	1.		1.
0.5	0.53		0.532
$\overline{0.5}$ Ans.	0.47	Ans.	0.468 Ans.
1.		1.	
0.5236		0.5235	988
0.4764	Ans.	0.4764	012 Ans.

14. I start on a journey of 3433 miles. The first day I make 428 miles; the second day, 511 miles; the third, 497 miles; the fourth, 513. How many miles of my journey remained for me at the close of each day? How many miles had I gone at the close of each day?

3433	
428	
3005 after first day.	428 end of first day.
511	511
2494 after second day.	939 end of second day.
497	497
1997 after third day.	$\overline{1436}$ end of third day.
513	513
1484 after fourth day.	$\overline{1949}$ end of fourth day.

15. Subtract 76,343 from the sum of 61,932, 51,387, 5193, 4674, and 8199; then subtract 23,657 from the remainder.

61,932		
51,387	131,385	
5,193	76,343	
4,674	55,042	
8,199	23,657	
131,385	31,385	Ans.

16. Jones bought a farm and stock for \$7633.90; sold the stock for \$305.75; then sold the farm for \$7325. How much did he lose?

\$ 305.75	\$ 7633.90	
7325.	7630.75	
\$7630.75	\$3.15	Ans.

17. If I gave \$4375 for my land, and paid for house, barn, sheds, and fences \$2789.50, also \$973.75 for horses, cattle, tools, etc., what did my farm and stock cost?

\$4375. 2789.50 973.75 \$8138.25 Ans.

18. If I paid \$8138.25 for land and cattle, and sold part of the land for \$675, and part of the cattle for \$217.50, what is the cost of the land and the cattle left?

\$ 675.	\$8138.25	
217.50	892.50	
\$ 892.50	\$7245.75	Ans.

19. John has 158 cents, James has 271 cents; James gives John 56 cents. Which has then more than the other, and how many cents more?

158	271
56	56
214 John.	$\overline{215}$ James.

Therefore, James has 1 cent more.

20. A cattle dealer had 228 oxen, 475 sheep, and 49 lambs; he sold 17 oxen, 64 sheep, and 7 lambs. How many animals of each kind did he then have, and how many all together?

228 oxen.	475 sheep.	49 lambs.	211
_17	64	7	411
211 oxen.	411 sheep.	42 lambs.	42
			664

Exercise 12. Page 29.

Find the product of:

1.	2.	3.	4.
0.5235988	0.7853982	3.14159265	8.75
6	4	5	30
$\overline{3.1415928}$	$\overline{3.1415928}$	15.70796325	262.50
		5	
		78.53981625	

5 .	6.	7 .	8.
6.975	7.81	65.432	7.85
0.07	700	8000	300
0.48825	5467.00	523,456.000	2355.00
_			
9.	10.	11.	12.
10,356.78	0.785398	0.785398	0.785398
0.009	7.37	8.56	1001
93.21102	5497786	4712388	785398
	2356194	3926990	785398
	5497786	6283184	786.183398
	5.78838326	6.7 2300688	
13.	14.	15.	16.
2150.42	2150.42	2150.42	1.4142136
0.083	0.75	0.075	0.7071
645126	1075210	1075210	14142136
1720336	1505294	1505294	98994952
178.48486	1612.8150	161.28150	98994952
			0.0000000000000000000000000000000000000
			0.99999043656
17.	18.	19.	
17 .	18.	19 .	20.
1.41421	1.732	2.23607	20 . 0.618
1.41421 1.4142	1.732 1.732	2.23607 2.236	20 . 0.618 618
$\frac{1.41421}{1.4142}$ $\frac{282842}{2}$	$ \begin{array}{r} 1.732 \\ \underline{1.732} \\ \hline 3464 \end{array} $	$ \begin{array}{r} 2.23607 \\ $	20. 0.618 618 4944
1.41421 1.4142 282842 565684	1.732 1.732 3464 5196	2.23607 2.236 1341642 670821	20. 0.618 618 4944 618
1.41421 1.4142 282842 565684 141421	1.732 1.732 3464 5196 12124	2.23607 2.236 1341642 670821 447214	20. 0.618 618 4944 618 3708
1.41421 1.4142 282842 565684 141421 565684	1.732 1.732 3464 5196 12124 1732	2.23607 2.236 1341642 670821 447214 447214	20. 0.618 618 4944 618
1.41421 1.4142 282842 565684 141421 565684 141421	1.732 1.732 3464 5196 12124	2.23607 2.236 1341642 670821 447214	20. 0.618 618 4944 618 3708
1.41421 1.4142 282842 565684 141421 565684	1.732 1.732 3464 5196 12124 1732	2.23607 2.236 1341642 670821 447214 447214	20. 0.618 618 4944 618 3708
1.41421 1.4142 282842 565684 141421 565684 141421	1.732 1.732 3464 5196 12124 1732	2.23607 2.236 1341642 670821 447214 447214	20. 0.618 618 4944 618 3708
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782	1.732 1.732 3464 5196 12124 1732 2.999824	$\begin{array}{r} 2.23607 \\ \underline{2.236} \\ 1341642 \\ 670821 \\ 447214 \\ \underline{447214} \\ 4.99985252 \end{array}$	20. 0.618 618 4944 618 3708 381.924
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21.	1.732 1.732 3464 5196 12124 1732 2.999824	2.236 2.236 1341642 670821 447214 447214 4.99985252	20. 0.618 618 4944 618 3708 381.924
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21. 0.618034	1.732 1.732 3464 5196 12124 1732 2.999824 22. 0.12936	2.23607 2.236 1341642 670821 447214 447214 4.99985252 23. 7.92801	20. 0.618 618 4944 618 3708 381.924
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21. 0.618034 0.618035	1.732 1.732 3464 5196 12124 1732 2.999824 22. 0.12936 12	2.23607 2.236 1341642 670821 447214 447214 4.99985252 23. 7.92801 0.9	20. 0.618 618 4944 618 3708 381.924 24. 58.383 0.39
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21. 0.618034 0.618035 3090170	$ \begin{array}{r} 1.732 \\ \underline{1.732} \\ 3464 \\ 5196 \\ 12124 \\ \underline{1732} \\ 2.999824 \end{array} $ $ \begin{array}{r} 22. \\ 0.12936 \\ \underline{12} \\ 25872 \end{array} $	2.23607 2.236 1341642 670821 447214 447214 4.99985252 23. 7.92801 0.9	20. 0.618 618 4944 618 3708 381.924 24. 58.383 0.39 525447
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21. 0.618034 0.618035 3090170 1854102	1.732 1.732 3464 5196 12124 1732 2.999824 22. 0.12936 12 25872 12936	2.23607 2.236 1341642 670821 447214 447214 4.99985252 23. 7.92801 0.9	20. 0.618 618 4944 618 3708 381.924 24. 58.383 0.39 525447 175149
1.41421 1.4142 282842 565684 141421 565684 141421 1.999975782 21. 0.618034 0.618035 3090170 1854102 4944272	1.732 1.732 3464 5196 12124 1732 2.999824 22. 0.12936 12 25872 12936	2.23607 2.236 1341642 670821 447214 447214 4.99985252 23. 7.92801 0.9	20. 0.618 618 4944 618 3708 381.924 24. 58.383 0.39 525447 175149

25.	26.	27 .	28.
0.28744	491.205	68.325	0.732
0.08	0.065	6.25	1.6
$\overline{0.0229952}$	2456025	341625	4392
	2947230	136650	732
	$\overline{31.928325}$	409950	1.1712
		427.03125	
29 .	30 .	31.	32 .
1208.88	0.0125	0.007	0.0001
0.438	498	7	1000
967104	1000	$\overline{0.049}$	0.1000
362664	1125		
483552	500		
529.48944	6.2250		
33 .	34 .	35 .	36.
10.24	0.00507702	$\boldsymbol{0.00752}$	0.0256
0.235	0.0283	89.3	74.1
5120	1523106	2256	256
3072	4061616	6768	1024
2048	1015404	6016	_1792_
2.40640	0.000143679666	0.671536	1.89696

Exercise 13. Page 30.

Express the product of:

1.

2.

$$7^{5} \times 7^{8} = 7^{5+8} = 7^{8}$$
. $3.01^{2} \times 3.01 = 3.01^{2+1} = 3.01^{8}$. $8^{2} \times 8 = 8^{2+1} = 8^{8}$. $0.67^{2} \times 0.67^{8} = 0.67^{2+8} = 0.67^{10}$. $2^{8} \times 2 = 2^{8+1} = 2^{9}$. $0.208 \times 0.208^{3} = 0.208^{1+8} = 0.208^{4}$. $5^{4} \times 5^{2} = 5^{4+2} = 5^{6}$.

3.

$$2.003^2 \times 2.003^4 = 2.003^2 + 4 = 2.003^6$$
.
 $20.03^8 \times 20.03 = 20.03^8 + 1 = 20.03^4$.
 $20.03 \times 20.03^2 = 20.03^1 + 2 = 20.03^8$.

Exercise 14. Page 32.

Find the following products, and test the accuracy by casting out the nines, and by casting out the elevens:

1.
21.3706
15.243
641118
854824
427412
1068530
213706
325.7520558
1.8954
13030082232
16287602790
29317685022
26060164464
3257520558
317.43044656332

The three remainders after the nines are cast out are 1, θ , and 0. $1 \times 6 \times 0 = 0$.

The remainder of the product after the nines are cast out is 0.

The three remainders after the elevens are cast out are 9, 8, and 1. $9 \times 8 \times 1 = 72$, or casting out the elevens, 6.

The remainder of the product after the elevens are cast out is 6.

The three remainders after the nines are cast out are 8, 0, 4. $8 \times 0 \times 4 = 0$.

The remainder of the product after the nines are cast out is 0.

The three remainders after the elevens are cast out are 7, 4, and 4. $7 \times 4 \times 4 = 112$, or casting out the elevens, 2.

The remainder of the product after the elevens are cast out is 2.

	3 .
	5.8281
	0.0012
	116562
	58281
	$\overline{0.00699372}$
	0.6827
	4895604
•	1398744
	5594976
	4196232
	0.004774612644

The three remainders after the nines are cast out are 6, 3, and 5. $6 \times 3 \times 5 = 90$, or after the nines are cast out, 0.

The remainder of the product after the nines are cast out is 0.

The three remainders after the elevens are cast out are 3, 1, and 7. $3 \times 1 \times 7 = 21$, or after the elevens are cast out, 10.

The remainder of the product after the elevens are cast out is 10.

The three remainders after the nines are cast out are 7, 6, and 8. $7 \times 6 \times 8 = 336$, or after the nines are cast out, 3.

The remainder of the product after the nines are cast out is 3.

The three remainders after the elevens are cast out are 9, 2, and 6. $9 \times 2 \times 6 = 108$, or after the elevens are cast out, 9.

The remainder of the product after the elevens are cast out is 9.

5 .
39.801
1.44
159204
159204
39801
57.31344
17.9645
28656720
229 25376
34388064
51582096
40119408
5731344
1029.607292880

The three remainders after the nines are cast out are 3, 0, and 5. $3 \times 0 \times 5 = 0$.

The remainder of the product after the nines are cast out is 0.

The three remainders after the elevens are cast out are 3, 1, and 4. $3 \times 1 \times 4 = 12$, or after the elevens are cast out, 1.

The remainder of the product after the elevens are cast out is 1.

6.

5.2817
0.0165
264085
316902
52817
0.08714805
0.8469
0.0100
78433245

78433245
78433245 52288830
78433245 52288830 34859220

The three remainders after the nines are cast out are 5, 3, and 0. $5 \times 3 \times 0 = 0$.

The remainder of the product after the nines are cast out is 0.

The three remainders after the elevens are cast out are 6, 0, and $10. 6 \times 0 \times 10 = 0.$

The remainder of the product after the elevens are cast out is 0.

7.
0.54237
16
325422
54237
8.67792
0.00176
5206752
6074544
867792
0.0152731392

The three remainders after the nines are cast out are 3, 7, and 5. $3 \times 7 \times 5 = 105$, or after the nines are cast out, 6.

The remainder of the product after the nines are cast out is 6.

The three remainders after the elevens are cast out are 7, 5, and 0. $7 \times 5 \times 0 = 0$.

The remainder of the product after the elevens are cast out is 0.

8.
24.271
3.6485
121355
194168
97084
145626
72813
88.5527435
15.271
885527435
6198692045
1771054870
4427637175
885527435
1352.2889459885

The three remainders after the nines are cast out are 7, 8, and 7. $7 \times 8 \times 7 = 392$, or after the nines are cast out, 5.

The remainder of the product after the nines are cast out is 5.

The three remainders after the elevens are cast out are 5, 9, and 3. $5 \times 9 \times 3 = 135$, or after the elevens are cast out, 3.

The remainder of the product after the elevens are cast out is 3.

9.
13.256
14.125
66280
26512
13256
53024
13256
187.241000

187.241000
30.254
748964000
936205
374482
561723
5664.789214000

The three remainders after the nines are cast out are 8, 4, and 5.

 $8 \times 4 \times 5 = 160$, or after the nir are cast out, 7.

The remainder of the produ after the nines are cast out is 7

The three remainders after t elevens are cast out are 1, 1, and $1 \times 1 \times 4 = 4$.

The remainder of the produ after the elevens are cast out is

Exercise 15. Page 34.

Find to the fifth decimal the value of:

1. 2.		3.		
0.49714987	0.79817987	1.09920986		
362218571	579924990	494758420		
497150	718361	219842		
348004	71835	43968		
24857	3192	8794		
3977	160	550		
50	71	76		
9	6	4		
1	$\overline{0.793625}$	1		
0.874048	0.79363. Ans.	0.273235		
0.87405. Ans.		0.27324. Ans.		
4.	5.	6.		
0.62208861	1.75812263	0.55630251		
266175610	369519502	573544330		
62209	3516245	166891		
37325	87906	16689		
3110	15823	2225		
435	176	222		
6	88	28		
4	15	2		
0.103089	1	0.186057		
0.10309. Ans.	3.620254	0.18606. Ans.		

3.62025. Ans.

7 . 8 .		9.		
0.75142506	0.05245506	0.33143325		
965899899	266175610	317362971		
6762825	5246	331433		
676283	3147	232003		
60124	262	29829		
6763	36	663		
676	1	199		
60	$\overline{0.008692}$	10		
4	0.00869. Ans.	2		
7.506735		0.594139		
7.50674. Ans.		0.59414. Ans.		
10.	11.	12.		
0.90633287	2.84657842	0.546794489		
67315545160	245596690	5947967482		
543799	2561920	1093589		
9063	170794	437435		
4532	17079	21871		
362	2561	3827		
. 45	142	328		
5	14	49		
1	1	4		
0.557807	2.752581	1.557103		
0.55781. Ans.	2.75258. Ans.	1.55710. Ans.		

Exercise 16. Page 38.

Find the quotient of:

1.	2.	3 .	4.
9) 126, 409	10) 13.31	11) 13.31	12) 1.728
14.04544	1.331	1.21	0.144
5.	6.	7.	8.
39) 3.7632	29) 4263.1	499) 964.64	699) 0.58775
1.2544	2131.55	241.16	0.09796
9.	10.	11.	12.
799) 752.30	89) 895.6	999) 982.54	7999) 82.610
107,47143	111.95	109,17111	11,80143

13.	14.	15 .	16.
599) 836.90	119) 9646.4	1299) 875.85	299) 274.85
167.38	876.94545	72.9875	137.425
17.	18.	19.	20.
002) 1001.	005)004.	004)743.2	0005)31000.
500.5	0.8	185.8	6200.
21.	22.	23 .	24.
0012) 480000.	00007) 9800000.	000009) 1098000.	009) 1098.
40000.	1400000.	122000.	
25 .	26 .	27 .	28.
000009) 10980.	009) 10.98	11) 144100.	11) 189.2
1220.	1.22	13100.	17.2

F

1220.	1.22	13100.	17.2
1	Exercise 17. Pa	nge 42 .	
Find the quotient of	:		
1.	2.		3.
83	6297		118033
91) 7553	73) 4593		76) 89713
728	438		76
273	213		137
273	. 146		76
	67		611
			<u>608</u>
			33
4.	5 .		6.
61011	10103	2 5	204538
88) 53691	35) 35372		408) 834561
528	35		816
89	37		1856
88_	35		1632
11	22		2241
			2040
			201

	TEACHERS' EDITION.	2
7.	8.	9.
1382333	2180345	439 1 1
247)341586	395) 861345	843) 370406
247	790	3372
945	713	3320
741	395_	2529
2048	3184	7916
1976	3160	<u>7587</u>
726	245	329
<u>494</u>		
232		
10.	11.	12.
1964141	1523 } 	469_{1289}^{189}
498) 978217	357) 543816	1289) 604730
498	357	5156
4802	1868	8913
4482	1785	7734
3201	831	11790
2988	714	11601
2137	1176	189
<u>1992</u>	1071	
145	105	
13.	14.	15.
2.475	71.12	0.045
132) 326.7	1121) 79725.52	906) 40.77
264	7847	3624
627	1255	4530
<u>528</u>	1121	<u>4530</u>
990	1345	
924	1121	
660	2242	
<u>660</u>	<u>2242</u>	

16.	18.	19.
9.007	3.1416	62. 5
1068) 9619.476	3937) 12368.4792	1926) 120375.
9612	11811	11556
7476	5574	4815
7476	3937	3852
	16377	9630
17.	15748	9630
70.	6299	
\$38745) \$2712150.	<u>3937</u>	
271215	23622	
0	<u>23622</u>	
20.	21.	22.
160000.	7.58	640.
00016) 2560000.	319) 2418.02	03125) 2000000.
16	2233	18750
96	1850	12500
96	1595	12500
0000	2552	<u>12000</u>
0000	2552	V
23.	24.	25 .
92.8	3.35977	1.75499
008302) 770425.6	0479) 1609.3295	0917) 1609.3295
74718	1437	917
23245	1723	6923
16604	1437	6419
66416	2862	5042
66416	2 395	4585
	4679	4579
	4311	3668
	3685	9115
	<u>3353</u>	8253
	3320	8620
		8253
		367

26.	27 .	28 .
94.66644	184.98040	1.76471
0017) 1609.3295	00087) 16093.295	17)30.
153	87	17
79	789	130
<u>68</u>	696	119
113	433	110
102	348	102
112	852	80
102	<u>783</u>	<u>68</u>
109	699	120
102	<u>696</u>	119
75	350	10
<u>68</u>	348	
7 29 .	30. .	31.
1.73410	1.73210	1.73200
173)300.	1732) 3000.	17321)30000.
173	1732	17321
1270	12680	126790
1211	12124	121247
590	5560	55430
519	5196	51963
710	3640	34670
692	3464	34642
180	1760	2800
173	<u>1732</u>	
70	280	
32.	33.	34.
0.00030479	1.41423	2.23614
5289)0.16093295	14142)20000.	2236)5000.
1584	14142	4472
2532	58580	5280
<u>2112</u>	56568	4472
4209	20120	8080
3696	14142	6708
5135	59780	13720
4752	56568	13416
383	32120	3040
0.000304		2238
	38360	8040

35.	36.	37.
\$ 213.67	11.00543	0.000064
117) \$25000.	1472)16200.	19899 0.01270
234	1472	1188
160	1480	820
117_	1472	792
430	8000	28
351	7360	
790	6400	
702	5888	
880	5120	
819	4416	
61	704	
\$213.68. Ans.		

38.	39.
0.34379	44.21057
16382) 05632.	42369) 187276.0
4 9146	1 6944
71740	17836
65528	16 944
62120	8920
49146	8472
129740	4480
114674	4236
150660	24400
147438	21180
3222	32200
	29652
	2548
	44.21058. An

40.	41.
9.83258	0.00114
19293) 189700.	00872)00001.
173637	872
160630	1280
154344	872
62860	4080
57879	3488
49810	592
38586	
112240	
96465	•
157750	
154344	
3406	0.00115. Ans.
42 .	43 .
7.76378	33.41590
18246) 141658.	\$30377)\$1015075.
127722 139360	91131
	103765
127722	91131
10000	
109476 69040 121508	
54738	48320
143020	30377
127722	179430
152980	151885
145968	275450
7012	273393
	20570
44.	33.4 1591. Ans.
\$12.62	
2473) \$31212.	45.
2473	\$17.70
6482	176) \$3115.20
<u>4946</u> <u>176</u>	
15360	
14838 1232	
5220	
4946	1232
274	<u> </u>

ADVANCED ARITHMETIC.

46 .	49. 311.12396
\$ 5 53.06	31113) 9680000.
5135) \$2840000.	<u>93339</u>
25875	34610
27250	<u>31113</u>
25675	34970
15750	<u>31113</u>
15405	38570
34500	31113
<u>8</u> 0810	74570
3690	62226
\$553.07. Ans.	123440
	93339
	301010
	280017
47 .	209930 186678
854.2	23252
3542) 1254576.4	311.12397. Ans.
10626	011.12001. 21765.
19197	50. 395708. 73 088
17710	64037) 25340000000.
14876	192111
14168	612890
7084	576333
7084	365570
	320185
	453850
	448259
40	559100
48.	512296
0.86605	468040
0866) 0750.	448259
6028	197810
5720	192111
<u>5198</u>	569900
5240	512298
<u>5198</u>	576040
4.44\0	51 2296
4400	
433 <u>0</u> 7 <u>0</u>	395,708.73089. Ans.



51.

0.0000025 2531999 0.0064037 52.

53.

54.

55.	56.	57.
\$17.36	4"2	\$79.92
14: 82:2	903 2-1700	178.2 \$14300.0 0
143	144	12:244
1952	200	177560
1991	273	161028
_ 6 .9	- 80	165320
715	72	161028
(1)	80	42:20
5.35	<u>72</u>	35784
82	80	7136
	72_	
\$17.57. Ana.	80	
	72	
	80	
	72	
	80	
	<u>72</u>	
	8	

58 .	59.	60.	
0.15454	286.96306	35.32532	
121) 18.7	1728) 495872.1765	5289) 18651.7725	
121	3456	1584	
- 660	15027	2811	
605	13824	2640	
550	12032	1717	
484	10368	1584	
UUO	16641	1337	
605	15552	1056	
550	10897	2812	
484	10368	2640	
60	5296	1725	
0.15455. Ans.	5184	1584	
	11250	1410	
	10368	1056	
	882	354	
	286.96307. Ans.	35.32533. Ans.	

\$213.78. Ans.

TEACHERS' EDITION.

61.	62.	63 .
243.66937	17.97170	68.02571
231) 56287.625	43569) 78284.7375	27225) 1852000.
462	4358	163350
1008	34724	218500
924	30492	217800
847	42327	70000
693	39204	54450
1546	31233	155500
1386	30492	136125
1602	7417	193750
1386	4358_	190575
2165	30615	31750
2079	30492	27225
860	1230	4525
693_		
1670		
1617	_	
53	·	
64.	65 .	66.
17.011	17 51.02040	\$213.77
215042) 3658117.	196) 10000.	1025) \$219120.
215042	980	2050
1507697	200	1412
1505294	196	1025
240300	400	3870
215042	392	3075
252580	800	7950
215042	784	7175
375380	160	7750
215042	51.02041.	Ans. 7175
160338	30	575

 $\frac{1505294}{98086}$

67.

68.	69 .	70 .
0.01239	65.58593 2.21	
1331) 0016.5	1152) 75555.	55056) 122000.
1331	6912	110112
3190	6435	118880
2662	5760	110112
5280	6750	87680
3993_	5760	55056
12870	8800	326240
11979	9216	275280
891	6840	509600
	5760	495504
0.01240. Ans.	10800	140960
	10368	110112
	4320	30848
	3456	
	864	2.21593. Ans.
	65.58594. Ans.	

71.		72.	73.
7.14	1842	9.11274	0.03156
107716) 770000.	72426) 66	30000.	1728) 54.55
754012	65	1834	5184
159880	_	81660	2710
107716		72426	1728
521640		92340	9820
430864	_	72426	8640
90776	0	199140	11800
86172	<u>8</u> _	144852	10368
4603	20	542880	1432
4308	<u>64</u>	506982	
294	560	358980	0.03157. Ans
215	432	289704	
	128	69276	
7.14843. Ans	9.11278	5. Ans.	
74.		7 5.	76 .
1.0482	23	0.00196	10.36515
44723) 46880.	444)	0.874	5289) 5472.8
44723		444	528
215700		4300	1928
178892		3996	1584
368080		3040	3440
357784		2664	3168
102960		376	2720
89446	_		2640
13514	0.0019	7. Ans.	800
13416	9		<u>528</u>
97	1		2720
			2640
			80
77 .	78 .	79 .	80 .
1130.	0.0081	1200900	. 0.0016
00018) 20340.	108) 0.8748	00037)44433300	2003) 3:2048
18	864	<u>37</u>	2003
23	108	74	12018
18 54 54	108	74	12018
54		333	·
<u>54</u>		333	-
0		0	U

Exercise 18. Page 44.

Reduce to a single expression:

1.
$$(16-11+2) \times 5 = 7 \times 5 = 35$$
.

2.
$$(4 \times 15) \div (2 \times 3) = 60 \div 6 = 10$$
.

3.
$$(84 \div 7) + (4 + 5 - 6) = 12 + 3 = 15$$
.

4.
$$(44-31) \times (14-11) = 13 \times 3 = 39$$
.

5.
$$(96 \div 6 + 5) - (6 \times 8 \div 16) = 21 - 3 = 18$$
.

6.
$$(52-5\times7)+(4\times5)-16\div2=17+20-8=29$$
.

7.
$$52-5\times7+4\times5-16\div2=52-35+20-8=29$$
.

8.
$$(62 + 3 - 15) \div 10 + (6 \times 7 - 30) \div 3 = 50 \div 10 + 12 \div 3$$

= $5 + 4 = 9$.

Exercise 19. Page 45.

By the use of reciprocals, find the value of:

1.
$$8 \times 0.25 = 8 \div 4 = 2$$
.

2.
$$171 \div 0.25 = 171 \times 4 = 684$$
.

3.
$$876 \times 1.25 = 876 \div 0.8 = 8760 \div 8 = 1095$$
.

4.
$$132 \times 2.5 = 132 \div 0.4 = 1320 \div 4 = 330$$
.

5.
$$591 \div 2.5 = 591 \times 0.4 = 236.4$$
.

6.
$$756 \div 0.125 = 756 \times 8 = 6048$$
.

7.
$$268 \times 25 = 268 \div 0.04 = 26,800 \div 4 = 6700$$
.

8.
$$753 \div 25 = 753 \times 0.04 = 30.12$$
.

9.
$$567 \div 625 = (567 \div 5) \times 0.008 = 113.4 \times 0.008 = 0.9072$$
.

10.
$$1764 \times 0.025 = 1764 \div 40 = 44.1$$
.

11.
$$5381 \div 0.025 = 5381 \times 40 = 215,240$$
.

12.
$$7452 \div 0.875 = 7452 \times 8 \div 7 = 59{,}616 \div 7 = 8516.6.$$

13.
$$651 \times 0.33333 = 651 \div 3 = 217$$
.

14.
$$456 \times 6.66667 = 456 \div 0.15 = 45,600 \div 15 = 3040$$
.

15.
$$1554 \times 0.16667 = 1554 \div 6 = 259$$
.

16.
$$432 \div 1.33333 = 432 \times 0.75 = 324$$
.

17.
$$375 \div 16.66667 = 375 \times 0.06 = 22.5$$
.

18.
$$225 \div 6.66667 = 225 \times 0.15 = 33.75$$
.

Exercise 20. Page 47.

Divide by the contracted method:

1. 11.4285285 by 3.1415927 to six decimal places.

2. 0.004239239 by 3.2783278 to five decimal places.

0.00129
32783278) 42392.39
32783
9609
6557
3052
2950

3. 437 by 215.253 to five decimal places.

4. 0.0053 by 72.654 to eight decimal places.

 $\begin{array}{r}
0.00007294 \\
7284) 5.30000 \\
\underline{508578} \\
21422 \\
\underline{14531} \\
6891 \\
\underline{6539} \\
352 \\
\underline{300}
\end{array}$

5. 6 by 0.1573 to three decimal places.

6. 0.11 by 1937.43 to eight decimal places.

7. 44.2 by 0.768547 to five decimal places.

8. 0.6587465 by 0.5475869 five decimal places.

1.20298

5475869) 6587465.

5475869
1111596
1095174
16422
10952
5470

442 438

4928

9. 46 by 0.00751515151 to thr decimal places.

6120.967

Exercise 21. Page 48.

Express the value of:

2.
$$10^{8} \div 10^{2} = 10^{8-2} = 10$$
.
 $10^{8} \div 10^{5} = 10^{8-5} = 10^{3}$.
 $10^{5} \div 10^{8} = \frac{1}{10^{8-5}} = \frac{1}{10^{3}}$.
 $10^{9} \div 10^{4} = 10^{9-4} = 10^{5}$.
3. $9.99^{4} \div 9.99^{2} = 9.99^{4-2} = 9.99^{2}$.
 $9.99^{108} \div 9.99^{110} = \frac{1}{9.99^{110-108}} = \frac{1}{9.99^{2}}$.
 $9.99^{16} \div 9.99^{18} = \frac{1}{9.99^{18-16}} = \frac{1}{9.99^{2}}$.
4. $1.01^{25} \div 1.01^{22} = 1.01^{25-22} = 1.01^{3}$.
 $1.01^{12} \div 1.01^{15} = \frac{1}{1.01^{15-12}} = \frac{1}{1.01^{8}}$.
 $1.01^{19} \div 1.01^{16} = 1.01^{19-16} = 1.01^{8}$.

Exercise 22. Page 49.

Find the following quotients and test the accuracy of the work by casting out the nines:

1. 73.03522 2. 215042)15705641.692 8.79530 5645376)49652789.6

The remainder after the nines are cast out from the divisor is 5; from the quotient, 4; from the remainder, 8; from the dividend, 1.

 $5 \times 4 + 8 = 28.$ $28 \div 9 = 3 \text{ with remainder 1.}$

The remainder after the nines are cast out from the divisor is 0; from the quotient, 5; from the remainder, 2; from the dividend, 2.

$$0 \times 5 + 2 = 2$$
.

3 .	030.01828
	31416) ZINUNUNUN.
	188496
	115040
	94248
	207920

 $\frac{251328}{11552}$

The remainder after the nines are cast out from the divisor is 6; from the quotient, 4; from the remainder, 5; from the dividend, 2.

$$6\times4+5=29.$$

 $29 \div 9 = 3$ with remainder 2.

$$\begin{array}{r}
 7854 \\
 \hline
 48430 \\
 \hline
 47124 \\
 \hline
 13060
 \end{array}$$

 $49360 \\ 47124 \\ \hline 2236$

The remainder after the nines are cast out from the divisor is 6; from the quotient, 8; from the remainder, 4; from the dividend, 7.

$$6 \times 8 + 4 = 52$$
.

 $52 \div 9 = 5$ with remainder 7.

.

1997.58881

1439874)2876276200.

 $\frac{12958866}{10926940}$

 $\frac{10079118}{8478220}$

 $\frac{7199370}{12788500}$

 $\frac{11518992}{12695080}$

The remainder after the nines are cast out from the divisor is 0; from the quotient, 2; from the remainder, 4; from the dividend, 4.

$$0 \times 2 + 4 = 4$$
.

6 .
1328.74761
658208)874711900.
658298
2164139
1974894
1892450
1316596
5758540
5266384
4921560
4608086
8134740
2633192
5015480
4608086
4073940
3949788
1241520
658298

583222

The remainder after the nines are cast out from the divisor is 2; from the quotient, 3; from the remainder, 4; from the dividend, 1.

$$2\times 3+4=10.$$

 $10 \div 9 = 1$ with remainder 1.

7.

191.94170
149796)28752100.
149796
1377250
1348164
290860
149796
1410640
1348164
624760
599184
255760
149796
1059640
1048572
110680

The remainder after the nines are cast out from the divisor is 0; from the quotient, 5; from the remainder, 7; from the dividend, 7.

$$0 \times 5 + 7 = 7$$
.

Exercise 23. Page 50.

Express in words:

1. 327.244.

Three hundred twenty-seven and two hundred forty-four thousandths.

2. 80.9056.

Eighty and nine thousand fifty-six ten-thousandths.

3. 0.390012.

Three hundred ninety thousand twelve millionths.

4. 20,000.002.

Twenty thousand and two thousandths.

5. 0.0000008.

Eight ten-millionths.

6. 41.27105.

Forty-one and twenty-seven thousand one hundred five hundred-thousandths.

Write in figures:

7. Two hundred thirty-five and eight hundred thirty-five thousandths.

235.835.

- 8. Seventy-four and two hundred three thousand six millionths. 74.203006.
- 9. Twelve hundred and eight thousand three ten-millionths. 1200.0008003.
- 10. Five thousand sixty-four millionths.

0.005064.

11. One million and four tenths.

1,000,000.4.

12. Six hundred-millionths.

0.00000008.

- 13. Multiply and divide 789.365 by 10; by 100; by 100,000. 7893.65; 78.9365; 78,936.5; 7.89365; 78,936,500; 0.00789365.
- 14. Multiply and divide 0.004 by 100; by 10,000; by 1000.
- 0.4; 0.00004; 40; 0.0000004; 4; 0.000004.
- 15. Multiply and divide 436 by 1,000,000; by 1000; by 10. 436,000,000; 0.000436; 436,000; 0.436; 4360; 43.6.
- 16. Multiply and divide 0.1 by ten; by ten millions. 1; 0.01; 1,000,000; 0.00000001.

Find the value of:

17. 21.3706 + 15.243 + 1.8954 + 0.026891 + 5.328 + 29.74.

21.3706

15.243

1.8954

0.026891

5.328

29.74

73.603891

19. 0.0012 + 10 + 5.8281 + 5 + 39.43 + 0.6827 + 1.

0.0012

1426.8527

10.

5.8281

5.

39.43

0.6827

 $\frac{1.}{61.942}$

20. 23.9875 - 12.4764; 35.14732 - 27.62815.

 $\begin{array}{ccc} 23.9875 & 35.14732 \\ 12.4764 & 27.62815 \\ \hline 11.5111 & 7.51917 \end{array}$

21. 102.1274 - 83.072; 39.801 - 17.9645.

 102.1274
 39.801

 83.072
 17.9645

 19.0554
 21.8365

22. 30 - 5.2817; 1.7 - 0.8469.

 $\begin{array}{ccc} 30. & & 1.7 \\ \underline{5.2817} & & \underline{0.8469} \\ \underline{24.7183} & & 0.8531 \end{array}$

23. 1 - 0.54237; 100 - 0.00176.

 $\begin{array}{ccc}
1. & 100. \\
\underline{0.54237} & \underline{0.00176} \\
\underline{0.45763} & 99.99824
\end{array}$

24. 24.271 - 3.6485 + 15.271 - 13.256 - 14.125.

25. 52 + 0.52 - 17.8946 - 30.254 - 0.5 + 21.12.

26. 41.289×0.5 ; 0.268×0.9 ; 0.112×0.2 .

27. 2.435×4.23 ; 71.651×3.37 ; 0.251×0.04 .

28. 0.0012×0.005 ; 2.26823×200 ; 5.6125×0.0768 .

29. $0.7 \times 7 \times 0.07$; $0.15625 \times 23.7 \times 0.00192 \times 5$.

0.7 0.15625 3.703125 23.7 0.00192 109375 4.9 7406250 46875 33328125 0.07 3703125 0.343 31250 3.703125 0.00711 5 0.03555

30.
$$(2.465 + 1.21) \times (3.2 - 2.89)$$
.
 $(2.465 + 1.21) \times (3.2 - 2.89)$
 $= 3.675 \times 0.31$
 $= 1.13925$.

31. $(3.01)^2$; $(0.045)^2$; $(0.0081)^2$; $(5.1004)^8$; $(0.76)^8$.

3.01 0.045 0.0081 3.01 0.0450.0081 301 225 81 903 180 648 9.0601 0.00006561 0.002025 5.1004 0.76 5.1004 0.76 456 204016 51004 **532** 0.5776 255020 26.01408016 0.76 34656 5.1004 10405632064 40432 2601408016 0.438976 13007040080 132.682214448064

32. $(0.125)^2 \times (0.32)^8$.

0.125 0.32 0.032768 0.125 0.320.015625 625 64 163840 250 65536 96 0.1024 125 196608 0.015625 0.32 163840 2048 32768 3072 0.000512 0.032768

33. Divide 291.84 by 6; 0.12936 by 12; 7.92801 by 0.9.

34. Divide 58.383 by 0.39; 0.28744 by 0.08; 491.205 by 0.065.

149.7		7557
39) 5838.3	8) 28.7 44	65) 491205
39	3.593	455
$\overline{193}$		362
156		325
378		370
351		325
273		455
273		<u>455</u>

35. Divide 68.325 by 6.25; 0.732 by 1.6; 1208.88 by 0.438.

10.932	0.4575	2760
625) 6832.5	16) 7.32	438) 1208880
625	64	876
5825	92	3328
5625	80	3066
2000	$\overline{120}$	2628
1875	112	2628
1250	80	0
1250	<u>80</u>	

36. Divide 498 by 0.0125; 7 by 0.007; 1000 by 0.0001.

The reciprocal of 0.0125 is 80.

37. Divide 0.235 by 10.24; 27 by 12; 0.00507702 by 0.0283.

0.02294				0.1794
1024) 23.5			<u>12) 27.</u>	283) 50.7702
2048			2.25	283
3020				2247
2048	0.02295.	Ans.		1981
9720				2660
9216				2547
5040				1132
4096				1132
944				

38. Divide 89.3 by 0.00752; 74.1 by 0.0256; 1 by 0.128.

11875	2894.53125	7.8125
752 8930000	256) 741000.	128) 1000.
752	512_	896
1410	2290	1040
752	2048	1024
6580	2420	160
6016	2304	128
5640	1160	320
5264	1024	256
3760	1360	640
3760	1280_	. 640
	800	
	768	
	320	
	256 _	
	640	
	512	
	1280	
	1280	

39. Divide 0.39842 by 3.7164; 281.5 by 13.789; 0.0005 by 0.0028.

0.10720	20.41482	0.17857
37164) 3984.2	13789) 281500.	28) 5.
37164	27578	28_
267800	57200	220
26 0148	55156	196
76520	20440	240
74328	13789	224
21920	66510	160
0.10721.	Ans. 55158	140_
	113540	200
	110312	196
	32280	4
	<u>27578</u>	
	4702	

40. Divide 63.04128 by 912.85; 287.209 by 0.00493; 2000 by 0.0059.

0.06905	58257.40365	338983.05084
91285) 6304.128	493) 28720900.	59) 20000000.
547710	246 5	177
827028	4070	230
821565	3944	177
546300	1269	530
456425	986	472
89875	2830	580
0.06906. Ans.	2465	531 _
	3650	490
	3451	472
	1990	180
	1972	<u>177</u>
	1800	300
	1479	295
	3210	500
	2958	472
	2520	280
	2465	236
	55	338,983.05085. Ans. 44

Exercise 24. Page 51.

1.667

Find the value of:

1. 1.4 + 2.08 + 3.895.

6.
$$6.913 - (2.85 - 0.937)$$

= $6.913 - 1.913$
= $5.$

7.
$$24 - 2.4 + (5 - 3.508) - 3.092$$

= $24 - 2.4 + 1.492 - 3.092$
= $25.492 - 5.492$
= $20.$

8.
$$10 - (4.25 - 2.5 + 2 - 0.625 - 0.4 - 2.02) - 0.295$$

= $10 - (6.25 - 5.545) - 0.295$
= $10 - 0.705 - 0.295$
= $10 - 1$
= 9 .

9.
$$1.5 \times 0.08 \times 0.5$$
.

$$\begin{array}{r}
1.5 \\
0.08 \\
\hline
0.12 \\
0.5 \\
\hline
0.06
\end{array}$$

11. $0.04 \times 3.25 \times 0.06$.

$$\begin{array}{r}
3.25 \\
0.04 \\
\hline
0.13 \\
0.06 \\
\hline
0.0078
\end{array}$$

10.
$$0.1204 \times 0.0168 \times 100$$
.

$$0.1204 \\ \underline{0.0168} \\ 9632 \\ 7224 \\ \underline{1204} \\ 0.00202272 \\ \underline{100} \\ 0.202272$$

12.
$$36 \times 0.002 \times 2.05 \times 0.00765$$
.

$$\begin{array}{ccc} 36 & 0.1476 \\ \underline{0.002} & \underline{0.00765} \\ \underline{0.072} & 7380 \\ \underline{2.05} & 8856 \\ \underline{360} & \underline{10332} \\ \underline{144} & 0.1476 \\ \end{array}$$

13.
$$0.139 \times 28 + 42 \times 0.002 + 6 \times 0.004 - 0.05 \times 20$$

= $3.892 + 0.084 + 0.024 - 1$
= $4 - 1$
= 3.

14.
$$(10-1.25) \times 0.2 + 0.02 \times 2.8 + (80.3 \times 0.1 - 5.3) \times 10 - 805.3 \times 0.02$$

= $8.75 \times 0.2 + 0.02 \times 2.8 + (8.03 - 5.3) \times 10 - 805.3 \times 0.02$
= $1.75 + 0.056 + 27.3 - 16.106$
= $29.106 - 16.106$
= $18.$

19. $0.28744 \div 800$.

8) 0.0028744 0.0003593

34	ADVANCEI	ARITHMETIC.
15.	. 28.8696 ÷ 1.49.	20 . 491 . 205 ÷ 650.
	19.04	0.7557
	149) 2836.96	65) 49.1205
	149	455
	1346	362
	1341	325
	596	370
	<u>598</u>	325
		455
		455
16.	$0.27 \div 0.00225.$	21. $68.325 \div 6250$.
	120	0.010932
	225) 27000	625) 6.8325
	225 _	625
	450	5825
	<u>450</u>	<u>5625</u>
	0	2000
		<u>1875</u>
		1250
17.	$8.8779 \div 175.8.$	<u>1250</u>
	0.0505	22. $0.732 \div 16,000$.
	1758) 88.779	0.00004575
	8790	16) 0.000732
	8790	64
	<u>8790</u>	92
		80
		120
18.	$0.0427 \div 92.3.$	112
	0.00046	80
	923) 0.427	<u>80</u>
	3692	23. $1208.88 \div 0.438$.
	5780	2760
	5538	438) 1208880
	242	876
		8328
		0044

24.
$$2 \div 0.01 - (0.2 \div 0.02 + 0.8 \div 10) + 36.48 \div 8 - (4 \div 0.05 - 2 + 0.6 \div 1.25)$$

= $200 - (10 + 0.08) + 4.56 - (80 - 2 + 0.48)$
= $200 - 10.08 + 4.56 - 78.48$
= $204.56 - 88.56$
= 116.

25.
$$72.2 \div 10 - 2 \div (0.5 \div 1.60) + 2.125 \div (1.75 - 0.5)$$

= $72.2 \div 10 - 2 \div 0.3125 + 2.125 \div 1.25$
= $7.22 - 6.4 + 1.7$
= $8.92 - 6.4$
= 2.52 .

Exercise 25. Page 52.

1. What number subtracted 88 times from 80,005 will leave 13 as a remainder?

	909
80005 .	88) 79992
13	792
79992	792
	792

2. If 7 men can build a wall in 16 days, how many men will it take to build a wall three times as long in half the time?

3. How many minutes are there between 25 minutes past 8 in the morning and midnight?

4. If the velocity of sound is 1090 feet per second, at what distance is a gun fired, the report of which I hear 11 seconds after seeing the flash? (5280 feet make a mile.)

	2.27083	
1090	5280) 11990.	
11	10560	
1090	14300	
1090	10560 2.270	83 miles.
11990	37400	Ans.
	36960	
	44000	
	42240	
	17600	
	15840	

5. How long will it take to travel 30.2375 miles at the rate of 8.85 miles per hour?

6. If the circumference of a circle is 3.1416 times the diameter, find the circumference of a circle whose diameter is 6.8 feet; also, find the diameter of a circle whose circumference is 20 inches.

	6.366		
3.1416	31416) 200000.		
6.8	188496		
251328	115040		
188496	94248		
21.36288	207920	6.366 inches.	Ans.
21.363 feet. Ans.	188496		
	194240		
	188496		

7. How much wire will be required to make a hoop 30 inches in diameter, allowing 2 inches for the joining?

96.248 inches. Ans.

8. How many times would the hoop of Ex. 7 turn in going half a mile?

	336.
2) 5280	94248) 31680000.
2640	282744
2640	340560
12	282744
5280	578160
2640	<u>565488</u>
31680	

9. Cork, whose weight is 0.24 of the weight of water, weighs 15 pounds per cubic foot. What is the weight of 6 cubic feet of oak, if the weight of oak is 0.934 of the weight of water?

62.5			
24) 1500.	62.5		
144	0.934		
60	2500		
48	1875		
120	5625		
120	58.375		
	·		
	350.25	350.25 pounds.	Ans.

10. From what number can 847 be subtracted 307 times, and leave a remainder of 49?

11. What is the 235th part of 141,235?

601

12. What will 343 barrels of flour cost at \$6.37 a barrel?

\$ 6.37	
343	
1911	
2548	
1911	
\$2184.91	

13. Twelve makes a dozen, and 12 dozen makes a gross. How many steel pens in 28 gross? What will a gross of eggs cost at 27 cents a dozen?

14. How much must be added to \$4429 to make the sum equal to $43 \times 241 ?

\$ 241
43
723
964
\$10363
4429
\$5934

15. What number deducted from the 26th part of 2262 will leave the 87th part of the same number?

87	26	
26) 2262	87) 2262	87
208	174	26
182	522	61
182	522	

16. At the ordinary rate, 123 words a minute, how long will it take a man to deliver a speech of 15 pages, each of 28 lines, each line containing 11 words? How long would it have taken Daniel Webster to deliver the same speech, whose rate was 93 words a minute?

	37.5	49.6
15	123) 4620.	93) 4620.
2 8	3 69	372
120	930	900
30	861	837
30 420	690	630
11	615	558
420	75	72
420		
4620	37.6 minutes	: 49.7 minutes. Ar

37.6 minutes; 49.7 minutes. Ans.

17. How long will it take a railway train to go from New York to San Francisco, 3310 miles, at the rate of 1973 feet a minute?

	8858
3310	1973) 17476800
5280	15784
264800	16928
6620	15784
16550	11440
17476800	9865
	15750

8858 minutes = 147 hours Ans.

18. How many hours will it take to count a million, at the rate of 67 a minute?

19. If you put into a box 17 cents a day, including Sundays, beginning January 1 and ending July 4, how much money will there be in the box?

20. If a man's income is \$3000 a year, and his daily expenses average \$7.68, what does he save in a year?

\$ 7.68	\$3000 .
365	2803.2 0
3840	\$196.80
4608	
2304	
\$ 2803.20	

21. In a question of division the quotient was 87.83, the divisor, 759. What was the dividend?

22. What is the nearest number to 7196 that will contain 372 without a remainder?

19	
372) 7196	7196
<u>372</u>	128
3476	7068
3348	
. 128	

23. It is 3.1416 times as far round a wheel as across it. How many times will a wheel 4.5 feet across turn in going 23 miles of 5280 feet each?

		8590	Ans
3.1416	5280	141372) 1214400000	
4.5	23	1130976	
157080	15840	834240	
125664	10560	706860	
14.1372	121440	1273800	
		12723 4 8	
		14520	

24. How many gallons of 231 cubic inches are contained in a cubic foot of 1728 cubic inches? in a bushel of 2150.42 cubic inches? How many cubic feet in a bushel? How many bushels in 31.5 gallons?

7.48		9.309
231) 1728.		231) 2150.42
1617		2079
1110		714
924		693
1860		2120
<u>1848</u>		2079
1.244		3.38
1728) 2150.42	31.5	215042) 727650.
1728	231	645126
4224	315	825240
34 56	945	645126
7682	630	1801140
6912	7276.5	1720336
7700		
<u>6912</u>		

25. Seven children had left to them \$7186 apiece; one died, and his share was divided among the surviving six. How much had each then?

26. How long will it take 2 men to do what 1 man can do in 6 days? what 4 men can do in 3 days? what 3 men can do in 4 days?

6 days
$$\div 2 = 3$$
 days.
2 \times 3 days = 6 days.
(3 \times 4 days) \div 2 = 6 days.

27. Divide \$1.80 among Thomas, Richard, and Henry in such a way that Henry shall receive 3 cents for every 5 cents that Thomas gets, and Richard shall receive 2 cents for every 3 cents that Henry gets.

2	10) \$1.80
3	\$0.18
_5	2
10	\$0.36, R.'s.
\$0.18	\$ 0.18
3	5
\$0.54, H.'s.	\$0.90, T.'s.

28. Divide \$87.84 between B and C so that C shall get \$19 as often as B gets \$17.

29. Three partners received for goods: one, \$371.63; the second, \$285.40; the third, \$411.91. They paid for the goods \$879.34, and divided the profit equally among them. How much did each receive?

30. If there are 12 inches in a foot, how many inches long is a wall 35 feet in length? If a brick and its share of mortar is 8.4 inches long, how many bricks in length is the wall?

$$\begin{array}{ccc}
35 & 50 \\
\underline{12} & 84 \overline{\smash)4200} \\
70 & \underline{420} \\
\underline{35} & 0
\end{array}$$

31. If a brick and its mortar is 2.4 inches high, how many bricks are required to build a wall 12 feet high, 35 feet long, if the width of the wall is the width of two bricks?

32. What is the total weight of the wall of Ex. 31, if a brick with its share of the mortar weighs 4.13 pounds? What is the weight after a long rain, when the weight is increased to 4.27 pounds for each brick?

$$\begin{array}{ccc}
4.13 & 4.27 \\
\underline{6000} & \underline{6000} \\
24780 & 25620
\end{array}$$

24,780 pounds; 25,620 pounds. Ans.

33. How many pounds does each foot in length of the wall of

Ex. 31 weigh?

34. If 60.98 cubic inches of brick weigh 4 pounds, how many cubic inches of brick weigh 1 pound? How many pounds will a cubic foot (1728 cubic inches) weigh?

4)60.98

113.34

15245) 1728000.

113.35 pounds. Ans.

35. If a cubic foot of water weighs 62.5 pounds, how many times as heavy as water is brick?

36. Light moves through the air at the rate of 186,500 miles a How many times can it go around the earth in a second, if the distance round the earth is 24,897.714 miles?

> 7.4 24897714) 186500000. 174283998 122160020 99590856 22569164 7.5. Ans.

37. Light moves through the air at the rate of 300,190 kilometers a second. How many times can it go around the earth in a second, if the distance round the earth is 40,007.5 kilometers?

> 7.5 400075) 3001900. 2800525 2013750 2000375

38. A minute is 60 seconds. How many miles and how many kilometers can light travel through air in a minute?

> 186500 11190000 300190 60 18011400 11,190,000 miles; 18,011,400 kilometers. Ans.

39. An hour is 60 minutes. How many miles and how many kilometers can light travel in an hour?

671,400,000 miles; 1,080,684,000 kilometers. Ans.

431.034
232) 100000.
928
720
696
240
232
800
698
1040
928
112

40. The distance round the earth, given in Ex. 37, is measured on a north and south line. Around the equator the distance is 40,075.45 kilometers. How many times could light move round the equator in one minute?

7.49
4007545) 30019000.
28052815
19661850
16030180
36316700
36067905
7.49
60
449.4

41. Find the reciprocal of the difference between 31.24 and 31.23768.

 $31.24 \\ \underline{31.23768} \\ 0.00232$

42. The Hanoverian mile is 25,400 Hanoverian feet long, and each foot is 0.9542 of an English foot. Find to four places of decimals the fraction that an English mile of 5280 English feet is of a Hanoverian mile.

43. Express in inches the length of a meter, given that a meter is one ten-millionth of a quarter of the earth's circumference, that the circumference is 3.14159 times the diameter, that the diameter of the earth is 7911.7 miles, and that a mile is 5280×12 inches.

39.3708 inches. Ass.

44. How must a number be altered that its reciprocal may be doubled?

Divided by 2.

45. What effect is produced on the sum of two numbers, if the same number is added to each of them? What effect on the difference?

It is increased by twice the number; no effect.

46. What effect is produced on the product of two numbers, if both numbers are multiplied by the same number? What effect on the quotient?

It is multiplied by the square of the number; no effect.

4820

47. What effect is produced on the remainder, if both divisor and dividend are multiplied by the same number? If both are divided by the same number?

It is multiplied by the number; it is divided by the number.

48. In going from one planet to another, light probably moves faster than in air. Suppose it moves at the rate of 309,800 kilometers a second, how many seconds would it take light to perform each of the following journeys:

Moon to Earth			•		375,	500 1	rilometers.
Sun to Earth .			•	•	. 147,250,	000	66
Sun to Mercury			•	•	. 56,900,	000	4.6
Sun to Venus .			•	•	. 106,400,	000	66
Sun to Mars .					. 224,100,		66
Sun to the Aster	oids		•		. 400,000,	000	6.6
Sun to Jupiter.					. 765,400,	000	66
Sun to Saturn.			•		1,403,000,	000	66
Sun to Uranus.			•		2,817,000,	000	66
Sun to Neptune			•		4,421,000,	000	66
Sun to the neares			24	,00	00,000,000,	000	66
1.21			475	.3			183.7
309800) 3755.	3098ø	g) 147	2500	<u> </u>		3098	3 99) 569000.
3098	,	123					3098
6570	23330						$\overline{25920}$
6196	21686						24784
3740	16440						11360
3098	15490						9294
		-	950	0			20660
			929				
343.4		7	723.4	ŀ		1	1291.2
309899 1084000.0	09899) 2241000.			3098\$\$\)\(\begin{align*} \begin{align*} align			
9294	21686			3098			
13460	7240			9020			
12392	6196			6196			
10680	10440				28240		
9294	_9294_				27882		
13860		1	1460)			3580
12392						3	3098_

2470.6	4528.7	9092.9
3)0800 7654000	अंग न्यम (कार्यकार)	309899) 28170000.
61:45	19:102	27882
14580	1-3(80)	28800
1232	154(4)	27 882
21550	OUNS	9180
21686	6196	6196
19400	27040	29840
<u>18588</u>	24784	27882
	22560	
	21686	
14270.5	77469335	
309890 44210000.	309800) 2400000000000	
3098	21686	
13230	23140	
12392	21686	
8380	14540	10380
6196	12392	9294
21840	21480	10860
21686	<u>18588</u>	9294
15400	28920	15660
	27882	15490

49. A kilometer is about 0.6214 of a mile. How many miles is each of the planets from the sun?

14725	5690	10640
6214	6214	6214
58900	22760	42560
14725	5690	10640
29450	11380	21280
88350	34140	63840
Earth, 91501150	Mercury, 35357660	Venus, 66116960
22410		76540
6214		6214
89640		306160
22410		7654 0
44820	6214	153080
134460	40000	459240
Mars, 139255740	Asteroids, 248560000	Jupiter, 475619560

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140300	281700	442100
6214	6214	6214
561200	1126800	1768400
140300	281700	442100
280600	563400	884200
841800	1690200	2652600
Saturn, 871824200	Uranus, 1750483800	Neptune, 2747209400

50. If 11.75 tons of coal cost \$82.25, what will 21.4 tons cost?

51. Find the number of hours it will take a locomotive running at the rate of 27 miles an hour to make the distance passed over in 13.25 hours by another locomotive that has a velocity of 43.5 miles an hour.

$$\begin{array}{c}
13.25 \\
\underline{43.5} \\
6625 \\
3975 \\
\underline{5300} \\
576.375
\end{array}$$

$$\begin{array}{c}
54 \\
36 \\
\underline{27} \\
93 \\
\underline{81} \\
127 \\
\underline{108} \\
195 \\
\underline{189} \\
60 \\
\underline{54} \\
6
\end{array}$$

Exercise 26. Page 60.

- 1. Change 5427^m to kilometers; to millimeters; to centimeters. $5427^m = 5.427^{km} = 5,427,000^{mm} = 542,700^{cm}$.
- 2. How many meters in 6853mm? how many centimeters? what part of a kilometer?

$$6853^{mm} = 6.853^{m} = 685.3^{m} = 0.006853^{m}$$

3. Write 49.7^m as centimeters; as millimeters; as the decimal of a kilometer.

$$49.7^{\rm m} = 4970^{\rm cm} = 49,700^{\rm mm} = 0.0497^{\rm km}$$
.

- 4. How many centimeters in 12.4^{km} ? how many millimeters? $12.4^{km} = 1,240,000^{cm} = 12,400,000^{mm}$.
- 5. Change 1230^{m} to kilometers; to centimeters. $1230^{m} = 1.23^{km} = 123,000^{cm}.$
- 6. Write 1230^{cm} as meters; as millimeters. $1230^{cm} = 12.3^{m} = 12.300^{mm}$.
- 7. Find in meters the value of $0.435^{m} + 852^{cm} + 4263^{mm} + 0.1595^{km}$.

8. Find in meters the value of 0.927km — 6495cm; 4.37cm — 42.87mm.

$$\begin{array}{ccc} 927.^{m} & 0.0437^{m} \\ \underline{64.95} & 0.04287 \\ \underline{862.05^{m}} & 0.00083^{m} \end{array}$$

9. Find in meters the value of 8×0.0457^{km} ; 3.04×60.93^{cm} ; 5.43×67.2^{mm} .

$$\begin{array}{c|ccccc} & & & & & & & & & & & \\ & 0.6093^m & & & & & & & \\ & & & & & & & & & \\ \hline & 3.04 & & & & & & \\ \hline 45.7^m & & 24372 & & 2688 \\ \hline & 8 & & 18279 & & 3360 \\ \hline & & & & 1.852272^m & 0.364896^m \\ \hline \end{array}$$

10. Find in meters the value of $38,019^{mm} \div 0.097$; $0.41^{km} \div 25.625$.

11. At \$1.87 a meter, what is the cost of 6.20^m of cloth?

12. At \$0.75 a meter, what is the cost of 60^m of cloth?

13. From a piece of cloth containing 47.60^m a tailor cuts off three pieces: the first of 3.80^m, the second of 1.30^m, and the third of 45^{cm}. How many meters of the cloth are left?

14. What is the value of 60cm of cloth at \$5.20 a meter?

15. If \$6.00 is paid for a rail-road ticket to travel 440km, what is the fare per kilometer?

16. If a train goes 288km in 9 hours, how many meters does it go in a minute? (1 hour = 60 minutes.)

60	533.33m
8	54) 28800.m
540	270
	180
	162
	180
	162
	180
	162
	180
	<u>162</u>

17. If a man walks at the rate of 6^{km} an hour, what part of an hour will it take him to walk 420^m?

$$6^{\text{km}} = 6000^{\text{m}}$$
 0.07
 $6000) 420.00$
 42000

18. A railroad carried 412 passengers 18km for \$88.992; at the same rate, what will it receive for carrying 350 passengers 35km?

412	\$0.012
<u>18</u>	7416) \$88.992
3296	7416
412	14832
7416	14832
350	12250
35	0.012
1750	24500
1050	1225
12250	147.000 \$147. Ans.

Exercise 27. Page 62.

1. Change 1,854,276qm to hektars; to square kilometers.

$$1,854,276q^{m} = 185.4276h^{a}$$

= $1.854276q^{km}$.

2. How many hektars in 2.78569km?

$$2.7856$$
qkm = 278.56 ha.

3. Write 1.7431qm as square centimeters; as square millimeters.

$$1.7431qm = 17,431qcm$$

= 1,743,100qmm.

4. How many square kilometers in 17,467.5ha?

17,467.5ha = 174.675qkm.

5. How many square meters in 1.3614qkm?

 $1.3614q^{km} = 1,361,400q^{m}$.

6. How many square meters in 2.25ha?

$$2.25^{ha} = 22,500^{qm}$$
.

7. How many square centimeters in 0.01379m?

$$0.0137qm = 137qcm$$
.

8. Write 3.571qcm as square millimeters.

$$3.571qcm = 357.1qmm$$
.

9. If a field contains 7500°, how many ars does it contain? What part of a hektar?

$$7500^{\text{ca}} = 75^{\text{a}} = 0.75^{\text{hs}}$$
.

10. How many square meters must be added to 22,612qm to make 4ha 62a 17ca?

$$4 \text{ ha } 62 \text{ a } 17 \text{ ca} = 46,217 \text{ ca} = 46,217 \text{ cm}$$

11. A field containing 72.4° is sold at 15 cents a square meter. What is received for the field?

$$72.4^{\circ} = 7240^{\circ}$$

12. If 62° 12° of land is sold for \$1366.64, what is the price per square meter?

$$62^a 12^{ca} = 6212^{qm}$$

13. How many square centimeters must be taken from 12,473qcm to leave 1qm 14qdm 53qcm?

$$1qm 14qdm 53qcm = 11,453qcm$$

12473qcm 11453 1020qcm Ans.

Exercise 28. Page 64.

1. Write 2.25cbm as cubic centimeters.

 $2.25^{\text{cbm}} = 2.250,000^{\text{ccm}}$. Ans.

2. Change 2,162,875^{cm} to cubic meters.

2,162,875 ccm = 2.162875 cbm. Ans.

3. Change 0.0175cbm to cubic millimeters.

 $0.0175^{\text{cbm}} = 17,500,000^{\text{cmm}}$. Ans.

4. Change 46,164ccm to cubic decimeters.

46.164ccm = 46.164cdm. Ans.

5. What is the equivalent of 0.875dkst in cubic meters? in cubic centimeters?

$$0.875$$
dkst = 8.75 nt = 8.75 ebm
= $8.750,000$ ecm.

6. How many sters are there in 14.75dkst of wood? how many decisters?

$$14.75$$
dkst = 147.5 st = 1475 dst.

7. What is the cost of 28.25dkst of wood at \$1.25 a ster?

8. Find the cost of an oak beam containing 1250cdm at \$25 a cubic meter.

$$1250^{\text{cdm}} = 1.25^{\text{cbm}}$$
.

 1.25
 $\frac{25}{625}$
 $\frac{250}{31.25}$
\$31.25. Ans.

9.

How many cubic centimeters must be added to 1,262,376ccm to make 2cbm 2cdm 2ccm?

$$2^{\text{cbm}} \ 2^{\text{cdm}} \ 2^{\text{ccm}} = 2,002,002^{\text{ccm}}.$$

$$2,002,002^{\text{ccm}}$$

$$\frac{1,262,376}{739,626^{\text{ccm}}} \ Ans.$$

10. How many cubic millimeters must be taken from 22,350,000,000cmm to leave 20cbm 22cdm 222ccm?

 $\begin{array}{c} \textbf{20ebm 22ecm} \\ &= 20,022,222,000\text{cmm}. \\ \textbf{22,350,000,000\text{cmm}} \\ \underline{\textbf{20,022,222,000}} \\ \hline \textbf{2,327,778,000\text{cmm}} \quad \textbf{\textit{Ans.}} \end{array}$

Exercise 29. Page 65.

1. How many liters in 1.7cbm? in 157,854ccm?

$$1.7^{\text{ebm}} = 1700^{1}$$

 $157,854^{\text{ccm}} = 157.854^{1}$.

2. How many cubic centimeters in 9.5¹? in 0.015¹?

$$9.5^{1} = 9500^{\text{cem}}$$
.
 $0.015^{1} = 15^{\text{cem}}$.

3. Change 1.25^{hl} to cubic centimeters; to the fraction of a cubic meter.

$$1.25^{\text{hl}} = 125^{\text{l}} = 125,000^{\text{ccm}}$$

= 0.125^{cbm} .

4. Change 431.881 to hektoliters; to the fraction of a cubic meter.

$$431.88^{l} = 4.3188^{hl}$$

= 0.43188cbm.

5. Write 0.375cbm as liters; as cubic centimeters.

$$0.375^{\text{cbm}} = 375^{\text{l}}$$

= $375,000^{\text{ccm}}$,

6. Write 734,159.651ccm as liters; as hektoliters; as cubic meters.

734,159.651ccm

 $=734.159651^{1}$

= 7.34159651hl

= 0.734159651cbm.

7. How many cubic meters in 8,573,412.867 ?

8,573,412.867ccm

= 8.573412867cbm.

8. Change 0.734578912cbm to cubic centimeters; to liters.
0.734578912cbm

=734,578.912ccm

 $=734.578912^{1}$.

9. Change 1731.51 to cubic meters; to cubic centimeters.

$$1731.5^{1} = 1.7315^{\text{ebm}}$$

= 1,731,500 ccm.

Exercise 30. Page 66.

1. How many kilos in 1.73t? in 0.341 of a ton?

 $1.73^{t} = 1730^{kg}$.

0.341t = 341kg.

2. How many kilos will a hektoliter of water weigh?

100kg. Ans.

3. Change 13,756^{mg} to grams; to the fraction of a kilo.

13,756mg = 13.756g = 0.013756kg.

4. What is the weight in grams of 346.1cm of water?

346.1s. Ans.

5. Find the weight in kilograms of 0.37615cbm of water.

376.15kg. Ans.

6. Change 0.6778kg to milligrams.

0.6778 kg = 677,800 mg.

7. How many milligrams in the third part of 17.48?

 $\frac{1}{5}$ of 17.4s = 5.8s = 5800mg. Ans.

Exercise 31. Page 67.

1. Add 17.3^m, 87.41^m, 271^{cm}, 380^{mm}, and 1.79^m.

17.3m 87.41 2.71 0.38 1.79 109.59m 2. Add 15.87m, 394.6dm, 47.52m, 7538cm, and 75.89m.

15.87^m
39.46
47.52
75.38
75.89
254.12^m

3. Add 187cm, 49.3m, 317mm, and 6.138m.

1.87^m
49.3
0.317
6.138
57.625^m

4. In a room the doorsill is 3cm high; the door, 2.34m; the finish over the door, 13.7cm; and the distance from the finish to the ceiling is 93cm. What is the height of the room?

0.03^m
2.34
0.137
0.93
3.437^m

5. The distance to the post-office is 3.31^{km} ; thence to the mill, 1.711^{km} ; thence to the store, 3.718^{km} ; thence home, 2.543^{km} . How long is the circuit?

3.31km 1.711 3.718 2.543 11.282km 6. The distance from Portland, Me., to Boston is 174km; Boston to Albany, 317km; Albany to Buffalo, 478km; Buffalo to Chicago, 863km; Chicago to Omaha, 789km; Omaha to Cheyenne, 830km. How far is it from Cheyenne to Portland? from Cheyenne to Albany? from Boston to Chicago? from Boston to Cheyenne?

(1) (2)

830km

789

863

478

317

174

3451km

(3) (4)
317km 317km
478 478
863 863
1658km 789
830
3277km

7. If I travel 789.7km a day, how far shall I go in 7 days? in 8.5? in 19.6? in 27.8? in 365?

		15478.12km	21953.68km	288240.5km
	6712.45km	7897	15794	23691
	63176	71073	55279	47382
5527.9km	39485	47382	63176	39485
7	8.5	19.6	27.8	<u> 365</u>
789.7km	789.7km	789.7km	789.7km	789.7km

8. How much will 3^m of cloth cost at \$1.37 a meter? How much will 5.38^m cost at \$2.63 a meter?

\$ 1.37	\$ 2.63
3	5.38
\$4.11 Ans.	2104
	789
	1315
	\$14.1494
	\$14.15. Ans.

9. How much will 13.4kg of opium be worth at \$8.48 a kilo? 28.79kg, at \$7.96 a kilo?

\$8.48	28.79		
13.4	7.96		
3392	17274		
2544	25911		
848	20153		
\$113.632	229,1684		
\$113.63. Ans.	\$ 229.17.	Ans.	

10. If one barrel of flour weighs 88.9kg, how many barrels can be filled from 444.5t of flour?

11. How many steps 80cm long will a man take in walking a kilometer?

$$1^{\text{km}} = 100,000^{\text{cm}}.$$

$$89) 100009$$

$$1250 Ans$$

12. At 16 cents a liter, what is the cost of 52.4^{hl} of olive oil?

52.4^{hl} = 5240^l.

13. What is the cost of 6dkst 4st of oak wood at \$1.75 per ster?

6dkst 4st = 64st.

14. If a pasture contains 22,408ca, how many ars does it contain? how many hektars?

$$22,408^{ca} = 224.08^{a}$$

= 2.2408^{ha} .

15. Find the circumference of a circle 1^m in diameter.

3.1416m. Ans.

16. Find to the nearest tenth of a millimeter the circumferences of circles whose diameters are, respectively, 83^m; 3.71^m; 32.8^m; 10.4^{cm}; 11.8^{cm}; 167.1^{mm}; 39.3^{mm}.

3.1416		3.1416	3.1416	
83000		3710	32800	
94248000		314160	$\overline{25132800}$	
251328		219912	62832	
260752.8		94248	94248	
260,752.8mm.	Ans.	$\overline{11655.3360}$	103044.4800	
200,:02.0		11,655.3mm. Ans.	103,044.5mm.	Ans.

3.1416	3.1416
104	118
125664	251328
31416	31416
326.7264	31416
326.7mm. Ans.	370.7088
	370.7mm. Ans.

 3.1416
 3.1416

 167.1
 39.3

 31416
 94248

 219912
 282744

 188496
 94248

 31416
 123.46488

 524.96136
 123.5mm. Ans.

 525mm. Ans.

17. What is the length of the earth's orbit, to the nearest meter, if the diameter of the orbit is 294,481,217km?

294481217km 3.1416 1766887302 294481217 1177924868 294481217 883443651 925,142,191.3272km 925,142,191,327m. Ans.

18. What is the circumference of a carriage wheel 1.31^m in diameter? How far will it go in turning once? 17 times?

(1) (2)
3.1416 4.115
m
. Ans.

 $\frac{1.31}{31416}$ (3)
94248 4.115 m
 $\frac{31416}{4.115496}$ $\frac{17}{28805}$
4.115 m . Ans. $\frac{4115}{69.955}$ Ans.

19. How many times must the wheel of Ex. 18 turn in going 69.429^m? 73.513^m? 17.27^{km}?

17 nearly
4115) 69429
4115
28279

18 nearly
4115) 73513
4115
32363

20. Find the reciprocal of 3.1416 to the fifth place.

0.31831. Ans.

21. How thick through is a tree whose girth is 2.97^m?

0.31831

2.97

222817

286479

63662

0.9453807

0.945^m. Ans.

0.31831 5.5 159155 159155 1.750705 1.75^m. Ans.

22. What is the diameter of a wheel that turns 19.5 times in going 107.25^m?

23. What is the diameter of a rope of which the circumference is 20cm?

Exercise 32. Page 69.

1. Find the area of a rectangle 17cm by 19cm.

19 17 133 19 323 323qem. Ans.

2. In a rectangular township 16km by 7km, how many hektars? If there are in it 47.3km of highway, averaging 11.7m wide, how much land is left for other uses?

 $\begin{array}{ccc}
47300 & 16 \\
 & \frac{11.7}{331100} & \frac{7}{112} \\
 & 473 & 112^{qkm} = 11,200^{hs}. \ \textit{Ans.} \\
 & \frac{473}{553410} & \frac{55.341}{11,144.659^{hs}} \ \textit{Ans.}
\end{array}$

3. In a rectangular field 751.3^m long and 189.3^m wide is a rectangular garden 31.4^m by 17.8^m. How many hektars in the field? How many exclusive of the garden?

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4. If my garden contains 941.65qm and my neighbor's 747.37qm, what is the area in hektars of both taken together?

$$941.65^{qm} = 0.094165^{ha}$$
 $747.37^{qm} = \frac{0.074737^{ha}}{0.168902^{ha}}$
 0.1689^{ha} . Ans.

5. If a painter can cover 8.786qm in an hour, how many square meters can be cover in 1.78 hours? in 3.86 hours? in 4.57 hours?

8.786qm	8.786qm	8.786qm
1.78	3.86	4.57
70288	52716	61502
61502	70288	43930
8786	26358	35144
15.63908qm	33.91396qm	40.15202qm
15.639qm. Ans.	33.914qm. Ans.	40.152qm. Ans.

6. How many hektars in each of three rectangular fields: one measuring 315.71m by 78.91m; a second, 293.6m by 84.84m; the third, 346.8^m by 71.82^m? How many in the three together?

315.71	293.6	346.8	
78.91	84.84	71.82	
31571	11744	6936	
284139	23488	27744	2.4913ha
252568	11744	3468	2.4909
220997	23488	24276	2.4907
24912.6761	24909.024	24907.176	7.4729ha Ans.
0.40101 4	0.4000ha 4	0.40085-	A -

2.4913ha. Ans. 2.4909ha. Ans. 2.4907ha. Ans.

7. Find the price of a rectangular field, 346.8^m by 71.82^m, at \$67.50 a hektar; at \$384 a hektar; and at \$2.375 a square meter.

From Example 6, the field contains 2.4907ha.

\$2.375 per square meter = \$23,750 per hektar.

\$23750 2.4907 166250 213750 95000 47500 \$59154.1250 \$59,154.13. Ans.

8. Find the length of a rectangle 17cm wide that contains 306qcm. What length of carpet 75cm wide is required to make 27qm?

18	36
17)308	75)2700
17	225
136	450
<u>136</u>	<u>450</u>
18cm. Ans.	36m. Ans

9. A room is 16^m long, 8^m wide, and 8^m high; another room is 7^m long, 7^m wide, and 3^m high. How many square meters of painting on the walls of both rooms, if no allowance is made for doors and windows? How many more square meters of painting on the walls of the larger room than on those of the smaller?

7m	14	16 ^m	24	384qm	384qm
7	2	8	2	84	84
14m	$\overline{28}$	24m	48	468qm Anc.	300qm Ans.
	3		8		,
	84		384		,

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10. What is the area of a circle 27cm in diameter? of a circle 1cm in diameter?

27

27

189

54

729

54978

572.5566

572.5566qem. Ans. $1 \times 1 \times 0.7854 = 0.7854$. 0.7854qm. Ans.

11. What is the area in hektars of a circular field 784^m in diameter?

 $\begin{array}{rrrr}
 784 & 614656q^{m} \\
 \hline
 784 & 0.7854 \\
 \hline
 3136 & 2458624 \\
 6272 & 3073280 \\
 \hline
 5488 & 4917248 \\
 \hline
 614656 & 4302592 \\
 \hline
 482750.8224q^{m} \\
 = 48.275h^{a}, Ans.$

12. Find the area of a circle 31cm in diameter.

 $0.7854 \\ \underline{961} \\ 7854 \\ 47124 \\ \underline{70686} \\ 754.7694$

754.7694qcm. Ans.

13. Find the area of a circle whose radius is 24^m.

3.1416 $\underline{576}$ 188496 219912 $\underline{157080}$ 1809.5616

1809.5616qm. Ans.

14. If a circle has a radius of 7cm, how many square centimeters does it contain?

 $\frac{7}{49}$

 $\begin{array}{r}
3.1416 \\
\underline{49} \\
282744 \\
\underline{125664} \\
153.9384
\end{array}$

153.9384qcm. Ans.

15. In a rectangular sheet of zinc 1.76^m long and 89^{cm} wide are two circular openings, one of which has a radius of 10.5^{cm}, the other a radius of 9.2^{cm}. What is the area of the zinc left?

10.5	3.1416	9.2	
10.5	110.25	9.2	
525	157080	184	
105	62832	828	
110.25	31416	84.64	
	31416		
	346.361400		
346.3614	qom = 0.03464qm.		
3.1416	0.02659qm	1.76	
84.64	0.03464qm	0.89	
125664	0.06123qm	1584	
188496		1408	
125664		1.5664	
251328		1.5664qm	
205.905024		1.06123	
$265.905024^{\rm qcm} = 0.0$	2659qm.	1.50517qm	Ans.

16. A piece of land in the form of a circle has a radius of 40^m; in the middle of it is a pond forming a circle of 15^m radius. What is the total surface? the surface of the pond? the surface of the land to cultivate?

3.1416	40	3.1416
225	40	1600
157080	1600	18849600
62832		31416
62832		5026.56
700.86		706.86
		4219.7

5026.56qm; 706.86qm; 4219.7qm. Ans.

17. How deep is a well, if the wheel whose diameter is 75cm makes 26 revolutions in raising the bucket?

$$26 \times 3.1416 \times 75^{\text{cm}} = 6126.12^{\text{cm}} = 61.2612^{\text{m}}$$
. Ans.
$$\begin{array}{ccc} 75 & & & & & & & & & \\ 26 & & & & & & & \\ \hline 450 & & & & & & \\ \hline 1950 & & & & & & \\ \hline 1950 & & & & & & \\ \hline 1950 & & & & & & \\ \hline 1950 & & & & & & \\ \hline 1950 & & & & & & \\ \hline \end{array}$$

18. How many square centimeters of surface on a ball 7cm in diameter?

$$\begin{array}{ccc}
7 & 3.1416 \\
\hline
7 & 49 \\
\hline
282744 \\
\underline{125664} \\
153.9384
\end{array}$$

153.9384qcm. Ans.

19. How many square centimeters of surface on a ball 18cm in diameter?

$$\begin{array}{ccc}
18 & 3.1416 \\
\underline{18} & 324 \\
144 & 125664 \\
\underline{18} & 62832 \\
\underline{324} & 94248 \\
\underline{1017.8784}
\end{array}$$

1017.8784qem. Ans.

20. How many square meters of surface on a hemispherical dome 11.27^m in diameter?

21. What is the interior surface of a hemispherical basin 12cm in diameter?

22. What is the interior surface of a hemispherical vase 70cm in diameter?

23. How many meters of carpet 60cm wide will be required for a room 6m long and 5.4m wide, the strips running lengthwise? how many meters would be required if the carpet were 80cm wide?

$$\frac{69)549}{9}$$
. Hence, 9 strips will be required.

$$9 \times 6^{m} = 54^{m}$$
. Ans.

 $\frac{80)540}{6.7}$. Hence, 7 strips would be required.

$$7 \times 6^m = 42^m$$
. Ans.

24. How many meters of carpet 56^{cm} wide will be required for a room 8.32^m long and 6.6^m wide, strips running lengthwise?

11 56)660 56	Hence, 12 strips will be required.
90	
100	8.32m
56	12
44	1664
	832
	99.84 ^m Ans.

25. How many meters of carpet 70^{cm} wide will be required for a room 7^m long and 5.4^m wide, strips running across the room?

$$\begin{array}{r}
 79)709 & 5.4^{m} \\
 \hline
 10 & \frac{10}{54^{m}} \quad Ans.
 \end{array}$$

26. How many meters of carpet 80cm wide will be required for a room 6m long and 5.47m wide, strips running across the room?

27. How many meters of carpet 90cm wide will be required for a room 5m long and 4.5m wide, strips running lengthwise? How much will it cost, at \$1.875 a meter?

28. How many meters of carpet 75^{cm} wide will be required for a room 5.25^m long and 4.75^m wide, strips running across the room? Find the cost, at \$2.125 a meter.

29. How many meters of carpet 75cm wide will be required for a room 5.6m square? How wide a strip will have to be turned under? How much will the carpet cost, at \$1.25 a meter?

Hence, 8 strips will be required.

75cm
35
40cm to turn under. Ans.
\$1.25
44.8
1000
500
500
\$56.000
\$56. Ans.

30. Find the area of the walls of a room whose length is 6.12^{m} , breadth 5.05^{m} , and height 3.5^{m} . Perimeter = $2 \times (6.12^{m} + 5.05^{m})$

$$= 22.34^{m}.$$

$$22.34$$

$$3.5$$

$$\overline{11170}$$

$$6702$$

$$\overline{78.19}$$

78.19qm. Ans.

31. How many rolls of paper 45cm wide and 8m long, allowing 11.19qm for doors and windows, will be required to paper the room of Ex. 30?

22

19 rolls. Ans.

32. Find the cost of papering a room 8^m long, 5.5^m wide, and 4.5^m high, with paper 50^{cm} wide and 7.5^m in a roll, at \$1.25 a roll, put on; if there is a baseboard 25^{cm} wide running round the room, and an allowance of 11^{qm} is made for doors and windows.

8	27
5.5	0.25
13.5	135
2	54
	6.75
4.5	11.
135	17.75
108	
121.5	7.5
17.75	0.5
103.75	3.75

Hence, 28 rolls will 375)10375 be required.

750	\$ 1.25
2875	28
2625	1000
250	250
200	\$ 35.00 Ans.

33. Find the cost of plastering the room of Ex. 32, at \$0.50 a square meter.

 $147.75 \times 60.50 = 673.88$. Ans.

The fine was a majoral around he done 4.9 wide, and the man with your files with a roll put in his wing men ar based are not been seen

Hence, 16 rolls will

			de required.
5 5	- 3	2000	\$0.375
4.1	1. 43	···)	16
20. 3		30,71	5250
2	3(4)	[657]	875
3.3	3 3	<u> </u>	\$14.00 Ars.
3.2			
4:3			
4.3			
标键			
1-4.			
33.92			

35. Find the cost of plastering the room of Ex. 34. at \$0.45 a square meter.

5.5	The first of the second	80.32		
4.5	Sign which	0.45		
440)	3 ().(24=	40160		
220		32128		
26.40		36.1440	\$36.14.	Ans.

36. Find the cost of papering a room 6th square and 3.5th high, with paper 45th wide and 7.5th in a roll, at \$0.75 a roll, put on; and of putting on a border, at 5 cents per running meter.

6		24	Hence, 25 rol	lls will be required.
В	7.5	3375 84000		
12	0.45	6750		
2	375	16500	\$ 0.75	
24	300	13500	25	
3.5	3.375	3000	375	24
120			150	0.05
72			\$18.75 A	ns. 1.20
84				\$1.20. Ans.

37. Find the cost of plastering the room of Ex. 36, at \$0.36 a square meter.

6	\$0.36
6	120
	720
84	. 36
120	\$43.20 Ans.

38. Find the cost of papering a room 13^m long, 12^m wide, and 7^m high, with paper 45^{cm} wide and 7.5^m in a roll, at \$1.50 a roll, put on; and of putting on a border, at \$0.30 a running meter, allowing 115^{qm} for baseboard, doors, etc.

13	7.5		Hence,	70 rolls
12	0.45	69	will be req	
<u></u> 25	375	3375)235000	\$1.50	
2	300	20250	70	
50	3.375	32500	\$ 105.00	Ans.
7		30375		
350		2125	\$0.30	
115			50	
235			\$15.00	Ans.

39. Find the cost of plastering the room of Ex. 36, at \$0.60 a square meter.

 $391 \times \$0.60 = \234.60 . Ans.

40. How many meters, board measure, in a board 8^m long, 20^{cm} wide, and 20^{mm} thick?

41. How many meters, board measure, in a joist 5^m long, 25^{cm} wide, and 75^{mm} thick?

$$\frac{5 \times 0.25 \times 73}{23} = 3.75.$$
3.75... Ans.

42. How many meters, board measure, in a stick of timber 15^m long and 40^{cm} square?

$$\frac{16}{25} = 96.$$
96^m. Ans.

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■ E w max* meses, burd President and the State of the Comment · 12. 金字 平 20. 20. 35字 25. 36. Villa a tiro tilbi, at \$14 a Printed Before *

66. Find the cost of ten joists 4 50 5 to 1500 wife, and 7.500 CLARES -

47. Find the cost of thirty-six and "5 think, at \$16 a bundred De cas.

Find the cost of three sticks of timber, each 8= long, 22.6cm wide, and 2000 thick, at \$17.50 a handred metera.

$$\frac{3 \times 8 \times 0.225 \times 299}{23} = 43.2.$$

$$\begin{array}{r} 30.175 \\ \underline{43.2} \\ \hline 350 \\ \underline{525} \\ 700 \\ \hline \$7.56 \ Ans. \end{array}$$

49. Find the cost of a heart # long, then wide at one culhim at the other and 31 25mm at \$0.80 a meter a - "Gen a Al nor

:15 · 13

50. Find the cost of a stick of timber 10^m long, 25^{cm} thick, 30^{cm} wide at one end and 25cm wide at the other, at \$14 a hundred meters.

$$\frac{1}{4}$$
 of $(30^{cm} + 25^{cm}) = 27.5^{cm}$.

$$\frac{10 \times 0.275 \times 259}{25} = 27.5.$$

$$\frac{27.5}{0.14}$$

$$\frac{0.14}{1100}$$

$$\frac{275}{3.850}$$
\$ 3.85. Ans.

51. Find the cost of the floor boards, 32mm thick, for a two-story building 16^{m} by 10.5^{m} at \$30 a hundred meters.

$$\frac{2 \times 16 \times 19.5 \times 32}{25} = 430.08.$$

$$\frac{2 \times 16 \times 19.5 \times 32}{25} = 430.08.$$

$$\frac{30}{129.0240} = 129.02. Ans.$$

Find the cost of the floor timbers, 25cm by 50mm, for the building of Ex. 51, if the timbers run lengthwise and are placed on edge 30cm apart, and are worth 4900 \$11.50 a hundred meters.

$$50^{\text{mm}} = 5^{\text{cm}}$$
.

: each timber with its space occupies $30^{cm} + 5^{cm} = 35^{cm}$ of space.

The width of the house is 10.5^m or 1050cm.

 \therefore each floor requires $\frac{1950}{5} = 30$ timbers, and both floors require 60 timbers.

$$\frac{60 \times 16 \times 0.25 \times \cancel{50}}{\cancel{25}} = 480.$$

$$\frac{480}{\cancel{92000}}$$

$$\cancel{4600}$$

$$\cancel{8}55.2000}$$

$$\cancel{8}55.20. Ans.$$

53. Find the cost of the fencing to inclose a field 150^m long and 75^m wide; the posts are set 2.5^m apart, and cost \$0.25 apiece; the fence is 5 boards high; the bottom board is 30cm, the top board 25cm, and the other three each 22.5cm wide, and the boards cost \$13.25 a hundred meters.

Perimeter =
$$2 \times (150^{m} + 75^{m})$$

= 450^{m} .
 $450 \div 2.5 = 180$, number of posts.
 $180 \times \$ 0.25 = \$ 45$.
Total width of the boards
= $30^{cm} + 25^{cm} + 3 \times 22.5^{cm}$
= $30^{cm} + 25^{cm} + 67.5^{cm} = 122.5^{cm}$.
 $\frac{551.25}{275625}$
 $\frac{0.1325}{275625}$
 $\frac{1.225}{450}$ $\frac{110250}{110250}$

165375

55125

73.040625

61250

551.250

8 73.04

45.

8 118.04 Ans.

Exercise 33. Page 77.

1. How many cubic centimeters in a block 9^{cm} long, 7^{cm} wide, and 6^{cm} deep?

9	63
7	6
63	$\overline{378}$ Ans.

2. If wood is cut into 120cm lengths, and a pile is 43.7m long and 1.4m high, how many steres of wood are there in the pile?

3. How many hektoliters of grain will a bin hold, 11.2^m long, 4.34^m wide, and 2.83^m deep?

11.2	48.608
4.34	2.83
448	145824
33 6	388864
448	97216
48.608	137.56064

 $137.56064^{\text{chm}} = 1375.6064^{\text{hl}}$. Ans.

4. If a liter of grain weighs 0.81 of the weight of a liter of water, find the weight of the grain in the bin of Ex. 3.

1375.6064^{hl} of water weighs 137,560.64^{kg}.

5. A bin 16^m by 9.7^m, and 2.8^m deep, is full of oats, worth \$0.98 a hektoliter. What is the whole worth?

LL I		
16	4345.6	
9.7	0.98	
112	347648	
144	391104	
155.2	4258.688	
2.8	\$ 4258.69.	Ans.
12416		
3104		
434.56		
434.58cbn	n = 4345.6hl.	

6. How many liters does a vat 197cm long, 87cm wide, and 63cm deep hold? What weight of water will be required to fill it?

107

101	11108
87	63
1379	51417
1576	102834
17139	1079757
$1,079,757^{\text{ccm}} =$	1079.757 ¹ . Ans.
	1079.757kg. Ans.

7. Add 1341ccm, 2311, and 2.13hl, and give the sum in terms of each of the three units.

8. If a spring delivers 467.81 each minute, how many hektoliters will it deliver in 60 minutes? in 37 minutes? in 78 minutes?

78 37424 32746 364.884hl Ans.

9. If 67.31 of oil in a vat with perpendicular sides fills it to a depth of 173mm, how deep will 13.7 times that quantity fill it? How many hektoliters will there be?

173mm	0.673hl	
13.7	13.7	
1211	4711	
519	2019	
173	673	
2370.1mm	9.2201hl	Ans.
=2.3701 ^m . Ans.		

10. One cask contains 171.41 of oil; another, 209.3° ; a third, 73.8° ; while a square vat, 137cm each way, is filled to a depth of 69cm. Find in liters and in hektoliters the amount of oil in the four vessels together.

$$\begin{array}{ccc}
137 & 18769 \\
\underline{137} & \underline{69} \\
959 & 168921 \\
411 & \underline{112614} \\
\underline{137} & 1295061
\end{array}$$

$$1,295,061^{\text{ccm}} = 1295.061^{\text{l}}.$$

$$171.4^{\text{l}}$$

$$209.3$$

$$73.8$$

$$\frac{1295.061}{1749.561^{\text{l}}.}$$

$$4ns.$$

$$17.49561^{\text{hl}}.$$
Ans.

11. How many liters of air in a room 7.8m long, 6.23m wide, and 3m high?

$$6.23$$

$$\frac{7.8}{4984}$$

$$\frac{4361}{48.594}$$

$$\frac{3}{145.782}$$

$$145.782^{\text{cbm}} = 145,782^{1}$$
. Ans.

12. If a person's breathing spoils the air at the rate of 0.2175cbm a minute, how long will

it take three persons sitting in the closed room of Ex. 11 to spoil the

223.42 minutes. Ans.

13. How long, at the same rate 22^m long, 16^m wide, and 7^m high last 280 persons?

22		0.2175cbm
16		280
132		174000
22		4350
352		60.9000cbm
7		
2464		
	40.4	
609)	24640.	
:	2436	
•	2800	40.5 minutes.
	2436	Ans.
	364	

- 14. How many cubic centimeters in a ball 10ccm in diameter? $0.5236 \times (10^3)^{\text{ccm}} = 523.6^{\text{ccm}}$. Ans.
- 15. Into a cubical box 20cm on an edge, and full of water, an iron ball 20cm in diameter is gently lowered until it touches the bottom. Find in liters and in cubic centimeters the volume of the water left in the box.

20	0.5236	
<u>20</u>	8000	
400	4188.8	
20		
8000	8000ccm	
	4188.8	
	3811.2cem. Ans.	
	3.8112 ¹ . Ans.	

16. If cast iron weighs 7.207 as in Ex. 11, will the air in a hall times as much as water, what is the weight of a cast iron ball 5cm in diameter?

 $0.5236 \times (5^{2})^{\text{ccm}} = 0.5236 \times 125^{\text{ccm}}$

0.5236	65.45	
<u> 125</u>	7.207	
2 6180	45815	
10472	13090	
52 36	45815	
65.4500	471.69815s	Ans.

17. A rubber ball is 6.2cm in diameter. What is the amount of rubber in the ball?

6.2	238.328ccm
6.2	0.5236
124	1429968
372	714984
38.44 6.2 7688 23064	476656 1191640
	124.7885408cem Ans.
238.328	

18. If the circumference of a cannon ball is 52cm, find the volume of the ball.

0.31831	16.55212
52	16.55212
63662	3310424
59155	1655212
16.55212	3310424
	8276060
	8276060
	9931272
	1655212
	273,9726764944

19. How many cubic centimeters of oil are there in a cylindrical cup 10^{cm} across when the oil is 38^{mm} deep?

```
38mm 78.54
= 3.8cm. 3.8
62832
23562
208.452
298.452ccm. Ans.
```

20. What is the capacity of a cylindrical cup 95^{mm} across and 11.08^{cm} deep?

$$95^{\text{mm}} = 9.5^{\text{em}}.$$

$$9.5$$

$$9.5$$

$$9.5$$

$$39270$$

$$15708$$

$$855$$

$$70686$$

$$70.88235$$

$$11.08$$

$$56705880$$

$$7088235$$

$$7088235$$

$$7088235$$

$$7088235$$

$$7088235$$

 $785.3^{\text{ccm}} = 0.785^{\text{l}}$. Ans.

21. What is the capacity of a cylindrical vessel 16.24cm across and 19.95cm deep? 75.4mm across and 87.9mm deep?

 $4132.433025^{\text{cem}} = 4.132^{\text{l}}$. Ans.

75.4 **75.4** 3016 3770 **5278** 5685.16 0.7854 2274064 2842580 4548128 3979612 4465.124664 4465.125 87.9 40186125 31255875 35721000 392484.4875

 $392,484.4875^{\text{ccm}} = 0.392^{\text{l}}$. Ans.

22. How many cubic meters of wood in a round stick of equal size throughout, 37cm in diameter, and 8.4m long?

37	0.7854	0.10752126	
37	1369	8.4	
259	70686	43008504	
111	47124	86017008	
1369	23562	0.903178584	
	7854	0.9032cbm. Ans.	
	1075.2126	2.000	

 $1075.2126^{\text{qcm}} = 0.10752126^{\text{qm}}$.

23. A cylindrical stand-pipe whose diameter is 12^m and whose height is 22^m is filled with water. Find the weight of the water.

$$0.7854 \times (12 \times 12 \times 22)^{\text{cbm}}$$

= 2488.1472cbm.

2488.1472cbm of water weighs 2488.1472t. Ans.

24. Find the number of liters of water in a well, if its diameter is 1.2^m and the depth of the water is 2^m.

$$0.7854 \times (1.2 \times 1.2 \times 2)^{\text{ebm}}$$

= 2.261952^{ebm}
= 2261.952^{l} . Ans.

$$\begin{array}{cccc}
1.2 & 0.7854 \\
1.2 & 2.88 \\
\hline
1.44 & 62832 \\
2 & 62832 \\
\hline
2.88 & 15708 \\
\hline
2.261952
\end{array}$$

25. A cylindrical cup 90^{mm} in diameter is partly filled with water. Into the cup is dropped a piece of iron, and the water rises 63^{mm}. What is the volume of the piece of iron?

$$0.7854 \times (90 \times 90 \times 63)^{qmm}$$

= $400,789.62^{cmm}$
= 400.78962^{ccm} . Ans.

90	0.7854
90	510300
8100	2356200
63	7854
24300	39270
486	400789.6200
510300	

Exercise 34. Page 79.

1. What is the weight, in kilograms, of a hektoliter of water? of 73.81 of water? of a cubic meter of water? of a cubic centimeter of water?

1^{hl} of water weighs 100^{kg}. Ans.
73.8^l of water weighs 73.8^{kg}. Ans.
1^{chm} of water weighs 1000^{kg}. Ans.
1^{ccm} of water weighs 0.001^{kg}. Ans.

2. If a man buys half a ton of potatoes for \$20, and retails them all, without waste, at 5 cents a kilogram, what profit does he make on the whole?

3. What is the weight of water required to fill a vat 98cm long, 71cm wide, and 38cm deep?

98	6958
71	38
98	55664
686	20874
69 58	264.404
	264.404 g. Ans.

4. If the vat of the last example is filled with brine weighing 1.04kg to the liter, what is the weight of the brine?

5. If the vat of Ex. 3 is filled with wine weighing 0.981 to the liter, what is the weight of the wine?

6. What is the total weight of 13 men averaging 73.48kg each?

7. How many kilograms, and how many tons, will 3.6175cbm of brick weigh, at 2 tons to a cubic meter? at 2.34 tons?

3.6175×2^{t}	3.6175
=7.235t	2.34
$=7235^{\mathrm{kg}}.$	144700
$3.6175 \times 2.34^{\circ}$	108525
$=8.46495^{t}$	72350
=8464.95kg.	8.46495

8. From a barrel containing How much is left in the barrel?

2.75ks 3		7.5 ¹ 4 4
8.25ks		31). 0 *8
	30. kg	
	8.25	
	38.25kg	
	67.14	
	38.25	
	28.75kg	Ans.

9. Into how many pills of 325mg each can a mass of 7.8g be divided?

10. A mass of 21.8g is divided into 60 pills. What is the weight of each pill?

11. A bag, when empty, weighs 674 of granulated sugar there are 213; when full of silver five-franc taken three parcels of 2.75 each. pieces, 20 5 134. A five-franc and four parcels of 7.50 each. piece weighs 25s. How many fivefranc pieces will the bag hold?

$$20 \times 5 \times 13 = 20,513$$
.
 $20,513 = 213 = 20,300$.
 812 Ans.
 $25)20300$
 200
 30
 25
 50
 50

12. A vessel, when empty. weighs 2.74; and when full of water 4235dkg. What would it weigh if filled with milk which is 1.03 times as heavy as water?

Exercise 35. Page 81.

1. If a stone weighs 1.3kg in air and 0.68kg in water, and the stone and a block of wood together weigh 1.55kg in air and 0.63kg in water, what is the specific gravity of the block of wood?

 $1.55^{kg} - 1.3^{kg} = 0.25^{kg}$, the weight of the wood in the air.

- 1.55 = 0.63 = 0.92 s, the weight of the water displaced by the stone and the wood.
- 1.3 = 0.68 = 0.62 s, the weight of the water displaced by the stone alone.

Therefore, $0.92^{kg} - 0.62^{kg} = 0.3^{kg}$, the weight of the water displaced by the wood.

 $0.25 \div 0.3 = 0.833$, the specific gravity of the wood.

2. What is the weight of 8.17^{hl} of alcohol, specific gravity 0.83?

3. What will 971 of alcohol weigh, of specific gravity 0.817? of specific gravity 0.819? of specific gravity 0.823? 0.838? 0.847?

0.817≒8	0.819kg	0.823kg	0.838kg	0.847kg
97	97	97	97	97
5719	5733	5761	5866	5929
7353	7371	7407	7542	7623
79.249kg	79.443kg	79.831kg	81.286kg	82.159kg

4. A bar of aluminum 113mm long, 17mm wide, and 13mm thick, is said to be of specific gravity 2.57. What does it weigh? If it really is of specific gravity 2.67, what does it weigh?

113	1921	24.973s	24.973
17	13	2.57	2.67
791	5763	174811	174811
113	1921	124865	149838
1921		49946	49946
	$24,973^{\text{cmm}} = 24.973^{\text{ccm}}$.	64.18s Ans.	66.677918
			66.68g. Ans.

5. What would be the specific gravity of the aluminum in Ex. 4 if the bar weighed 65.1378?

	2.608	Ans.
24973)65	137.	
49	946	
15	1910	
14	9838	
	207200	
	199784	

6. What is the weight of a bar of aluminum 371^{mm} by 63^{mm} by 84^{mm}, specific gravity being 2.63?

371	
63	
1118	1.963332kg
2226	2.63
23373	5889996
84	11779992
93492	3926664
186984	5.16356316 kg
1963332	5.1636kg. Ans.

7. An irregular mass of copper, gently lowered into a pail brimful of water, caused 1.3741 to run over. What did it weigh if of specific gravity 8.91? if 8.89?

1.374₺₡	1.374kg
8.91	8.89
1374	12366
12366	10992
10992	10992
12.242 ^{kg} Ans.	12.21486kg
	12.215kg. Ans.

8. What would be the specific gravity of the copper in Ex. 7 if the mass weighed 12.3016 ?

9. A plate of iron 137cm long, 64.3cm wide, and 4.31cm thick weighs 277.54kg. What is its specific gravity? What would the same mass weigh at specific gravity 7.47? at 7.79?

137	8809.1
64.3	4.31
411	88091
548	264 273
822	352364
8809.1	37967.221
	$37,967.221^{\text{ccm}} = 37.97^{\text{l}}.$

7.309 Ans.

10. What is the specific gravity of sea water when a hektoliter weighs 102.58 **? when 31 weighs 3077 **?

11. What is the specific gravity of a substance of which 7.3ccm weighs 31.5s?

12. If a cubic meter of sand reighs 1723kg, what is its specific ravity? If 3.4cbm of gravel weighs 134 tons, what is its specific ravity?

13. If a cubic centimeter of metal weighs 7.3g, what is its specific gravity?

7.3. Ans.

14. What is the specific gravity of a fluid weighing 2.317kg to a liter?

2.317. Ans.

15. If a body weighs 3.71kg in air and 2.38kg in water, what is its specific gravity?

3.71kg	2.789 Ans.
2.38	133)371.
1.33kg	266
	1050
	931
	1190
	1064
	1260
	<u>1197</u>

16. A piece of ore weighing 3.77kg weighs in water only 2.53kg. What is its specific gravity?

17. How many cubic centimeters in a stone which loses 17.84 of its weight when weighed in water? What is its specific gravity if it weighs 33.74 in air?

17.8cem. Ans.

1.893 Ans.

18. In a wrought-iron bottle I find 2.63 of quicksilver, weighing 35.81 in another 2.50, weighing 35.193 in a third, 2.617, weighing 35.571 is. What is the specific gravity of each? What would be the specific gravity of the mixture if the three were emptied into one vessel?

13.588 Ans.

106.574*# $\div 7.887$ *# = 18.599. Ans

2.63

2.59

2.617

7.8371

5234

35.814

35.193

35.571

106.574hs

19. A plate of iron 89cm b 17cm by 7cm weighs 79.43ks. Wha is its specific gravity?

89	7.5	Ans
17	10591)79430.	
623	74137	
89	52930	
1513		
7		
10591		

20. What is the specific gravity of a rectangular block of wood 1.6m long, 0.3m wide, and 0.15m thick, if, floating in water on its face 0.3^m wide, it sinks to a depth of 0.12^m?

Volume of the block is $(1.6 \times 0.3 \times 0.15)^{cbm}$.

Volume of the water displaced is $(1.6 \times 0.3 \times 0.12)^{\text{cbm}}$.

Weight of the water displaced is $(1.6 \times 0.3 \times 0.12)^t$.

Weight of the block is $(1.6 \times 0.3 \times 0.12)^{t}$.

Therefore, the specific gravity of the wood

$$= \frac{1.6 \times 9.3 \times 9.12}{1.6 \times 9.3 \times 9.12} = \frac{4}{5} = 0.8. \text{ Ans.}$$

Exercise 36. Page 83.

1. If 3 men eat 8kg of bread a week, how much will 1 man eat at the same rate? How much will 7 men? How much will 3 men eat in I day? How much will 1 man eat in 1 day? How much will 7 men eat in 1 day? in 1 week? in 5 weeks?

how much will 17 men eat in 3 Weeks and 4 days?

3 weeks 4 days = 25 days.

2. At the same rate as in Ex. 1, for 1 horse 1 week? for 1 horse 7 weeks? for 11 horses 17 weeks?

$$5)1.0^{\rm hl}$$
 201
 $0.2^{\rm hl} = 20^{\rm l}$ Ans. $\frac{7}{140^{\rm l}}$ Ans.
 $\frac{17}{117}$ $\frac{11}{17}$ $\frac{17}{187}$ $187 \times 20^{\rm l} = 3740^{\rm l}$. Ans.

4. If 2hl of grain is enough for 3 horses 5 days, how much is 3. If 1hl of oats is enough for 5 enough for 3 horses 1 day? for 1 horses 1 week, how much is enough | horse 1 day? for 7 horses 6 days?

5. Mix 17¹ of vinegar, costing 6 cents a liter, with 39¹ at 5 cents, 21¹ at 7 cents, and 13¹ of water costing nothing. Find the number of liters, and the cost.

6. For how much a liter must I sell the mixture of Ex. 5 to gain 96 cents? to gain \$1.41?

\$4.44	\$0.06
0.96	90)\$5.40
\$5.40	540
\$4.44	\$0. 065
1.41	90)\$ 5.85
\$5.85	540
	450
	450
	

7. A grocer sold 421 kegs of butter for \$4995.25; 56 kegs brought \$12.50 a keg, 91 brought \$11.75 a keg, and 100 kegs brought \$12.25 a keg. For how much a keg were the other kegs sold?

\$ 12.50	\$11.75
56	91
7500	1175
6250	10575
\$ 700.00	\$ 1069.25
\$ 12.25	700.00
	1225.00
8 1225.00	\$ 2994.25

\$4995.25 2994.25 \$2001.00 56 421 91 247

174

100

8. If 3 tons of coal cost \$15.75, how many tons will \$36.75 buy?

9. If 5^m of cloth cost \$18.75, what will 7^m cost?

10. If a tap running 3.51 a minute fills a tub in 16 minutes, how long will a tap delivering 51 a minute be in filling the same tub?

11. If both taps of the last example are opened at once, how soon will they fill the tub?

6.6 minutes. Ans.

12. If 3 men can dig 378^m of ditch in 2 days, how long will it take 5 men, at the same rate, to dig 787^m?

13. Into a tub that will hold 48¹, one tap is delivering water at the rate of 3.7¹ a minute; while out of it, by another tap, the water is running at 2.5¹ a minute. How long will it take to fill the tub, beginning with it empty?

$$\frac{3.7^{1}}{2.5}$$
 $\frac{12)480}{40}$
 $\frac{1.2^{1}}{40}$
40 minutes. Ans.

14. A tap discharges into a tub 4.21 a minute; from the tub water is also running, by a second tap; the water in the tub gains 301 in 18 minutes. How fast is the second tap discharging?

4.21	2.5^{1}
18	$18)\overline{45.61}$
336	36
42	96
75.6 ¹	90
30 .	•
45.61	

 2.5^{1} a minute. Ans.

15. If a wheel is 1.2^m across, how many times will it turn in going one kilometer?

16. How many times in a minute does the wheel of the last example turn, when the carriage is driven at the rate of 14km an hour?

60	86
38	8.7
98	686
	784
	852.6

852.6kg. Ans.

 $\begin{array}{r}
 265 \\
 265 \\
 \hline
 0.23 \\
 \hline
 795 \\
 \hline
 530 \\
 \hline
 60.95
 \end{array}$

18. If we replace the water of Ex. 17 with oil worth \$18.75 a hektoliter, what will the contents of the tank be worth?

8.526^{hl} of water are required to weigh 852.6^{kg}.

 $8.526 \\ \underline{18.75} \\ 42630 \\ 59682 \\ \underline{68208} \\ 8526 \\ \underline{159.86250}$

17. What is the weight of the

water in a tank if it takes 1 hour and 38 minutes, at the rate of 8.71, a minute, to empty the tank?

\$ 159.86. Ans.

Exercise 37. Page 85.

1. A train leaves Paris at 11 o'clock A.M., and reaches Lyons at 10 o'clock P.M. How many meters does it travel in an hour, the distance from Paris to Lyons being 512.7km?

There are 11 hours between 11 A.M. and 10 P.M.

61 times. Ans.

$$512.7^{\text{km}} \div 11 = 46.609^{\text{km}} = 46,609^{\text{m}}$$
. Ans.

2. A railroad has a single track 11.450km long. How many rails 4.569m in length did it require to lay the track?

There are two lines of rails. Therefore the length of the rails is $2 \times 11.450^{\text{km}} = 22.900^{\text{km}} = 22.900^{\text{m}}$.

$$\begin{array}{r}
5012 \\
4569)22900000 \\
\underline{22845} \\
5500 \\
\underline{4569} \\
0010
\end{array}$$

9310 9138

The number of rails required was 5013. Ans.

3. A book is 2.1cm in thickness; each leaf is 0.05mm thick. Find the number of pages in the book.

The number of leaves is $21 \div 0.05 = 420$.

The number of pages is $2 \times 420 = 840$. Ans.

4. The cost of opening a canal amounts to \$25,400 a kilometer. How much will a canal cost which is 113.253km in length?

\$2,876,626.20. Ans.

5. The expense of laying out a paved road is \$12,500 a kilometer. How much will a road cost which is 72.053km long?

\$900,662.50. Ans.

6. The cost of building a railroad is about \$78,000 a kilometer in France, and only \$25,000 in the United States. How much will it cost in each country to make a road 295.671km long?

295.671 78000 2365368000 2069697 23062338.00a) -

\$23,062,338, France; } Ans.

7. If you must go up 211 steps to reach the top of a tower, and each step is 195mm high, what is the height of the tower?

8. A house has 5 stories, each story has 19 stairs, each stair is 16cm in height. Find the height of the floor of the fifth story from the ground.

$$16^{\text{cm}} = 0.16^{\text{m}}.$$

$$0.16^{\text{m}}$$

$$\frac{19}{144}$$

$$\frac{16}{3.04^{\text{m}}}$$

$$\frac{4}{12.16^{\text{m}}} Ans.$$

9. A ream of paper contains 20 quires, each quire has 24 sheets; the ream is 13.5cm in thickness. Find the thickness of each sheet.

In one ream there are 20×24 sheets = 480 sheets. If 480 sheets are 13.5^{cm} thick, the thickness of one sheet = $13.5^{cm} \div 480 = 0.028^{cm}$. Ans.

10. The equator on a terrestrial globe measures 0.80^m in circumference. By the aid of a tape measure we find that the distance between two cities on this globe is 0.046^m. What is really the distance in kilometers between the two cities? (The earth's equator is 40,075.45^{km}.)

The ratio of the distance on the globe between the two cities to the equator is $0.046^{\rm m} + 0.80^{\rm m} = 0.0575$. Therefore the actual distance between the two cities is $0.0575 \times 40,075.45^{\rm km} = 2304.338^{\rm km}$. Ans.

$$\begin{array}{c} 8)0.46 \\ \hline 0.0575 \\ \hline & 20037725 \\ \hline 28052815 \\ \hline 20037725 \\ \hline 2304.338375^{km} \\ \end{array}$$

11. Upon a military map we find that the distance from Paris to St. Denis is 78^{mm}. What is the distance in kilometers from Paris to St. Denis? The map is made on the scale of 1 to 80,000; that is, 1^m on the map represents 80,000^m of actual measurement upon the ground.

The actual distance is 80,000 times the distance on the map; that is, $80,000 \times 78^{mm} = 6,240,000^{mm} = 6.24^{km}$. Ans.

12. Find the number of revolutions made by the wheels of a carriage in traveling 82km. The wheels are 1354mm in diameter.

$$82^{km} = 82,000,000^{mm}$$
.

The circumference of the wheels is $3.1416 \times 1354^{\text{mm}} = 4253.7264^{\text{mm}}$. The number of revolutions is the total distance divided by the circumference of the wheel, or $82,000,000^{\text{mm}} \div 4253.7264^{\text{mm}} = 19,277$. Ans.

3.1416	19277
1354	42537264)820000000000
125664	42537264
157080	394627360
94248	382835376
31416	117919840
4253.7264	85074528
	328453120
	297760848
	306922720
	297760848
	

13. How many hektars in a square kilometer? how many ars? how many square meters?

$$1^{qkm} = 100^{ha},$$

= $10,000^{a},$
= $1,000,000^{qm}.$

14. France has about 542,000qkm. How many hektars does it measure?

$$542,000^{qkm} = 542,000 \times 100^{ha}$$

= $54,200,000^{ha}$. Ans.

15. A piece of land 1224.5^m square is sold at \$140 a hektar. How much does the land bring?

1224.5	149.94	
1224.5	140	
61225	599760	
48980	14994	
24490	20991.60	
24490	\$20,991.60. Ans.	
12245	\$20,881.00. Alls.	
1499400.25		

 $1,499,400.25^{qm} = 149.94^{ha}$.

16. The total surface measurement of the glass in the windows of a house is 182qm. How many panes of 53cm by 48cm will it take to supply the windows?

 $182^{qm} = 1,820,000^{qcm}$.

53		715.4
48		2544)1820000.
424		17808
212		3920
2544		2544
		13760
		. 12720
		10400
	716 panes. Ans.	10176
		

17. How many square slabs of marble 150qcm on the surface will it require to pave a court whose area is 25.35qm?

 $25.35^{qm} = 253,500^{qcm}$.

The number of slabs required is $253,500^{\text{qcm}} \div 150^{\text{qcm}} = 1690$. Ans.

$$\begin{array}{r}
 1690 \\
 \hline
 15)25350 \\
 \hline
 15 \\
 \hline
 103 \\
 \hline
 90 \\
 \hline
 135 \\
 \hline
 135 \\
 \hline
 0
 \end{array}$$

18. A speculator bought 31.0728ha of land for \$1296 a hektar. For how much a square meter must be sell it to realize a profit of \$1937?

31.0728 1296 \$ 0.136 Ans. 1864368 310728) \$ 42207.35 2796552 310728 621456 310728 1113455 932184 40270.3488 1812710 \$40,270.35 cost. 1,937. profit. **\$42,207.35** selling price.

19. A man is offered \$6000 for 2.5° of land. He declines to sell; and soon after, the town gives him \$25.20 a square meter. How much did he make by refusing the first offer?

$$2.5^{\circ} = 250^{\circ}$$

 25.20
 250
 126000
 5040
 6300.00
 6000
 300
 400

20. A man surveys a piece of land and finds that it measures 14.0715hs. He afterwards discovers that his chain was too short by 0.03m. How can he calculate the real superficial measurement of the land without surveying it again? (A surveyor's chain is 10m long.)

$$\begin{array}{c} 10.00-0.03=9.97.\\ 9.97\div 10=0.997.\\ \hline 0.997\\ \hline 6979\\ \hline 8973\\ \hline 0.994009\\ \hline \hline 0.994009\\ \hline \end{array}$$

21. A pile of wood is 4.25^m long, 1.33^m thick, and 2.60^m high. How many sters are there in it?

4.25	5.6525
1.33	2.6
1275	339150
1275	113050 .
425	14.69650
5.6525	14.6965 st . Ans.

22. The railroad from Paris to Orleans has a double track; each rail is 4m long, and the distance from Paris to Orleans is 121km. What is the number of rails used in laying the track? If the width of the road is 15^m, how many hektars of land does the road include?

There are four lines of rails. $4 \times 121^{km} = 484^{km} = 484,000^{m}$ of rails. If one rail is 4^{m} long, in $484,000^{m}$ there are $484,000 \div 4 = 121,000$ rails. $15^{m} = 0.015^{km}$. The area of the road is

$$(121 \times 0.015)^{qkm} = 1.815^{qkm} = 181.5^{ha}$$
. Ans.
 121^{km} 4)484000 121
 $\frac{4}{484^{km}}$ 0.015
 $\frac{121}{605}$ 121
 $\frac{121}{1.815}$

23. Find the number of ars in a surface which a ream of paper (480 sheets) will cover. The sheets are 30.3cm long and 195mm wide.

 $195^{mm} = 19.5^{cm}$.

283,608qcm = 28.36qm = 0.2836s. Ans.

24. A beam is $7.070^{\rm m}$ long; its two other dimensions are $0.258^{\rm m}$ and 87mm. Find its volume.

 $87^{mm} = 0.087^{m}$

0.258	0.022446
0.087	7.07
1806	157122
2064	157122
0.022446	0.15869322

0.15869cbm. Ans.

25. A bar of iron 3^m long measures 45^{mm} square on the end where it has been evenly cut. The bar is heated and drawn out to a greater length by being passed through an orifice 24^{mm} square. What is the length of the bar after the operation?

$$45^{\text{mm}} = 0.045^{\text{m}}, \quad 24^{\text{mm}} = 0.024^{\text{m}}.$$

The volume of the bar is $(0.045 \times 0.045 \times 3)^{cbm} = 0.006075^{cbm}$. The area of the end, after the bar has been heated, is

$$(0.024 \times 0.024)^{qm} = 0.000576^{qm}$$
.

Therefore the length of the bar is $(0.006075 + 0.000576)^{m} = 10.547^{m}$. Ans.

10.54	0.024	0.045
576)6075.	0.024	0.045
576	96	225
3150	48	180
2880	0.000576	0.002025
2700		3
2304		0.006075
3960		

26. A reservoir is 1.50^m wide, 2.80^m long, and 1.25^m deep. Find how many liters it contains when full, and to what height it would be necessary to raise it that it might contain 10^{cbm}.

The volume of the reservoir is $(1.5 \times 2.8 \times 1.25)^{\text{cbm}} = 5.25^{\text{cbm}} = 5250^{\text{l}}$.

Ans.

The area of the bottom is $(1.5 \times 2.8)^{qm} = 4.2^{qm}$; therefore, in order to contain 10^{cbm} , the height must be $(10 \div 4.2)^m = 2.38^m$. Ans.

1.5	2.38
2.8	42)100.
120	84
30	160
4.20	126
1.25	340
2100	836
840	
420	
5.2500	

27. Suppose a box to be 3.75^m long, 3.50^m wide, and 0.50^m high. How much lime would it take to fill it with mortar, reckoning that 1^{cbm} of lime after being slaked becomes 1.80^{cbm} of mortar?

The volume of the box is $(3.75 \times 3.50 \times 0.50)^{\text{cbm}} = 6.5625^{\text{cbm}}$. Since 1^{cbm} of mortar when slaked becomes 1.8^{cbm} , the box will hold 6.5625^{cbm} of slaked mortar, which is the same as $6.5625^{\text{cbm}} \div 1.8 = 3.646^{\text{cbm}}$ of dry mortar.

3.75	3.646
3.5	18)65.625
1875	54
1125	116
13.125	108
0.5	82
6.5625	72
	105

3.646cbm. Ans.

28. A chest has the following dimensions: 1.17^m, 0.90^m, 1.04^m. If 0.12 of the volume of the chest is deducted for packing, how many cakes of soap 13^{cm} square on the bottom and 29^{cm} thick could be put in it?

The volume of a cake of soap is $(13 \times 13 \times 29)^{\text{ccm}} = 4901^{\text{ccm}}$. The volume of the chest, deducting waste of room in packing, is

 $0.88 \times (1.17 \times 0.90 \times 1.04)^{\text{cbm}} = 0.9637056^{\text{cbm}} = 963,705.6^{\text{ccm}}.$

Therefore, the chest will hold (963,705.6 \div 4901) cakes of soap.

13	1.17	196
13	1.04	4901)963705.6
39	468	4901
13	117	47360
169	1.2168	44109
29	0.9	32515
1521	1.09512	29406
338	0.88	
4901	876096	
	876096	
	0.9637056	196. Ans.

29. A cubic meter of dry plaster makes 1.18cbm when tempered; tempered plaster increases 1 in every 100, twenty-four hours after it is mixed. What volume of tempered plaster would be obtained from 55 sacks of 251 each of dry plaster?

 $25^{1}=0.025^{cbm}$. The volume of the plaster is $55\times0.025^{cbm}=1.375^{cbm}$. As 1^{cbm} makes 1.18^{cbm} when tempered, 1.375^{cbm} will make $1.375\times1.18^{cbm}=1.6225^{cbm}$. In twenty-four hours its volume will be $1.01\times1.6225^{cbm}=1.6387^{cbm}$. Ans.

0.025	1.375	1.6225
55	1.18	1.01
125	11000	16225
125	1375	16225
1.375	1375	1.638725
2.070	1.62250	2,000,20

30. A reservoir is 2.80^m long, 1.50^m wide, and 1.25^m deep. How many liters will be required to fill 0.80 of it?

1.5	4.20	525 0 ¹
2.8	1.25	0.8
120	2100	4200.1 Ans.
30	840	
4.20	420	
	5.2500	
	$5.25^{\text{ebm}} = 5250^{\text{l}}$.	

31. A man buys 1415^{hl} of wheat for \$3.50 a hektoliter; but the measure used proves too small, the mistake amounting to 3^l in every hektoliter. What was the quantity of wheat delivered to the purchaser, the cost, and the reduction which ought to be made to him on account of the error?

The mistake was 3^{1} in 100^{1} , or he received only 0.97 of 1415^{h} = 1372.55^{h1} . If 1^{h1} of wheat cost \$3.50, 1415^{h1} cost $1415 \times 3.50 = \$4952.50. A reduction of 0.03 of \$4952.50 = \$148.58 ought to be made.

1415 ^{hl}	1415	\$ 4 952.50
0.97	3.50	0.03
9905	70750	\$ 148.5750
12735	4245	
1372.55hl	4952.50	

32. The dimensions of a tile are as follows: length 22^{cm}, width 11^{cm}, thickness 55^{mm}. Find the volume of the tile, and the number of tiles in a pile of 25^{cbm}.

 $55^{\text{mm}} = 5.5^{\text{cm}}$. The volume of a tile is $(22 \times 11 \times 5.5)^{\text{cem}} = 1331^{\text{cem}}$. $25^{\text{cbm}} = 25,000,000^{\text{cem}}$. In the pile there will be $25,000,000 \div 1331 = 18,782$ tiles.

18	8782
1331)25000	0000
1331	
11696	0
10649	8
1049	 20
93	17
110	030
100	648
	3820
:	2662
•	

33. The measurement of a pile of wood shows that a ster could be filled from it 25.68 times. Find the volume of the pile in cubic meters, reckoning the length of the logs to be 1.15^m.

The volume of the pile is $25.68 \times (1 \times 1 \times 1.15)^{cbm} = 29.532^{cbm}$. Ans.

34. A liter of air weighs 1.273s. How much does a cubic meter of air weigh? How many times as heavy as air is water?

 $1^{\text{cbm}} = 1000^{\text{l}}$. Therefore 1^{cbm} of air weighs $1000 \times 1.273^{\text{g}} = 1273^{\text{g}} = 1.273^{\text{kg}}$. Ans.

1cbm of water weighs 1000kg.

Therefore, water is $1000 \div 1.273 = 785.55$ times as heavy as air.

TEACHERS' EDITION.

35. A package of candles that weighs 465% is sold for 28 cents. At the same rate what is the price of a kilogram of candles?

1s of candles costs \$0.28 + 465 = \$0.000602. Therefore 1^{kg} costs $1000 \times $0.000602 = 0.602 . \$0.60. \$0.60. \$0.60.

- 36. How many times will 3.243^t of water fill a liter measure? As 1^t of water will fill a cubic meter, 3.243^t will fill $3.243^{cbm} = 3243^t$. 3243 times. Ans.
- 37. Express in kilograms the weight of 43.4578^{ccm} of pure water. 43.4578^{ccm} of water weighs $43.4578^{\text{gc}} = 0.0434578^{\text{kg}}$. Ans.
- 38. The volume of the axle of an engine is 0.245cbm. Find its weight, if the specific gravity of the iron is 7.8.
 - 0.245cbm of water weighs 0.245t, and 0.245cbm of iron weighs

$$7.8 \times 0.245^{t} = 1.911^{t}$$
. Ans.
$$0.245$$

$$\begin{array}{r} 7.8 \\ \hline 1960 \\ \hline 1715 \\ \hline 1.9110 \end{array}$$

39. Find the volume of a gram of the following substances: proof spirit, specific gravity 0.865; tin, specific gravity 7.291; lead, specific gravity 11.35; copper, specific gravity 8.85; silver, specific gravity 10.47; cork, specific gravity 0.240.

1ccm of water weighs 1s. Hence, the volume of a substance equals 1ccm divided by its specific gravity.

(i.)	(iii.)	(v.)
1.16	0.088	0.095
865)1000.	1135)100.00	1047)100.00
865	9080	9423 ,
1350	9200	5770
865	9080	5235
4850	0.088ccm. Ans.	0.095°cm. Ans.
1.16°cm. Ans.		
	(iv.)	(vi.)
(ii.)	0.113	4.167
0.14	885)100.0	24)100.
7291)1000.0	885	<u>96</u>
7291	1150	40
27090	885	<u>24</u>
0.14ccm. Ans.	2650	160
	0.113ccm. Ans.	144
		4.167ccm. Ans.

40. Olive oil costs 60 cents a | As 1kg costs \$1.87, 11 costs 0.792 kilogram. What is the price of a The specific gravity of liter? olive oil is 0.914.

11 of olive oil weighs 0.914kg. As 1kg costs \$0.60, 11 costs 0.914 \times \$0.60 = \$0.548. Ans.

$$0.914 \\ -0.60 \\ \hline 0.54840$$

41. Pure alcohol costs \$1.87 a kilogram. What is the price of a liter? The specific gravity of alcohol is 0.792.

 \times \$1.87 = \$1.48. Ans.

42. A man wishes to build a shed large enough to hold 135st if the shed is to be of wood: 3^m high and 5^m wide, how long must it be?

 $135^{\text{ct}} = 135^{\text{cbm}}$. The area of one end is $(3 \times 5)^{qm} = 15^{qm}$. Therefore, 11 of alcohol weighs 0.792 kg. the length must be $(135 \div 15)$ m = 9m. 43. In a country where firewood is cut 1.16^m long, what must be the height of the ster that it may hold a cubic meter?

The height must be

$$(1+1.16)^{m} = 0.86207^{m} \cdot Ans.$$

\$20.00, how much would 100kg cost, the cork weighing 0.25 as much as water?

1st of cork weighs 250^{kg} , and costs \$20.00. 100^{kg} will cost $\frac{100}{150}$ of \$20.00 = 0.4 of \$20.00 = \$8.00. Ans.

45. A liter of powder weighs 825s. What will be the volume in cubic centimeters of a charge for a gun if the charge weighs 5s?

The specific gravity of powder is 0.825. It takes $(1 \div 0.825)^{\text{ccm}}$ of powder to weigh 1s; therefore to weigh 5s it takes $(5 \div 0.825)^{\text{ccm}}$ = 6.06^{ccm} . Ans.

46. Out of gold which weighs 19.362 times as much as water, sheets of gold foil are made which are 0.010mm in thickness. What surface will 35 of gold cover?

 $0.010^{\text{mm}} = 0.001^{\text{cm}}$. The volume of the gold is $3^{\text{ccm}} \div 19.362 = 0.154943^{\text{ccm}}$. Therefore the surface is $(0.154943 \div 0.001)^{\text{qcm}} = 154.943^{\text{qcm}}$. Ans.

0.154942
19362)3000.0
19362
106380
96810
95700
77448
182520
174258
82620
77448
51720
38724
12996

47. Find the weight of an oak board 3.25^m long, 0.31^m wide, and 0.04^m thick, if the specific gravity of the oak is 0.808.

 $0.808^{i} = 0.0325624^{i} = 32.5624^{ks}$. gravity of the iron is 7.8.

The volume of the board is 48. Find the weight of a bar $(3.25 \times 0.31 \times 0.04)^{\text{cbm}} = 0.0403^{\text{cbm}}$. of iron having the following 1cbm of oak weighs 0.808t; there-dimensions: length 3.6m, width fore 0.0403^{cbm} weighs 0.0403×6^{cm} , thickness 2^{cm} , if the specific

	Ans.	
3.25	4	$3.6^{\rm m} = 360^{\rm cm}$.
0.31	!	360
325		6
975		2160
1.0075		2
0.04		4320
0.040300		4320
0.0403		7.8
0.808		34560
3224		30240
3224		33696.0
0.0325624		33,6968 = 33.696 kg. Ans.

49. How many lead balls each weighing 27s can be obtained by melting a cubic mass of lead 0.356m on an edge, if the specific gravity of the lead is 11.35?

 $0.355^{\mathrm{m}} = 35.6^{\mathrm{cm}}$.

35.6	45118.016	18966
35.6	11.35	27)512089
2136 1780 1068 1267.36 35.6	225590080 135354048 45118016 45118016 512089.48160g	$ \begin{array}{r} $
760416 633680 380208		178 162
45118.016	18,96 6 . Ans.	169 162

50. Marble costs \$30.95 a cubic meter, and the specific gravity of marble is 2.73. If a block of marble weighs 1260kg, what is its volume and what is it worth?

1^{cbm} of marble weighs 2.73^t . $1260^{kg} = 1.26^t$.

0.4615	0.4615
273)126.0	30.95
1092	23075
1680	41535
1638	13845
420	14.283425
273	
1470	$Volume = 0.4615^{cbm};$
1365	cost = \$14.28. Ans.
<u></u>	•

51. Sea water contains 28 parts, by weight, of salt in 1000. A liter of sea water weighs 1.025^{kg}. How many kilograms of salt can be obtained from 126.276842^{cbm} of sea water?

1ks of sea water contains 0.028ks of salt.

3624.145kg. Ans.
3624.145364
25 8867526
1035470104
0.028
129433.763

52. An empty cask weighs 17.06kg; when filled with water it weighs 275.8kg. How many liters does it hold? How many casks of this size will it take for the wine from a vat containing 3.008cbm?

The cask will hold $275.8^{kg} - 17.06^{kg} = 258.74^{kg}$ of water. It takes 258.74^{l} of water to weigh 258.74^{kg} . Therefore the cask will hold 258.74^{l} . Ans.

 $3.008^{\text{cbm}} = 3008^{\text{l}}$. If one cask holds 258.74^{l} , to hold 3008^{l} it will take $3008 \div 258.74 = 12$ casks. Ans.

275.80kg	12
17.06	25874)300800
258.74kg	25874
200.14-6	42060

53. It takes about 2.048^{hl} of wheat to sow a hektar. How many cubic meters will it take to sow a square kilometer?

 $1^{\text{qkm}} = 100^{\text{ha}}$. 1^{ha} will require $100 \times 204.8^{\text{l}} = 20.480^{\text{l}} = 20.48^{\text{cbm}}$. Ans.

54. A piece of road 1^{km} long and 7^m wide is to be macadamized to the depth of 33^{cm}. What will the work cost at 43 cents a cubic meter?

 $1^{km} = 1000^{m}$; $33^{cm} = 0.33^{m}$.

0.33	2310	
7	0.43	
$\overline{2.31}$	6930	
1000	9240	
2310.	993.30 \$ 993.30. Ans.	

55. A gasometer holds 28,000cbm of gas. How many jets will this gasometer feed for an evening, when each jet burns 1251 an hour, and is used 4 hours?

Each jet will burn $4 \times 125^1 = 500^1$ each evening. $28,000^{\text{cbm}} = 28,000,000^1$. The gasometer will feed $28,000,000 \div 500 = 56,000$ jets.

56. The city of Venice is situated in the midst of a great lake of salt water, communicating with the sea, and all the rain water is caught for the cisterns. Ordinary years the fall of rain in Venice is 82^{cm}; the surface of the city, after the canals have been deducted, is 520^{ha}. Reckoning the population at 115,530, how many liters a day of rain water can each inhabitant have?

 $520^{\text{ha}} = 5,200,000^{\text{qm}}$; $82^{\text{cm}} = 0.82^{\text{m}}$.

The average amount of rain water is $(5,200,000 \times 0.82)^{\text{cbm}} = 4,264,000^{\text{cbm}} = 4,264,000,000^{\text{l}}$.

Each person can use per year $4,264,000,000^{1} \div 115,530$, or, per day, $4,264,000,000^{1} \div (115,530 \times 365) = 101.118^{1}$. Ans.

0.82	115530	101.118
5200000	365	4216845)426400000.
16400000	577650	4216845
410	693180	4715500
4264000.00	346590	4216845
	42168450	4986550
		4216845
		7697050
		4216845
		34802050
		83734760

57. Find the weight of a bar of iron 5.35^m long, 4.56^{cm} thick, and 3.54^{cm} wide. Find, also, the width of an oak beam 4.30^m long, 9.12^{cm} thick, which has the same weight. The specific gravity of the oak to be reckoned at 1.026, that of the iron at 7.788.

 $5.35^{m} = 535^{cm}$. $4.30^{m} = 430^{cm}$. $535 \times 4.56 \times 3.54 \times 7.788 = 67,258.6$. Therefore the weight of the iron is $67,259.6^{kg}$. Ans.

The volume of the oak beam is $67,258.596992^{\text{ccm}} \div 1.026 = 65,554.2^{\text{ccm}}$. The area of one side of the oak beam is $(430 \times 9.12)^{\text{qcm}} = 3921.6^{\text{qcm}}$; therefore the thickness is $(65,554.2 \div 3921.6)^{\text{cm}} = 16.72^{\text{cm}}$.

4.56	16.1424	8636.184
3.54	535	7.788
1824	807120	69089472
2280	4 84272	69089472
1368	807120	60453288
16.1424	8636.1840	60453288
		67258.600992

65554.2	
1026)67258600.992	16.72
6156	3921 6)6555 42 .
5698	39216
5130	263382
5686	235296
5130 ·	280860
***************************************	274512
5560 5130	63480
4300	16.72cm. Ans.
4104	
1969	

58. Find the specific gravity and volume of a body weighing 35kg in air and 30kg in water.

The weight of the water displaced by the body is 5kg.

The weight of the body in air is 35kg.

Therefore the specific gravity is $35 \div 5 = 7$. 5^{kg} of water occupies 5^{l} of space. 5^{l} . Ans.

59. A ster of piled oak wood weighs 425kg; the specific gravity of the wood is 0.74. What is the volume occupied by the spaces between the logs? For how much must 100kg of separate sticks be sold to bring the same amount as when sold at \$2.20 a ster?

If there were no spaces between the logs, the ster of wood would weigh 740^{kg} . Therefore the spaces, if filled with wood, would weigh $740^{kg} - 425^{kg} = 315^{kg}$. Therefore, the volume of the spaces is $(315 \div 740)^{cbm} = 0.42568^{cbm}$. 100^{kg} ought to be sold for $\frac{199}{425}$ of 32.20 = $220 \div 425 = 30.518$.

0.42568	\$ 0.518
74)31.5	425)\$ 220.0
296	2125
190	750
148	425
420	3250
370	
500	0.42568cbm;
444	\$ 0.518. Ans.
	

- 60. Wrought iron sells for \$7.00 per 100kg. A bar of iron 4.5cm wide, 3.3cm thick costs \$5.08; what is its length, reckoning the specific gravity of the iron at 7.4?
- \$7.00 per 100^{kg} is the same as \$0.07 per kilogram. An iron bar that costs \$5.08 must weigh $(5.08 \div 0.07)^{\text{kg}} = 72.57143^{\text{kg}}$, and its volume is $(72.57143 \div 7.4)^{\text{l}} = 9.8069^{\text{l}} = 9806.9^{\text{ccm}}$. The area of an end of the bar is $(4.5 \times 3.3)^{\text{qcm}} = 14.85^{\text{qcm}}$. Therefore the length is $(9806.9 \div 14.85)^{\text{cm}} = 660.4^{\text{cm}} = 6.604^{\text{m}}$. Ans.

9.8069	660.4
74)725.7143	1485)980690.0
666	8910
597	8969
592	8910
514	5900
444	
703	
666	

61. Experiment shows that water weighs 770 times as much as air; and the specific gravity of mercury is 13.6. How many liters of air will it take to weigh as much as a liter of mercury?

Water is 770 times as heavy as air, and mercury is 13.6 times as heavy as water. Therefore mercury is 13.6×770 times as heavy as air.

$$\begin{array}{r}
 13.6 \\
 \hline
 770 \\
 \hline
 9520 \\
 \hline
 9520 \\
 \hline
 10472.0
 \end{array}$$

10,4**5**2¹. Ans.

62. A mass of lead weighing 753ks is made into sheets 0.1mm thick. Find in square meters the surface which can be covered by

the sheets thus obtained. The specific gravity of the lead is 11.3. The volume of the lead is $(753 \div 11.3)^1 = 66.637^1 = 0.066637^{\text{cbm}}$.

 $0.1^{mm} = 0.0001^{m}$. The surface of the lead is

 $(0.066637 \div 0.0001)^{qm} = 666.37^{qm}.$ Ans.

63. A rectangular sheet of tin of uniform thickness is 85cm wide, 1.35m long, and weighs 268s. What is its thickness, if the specific gravity of tin is 7.3?

The volume of the tin is $(268 \div 7.3)^{\text{ccm}} = 33.7109^{\text{ccm}}$; $1.35^{\text{m}} = 135^{\text{cm}}$. The area of the tin is $(135 \times 85)^{\text{qcm}} = 11,475^{\text{qcm}}$; therefore its thickness is $(36.7109 \div 11475)^{\text{cm}} = 0.0032^{\text{cm}}$. Ans.

64. The fine coal which collects about the shafts of the mines and in the coal yards, was for a long time wasted, because it could not be burned in stoves and grates. Now this dust is mixed with tar in proportion of 92^{kg} of dust and 8^{kg} of tar; the mixture is heated, and afterwards pressed in rectangular moulds 14.75^{cm}, by 18.5^{cm}, by 29^{cm}; each one of these blocks weighs 10^{kg}. They are sold at \$3.00 a ton, and make excellent fuel for heating steam boilers. Find the specific gravity of this fuel; also, the sum which would be realized in thus utilizing 800,000^t of coal dust, the cost of tar, mixing, etc., being \$0.50 a ton.

Volume of a block is $(14.75 \times 18.5 \times 29)^{\text{ccm}} = 7913.375^{\text{ccm}} = 7.913375^{\text{l}}$. Specific gravity is $10 \div 7.913375 = 1.264$. $800,000^{\text{t}}$ of coal dust will make $800,000^{\text{t}} \div 0.92 = 869,565.217^{\text{t}}$ of the mixture. $869,565.217^{\text{t}}$ at \$2.50 per ton $= 869,565.217 \times $2.50 = $2,173,913.04$. Ans.

14.75	869565.217	
18.5	92)80000000.	
7375	736	
11800	640	
1475	552	
272.875	880	
29	828	
24 55875	520	
545750	<u>460</u>	
7913.375	600	
(010.010	<u>552</u>	
	480	
1.264	$\frac{460}{200}$	
7913375)10000000.	184	
7913375	160	
20866250	92	
15826750	680	
50395000	644	
47480250	869565.217	
29147500	2.50	
20221000	43478260850	
	1739130434	
	2173913.04250	

65. A bar of iron a millimeter square on the end will break under a tension of 30kg. Find the length at which a suspended bar of iron will break from its own weight, if the specific gravity of the iron is 7.8.

30 kg = 0.03.

The volume of the iron bar is $(0.03 \div 7.8)^{\text{cbm}} = 0.00384615^{\text{cbm}}$. The area of an end of the bar is $1^{\text{qmm}} = 0.000001^{\text{qm}}$. Therefore the length of the bar is

 $(0.00384615 + 0.000001)^{m}$ = 3846.15^{m} .

66. Fifty-three kilograms of starch are obtained from 100kg of wheat. A hektar of land produces 1363 of wheat; a hektoliter of wheat weighs 78kg. If the wheat harvested from a field measuring 2hs and 33qm is taken

to a starch factory, how much starch will be made from it?

 0.53^{kg} of starch is obtained from 1^{kg} of wheat. 1^{l} of wheat weighs 0.78^{kg} . 1^{ha} produces 1363×0.78^{kg} of wheat = 1063.14^{kg} . $2^{ha} 33^{qm} = 2.0033^{ha}$. 2.0033^{ha} produces $2.0033 \times 1063.14^{kg} = 2129.788362^{kg}$ of wheat. The amount of starch is

 $0.53 \times 2129.788362 \text{kg} = 1128.7878 \text{kg}$.

67. A gardener wishes to provide glass for his hotbeds. The beds cover 2.65°; the panes will cover 0.75 of the whole surface, the rest being taken up by the frames and alleys. First, find how many panes measuring 45cm by 37cm it will take to cover the beds; then find the price of the glass, at a cost of 95 cents a square meter.

 $45^{cm} = 0.45^{m}$; $37^{cm} = 0.37^{m}$; $2.65^{a} = 265^{qm}$.

Total area of the glass is 0.75 of $265^{qm} = 198.75^{qm}$. The area of one pane is $(0.45 \times 0.37)^{qm} = 0.1665^{qm}$. Therefore the number of panes needed is $198.75 \div 0.1665 = 1194$. At \$0.95 per square meter, 198.75^{qm} will cost $198.75 \times $0.95 = 188.81 .

0.45	1194	198.75
0.37	1665)1987500	0.95
315	1665	99375
135	3225	178875
0.1665	1665	188.8125
	15600	1194 panes; \$ 188.81. Ans.
	14985	
	6150	

68. A jar full of water weighs 1.325kg; filled with mercury it weighs 12.540ks. Find the capacity and the weight of the jar, if the specific gravity of the mercury is 13.59.

The weight of the jar and the jar full of mercury is 12.540^{kg} . Therefore the difference in weight between the mercury and the water is $12.540^{kg} - 1.325^{kg} = 11.215^{kg}$. 13.59 - 1 = 12.59, the specific gravity of a liquid of which the jar full without the jar weighs 11.215^{kg} . Hence the capacity of the jar is $(11.215 \div 12.59)^1 = 0.89078^1$. 0.89078^k of water weighs 0.89078^k . Hence, the weight of jar is $1.325^{kg} - 0.89078^{kg} = 0.43422^{kg} = 434.22^{g}$.

12.540	0.89078	1.325
1.325	1259)1121.5	0.89078
11.215	10072	0.43422
	11430	
	11331	
	9900	
	8813	
	10870 Cap	pacity=0.890781;)
	10072 wei	$ \begin{array}{ll} \text{pacity} = 0.89078^{1}; \\ \text{ght} = 434.228. \end{array} $

69. A hektoliter of rape seed weighs 63kg, and 32l of oil can be extracted from it. How many kilograms of the seed will it take to make a hektoliter of oil?

 $1^{hl} = 100^{l}$. If 32^{l} of oil can be extracted from 63^{kg} of seed, 1^{l} of oil can be extracted from $63^{kg} \div 32 = 1.96875^{kg}$ of seed, and 100^{l} of oil can be extracted from $100 \times 1.96875^{kg} = 196.875^{kg}$ of seed.

1.96875
32)63.
32
310
288
220
192
280
256
240
224_
160
160

196.875^{kg}. Ans.

70. Common burning gas is 0.97 of the weight of air, and a liter of air weighs 1.2935. In a shop there are 65 jets, each one of which burns 1231 an hour, and is used 5 hours in the winter evenings. Find the weight of the gas used in a month of 26 days, and the expense of lighting the shop, when gas costs 6 cents a cubic meter.

1º of gas weighs $0.97 \times 1.293^{g} = 1.25421^{g}$. 65 jets, each burning 123^{l} an hour, and used 5 hours an evening for 26 days, will use $65 \times 5 \times 26 \times 123^{l} = 1,039,350^{l}$, the weight of which is $1,039,350 \times 1.25421^{g} = 1,303,563.16^{g} = 1303.563^{l}g$. $1,039,350^{l} = 1039.35^{cbm}$. The expense at \$0.96 per cubic meter is $1039.35 \times \$0.06 = \62.36 .

1.293¤	1231	1.25421	1039.35	
0.97	65	1039350	0.06	
9051	6 15	6271050	62.3610	
11637	738	376263	\$ 62.36.	Ans.
1.254215	79951	1128789	w 021001	
	5	376263		
	399751	125421		
	26	1303563.16350		
	239850			
	799 50			
	1039350			

71. A merchant buys one kind of wine at 30 cents a liter, another kind at 21 cents a liter; he mixes the two kinds by putting 51 of the first with 81 of the second. For how much a liter must he sell the mixture in order to gain \$3.75 a hektoliter?

51 at \$0.30 per liter costs \$1.50.

81 at \$0.21 per liter costs \$1.68.

Therefore 13^1 of the mixture costs \$1.50+\$1.68=\$3.18, and 1^1 costs $$3.18 \div 13 = 0.2446 . Again, if \$3.75 per hektoliter is equivalent to a gain of \$0.0375 per liter, to make \$3.75 per hektoliter the merchant must sell the wine for \$0.0375 + \$0.2446 = \$0.2821 per liter. Ans.

\$ 0.30	\$ 0.21	0.2446
5	8	13)3.18
\$ 1.50	\$ 1.68	26
	1.50	
	\$ 3.18	52
		60
		52
		80
		78

72. If it requires 360 tiles to drain an ar of land, what will it cost to drain 17.784ha, when the tiles cost \$20 a thousand, and the expense of laying is the same as the cost of the tiles?

The expense of laying the tiles and their cost is \$40 per thousand. $17.784^{ha} = 1778.4^{a}$. To drain 1778.4^{a} of land 1778.4×360 tiles = 640.224 tiles = 640.224 thousand are needed. 640.224 thousand at \$40 per thousand cost $640.224 \times $40 = $25,608.96$. Ans.

1778.4	640.224
360	40
1067040	256 08 .960
53352	
640224.0	

73. Hewn stone of medium durability ought not to support, as a permanent weight, more than 0.07 of the weight that is required to crush it. A certain kind of stone used for building will be crushed

under a weight of 250kg a square centimeter. What is the greatest height to which a wall constructed of this material can be safely carried, if the specific gravity of the stone is 2.1?

250 per square centimeter is equivalent to 250,000 per square centimeter. 0.07 of 250,000 = 17,500 ought to be the pressure on a square centimeter. Therefore the volume of the imaginary prism ought to be $(17,500 \div 2.1)^{ccm} = 8333.33^{ccm}$, or the height ought to be $8333.33^{ccm} = 83.333^{ccm}$.

83.333m. Ans.

74. Several different kinds of wines are mixed as follows: 2451 at 20 cents a liter, 5471 at 15 cents a liter, 3441 at 25 cents a liter. How much does the mixture cost a liter?

245¹ at \$0.20 per liter costs \$49.00 547¹ at \$0.15 per liter costs \$82.05 344¹ at \$0.25 per liter costs \$86.00 1136¹ of the mixture costs \$217.05

Therefore $1^1 \cos 8217.05 \div 1136 = \0.191 . Ans.

75. A farmer wishes to drain a field of 8.75ha. Each hektar requires 750m of ditches. The opening of these ditches costs 10 cents a running meter; the tiles are 30cm long, and cost \$15 a thousand. He pays 2 cents a meter for laying the tiles, and 4 cents a meter for filling the ditches. What is the cost of draining the field?

There are required $8.75 \times 750^{\rm m} = 6562.5^{\rm m}$ of ditches. The expense of opening the ditches, laying the tiles, and filling the ditches is \$0.10 + \$0.02 + \$0.04 = \$0.16 per meter. $6562.5^{\rm m}$ will cost $6562.5^{\rm m} \times \$0.16 = \1050.00 . $30^{\rm cm} = 0.3^{\rm m}$. For $6562.5^{\rm m}$, $6562.5 \div 0.3 = 21,875$ tiles are necessary. The tiles cost \$15 per thousand. Therefore 21.875 thousand cost $21.875 \times \$15 = \328.13 . Hence cost of draining the field is \$1050.00 + \$328.13 = \$1378.13.

8.75	6562.5	21.875	\$ 1050.	
750	0.16	15	328.13	
43750	393750	109375	\$ 1378.13	Ans.
6125	65625	21875	·	
6562.50	1050.000	328.125		

76. A silver five-franc piece weighs 25%, and is composed of 9 parts of pure silver and 1 part of pure copper. A silver two-franc piece weighs 10%, and is composed of 835 parts of pure silver and 165 parts of pure copper. A silver twenty-centime piece weighs 1%, and has the same composition as the two-franc piece. Find the total weight of pure silver and of pure copper contained in 272 five-franc pieces, 145 two-franc pieces, and 179 twenty-centime pieces.

$$272 \times 25g = 6800g$$
.
 $0.1 \times 6800g = 680g$, copper.
 $6800g - 680g = 6120g$, silver.
 $145 \times 10g = 1450g$.

 $179 \times 1g = 179g$; 1450g + 179g = 1629g.

7480.2155 Ans.

1629 s 0.165	1629€. 268.785
8145 9774 1629	1360.215s, silver.
268.785g, copper.	
1360.215g	268.785■
6120.	680.

948.7858 Ans.

77. The dimensions of the bottom of a rectangular box are 70cm by 50cm. If the box contains exactly a hektoliter of wheat when full, what is the height of the box?

$$1^{\text{hl}} = 100^{\text{l}} = 100,000^{\text{ccm}}.$$

$$\frac{200}{79 \times 59} = \frac{200^{\text{cm}}}{7} = 28.571^{\text{cm}}. \text{ Ans.}$$

78. If a stick of oak timber 54 centimeters wide and 65 centimeters thick costs \$25 at \$16 a cubic meter, what is the length of the stick?

The volume of the stick of timber = $\frac{250000000}{18}$ = $\frac{250000000}{1}$ = 1,562,500000.

	- 1,002,000 .
54	445.156
65	351ø)158250.
270	1404
324	1585
3510	1404
	1810
	1755
	550
	351
	1990
	1755
	2350
•	2106
$445.157^{cm} = 4.45157^{m}$. Ans.	244

79. A rectangular box whose bottom is a square 28cm on a side, and whose height is 19.2cm, is exactly filled with gold twenty-franc pieces, in piles touching each other. If a twenty-franc piece is 35mm in diameter, and 1.28mm thick, what is the value of the gold in the box?

Hence, the number of piles of pieces is 8×8 , or 64, and the number in a pile is 150.

Therefore, the number of pieces = $64 \times 150 = 9600$.

 $9600 \times 20 \text{ francs} = 192,000 \text{ francs. } Ans.$

80. If 1^{hl} of coal yields 1854^{cbin} of gas, and one burner consumes 140^l of gas in an hour, how many hektoliters of coal are required to supply 2800 burners for 144 hours?

144	$140^{l} = 0.14^{cbm}$.	30.44
2800	403200	1854)56448.
115200	0.14	5562
288	1612800	8280
403200	4032	7416
•	56448.00	8640
		7416
		1224
		30.45 ^{hl} . Ans

81. How many liters of water in a cylindrical well 1.96^m in diameter, if the water is 2.84^m deep?

1.96	3.8416
1.96	0.7854
· 1176	153664
1764	192080
196	307328
3.8416	268912
	3.01719264
	2.84
	1206877056
	2413754112
	603438528
	8.5688270976
	$8.568827^{\text{cbm}} = 8568.827$

TEACHERS' EDITION.

Exercise 38. Page 98.

Find the prime factors of:

1. 2. 3. 4.
$$2^{2} \frac{148}{37}$$
 $2^{8} \frac{264}{33}$ $2 \frac{178}{89}$ $3 \frac{183}{61}$ $2^{2} \times 37$. Ans. 11 2 × 89. Ans. 3 × 61. Ans. $2^{3} \times 3 \times 11$. Ans. $2^{3} \times 3 \times 11$. Ans. 11 $\frac{173}{173}$ 11 $\frac{187}{17}$ 2 $\frac{346}{173}$ 78 $\frac{343}{173}$ 1 × 173. Ans. 11 × 17. Ans. 2 × 173. Ans. 78. Ans.

9. 10. 11. 12.
$$2 | 210$$
 $1 | 353$ $2^{5} | 5280$ $3 | 231$ $7 | 77$ $1 | 353$ $3 | 165$ 1×353 . Ans. $5 | 55$ 11 $3 \times 7 \times 11$. Ans.

 $2\times3\times5\times7$. Ans.

 $2^5 \times 3 \times 5 \times 11$. Ans.

1	.3.	14 .	15 .
28	31416	37 1369	28 1368
3	3927	37	3 ² 171
7	1309	37×37 . Ans.	19
11	187		$2^8 \times 3^2 \times 19$. Ans.
	17		

 $2^3 \times 3 \times 7 \times 11 \times 17$. Ans.

16.	17.	18.	19.
13 247	3 327	1 179	1 83
19	109	179	83
13×19 . Ans.	3×109 . Ans.	1×179 . Ans.	1×83 . Ans.
20.	21.		22 .
53 2125	13 2353		1 2333
17	181		2333
$5^3 \times 17$. Ans.	13×181 .	Ans. 1	\times 2333. Ans.

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48. 49. 50. 51.
$$\frac{2^2 \left| 868 \right|}{7} \frac{3^8 \left| 999 \right|}{217} \frac{2 \left| 822 \right|}{37} \frac{2 \left| 822 \right|}{37} \frac{2 \left| 1346 \right|}{673} \frac{673}{31} \frac{3^8 \times 37. \ \textit{Ans.}}{2 \times 3 \times 137. \ \textit{Ans.}}$$
 2 × 673. $\textit{Ans.}$

 $2 \times 3^2 \times 5 \times 7 \times 13$. Ans.

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52.53.54.
$$3^{8} | 7641$$
 $2 | 6234$ $2 | 234$ 283 $3 | 3117$ $3^{2} | 117$ $3^{8} \times 283$. Ans. 1039 13 $2 \times 3 \times 1039$. Ans. $2 \times 3^{2} \times 13$. Ans.

55.56.57.58.
$$3 \lfloor 579 \rfloor$$
 $1 \lfloor 577 \rfloor$ $2^2 \lfloor 212 \rfloor$ $2 \lfloor 126 \rfloor$ 193 577 53 $3^2 \lfloor 63 \rfloor$ 3×193 . Ans. 1×577 . Ans. $2^2 \times 53$. Ans. 7 $2 \times 3^2 \times 7$. Ans.

59. 60. 61.
$$2^{7} | 128$$
 $2^{18} | 8192$ $2 | 8190$ $3^{2} | 4095$ 2^{7} . Ans. 2^{18} . Ans. $5 | 455 | 91$ 13

66.67.
$$3^2 \mid 78309$$
 $3 \mid 25179$ $7 \mid 8701$ $7 \mid 8393$ $11 \mid 1243$ $11 \mid 1199$ 118 109 $3^2 \times 7 \times 11 \times 113$. Ans. $3 \times 7 \times 11 \times 109$. Ans.

	68 .		69 .		70 .	
28	81600	28	48048	2	401478	
22	7700	2	6006	3	200739	
52	1925	3	3003	7	66913	
7	77	7	1001	11	9559	
	11	11	143		869	
$2^5 \times 5^2 \times 7$	×11. Ans.	·	13	$2\times3\times7\times$	11×869. A	ns.

 $2^4 \times 3 \times 7 \times 11$. Ans.

71 .			72 .	
28	278208		3	493185
28	34776		5	164395
32	4347		7	32879
3	483		7	4697
7	161		11	671
	23		·	61
Вх	7×23 .	Ans.	$3 \times 5 \times 7^2$	× 11 ×

 $2^6 \times 3^8 \times 7$

 1×61 . Ans.

Exercise 39. Page 99.

Find the prime factors of:

1. 2. 3. 4.

$$8.4 = 84 \times 0.1$$
. $7.6 = 76 \times 0.1$. $1.08 = 108 \times 0.01$. $0.144 = 144 \times 0.001$.
 $2^{2} \begin{vmatrix} 84 \\ 3 \end{vmatrix} 21$ $2^{2} \begin{vmatrix} 76 \\ 19 \end{vmatrix}$ $2^{2} \begin{vmatrix} 108 \\ 3^{2} \end{vmatrix} 27$ $2^{2} \begin{vmatrix} 108 \\ 3 \end{vmatrix} 27$

 $2^2 \times 3 \times 7 \times 0.1$. Ans. $2^2 \times 19 \times 0.1$. Ans. $2^2 \times 3^8 \times 0.01$. Ans. $2^4 \times 3^2 \times 0.001$. Ans.

5. 6. 7.
$$0.036 = 36 \times 0.001$$
. $0.037 = 37 \times 0.001$. $21.45 = 2145 \times 0.01$. $2^{2} \begin{vmatrix} 36 \\ 3^{2} \end{vmatrix} \frac{1}{9}$ 37 $5 \begin{vmatrix} 715 \\ 715 \\ 1 \end{vmatrix}$ $1 \times 37 \times 0.001$. Ans. $11 \begin{vmatrix} 143 \\ 143 \end{vmatrix}$ $2^{2} \times 3^{2} \times 0.001$. Ans. $2^{2} \times 3^{2} \times 0.001$. Ans.

 $3 \times 5 \times 11 \times 13 \times 0.01$. Ans.

8. 9. 10.
$$14.6 = 146 \times 0.1.$$
 $2.61 = 261 \times 0.01.$ $21.2 = 212 \times 0.1.$
$$2 \underbrace{146}_{73}$$
 $3^2 \underbrace{261}_{29}$ $2^2 \underbrace{212}_{53}$
$$2 \times 73 \times 0.1.$$
 Ans. $3^2 \times 29 \times 0.01.$ Ans. $2^2 \times 53 \times 0.1.$ Ans.

 $2 \times 3 \times 7 \times 11 \times 17 \times 0.01$. Ans.

$$0.00052 = 52 \times 0.00001.$$

$$2^{2} \lfloor \underline{52} \\ 13$$

 $2^2 \times 13 \times 0.00001$. Ans.

14.

$$8.67 = 867 \times 0.01.$$

$$3 \mid 867$$

$$17^2 \mid 289$$

 $3 \times 17^2 \times 0.01$, Ans.

15.

$$48.3 = 483 \times 0.1.$$

$$\begin{array}{r}
3 \mid 483 \\
7 \mid 161 \\
\hline
23
\end{array}$$

 $8 \times 7 \times 23 \times 0.1$. Ans.

16.

$$99.99 = 9999 \times 0.01$$
.

 $3^2 \times 11 \times 101 \times 0.01$. Ans.

17.

$$5.04 = 504 \times 0.01$$
.

$$\begin{array}{c|c}
 2^{8} & 504 \\
 \hline
 3^{2} & 63 \\
 \hline
 7
 \end{array}$$

18.

$$1.485 = 1485 \times 0.001$$
. $0.216 = 216 \times 0.001$.

19.

$$0.216 = 216 \times 0.001$$

 $2^8 \times 3^2 \times 7 \times 0.01$. Ans. $3^8 \times 5 \times 11 \times 0.001$. Ans. $2^8 \times 3^8 \times 0.001$. Ans.

20.

$$34.87 = 3487 \times 0.01$$
.

 $11 \times 317 \times 0.01$. Ans.

21.

$$32.4 = 324 \times 0.1$$
.

 $2^2 \times 3^4 \times 0.1$. Ans.

22.

$$5.115 = 5115 \times 0.001$$
.

 $3 \times 5 \times 11 \times 31 \times 0.001$. Ans.

23.

89

$$71.2 = 712 \times 0.1.$$

$$2^{8} | 712$$

 $2^8 \times 89 \times 0.1$. Ans.

24.

$$2.993 = 2993 \times 0.001.$$

41 | 2993 73

 $41 \times 73 \times 0.001$. Ans.

Exercise 40. Page 102.

- 1. Find the G. C. M. of 27 and 33.
 - $3 \lfloor 27 \rfloor$
- 3. Ans.
- 2. Find the G. C. M. of 13 and

89. 13 | 13

39

13. Ans.

3. Find the G.C.M. of 8 and 28.

$$2^{2} \begin{bmatrix} 8 & 28 \\ 2 & 7 \end{bmatrix}$$
 $2^{2} = 4$. Ans.

4. Find the G. C. M. of 27 and 45.

5. Find the G. C. M. of 81 and 108.

6. Find the G.C.M. of 4, 10, 12.

2. Ans.

7. Find the G.C.M. of 4, 6, 10.

2. Ans.

8. Find the G. C. M. of 9, 12, 21.

3. Ans.

9. Find the G. C. M. of 10, 15, 25.

5. Ans.

10. Find the G.C.M. of 14, 98, 42.

11. Find the G.C.M. of 30, 18, 54.

12. Find the G.C.M. of 14, 56, 42.

13. Find the G.C.M. of 96, 36, 48.

14. Find the G.C.M. of 84, 105, 63.

15. Find the G.C.M. of 24, 60, 84, 128.

16. Find the G.C.M. of 45, 81, 27, 90.

17. Find the G. C. M. of 78, 18, 54, 42.

18. Find the G. C. M. of 98, 28, 70, 42.

19. Find the G.C.M. of 96, 112, 80, 32.

20. Find the G.C.M. of 24, 96, 48, 120.

21. Find the G.C.M. of 84, 252, 168, 210.

22. Find the G. C. M. of 33, 88, 77, 55.

23. Find the G. C. M. of 252, 315, 420, 504.

24. Find the G. C. M. of 128, 192, 320, 368, 432.

25. Find the G. C. M. of 136, 204, 357, 459.

26. Find the G. C. M. of 909, 1414, 2323, 4242.

Exercise 41. Page 104.

1. Find the G.C.M. of 2479 and 3589.

$$2479)3589(1)$$

$$2479$$

$$10 1110$$

$$3 111$$

$$37)2479(67)$$

$$222$$

$$259$$

$$37. Ans. 259$$

2. Find the G. C. M. of 3045 and 6195.

3. Find the G.C.M. of 568 and 712.

4. Find the G. C. M. of 11,023 and 6493.

5. Find the G.C.M. of 1485 and 2160.

6. Find the G.C.M. of 7040 and 7392.

7. Find the G. C. M. of 2760 and 4485.

8. Find the G.C.M. of 1177 and 2675.

9. Find the G. C. M. of 78,473 and 94,653.

10. Find the G. C. M. of 35,143 and 10,283.

$$10283)35143(3)$$

$$30849$$

$$2 \overline{)4294}$$

$$19 \overline{)2147}$$

$$113)10283(91)$$

$$\underline{)1017}$$

$$113$$

$$113. Ans. 113$$

11. Find the G.C.M. of 44,323 and 61,087.

12. Find the G. C. M. of 232,353 and 39,699.

13. Find the G. C. M. of 33,853 and 35,017.

14. Find the G.C.M. of 5115 and 7254.

15. Find the G.C.M. of 2268 and 3348.

16. Find the G.C.M. of 1003 and 2419.

17. Find the G. C. M. of 419 and 52,301.

19. Find the G.C.M. of 4257 and 10,836.

18. Find the G.C.M. of 30,072 and 133,784.

20. Find the G.C.M. of 17,104 and 27,794.

Exercise 42. Page 104.

1. Find the G. C. M. of 855, 1197, 1596.

3	855	1197	1596	
3	285	399	4 532	
5	95	7 133	$7\overline{133}$	
1	19	19	19	
		3×19	$\theta = 57. \ \Delta$	4ns.

2. Find the G. C. M. of 3864, 3404, 3657.

3. Find the G. C. M. of 15,581, 11,115, 13,585.

4. Find the G. C. M. of 2943, 2616, 4578.

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5. Find the G.C.M. of 1177, 1391, 1819.

6. Find the G.C.M. of 4939, 1347, 3143.

7. Find the G. C. M. of 740, 333, 296.

8. Find the G. C. M. of 833, 1785, 1309.

9. Find the G. C. M. of 4994, 7491, 9988, 12,485, 16,571.

Exercise 43. Page 107.

1. Find the L. C. M. of 6, 14, 21.

2. Find the L. C. M. of 8, 12, 3, 24.

24. Ans.

3. Find the L. C. M. of 6, 10, 15.

4. Find the L. C. M. of 9, 12, 18, 4.

5. Find the L.C.M. of 15, 21, 35.

6. Find the L. C. M. of 12, 20, 24.

 $2^2 \times 5 \times 6 = 120$. Ans.

7. Find the L. C. M. of 14, 24, 28.

 $2^2 \times 6 \times 7 = 168$. Ans.

8. Find the L. C. M. of 12, 15, 20.

9. Find the L. C. M. of 16, 24, 32.

 $2^8 \times 3 \times 4 = 96$. Ans.

10. Find the L.C.M. of 21, 33, 77.

11. Find the L.C.M. of 27, 33, 99.

12. Find the L.C.M. of 7, 11, 13.

$$[7 \ 11 \ 13]$$
 $7 \times 11 \times 13 = 1001$. Ans.

13. Find the L. C. M. of 77, 55, 35.

14. Find the L.C.M. of 16, 18, 27, 72.

15. Find the L.C.M. of 10, 12; 22, 33, 60.

 $2 \times 3 \times 11 \times 10 = 660$. Ans.

16. Find the L. C. M. of 15, 16, 18, 20, 22, 24.

 $2^4 \times 3^2 \times 5 \times 11 = 7920$. Ans.

17. Find the L. C. M. of 56, 64, 70, 84, 112.

 $2^6 \times 3 \times 5 \times 7 = 6720$. Ans.

18. Find the L.C.M. of 48, 54, 81, 144, 162.

 $2^4 \times 3^4 = 1296$. Ans.

19. Find the L. C. M. of 75, 100, 120, 150, 180.

10	75	100	120	150	180
2		10	12	15	18
3		ß	в	15	8
			2	5	3

 $2^8 \times 3^2 \times 5^2 = 1800$. Ans.

20. Find the L. C. M. of 112, 168, 196, 224.

 $2^{5} \times 3 \times 7^{2} = 4704$. Ans.

21. Find the L.C.M. of 7, 14, 15, 21, 45.

 $3 \times 14 \times 15 = 630$. Ans.

22. Find the L.C.M. of 16, 25, 81.

 $16 \times 25 \times 81 = 32,400$. Ans.

23. Find the L.C.M. of 26, 39, 52, 65.

 $13 \times 3 \times 4 \times 5 = 780$. Ans.

24. Find the L.C.M. of 80, 72, 225, 48.

 $2^4 \times 225 = 3600$. Ans.

25. Find the L.C.M. of 10, 20, 30, 40, 50, 60.

 $2^8 \times 3 \times 5^2 = 600$. Ans.

26. Find the L.C.M. of 30, 42, 105, 70.

27. Find the L.C.M. of 36, 24, 35, 20.

 $2^8 \times 3^2 \times 35 = 2520$. Ans.

28. Find the L.C.M. of 7, 11, 14, 15.

$$11 \times 14 \times 15 = 2310$$
. Ans.

29. Find the L.C.M. of 12, 18, 27, 63, 28.

 $2^2 \times 3^8 \times 7 = 756$. Ans.

30. Find the L. C. M. of 34, 26, 65, 85, 51, 39.

2	34	26	65	85	51	39
5	17	26 13	65	85	51	39
3			13	17	51	39
					17	13

 $2 \times 3 \times 5 \times 13 \times 17 = 6630$. Ans.

31. Find the L.C.M. of 12, 18, 96, 144.

 $2^5 \times 3^5 = 288$. Ans.

32. Find the L. C. M. of 84, 156, 63, 99.

 $2^{2} \times 3^{2} \times 7 \times 11 \times 13 = 86,036$. Ans.

33. Find the L. C. M. of 17, 51, 119, 210.

$$17 \underbrace{ \begin{bmatrix} 17 & 51 & 119 & 210 \\ \hline 3 & 7 & 210 \end{bmatrix}}_{17 \times 210 = 3570. Ans.}$$

34. Find the L. C. M. of 16, 30, 48, 56, 72.

 $2^{4} \times 3^{2} \times 5 \times 7 = 5040$. Ans.

35. Find the L. C. M. of 27, 33, 54, 69, 132.

2×31×23×22=27,324. Ans.

36. Find the L. C. M. of 15, 26, 39, 65, 180.

 $2^2 \times 3^2 \times 5 \times 13 = 2340$. Ans.

37. Find the L. C. M. of 44, 126, 198, 280, 330.

2	44	126	198	280	330
2	22	63	99	140	W
3	11	63	90	70	165
7		21	33	70	5.6
5		3	83	10	55
			33	2	11

 $2^4 \times 3^2 \times 5 \times 7 \times 11 = 27,720$. Ans.

38. Find the L. C. M. of 50, 338, 675, 975.

 $5^2 \times 3^8 \times 338 = 228,150$. Ans.

39. Find the L. C. M. of 552, 575, 920.

 $2^{4} \times 23 \times 3 \times 25 = 18,800$. Ans.

40. Find the L. C. M. of 228, 304, 342.

 $2^4 \times 3^2 \times 19 = 2736$. Ans.

41. Find the L. C. M. of 1080 and 1260.

$$\begin{array}{c|cccc}
10 & 1080 & 1260 \\
2 & 108 & 126 \\
3^2 & 54 & 63 \\
\hline
6 & 7
\end{array}$$

 $2^8 \times 3^8 \times 5 \times 7 = 7560$. Ans.

42. Find the L.C.M. of 600 and 480.

 $2^{5} \times 3 \times 5^{2} = 2400$. Ans.

43. Find the L.C.M. of 1584 and 1932.

 $2^2 \times 23 \times 17 \times 21 = 32,844$. Ans.

44. Find the L.C.M. of 2530 and 1760.

 $2^{5} \times 5 \times 11 \times 23 = 40,480$. Ans.

45. Find the L.C. M. of 936 and 2925.

 $2^8 \times 3^2 \times 5^2 \times 13 = 23,400$. Ans.

46. Find the L. C. M. of 3432 and 4032.

 $2^8 \times 3 \times 143 \times 168 = 576,576$. Ans.

47. Find the L.C.M. of 1875 and 2425.

 $5^2 \times 75 \times 97 = 181,875$. Ans.

48. Find the L.C.M. of 1632 and 2976.

28	1632	2976
2 ²	204	372
3	51	93
•	17	31

 $2^{5} \times 3 \times 17 \times 31 = 50,592$. Ans.

49. Find the L. C. M. of 1001 and 2233.

 $7 \times 11 \times 13 \times 29 = 29,029$. Ans.

50. Find the L. C. M. of 539 and 1463.

 $7^2 \times 11 \times 19 = 10,241$. Ans.

Exercise 44. Page 108.

1. Find the L. C. M. of 424 and 583.

L. C. M. = $11 \times 424 = 4664$. Ans.

2. Find the L. C. M. of 319 and 407.

L. C. M. $=29 \times 407 = 11,803$. Ans.

3. Find the L. C. M. of 1679 and 1932.

$$\begin{array}{c|c}
4 & 1932 \\
\hline
3 & 161 \\
\hline
23)1679(73) \\
\underline{161} \\
69 \\
69
\end{array}$$

L. C.M. = $73 \times 1932 = 141,036$. Ans.

4. Find the L. C. M. of 1003 and 2419.

$$\begin{array}{r}
 2008 \\
 7 \overline{\smash{\big)}\,413} \\
 \hline
 59)1003(17) \\
 \underline{59} \\
 413 \\
 413
 \end{array}$$

L.C.M. = $17 \times 2419 = 41,123$. Ans.

5. Find the L.C.M. of 1003 and 1357.

L.C.M. = $17 \times 1357 = 23,069$. Ans.

6. Find the L. C. M. of 899 and 961.

$$899)961(1)$$

$$2 | \underline{62}$$

$$31)899(29)$$

$$\underline{62}$$

$$\underline{279}$$

$$279$$

L. C. M. $=29 \times 961 = 27,869$. Ans.

7. Find the L. C. M. of 407, 703, 444.

L. C. M. = $11 \times 19 \times 444 = 92,796$.

Ans.

8. Find the L. C. M. of 411, 959, 2055.

L. C. $M = 7 \times 2055 = 14,385$. Ans.

9. Find the L.C.M. of 221 and 351.

$$\begin{array}{c}
221)351(1) \\
221 \\
10 \overline{\smash{\big)}\ 130} \\
13)221(17) \\
\underline{13} \\
91 \\
91
\end{array}$$

L. C. M. = $17 \times 351 = 5967$. Ans.

10. Find the L. C. M. of 1426 and 989.

 $L.C.M. = 2 \times 31 \times 989 = 61,318.$ Ans.

11. Find the L. C. M. of 3864, 3404, 3657.

12. Find the L. C. M. of 539 and 253.

L. C. M. $=23 \times 539 = 12,397$. Ans.

13. Find the L.C.M. of 2943, 2616, 4578.

14. Find the L.C.M. of 2863 and 1151.

L. C. M. =
$$1151 \times 2863$$

= $3,295,313$. Ans.

15. Find the L. C. M. of 1177, 1391, 1819.

$$107 \underbrace{1177 \quad 1391 \quad 1819}_{11}$$

$$11 \underbrace{1177}_{107}$$

$$107)1391(13)$$

$$\underbrace{\frac{107}{321}}_{321}$$

$$\underbrace{321}_{21}$$

$$L. C. M. = 13 \times 17 \times 1177$$

$$= 260,117.$$
 Ans.

16. Find the L. C. M. of 5317 and 2863.

$$7 \underbrace{2863}_{409)5317(13}$$

$$\underbrace{\frac{409}{1227}}_{1227}$$
L. C. M. = $13 \times 2863 = 37,219$.

Ans.

17. Find the L. C. M. of 12,703 and 12,879.

L. C. M. =
$$12,703 \times 12,879$$

= $163,601,937$. Ans.

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18. Find the L. C. M. of 28,809 and 10,753.

Find the L. C. M. of 4989 and 3143.

L. C. M. = 11 × 3143 = 84,573. Ans. | L.C.M. = 13 × 6137 = 79,891. Ans.

20. Find the L. C. M. of 4199 and 6137.

Exercise 45. Page 112.

Reduce to a whole or a mixed number:

$$\blacksquare \quad \stackrel{\mathbf{44}}{\mathbf{4}} = 24.$$

12.
$$\frac{41}{16} = 3\frac{4}{16}$$
.

3.
$$\frac{31}{4} = 6\frac{1}{2}$$
.

13.
$$\frac{44}{15} = 3$$
.

90
$$\frac{100}{300} = 13.$$

$$241 \quad \frac{133}{33} = 187$$

$$107 \quad \frac{232}{33} = 1833.$$

$$20 \quad ^{4879} = 359.$$

8.
$$\frac{44}{5} = 8\frac{4}{5}$$
.

9.
$$\frac{3}{2} = 4\frac{1}{2}$$
.

19.
$$\frac{1}{16} = 13\frac{5}{16}$$
.

101
$$\frac{19}{2} = 6\frac{1}{3}$$
. 20. $\frac{342}{2} = 11$.

Exercise 46. Page 113.

Reduce to an improper fraction:

4.
$$8 = \frac{44}{6}$$
.

7.
$$8 = \frac{17}{5}$$
.

10.
$$18 = \frac{104}{11}$$
.

8.
$$14 = \frac{148}{18}$$
.

11.
$$12 = \frac{144}{11}$$
.

3.
$$6 = \frac{\pm 0}{5}$$
.

9.
$$9 = \frac{134}{16}$$
.

12.
$$16 = \frac{254}{15}$$
.

Exercise 47. Page 113.

Reduce to an improper fraction:

3.
$$12\frac{4}{11} = \frac{134}{11}$$
.

5.
$$25\frac{1}{3} = \frac{137}{3}$$
.

2.
$$5\frac{a}{10} = \frac{a}{10}$$
.

7.
$$8\frac{5}{12} = \frac{101}{12}$$
.

8.
$$9\frac{9}{14} = \frac{135}{14}$$
.

9.
$$162_{11}^{8} = \frac{1780}{1}$$
. **19.** $14_{11}^{17} = \frac{288}{1}$.

12.
$$3\frac{4}{3} = \frac{1}{4}\frac{7}{5}$$
.

13.
$$10\frac{7}{19} = \frac{197}{19}$$
.

14.
$$12\frac{18}{15} = \frac{198}{15}$$
.

15.
$$84\frac{17}{20} = \frac{1697}{10}$$
.

16.
$$16\frac{1}{2}\frac{3}{3}=\frac{3}{2}\frac{6}{3}$$
.

17.
$$17\frac{1}{12} = \frac{11}{12}$$
.

10.
$$446 = \frac{8}{1}4$$
. **20.** $21\frac{17}{100} = \frac{2117}{100}$. **30.** $37\frac{1}{5} = \frac{296}{75}$.

11.
$$2\frac{108}{108} = \frac{328}{108}$$
. **21.** $6\frac{41}{50} = \frac{341}{50}$.

22.
$$16\frac{8}{25} = \frac{408}{25}$$
.

24.
$$8_{16}^{9} = \frac{187}{16}$$
.

25.
$$12\frac{3}{4} = \frac{51}{4}$$
.

26.
$$27\frac{1}{4} = \frac{5.5}{2}$$
.

27.
$$111\frac{2}{3} = \frac{885}{3}$$
.

18.
$$19\frac{5}{5} = \frac{176}{5}$$
. **28.** $36\frac{35}{35} = \frac{3148}{15}$.

29.
$$11\frac{109}{1000} = \frac{11109}{1000}$$
.

30.
$$371 = 295$$

31.
$$16\frac{1}{12} = \frac{208}{12}$$
.

23.
$$11\frac{19}{24} = \frac{283}{24}$$
. **33.** $108\frac{6}{25} = \frac{2796}{25}$.

34.
$$51\frac{3}{17} = \frac{870}{7}$$
.

35.
$$40\frac{1}{9} = \frac{776}{19}$$
.

36.
$$864\frac{13}{97} = \frac{88821}{97}$$
.

Exercise 48. Page 115.

Reduce to lowest terms:

1.
$$\frac{120}{162} = \frac{1}{1} = \frac{5}{1}$$
. Ans.

2.
$$\frac{105}{135} = \frac{21}{11} = \frac{7}{9}$$
. Ans.

3.
$$\frac{928}{1820} = \frac{116}{165}$$
. Ans.

4.
$$\frac{1}{2}$$
 $\frac{1}{4}$ $\frac{1}{8}$ = $\frac{1}{8}$ $\frac{1}{8}$ = $\frac{1}{1}$ $\frac{1}{8}$. Ans.

5.
$$\frac{1296}{6561} = \frac{144}{126} = \frac{16}{81}$$
. Ans.

6.
$$\frac{2310}{1000} = \frac{231}{100} = \frac{21}{20} = \frac{2}{10}$$
. Ans.

7.
$$\frac{1}{2}\frac{3}{3}\frac{1}{5}\frac{3}{3} = \frac{2}{2}\frac{3}{3}\frac{1}{4} = \frac{7}{6}\frac{7}{8} = \frac{1}{1}\frac{1}{4}$$
. Ans.

8.
$$\frac{3960}{13672} = \frac{495}{1564} = \frac{55}{176} = \frac{5}{16}$$
. Ans.

9.
$$\frac{1818}{1008} = \frac{616}{1001} = \frac{68}{148} = \frac{8}{18}$$
. Ans.

10.
$$\frac{924}{1092} = \frac{231}{273} = \frac{77}{91} = \frac{11}{13}$$
. Ans.

11.
$$\frac{2640}{2570} = \frac{88}{99} = \frac{5}{9}$$
. Ans.

12.
$$\frac{324}{1092} = \frac{31}{273} = \frac{27}{97}$$
. Ans.

13.
$$\frac{6782}{9768} = \frac{1683}{2277} = \frac{153}{207} = \frac{17}{23}$$
. Ans.

14.
$$\frac{6840}{37860} = \frac{171}{684} = \frac{19}{18} = \frac{1}{4}$$
. Ans.

15.
$$\frac{5760}{7000} = \frac{576}{700} = \frac{146}{148}$$
. Ans.

16.
$$\frac{$75}{10000} = \frac{7}{80}$$
. Ans.

17.
$$\frac{2308}{4140} = \frac{552}{1035} = \frac{184}{115} = \frac{8}{15}$$
. Ans.

18.
$$\frac{1915}{1966} = \frac{35}{54}$$
. Ans.

19.
$$\frac{516}{2107} = \frac{12}{49}$$
. Ans.

20.
$$\frac{8872}{91807} = \frac{352}{6187} = \frac{32}{767}$$
. Ans.

21. Reduce to lowest terms 39473.

$$78473)94653(1)$$

$$78473$$

$$10 \overline{\smash{\big|}\,\,} 16180$$

$$2 \overline{\smash{\big|}\,\,} 1618$$

$$809)78473(97)$$

$$\underline{7281}$$

$$\underline{5663}$$

$$5663$$

G. C.
$$M_{\cdot} = 809$$
.

$$\frac{78478}{94658} = \frac{97}{117}$$
. Ans.

$$G. C. M. = 83.$$

$$\frac{17596}{26145} = \frac{212}{315}$$
. Ans.

23. Reduce to lowest terms #1823.

$$44323)61087(1)$$

$$44323$$

$$4 16764$$

$$3 4191$$

$$11 1397$$

$$127)44323(349)$$

$$381$$

$$622$$

$$508$$

$$1143$$

$$1143$$

G. C. M. = 127. $\frac{44823}{61027} = \frac{349}{242}$. Ans.

24. Reduce to lowest terms 1243.

G. C. $M_{\bullet} = 113$.

$$\frac{389}{1243} = \frac{8}{11}$$
. Ans.

25. Reduce to lowest terms \(\frac{1}{2}\frac{77}{7}\).

G. C. M = 107.

$$\frac{1177}{1675} = \frac{11}{25}$$
. Ans.

26. Reduce to lowest terms 11448.

$$\frac{1}{1}\frac{1}{3}\frac{1}{3}\frac{1}{3}\frac{1}{3}=\frac{3}{1}\frac{1}{3}\frac{1}{3}=\frac{3}{1}\frac{1}{3}$$
. Ans.

G.C.M. = 109.

27. Reduce to lowest terms 14141.

G. C. M.=179.

$$\frac{14141}{6289} = \frac{79}{91}$$
. Ans.

28. Reduce to lowest terms 425571.

$$\frac{128571}{100000} = \frac{47619}{11111} = \frac{15878}{10000} = \frac{1448}{10000}$$
$$= \frac{1}{11} = \frac{3}{1}. \quad Ans.$$

Exercise 49. Page 115.

1. Reduce ‡ to 20ths.

$$\frac{3}{4} = \frac{5 \times 3}{5 \times 4} = \frac{15}{20}.$$

2. Reduce 3 to 24ths.

$$\frac{2}{3} = \frac{8 \times 2}{8 \times 3} = \frac{16}{24}$$

3. Reduce § to 50ths.

$$\frac{3}{5} = \frac{10 \times 3}{10 \times 5} = \frac{30}{50}$$

4. Reduce $\frac{7}{13}$ to 39ths.

$$\frac{7}{13} = \frac{3 \times 7}{3 \times 13} = \frac{21}{39}$$

5. Reduce $\frac{5}{18}$ to 90ths.

$$\frac{5}{18} = \frac{5 \times 5}{5 \times 18} = \frac{25}{90}$$

6. Reduce 3 to 108ths.

$$\frac{2}{9} = \frac{12 \times 2}{12 \times 9} = \frac{24}{108}.$$

$$\frac{3}{16} = \frac{9 \times 3}{9 \times 16} = \frac{27}{144}.$$

8. Reduce 7 to 144ths.

$$\frac{7}{18} = \frac{8 \times 7}{8 \times 18} = \frac{56}{144}.$$

$$\frac{7}{12} = \frac{13 \times 7}{13 \times 12} = \frac{91}{156}.$$

Exercise 50. Page 116.

1. Find the product of
$$\frac{3}{4} \times 2$$
.

$$\frac{3}{4} \times 2 = \frac{3}{2} = 1\frac{1}{2}$$
. Ans.

2. Find the product of
$$\frac{1}{4} \times 9$$
.

$$\frac{3}{4} \times 9 = \frac{27}{4} = 6\frac{3}{4}$$
. Ans.

3. Find the product of
$$10 \times \frac{3}{4}$$
.

$$\frac{2}{10} \times \frac{2}{5} = 4. Ans.$$

4. Find the product of
$$15 \times \frac{3}{5}$$
.

$$15 \times \frac{3}{3} = 15$$
. Ans.

5. Find the product of
$$\frac{9}{21} \times 7$$
.

$$\frac{3}{9} \times 7 = 3$$
. Ans.

6. Find the product of
$$16 \times \S$$
.

$$\overset{2}{\cancel{16}} \times \frac{5}{\cancel{8}} = 10. Ans.$$

7. Find the product of
$$\frac{1}{4} \times 2$$
.

$$\frac{5}{8} \times 2 = \frac{5}{4} = 1\frac{1}{4}$$
. Ans.

8. Find the product of
$$\frac{2}{15} \times 5$$
.

$$\frac{2}{15} \times 5 = \frac{2}{5}. Ans.$$

9. Find the product of
$$27 \times \S$$
.

$$\frac{3}{27} \times \frac{5}{9} = 15$$
. Ans.

10. Find the product of
$$\frac{18}{10} \times 2$$
.

$$\frac{13}{20} \times 2 = \frac{13}{10} = 1_{10}^{8}. Ans.$$

11. Find the product of
$$\frac{1}{2} \times 3$$
.

$$\frac{13}{20} \times 3 = \frac{39}{20} = 1\frac{19}{20}. Ans.$$

12. Find the product of
$$\frac{18}{18} \times 4$$
.

$$\frac{13}{20} \times 4 = \frac{13}{5} = 2\frac{3}{5}. Ans.$$

13. Find the product of $5 \times \frac{13}{13}$.

$$5 \times \frac{13}{29} = \frac{13}{4} = 31$$
. Ans.

14. Find the product of
$$6 \times \frac{18}{20}$$
.

$$\overset{3}{\cancel{6}} \times \frac{13}{\cancel{20}} = \frac{39}{10} = 3_{\cancel{10}}^{\cancel{9}}. \text{ Ans.}$$

- 15. Find the product of $7 \times \frac{13}{20}$. $7 \times \frac{13}{20} = \frac{91}{20} = 4\frac{1}{20}$. Ans.
- 16. Find the product of $8 \times \frac{13}{20}$. $8 \times \frac{13}{29} = \frac{26}{5} = 5\frac{1}{3}$. Ans.
- 17. Find the product of $\frac{13}{20} \times 10$. $\frac{13}{20} \times 10 = \frac{13}{2} = 6\frac{1}{2}$. Ans.
- 18. Find the product of $\frac{13}{20} \times 12$. $\frac{13}{20} \times 12 = \frac{39}{5} = 7\frac{4}{5}$. Ans.
- 19. Find the product of $\frac{13}{20} \times 15$. $\frac{13}{20} \times 15 = \frac{39}{4} = 9\frac{3}{4}$. Ans.
- 20. Find the product of $\frac{18}{20} \times 20$. $\frac{13}{20} \times 20 = 13$. Ans.
- 21. Find the product of $\frac{5}{36}$ of 324. $\frac{5}{36}$ of 324 = 45. Ans.
- 22. Find the product of $\frac{7}{13}$ of 273. $\frac{21}{13}$ of $\frac{21}{273} = 147$. Ans.
- 23. Find the product of $\frac{19}{11}$ of 242. $\frac{10}{11}$ of $\frac{22}{242} = 220$. Ans.

- 24. Find the product of $340 \times \frac{8}{17}$.

 20. $\frac{8}{349} \times \frac{8}{17} = 160$. Ans.
- 25. Find the product of $450 \times \frac{7}{10}$.

 45. $\frac{45}{439} \times \frac{7}{19} = 315$. Ans.
- 26. Find the product of $\frac{6}{100} \times 1000$. $\frac{6}{100} \times 1000$. $\frac{6}{100} \times 1000 = 60$. Ans.
- 27. Find the product of $\frac{9}{50} \times 210$. $\frac{9}{50} \times 210 = \frac{189}{5} = 37\frac{4}{5}$. Ans.
- 28. Find the product of $\frac{12}{25} \times 90$. $\frac{12}{25} \times \frac{18}{90} = \frac{216}{5} = 43\frac{1}{5}. \text{ Ans.}$
- 29. Find the product of § of 434. $\frac{62}{7}$ of 434 = 310. Ans.
- 30. Find the product of $468 \times \frac{1}{9}$. $\frac{52}{468} \times \frac{11}{9} = 572$. Ans.
- 31. Find the product of $30 \times \frac{12}{11}$. $30 \times \frac{12}{11} = \frac{360}{11} = 32\frac{8}{11}$. Ans.
- 32. Find the product of $100 \times \frac{16}{15}$. $100 \times \frac{16}{15} = \frac{320}{3} = 106\frac{2}{3}$. Ans.

33. Find the product of
$$\frac{35}{12} \times 54$$
.

$$\frac{25}{12} \times \frac{9}{54} = \frac{225}{2} = 112\frac{1}{2}. \quad Ans.$$

$$\frac{9}{72} \times \frac{19}{16} = \frac{171}{2} = 85\frac{1}{2}. \quad Ans.$$

34. Find the product of
$$\frac{1}{44} \times 48$$
.

34. Find the product of
$$\frac{31}{32} \times 48$$
. $\frac{21}{32} \times 48 = \frac{63}{2} = 31\frac{1}{2}$. Ans.

35. Find the product of
$$72 \times \frac{13}{18}$$
.

$$\frac{9}{72} \times \frac{19}{16} = \frac{171}{2} = 85\frac{1}{2}. Ans.$$

$$\frac{15}{32}$$
 of $128 = 60$. Ans.

Exercise 51. Page 118.

Find the product of:

$$\frac{2}{3}$$
 of $\frac{7}{11} = \frac{14}{15}$. Ans.

$$\frac{3}{7} \text{ of } 2\frac{1}{10} = \frac{3}{7} \times \frac{21}{10} = \frac{9}{10}. \text{ Ans.} \qquad \qquad 2\frac{2}{5} \times 2\frac{1}{2} = \frac{12}{5} \times \frac{3}{2} = 6. \text{ Ans.}$$

$$\frac{3}{7} \text{ of } \frac{5}{9} = \frac{5}{21} \cdot Ans.$$

4.
$$23 \times 21$$

$$2\frac{2}{5} \times 2\frac{1}{2} = \frac{12}{5} \times \frac{5}{2} = 6$$
. Ans.

5.
$$44 \times 24$$
.

$$4\frac{4}{5} \times 2\frac{1}{7} = \frac{24}{5} \times \frac{15}{7} = \frac{72}{7} = 10^{2}$$
. Ans.

6.
$$44 \times 91$$
.

$$4\frac{5}{8} \times 9\frac{1}{8} = \frac{29}{6} \times \frac{28}{3} = \frac{406}{9} = 45\frac{1}{9}$$
. Ans.

7. $\frac{1}{2}$ of $\frac{3}{2}$ of 10.

$$\frac{1}{3} \text{ of } \frac{3}{5} \text{ of } 19 = 2. Ans.$$

8. 4 of 4 of 4.

$$\frac{2}{3}$$
 of $\frac{3}{4}$ of $\frac{2}{3} = \frac{1}{3}$. Ans.

9.
$$\frac{1}{2} \times \frac{5}{6} \times \frac{5}{7} \times \frac{4}{3}$$
.

$$\frac{4}{5} \times \frac{5}{6} \times \frac{8}{7} \times 4\frac{1}{5} = \frac{2}{5} \times \frac{3}{6} \times \frac{3}{7} \times \frac{21}{5} = \frac{6}{5} = 1\frac{1}{5}. Ans.$$

10.
$$\frac{5}{6} \times 4\frac{1}{2}$$
. $\frac{5}{6} \times 4\frac{1}{2} = \frac{5}{6} \times \frac{9}{2} = \frac{15}{4} = 3\frac{3}{4}$. Ans.

11. \$ of \$\tag{0}\$ of \$ of \$ of \tag{15}\$.

$$\frac{8}{9} \text{ of } \frac{9}{10} \text{ of } \frac{5}{7} \text{ of } \frac{3}{4} \text{ of } \frac{1}{5} \text{ of } 15\frac{3}{4} = \frac{\cancel{3}}{\cancel{9}} \times \frac{\cancel{9}}{\cancel{10}} \times \frac{\cancel{5}}{\cancel{7}} \times \frac{\cancel{3}}{\cancel{4}} \times \frac{\cancel{1}}{\cancel{5}} \times \frac{\cancel{93}}{\cancel{4}} = \frac{27}{20} = 1\frac{7}{20}. \text{ Ans.}$$

12. $5\frac{4}{5} \times 8\frac{3}{5}$.

$$5\frac{3}{4} \times 8\frac{3}{5} = \frac{23}{4} \times \frac{42}{5} = \frac{483}{10} = 48\frac{3}{10}$$
. Ans.

13. $\frac{7}{4} \times \frac{4}{7} \times \frac{7}{15} \times 7\frac{1}{2}$

$$\frac{2}{3} \times \frac{4}{7} \times \frac{7}{15} \times 7_{\frac{1}{2}} = \frac{2}{3} \times \frac{4}{7} \times \frac{7}{15} \times \frac{15}{2} = \frac{4}{3} = 1_{\frac{1}{3}}. Ans.$$

14. \(\frac{3}{5}\) of \(\frac{10}{27}\) of \(\frac{9}{20}\) of \(8\frac{1}{3}\).

$$\frac{3}{5}$$
 of $\frac{10}{27}$ of $\frac{9}{20}$ of $8\frac{1}{5} = \frac{3}{5} \times \frac{19}{27} \times \frac{9}{29} \times \frac{25}{3} = \frac{5}{6}$. Ans.

15. $\frac{1}{11} \times \frac{20}{21} \times \frac{25}{45} \times 2\frac{10}{10}$.

$$\frac{8}{11} \times \frac{20}{21} \times \frac{35}{48} \times 2\frac{10}{19} = \frac{8}{11} \times \frac{20}{21} \times \frac{35}{48} \times \frac{48}{19} = \frac{800}{627} = 1\frac{17}{8}. Ans.$$

16.
$$\frac{42}{43} \times \frac{13}{105} \times 1_{\frac{7}{308}}$$
. $\frac{21}{42} \times \frac{13}{105} \times \frac{13}{105} \times 1_{\frac{7}{308}} = \frac{\cancel{42}}{\cancel{43}} \times \frac{\cancel{13}}{\cancel{105}} \times \frac{\cancel{315}}{\cancel{308}} = \frac{117}{946}$. Ans.

17. $\frac{5}{8} \times \frac{120}{121} \times \frac{55}{85} \times 17$.

$$\frac{3}{8} \times \frac{129}{121} \times \frac{69}{83} \times 17 = \frac{90}{11} = 8\frac{2}{11}. Ans.$$

18. $\frac{25}{25} \times \frac{27}{27} \times \frac{58}{88} \times 1\frac{29}{25}$.

$$\frac{38}{39} \times \frac{52}{57} \times \frac{69}{86} \times 1_{\frac{20}{3}} = \frac{\cancel{38}}{\cancel{39}} \times \frac{\cancel{52}}{\cancel{57}} \times \frac{\cancel{69}}{\cancel{86}} \times \frac{\cancel{43}}{\cancel{23}} = \frac{4}{3} = 1_{\frac{1}{2}}. \text{ Ans.}$$

19. $\frac{1}{2}$ of $\frac{3}{4}$ of $\frac{3}{4}$ of $\frac{3}{4}$ of $\frac{3}{4}$ of $\frac{3}{10}$ of 10.

$$\frac{1}{2}$$
 of $\frac{2}{8}$ of $\frac{3}{4}$ of $\frac{5}{8}$ of $\frac{6}{7}$ of $\frac{7}{8}$ of $\frac{9}{9}$ of $\frac{9}{19}$ of $19 = \frac{5}{4} = 1$. Ans.

20. 7 of 4 of 80.

$$\frac{7}{25}$$
 of $\frac{8}{11}$ of $39 = \frac{336}{55} = 6\frac{6}{55}$. Ans.

21. $\frac{118}{158} \times \frac{85}{126} \times \frac{13}{15} \times 1\frac{3}{2}$.

$$\frac{113}{355} \times \frac{85}{226} \times \frac{12}{35} \times 1\frac{1}{4} = \frac{113}{355} \times \frac{85}{226} \times \frac{12}{35} \times \frac{7}{4} = \frac{51}{710}. Ans.$$

22. $\frac{7}{4} \times \frac{8}{4} \times \frac{4}{10} \times \frac{4}{5}$ of $\frac{5}{4}$ of $\frac{3}{4}$ of 8.

$$\frac{7}{8} \times \frac{3}{4} \times \frac{8}{11} \times \frac{4}{5}$$
 of $\frac{5}{8}$ of $\frac{3}{4}$ of $8 = \frac{63}{44} = 1\frac{19}{44}$. Ans.

23. 13 of \$8 of \$17.

$$\frac{2}{13} \text{ of } \frac{39}{49} \text{ of } \frac{13}{52} = \frac{1}{15}. \text{ Ans.}$$

$$\frac{2}{13} \text{ of } \frac{39}{49} \text{ of } \frac{52}{117} = \frac{1}{15}.$$

24. $\frac{3}{11} \times \frac{7}{12} \times \frac{22}{68} \times 48.$

$$\frac{g}{11} \times \frac{7}{12} \times \frac{22}{63} \times \frac{8}{48} = 8.$$
 Ans.

25. 18 of 7 of 15 of 12.

$$\frac{39}{49}$$
 of $\frac{7}{65}$ of $\frac{25}{42}$ of $12 = \frac{3}{4}$. Ans.

26. 13 × 41 × 1.

$$1\frac{2}{3} \times 4\frac{1}{2} \times \frac{3}{8} = \frac{5}{3} \times \frac{9}{2} \times \frac{3}{8} = \frac{45}{16} = 2\frac{18}{16}$$
. Ans.

27. $2\frac{1}{5} \times 1\frac{3}{7} \times 1\frac{1}{15} \times 8$.

$$24 \times 14 \times 113 \times 8 = \frac{22}{9} \times \frac{19}{7} \times \frac{28}{15} \times 8 = \frac{1408}{27} = 52\frac{4}{27}$$
. Ans.

28.
$$3\frac{1}{7} \times 2\frac{1}{2}$$
 of $1\frac{4}{13} \times 1\frac{4}{11}$.

$$3\frac{5}{7} \times 2\frac{1}{2}$$
 of $1\frac{5}{13} \times 1\frac{4}{11} = \frac{26}{7} \times \frac{5}{2} \times \frac{21}{13} \times \frac{15}{11} = \frac{225}{11} = 20\frac{5}{11}$. Ans.

29.
$$\frac{11}{12} \times 5\frac{1}{3} \times 4\frac{1}{3} \times \frac{7}{22} \times 5$$
.

$$\frac{11}{12} \times 5\frac{1}{8} \times 4\frac{1}{8} \times \frac{7}{22} \times 5 = \frac{11}{12} \times \frac{\cancel{16}}{\cancel{3}} \times \frac{\cancel{33}}{\cancel{8}} \times \frac{7}{\cancel{22}} \times 5 = \frac{385}{12} = 32\frac{1}{12}. Ans.$$

30.
$$\frac{2}{5}$$
 of $\frac{7}{15} \times 8^2 \times \frac{6}{29}$ of $1\frac{1}{18}$.

$$\frac{2}{5} \text{ of } \frac{7}{15} \times 8\frac{7}{7} \times \frac{6}{29} \text{ of } 1\frac{17}{18} = \frac{2}{5} \times \frac{7}{15} \times \frac{58}{7} \times \frac{2}{29} \times \frac{35}{18} = \frac{28}{45} \text{ Ans.}$$

31.
$$\frac{17}{12} \times \frac{27}{15} \times \frac{128}{158}$$
.

$$\frac{17}{82} \times \frac{9}{27} \times \frac{41}{123} = \frac{9}{76} \quad Ans.$$

32.
$$\frac{188}{188} \times \frac{17}{63} \times \frac{248}{1719}$$
.

$$\frac{\frac{4}{292}}{\frac{465}{465}} \times \frac{\frac{191}{573}}{\frac{657}{657}} \times \frac{\frac{248}{248}}{\frac{1719}{9}} = \frac{32}{405} \quad Ans.$$

$$\frac{5}{1205} = \frac{2}{8}$$

$$\frac{712}{2763} = \frac{5}{1535}$$

$$\frac{1535}{1968} = \frac{50}{243}$$
Ans.

34.
$$\frac{4}{25} \times 7\frac{1}{7} \times 6\frac{2}{3} \times \frac{21}{80}$$
.

$$\frac{4}{25} \times 7\frac{1}{7} \times 6\frac{2}{3} \times \frac{21}{80} = \frac{4}{23} \times \frac{20}{7} \times \frac{20}{3} \times \frac{21}{80} = 2. \quad Ans.$$

35.
$$12\frac{1}{2} \times \frac{8}{15} \times 16\frac{2}{8} \times \frac{9}{50}$$
.

$$12\frac{1}{2} \times \frac{8}{15} \times 16\frac{2}{3} \times \frac{9}{50} = \frac{2\cancel{5}}{\cancel{2}} \times \frac{\cancel{5}}{\cancel{5}} \times \frac{\cancel{5}\cancel{9}}{\cancel{3}} \times \frac{\cancel{9}}{\cancel{5}\cancel{9}} = 20. \quad Ans.$$

36.
$$37\frac{1}{2} \times \frac{1}{2}\frac{3}{5} \times \frac{19}{19} \times \frac{1}{2}\frac{1}{3}$$
.

$$37\frac{1}{4} \times \frac{12}{25} \times \frac{10}{11} \times \frac{11}{40} = \frac{73}{2} \times \frac{12}{23} \times \frac{19}{11} \times \frac{11}{49} = \frac{9}{2} = 4\frac{1}{2}$$
. Ans.

37.
$$\frac{5}{16} \times \frac{9}{20} \times \frac{4}{21} \times 2\frac{1}{3}$$
.

$$\frac{5}{16} \times \frac{9}{20} \times \frac{4}{21} \times 2\frac{1}{3} = \frac{5}{16} \times \frac{\cancel{9}}{\cancel{20}} \times \frac{\cancel{4}}{\cancel{21}} \times \cancel{\cancel{3}} = \frac{1}{16} \quad Ans.$$

38.
$$8\frac{1}{2} \times \frac{4}{12} \times 1\frac{1}{17} \times \frac{4}{5}$$
.

$$8\frac{1}{4} \times \frac{5}{12} \times 1\frac{1}{17} \times \frac{4}{5} = \frac{17}{2} \times \frac{5}{12} \times \frac{18}{17} \times \frac{4}{5} = 3.$$
 Ans.

39.
$$62\frac{1}{2} \times \frac{9}{50} \times \frac{2}{5} \times 15$$
.

$$62\frac{1}{2} \times \frac{9}{50} \times \frac{2}{3} \times 15 = \frac{\cancel{125}}{\cancel{2}} \times \frac{\cancel{9}}{\cancel{50}} \times \frac{\cancel{2}}{\cancel{3}} \times 15 = \frac{225}{\cancel{2}} = 112\frac{1}{\cancel{2}}. \quad Ans.$$

$$\frac{8}{75} \times 87\frac{1}{2} \times \frac{3}{10} \times \frac{1}{7} = \frac{\cancel{3}}{\cancel{3}} \times \frac{\cancel{173}}{\cancel{2}} \times \frac{\cancel{3}}{\cancel{10}} \times \frac{1}{\cancel{7}} = \frac{2}{5} \cdot Ans.$$

$$1\frac{1}{8} \times 1\frac{1}{10} \times 3\frac{3}{11} \times \frac{1}{16} = \frac{19}{9} \times \frac{11}{19} \times \frac{36}{11} \times \frac{1}{16} = \frac{1}{4}$$
. Ans.

$$6\frac{3}{8} \times \frac{15}{22} \times \frac{8}{9} \times \frac{3}{8} = \frac{33}{33} \times \frac{3}{15} \times \frac{8}{9} \times \frac{3}{8} = \frac{3}{2} = 1\frac{1}{2}$$
. Ans.

43.
$$\frac{7}{18}$$
 of $\frac{9}{14}$ of $\frac{85}{86}$ of 10^{2} .

$$\frac{7}{18}$$
 of $\frac{9}{14}$ of $\frac{35}{36}$ of $10^2_1 = \frac{7}{18} \times \frac{9}{14} \times \frac{35}{36} \times \frac{72}{7} = \frac{5}{2} = 2\frac{1}{2}$. Ans.

44.
$$\frac{11}{68} \times 2\frac{19}{88} \times 1\frac{5}{8} \times 27$$
.

$$\frac{11}{68} \times 2\frac{19}{88} \times 1\frac{5}{8} \times 27.$$

$$\frac{11}{68} \times 2\frac{19}{88} \times 1\frac{5}{8} \times 27 = \frac{11}{68} \times \frac{85}{33} \times \frac{14}{9} \times 27 = \frac{35}{2} = 17\frac{1}{2}. Ans.$$

45.
$$2\frac{1}{28} \times 1\frac{3}{68} \times \frac{7}{180} \times 2\frac{4}{19}$$
.
 $2\frac{1}{28} \times 1\frac{3}{68} \times \frac{7}{180} \times 2\frac{4}{19} = \frac{19}{\cancel{57}} \times \frac{\cancel{5}}{\cancel{63}} \times \frac{\cancel{7}}{\cancel{180}} \times \frac{\cancel{42}}{\cancel{19}} = \frac{19}{72}$. Ans.

46. $\frac{27}{120} \times \frac{13}{120} \times \frac{13}{12} \times 12\frac{2}{12}$.

$$\frac{27}{44} \times 1_{\frac{29}{120}} \times \frac{13}{60} \times 12_{\frac{2}{9}} = \frac{\cancel{27}}{\cancel{44}} \times \frac{\cancel{149}}{\cancel{129}} \times \frac{\cancel{13}}{\cancel{60}} \times \frac{\cancel{119}}{\cancel{9}} = \frac{\cancel{1937}}{\cancel{960}} = 2_{\frac{17}{960}}. Ans.$$

47.
$$\frac{112}{119} \times 1_{\frac{3}{25}} \times \frac{35}{38} \times \frac{7}{32}$$
.
$$\frac{112}{119} \times 1_{\frac{3}{25}} \times \frac{85}{98} \times \frac{7}{32} = \frac{112}{119} \times \frac{28}{25} \times \frac{85}{98} \times \frac{7}{32} = \frac{1}{5}$$
. Ans.

48.
$$3\frac{1}{5} \times 2\frac{5}{36} \times 1\frac{5}{21} \times \frac{14}{35}$$
.

$$3\frac{1}{5} \times 2\frac{5}{36} \times 1\frac{5}{21} \times \frac{18}{35} = \frac{\cancel{28}}{\cancel{9}} \times \frac{\cancel{77}}{\cancel{36}} \times \frac{\cancel{27}}{\cancel{22}} \times \frac{\cancel{18}}{\cancel{35}} = \frac{21}{5} = 4\frac{1}{5}$$
. Ans.

49.
$$1\frac{1}{25} \times \frac{22}{63} \times \frac{7}{18} \times 1\frac{1}{44}$$
.
 $1\frac{1}{25} \times \frac{22}{63} \times \frac{7}{18} \times 1\frac{1}{44} = \frac{\cancel{36}}{\cancel{25}} \times \frac{\cancel{22}}{\cancel{63}} \times \frac{\cancel{7}}{\cancel{18}} \times \frac{\cancel{45}}{\cancel{44}} = \frac{1}{5}$. Ans.

50.
$$15\frac{3}{7} \times \frac{7}{36} \times \frac{19}{63} \times \frac{42}{57}$$
.
 $15\frac{3}{7} \times \frac{7}{36} \times \frac{19}{63} \times \frac{42}{57} = \frac{\cancel{108}}{\cancel{7}} \times \frac{\cancel{7}}{\cancel{36}} \times \frac{\cancel{19}}{\cancel{63}} \times \frac{\cancel{42}}{\cancel{57}} = \frac{2}{3}$. Ans.

$$\frac{\cancel{162}}{\cancel{637}} \times \frac{\cancel{91}}{\cancel{9}} \times \frac{1}{\cancel{25}} \times \frac{\cancel{35}}{\cancel{54}} = \frac{1}{15} \cdot Ans.$$

52.
$$1\frac{9}{247} \times 1\frac{28}{58} \times \frac{828}{432} \times \frac{117}{242}$$
.
$$1\frac{9}{247} \times 1\frac{28}{58} \times \frac{323}{432} \times \frac{117}{272} = \frac{236}{247} \times \frac{81}{53} \times \frac{323}{432} \times \frac{117}{272} = \frac{27}{53}$$
. Ans.

53.
$$\frac{4}{4} \times \frac{6}{11} \times 6\frac{3}{7} \times 9\frac{3}{5} \times 2\frac{1}{2} \times 63 \times \frac{13}{144}$$
.

$$\frac{4}{9} \times \frac{3}{11} \times 63 \times 93 \times 21 \times 63 \times \frac{13}{144} = \frac{2}{9} \times \frac{3}{11} \times \frac{43}{7} \times \frac{48}{5} \times \frac{5}{2} \times \frac{9}{3} \times \frac{13}{144} = 104. \text{ Ans.}$$

54.
$$6\frac{1}{4} \times 11\frac{3}{7} \times 16\frac{4}{11} \times \frac{2}{13}$$
 of $\frac{7}{80}$ of $\frac{1}{80}$ of $\frac{1}{80}$.

 $\frac{2}{7} \times 11\frac{3}{7} \times 16\frac{4}{11} \times \frac{2}{13}$ of $\frac{7}{80}$ of $\frac{1}{90} = \frac{13}{2} \times \frac{89}{7} \times \frac{180}{11} \times \frac{2}{13} \times \frac{7}{80} \times \frac{1}{90} = \frac{2}{11}$. Ans.

55.
$$2\frac{3}{4} \times 7\frac{7}{11} \times 2 \times 1\frac{1}{4} \times \frac{3}{56} \times \frac{7}{27} \times \frac{27}{49}$$
.

$$2\frac{1}{4} \times 7\frac{7}{11} \times 2 \times 1\frac{1}{4} \times \frac{3}{56} \times \frac{7}{27} \times \frac{27}{49} = \frac{11}{4} \times \frac{84}{11} \times 2 \times \frac{4}{3} \times \frac{3}{56} \times \frac{7}{27} \times \frac{27}{49} = \frac{3}{7} \cdot Ans.$$

Exercise 52. Page 119.

Find the product of:

1.
$$9 \times 6\frac{5}{6} = 61\frac{1}{2}$$
. **17.** $15 \times 39\frac{1}{2} = 3142\frac{1}{2}$. **33.** $12 \times 48\frac{24}{25} = 587\frac{13}{25}$.

2.
$$8 \times 17\frac{1}{5} = 137\frac{3}{5}$$
. **18.** $6 \times 8\frac{3}{5} = 51\frac{3}{5}$. **34.** $11 \times 24\frac{4}{5} = 268\frac{3}{5}$.

3.
$$19 \times 5\frac{1}{4} = 99\frac{3}{4}$$
. 19. $11 \times 8\frac{4}{5} = 96\frac{4}{5}$. 35. $7 \times 19\frac{3}{5} = 137\frac{1}{5}$.

4.
$$7 \times 12\frac{1}{3} = 86\frac{1}{3}$$
. 20. $100 \times 6\frac{2}{3} = 666\frac{2}{3}$. 36. $8 \times 16\frac{1}{4} = 130$. 5. $10 \times 15\frac{1}{2} = 155$. 21. $5 \times 3\frac{1}{3} = 15\frac{2}{3}$. 37. $5 \times 29\frac{1}{5} = 145\frac{2}{3}$.

6.
$$6 \times 1\frac{7}{8} = 11\frac{1}{4}$$
. 22. $6 \times 17\frac{1}{7} = 102\frac{4}{7}$. 38. $16 \times 3\frac{3}{7} = 54\frac{4}{7}$.

7.
$$12 \times 2\frac{1}{4} = 33$$
. 23. $32 \times 6\frac{1}{4} = 204\frac{1}{4}$. 39. $19 \times 12\frac{1}{17} = 229\frac{2}{17}$.

8.
$$17 \times 6\frac{1}{3} = 104\frac{1}{3}$$
. **24.** $13 \times 3\frac{1}{3} = 44\frac{1}{3}$. **40.** $23 \times 42\frac{1}{5} = 985\frac{1}{6}$.

9.
$$19 \times 1_{\frac{1}{19}} = 20$$
. 25. $12 \times 6_{\frac{3}{5}} = 79_{\frac{1}{5}}$. 41. $18 \times 12_{\frac{7}{5}} = 231_{\frac{3}{4}}$.

10.
$$24 \times 16\frac{5}{6} = 404$$
. **26.** $8\frac{2}{11} \times 12 = 98\frac{2}{11}$. **42.** $22 \times 22\frac{1}{22} = 485$.

11.
$$32 \times 22\frac{3}{5} = 716$$
. **27.** $20\frac{1}{4} \times 5 = 101\frac{1}{4}$. **43.** $12 \times 161\frac{1}{16} = 1942\frac{1}{16}$.

12.
$$40 \times 8\frac{1}{6} = 328$$
. **28.** $6\frac{2}{3} \times 18 = 120$. **44.** $9 \times 144\frac{1}{6} = 1297\frac{1}{2}$.

13.
$$41 \times 9\frac{1}{6} = 375\frac{6}{6}$$
. **29.** $11 \times 11\frac{1}{6} = 122\frac{2}{6}$. **45.** $10 \times 112\frac{7}{6} = 1127\frac{7}{6}$.

14.
$$18 \times 7\frac{1}{5} = 140\frac{1}{5}$$
. **30.** $18 \times 12\frac{1}{5} = 230\frac{1}{5}$. **46.** $14 \times 42\frac{1}{5} = 595\frac{1}{5}$.

15.
$$19 \times 6\frac{4}{18} = 119\frac{1}{3}$$
. **31.** $36 \times 4\frac{1}{6} = 150$. **47.** $161 \times 4\frac{2}{6} = 751\frac{1}{3}$.

16.
$$20 \times 5\frac{1}{2} = 106\frac{2}{3}$$
. **32.** $12 \times 20\frac{2}{3} = 243\frac{2}{3}$. **48.** $140 \times 5\frac{7}{12} = 781\frac{2}{3}$.

Exercise 53. Page 120.

1. Divide 34 by 6.

$$\frac{24}{35} \div 6 = \frac{1}{6} \times \frac{24}{35} = \frac{4}{35}. Ans.$$

2. Divide # by 5.

$$\frac{10}{11} \div 5 = \frac{1}{5} \times \frac{\cancel{10}}{11} = \frac{2}{11}. Ans.$$

3. Divide # by 8.

$$\frac{3}{7} \div 8 = \frac{1}{8} \times \frac{3}{7} = \frac{3}{56}$$
. Ans.

4. Divide 183 by 7.

$$18\frac{3}{5} \div 7 = \frac{1}{7} \times \frac{56}{3} = 2\frac{3}{5}. Ans.$$

5. Divide § by §.

$$\frac{5}{8} \div \frac{3}{4} = \frac{4}{3} \times \frac{5}{8} = \frac{5}{6}$$
. Ans.

6. Divide 13 by 3.

$$\frac{12}{16} + \frac{3}{8} = \frac{\cancel{8}}{\cancel{3}} \times \frac{\cancel{12}}{\cancel{16}} = 2. \text{ Ans.}$$

7. Divide 1½ by 3½.

$$1\frac{3}{4} \div 3\frac{1}{4} = \frac{7}{4} \div \frac{10}{3} = \frac{3}{10} \times \frac{7}{4} = \frac{21}{40}$$
. Ans.

8. Divide 51 by 43.

$$5\frac{1}{5} \div 4\frac{2}{5} = \frac{26}{5} \div \frac{14}{3} = \frac{3}{14} \times \frac{13}{5} = \frac{39}{35} = 1\frac{4}{35}$$
. Ans.

9. Divide 83 by 41.

$$8\frac{2}{9} + 4\frac{1}{9} = \frac{74}{9} + \frac{37}{9} = \frac{9}{37} \times \frac{74}{9} = 2$$
. Ans.

10. Divide 71 by 43.

$$7\frac{1}{5} \div 4\frac{2}{7} = \frac{36}{5} \div \frac{30}{7} = \frac{7}{30} \times \frac{30}{5} = \frac{42}{25} = 1\frac{1}{25}$$
. Ans.

11. Divide 64 by 91.

$$6\frac{3}{4} \div 9\frac{1}{2} = \frac{27}{4} \div \frac{19}{2} = \frac{2}{19} \times \frac{27}{4} = \frac{27}{38}$$
. Ans.

12. Divide 83 by 43.

$$8\frac{2}{3} \div 4\frac{2}{3} = \frac{26}{3} + \frac{14}{3} = \frac{3}{14} \times \frac{26}{3} = \frac{13}{7} = 14$$
. Ans.

13. Divide 3 by 14.

$$3\frac{1}{9} \div \frac{1}{17} = \frac{35}{9} \div \frac{14}{27} = \frac{27}{14} \times \frac{35}{9} = \frac{15}{2} = 7\frac{1}{2}$$
. Ans.

14. Divide 4\$ by 6\$.

$$4\frac{3}{7} \div 6\frac{5}{9} = \frac{31}{7} \div \frac{62}{9} = \frac{9}{32} \times \frac{31}{7} = \frac{9}{14}$$
. Ans.

15. Divide 5 by 43.

$$5 \div 4\frac{3}{7} = 5 \div \frac{30}{7} = \frac{7}{30} \times 5 = \frac{7}{6} = 1\frac{1}{6}$$
. Ans.

16. Divide 43 by 3.

$$4\frac{2}{3} + \frac{7}{8} = \frac{14}{3} \div \frac{7}{8} = \frac{8}{7} \times \frac{14}{3} = \frac{16}{3} = 5\frac{1}{3}$$
. Ans.

17. Divide 8 by 6.

$$8\frac{2}{5} \div 6\frac{1}{7} = \frac{43}{5} \div \frac{43}{7} = \frac{7}{43} \times \frac{43}{5} = \frac{7}{5} = 1\frac{2}{5}$$
. Ans.

18. Divide 84 by 110.

$$8\frac{1}{5} + 1\frac{1}{10} = \frac{44}{5} + \frac{11}{10} = \frac{19}{11} \times \frac{44}{5} = 8$$
. Ans.

19. Divide 100 by 63.

$$100 + 6\frac{3}{3} = 100 + \frac{20}{3} = \frac{3}{20} \times 100 = 15$$
. Ans.

20. Divide 14 by 18.

$$\frac{14}{15} + \frac{12}{25} = \frac{25}{12} \times \frac{14}{15} = \frac{35}{18} = 1\frac{17}{18}. \quad Ans.$$

21. Divide 31 by 5.

$$3\frac{1}{8} + 5 = \frac{25}{8} + 5 = \frac{1}{8} \times \frac{25}{8} = \frac{5}{8} \cdot Ans.$$

22. Divide 100 by 331.

$$100 \div 33\frac{1}{3} = 100 \div \frac{100}{3} = \frac{3}{199} \times 199 = 3$$
. Ans.

23. Divide 100 by 374.

$$100 \div 37\frac{1}{2} = 100 \div \frac{75}{2} = \frac{2}{73} \times \cancel{100} = \frac{8}{3} = 2\frac{1}{3}. Ans.$$

24. Divide 71 by 61.

$$7\frac{1}{7} \div 6\frac{1}{4} = \frac{50}{7} \div \frac{25}{4} = \frac{4}{25} \times \frac{20}{7} = \frac{8}{7} = 1\frac{1}{7}$$
. Ans.

25. Divide 1 by 1.

$$\frac{1}{9} \div \frac{1}{11} = 11 \times \frac{1}{9} = \frac{11}{9} = 13$$
. Ans.

26. Divide 63 by 32.

$$6\frac{2}{5} \div 32 = \frac{32}{5} \div 32 = \frac{1}{32} \times \frac{32}{5} = \frac{1}{5}$$
. Ans.

27. Divide 31 by 31.

$$3\frac{1}{7} \div 3\frac{3}{7} = \frac{22}{7} \div \frac{24}{7} = \frac{7}{24} \times \frac{11}{7} = \frac{11}{12}$$
 Ans.

28. Divide $1\frac{7}{15}$ by $\frac{11}{25}$.

$$1_{15}^{7} \div \frac{11}{25} = \frac{22}{15} \div \frac{11}{25} = \frac{5}{25} \times \frac{2}{22} = \frac{10}{3} = 3\frac{1}{3}$$
. Ans.

29. Divide 113 by §.

$$11\frac{1}{8} \div \frac{8}{9} = \frac{56}{5} \div \frac{8}{9} = \frac{9}{8} \times \frac{56}{5} = \frac{63}{5} = 12\frac{3}{5}. \text{ Ans.}$$

30. Divide 100 by 831.

$$100 \div 83\frac{1}{3} = 100 \div \frac{250}{3} = \frac{3}{250} \times 100 = \frac{6}{5} = 1\frac{1}{3}. \text{ Ans.}$$

31. Divide 50 by 163.

$$50 + 16\frac{3}{3} = 50 + \frac{50}{3} = \frac{3}{50} \times 50 = 3$$
. Ans.

32. Divide 11 by 11.

$$\frac{15}{22} \div 1\frac{1}{2} = \frac{15}{22} \div \frac{3}{2} = \frac{2}{3} \times \frac{15}{22} = \frac{5}{11}. \quad Ans.$$

33. Divide 111 by 12.

$$1\frac{13}{38} + 1\frac{2}{19} = \frac{51}{38} + \frac{21}{19} = \frac{19}{21} \times \frac{51}{38} = \frac{17}{14} = 1\frac{3}{14}$$
. Ans.

34. Divide 201 by 5.

$$20\frac{1}{4} \div 5 = \frac{81}{4} \div 5 = \frac{1}{5} \times \frac{81}{4} = \frac{81}{20} = 4\frac{1}{20}$$
. Ans.

35. Divide 163 by 4.

$$16\frac{3}{4} \div \frac{4}{9} = \frac{50}{3} \div \frac{4}{9} = \frac{\cancel{9}}{\cancel{4}} \times \frac{\cancel{50}}{\cancel{3}} = \frac{75}{2} = 37\frac{1}{2}. \quad Ans.$$

36. Divide 22 by 16 3.

$$22\frac{2}{9} + 16\frac{2}{9} = \frac{200}{9} \div \frac{50}{3} = \frac{3}{50} \times \frac{200}{9} = \frac{4}{3} = 1\frac{1}{3}. \quad Ans.$$

37. Divide 20% by 11%.

$$20\frac{5}{9} \div 1\frac{19}{27} = \frac{185}{9} \div \frac{37}{27} = \frac{27}{37} \times \frac{185}{9} = 15. \quad Ans.$$

38. Divide 163 by 111.

$$16\frac{3}{3} \div 11\frac{1}{3} = \frac{50}{3} \div \frac{100}{9} = \frac{\frac{3}{9}}{\frac{199}{2}} \times \frac{\cancel{59}}{\cancel{3}} = \frac{3}{2} = 1\frac{1}{2}. \quad Ans.$$

39. Divide 331 by 284.

$$33\frac{1}{3} \div 28\frac{1}{3} = \frac{100}{3} \div \frac{200}{7} = \frac{7}{200} \times \frac{100}{3} = \frac{7}{6} = 1\frac{1}{6}. \quad Ans.$$

40. Divide 477 by 173.

$$47\frac{7}{6} + 17\frac{1}{6} = \frac{430}{9} + \frac{86}{5} = \frac{5}{86} \times \frac{\cancel{430}}{9} = \frac{25}{9} = 2\frac{7}{6}$$
. Ans.

41. Divide 18# by $1\frac{5}{21}$.

$$18\frac{1}{7} \div 1\frac{1}{21} = \frac{130}{7} \div \frac{26}{21} = \frac{3}{26} \times \frac{130}{7} = 15. \quad Ans.$$

42. Divide 374 by 147.

$$37\frac{4}{5} \div 1\frac{4}{17} = \frac{189}{5} \div \frac{21}{17} = \frac{17}{21} \times \frac{189}{5} = \frac{153}{5} = 30\frac{2}{5}$$
. Ans.

43. Divide 34 of 21 by 11 of 21.

34 of
$$2\frac{1}{3} \div 1\frac{1}{3}$$
 of $2\frac{1}{3} = \frac{19}{5}$ of $\frac{5}{2} \div \frac{3}{2}$ of $\frac{19}{9} = \frac{19}{5} \times \frac{5}{2} \times \frac{2}{3} \times \frac{3}{19} = 3$. Ans.

44. Divide $2\frac{1}{7}$ by $3\frac{1}{7}$ of $1\frac{1}{18}$.

$$2\frac{3}{7} + 3\frac{1}{8} \text{ of } 1\frac{1}{15} = \frac{16}{7} \div \frac{10}{3} \text{ of } \frac{16}{15} = \frac{\cancel{16}}{\cancel{7}} \times \frac{\cancel{3}}{\cancel{16}} \times \frac{\cancel{15}}{\cancel{16}} = \frac{\cancel{9}}{\cancel{14}}$$
 Ans.

45. Divide $2\frac{9}{17}$ of $5\frac{1}{2}$ by $7\frac{3}{4}$.

$$2\frac{9}{11}$$
 of $5\frac{1}{2} + 7\frac{3}{4} = \frac{31}{11}$ of $\frac{11}{2} + \frac{31}{4} = \frac{31}{11} \times \frac{11}{2} \times \frac{2}{31} = 2$. Ans.

46. Divide $5\frac{9}{4}$ of $8\frac{1}{4}$ of $1\frac{4}{7}$ by $2\frac{1}{10}$ of $5\frac{9}{4}$.

$$5\frac{3}{5} \text{ of } 8\frac{1}{5} \text{ of } 1\frac{4}{7} \div 2\frac{1}{10} \text{ of } 5\frac{5}{5} = \frac{28}{5} \text{ of } \frac{25}{3} \text{ of } \frac{11}{7} \div \frac{21}{10} \text{ of } \frac{50}{9}$$

$$= \frac{28}{5} \times \frac{25}{3} \times \frac{11}{7} \times \frac{2}{7} \times \frac{2}{59} = \frac{44}{7} = 6\frac{3}{7}. \text{ Ans.}$$

Exercise 54. Page 121.

Find the quotient of:

1.
$$31\frac{7}{4} \div 5 = 6\frac{8}{6}$$
. 5. $42\frac{9}{7} \div 6 = 7\frac{1}{7}$. 9. $48\frac{24}{25} \div 12 = 4\frac{2}{3}$.

9.
$$4834 \div 12 = 43$$

2.
$$16\frac{7}{6} + 6 = 2\frac{43}{54}$$
.

$$6. \ 49\frac{4}{5} \div 7 = 7\frac{4}{35}.$$

2.
$$16\frac{7}{5} + 6 = 2\frac{43}{5}$$
. **6.** $49\frac{4}{5} + 7 = 7\frac{4}{35}$. **10.** $24\frac{4}{5} + 11 = 2\frac{2}{5}$.

3.
$$147 \div 2 = 77$$
.

7.
$$524 \div 8 = 64$$

3.
$$14\frac{3}{7} + 2 = 7\frac{1}{7}$$
. 7. $52\frac{4}{7} + 8 = 6\frac{4}{7}$. 11. $19\frac{3}{5} \div 7 = 2\frac{4}{5}$.

4.
$$33\frac{1}{4} \div 7 = 4\frac{16}{31}$$

4.
$$33\frac{1}{8} \div 7 = 4\frac{16}{11}$$
. **8.** $44\frac{4}{11} \div 12 = 3\frac{23}{13}$. **12.** $29\frac{1}{6} \div 8 = 3\frac{3}{12}$.

12.
$$29\frac{1}{6} \div 8 = 3\frac{3}{4}\frac{1}{6}$$
.

Exercise 55. Page 122.

Find the value of:

1.
$$2\frac{1}{5}$$
 of $2\frac{1}{2} + \frac{3}{14}$ of $3\frac{2}{3} = \frac{11}{5} \times \frac{5}{2} \times \frac{14}{3} \times \frac{3}{11} = 7$.

2.
$$\frac{5}{9}$$
 of $6\frac{2}{3}$ of $\frac{6}{25} \div 5\frac{1}{2} = \frac{5}{9} \times \frac{\frac{4}{29}}{\frac{29}{3}} \times \frac{\frac{2}{9}}{\frac{25}{3}} \times \frac{2}{11} = \frac{16}{99}$

3.
$$\frac{3}{10} \div \frac{2}{5}$$
 of $2\frac{1}{4}$ of $1\frac{5}{7} = \frac{3}{19} \times \frac{3}{2} \times \frac{4}{9} \times \frac{7}{12} = \frac{7}{36}$.

4.
$$\frac{3}{10} \div \left(\frac{2}{5} \times 2\frac{1}{4} \times 1\frac{5}{7}\right) = \frac{3}{10} \times \frac{3}{2} \times \frac{4}{9} \times \frac{7}{12} = \frac{7}{36}$$
.

5.
$$\frac{7}{9}$$
 of $\frac{15}{16} + 1_{27}$ of $1_{\frac{11}{15}} = \frac{7}{9} \times \frac{15}{16} \times \frac{27}{28} \times \frac{35}{46} = \frac{1565}{2944}$

6.
$$\frac{3}{4}$$
 of $\frac{5}{6} + \left(\frac{5}{8} \times \frac{4}{11}\right) = \frac{3}{4} \times \frac{5}{6} \times \frac{2}{5} \times \frac{11}{4} = \frac{11}{4} = 2\frac{3}{4}$.

7.
$$\frac{3}{7}$$
 of $\frac{14}{27} \div \frac{11}{13}$ of $\frac{26}{27} = \frac{3}{7} \times \frac{\cancel{14}}{\cancel{27}} \times \frac{\cancel{13}}{11} \times \frac{\cancel{27}}{\cancel{26}} = \frac{3}{11}$.

8.
$$\frac{3}{8}$$
 of $\frac{32}{33} \div \frac{18}{19}$ of $\frac{76}{81} = \frac{3}{8} \times \frac{\cancel{32}}{\cancel{33}} \times \frac{\cancel{19}}{\cancel{18}} \times \frac{\cancel{9}}{\cancel{18}} = \frac{9}{22}$.

9.
$$\frac{2}{7}$$
 of $1\frac{7}{16} \div \frac{27}{43}$ of $\frac{53}{81} = \frac{2}{7} \times \frac{23}{16} \times \frac{43}{27} \times \frac{81}{53} = \frac{2967}{2968}$.

10.
$$\frac{4}{7}$$
 of $\frac{23}{30} \div \frac{8}{35}$ of $4 = \frac{4}{7} \times \frac{23}{39} \times \frac{35}{8} \times \frac{1}{4} = \frac{23}{48}$

11.
$$\frac{9}{10}$$
 of $\frac{110}{111} \div \frac{3}{4}$ of $1\frac{1}{11} = \frac{\frac{3}{9}}{\frac{19}{19}} \times \frac{\frac{11}{119}}{111} \times \frac{4}{3} \times \frac{11}{\frac{12}{3}} = \frac{121}{111} = 1\frac{10}{111}$.

12.
$$\frac{2}{5}$$
 of $\frac{26}{27}$ of $\frac{5}{13} \div \left(\frac{1}{2} \times \frac{3}{4}\right) = \frac{2}{5} \times \frac{\frac{2}{26}}{\frac{27}{3}} \times \frac{5}{13} \times 2 \times \frac{4}{3} \times \frac{9}{4} = \frac{8}{9}$

13.
$$\frac{2}{5}$$
 of $\frac{5}{6}$ of $\frac{16}{25} \div \frac{4}{3}$ of $\frac{1}{15}$ of $1\frac{7}{11}$

$$= \frac{2}{3} \times \frac{3}{6} \times \frac{\cancel{16}}{\cancel{25}} \times \frac{\cancel{3}}{\cancel{4}} \times \cancel{15} \times \frac{11}{\cancel{18}} = \frac{22}{15} = 1\frac{7}{15}.$$

14.
$$\binom{7}{9} \div \frac{11}{18} \div (5\frac{6}{17} \div 4\frac{13}{14}) = \frac{7}{9} \times \frac{\cancel{18}}{11} \times \frac{\cancel{17}}{\cancel{91}} \times \frac{\cancel{189}}{\cancel{34}} = \frac{13}{11} = 1\frac{2}{11}.$$

15.
$$(14\frac{2}{5} + 4\frac{8}{5}) \div (3\frac{1}{12} \div 9\frac{2}{5}) = \frac{44}{3} \times \frac{9}{44} \times \frac{12}{47} \times \frac{47}{5} = \frac{36}{5} = 7\frac{1}{5}.$$

16.
$$\frac{3}{5}$$
 of $\frac{10}{33}$ of $8\frac{1}{4} + 3\frac{1}{11}$ of $\frac{1}{17}$ of $5\frac{1}{2}$

$$= \frac{3}{5} \times \frac{\cancel{10}}{\cancel{33}} \times \frac{\cancel{33}}{\cancel{4}} \times \frac{\cancel{33}}{\cancel{4}} \times \cancel{17} \times \frac{\cancel{2}}{\cancel{11}} = \frac{3}{2} = 1\frac{1}{2}.$$

Exercise 56. Page 122.

1. If § of a ton of hay costs \$ 15, what is the cost of one ton?

\$
$$15 \div \frac{5}{6} = \frac{6}{5} \times \$ \stackrel{3}{\cancel{15}} = \$ 18$$
. Ans.

2. 15 is § of what number?

$$15 \div \frac{5}{6} = \frac{6}{5} \times 15 = 18$$
. Ans.

3. If \$ of a roll of carpeting is worth \$75, what is the whole roll worth?

$$\$75 \div \frac{6}{7} = \frac{7}{6} \times \$75 = \frac{\$175}{2} = \$87.50.$$
 Ans.

4. A man sold $6\frac{2}{3}$ yards of cloth, which was $\frac{4}{15}$ of the whole piece. How many yards were there in the piece?

$$6\frac{3}{3} \div \frac{4}{15} = \frac{5}{4} \times \frac{5}{20} = 25$$
. Ans.

5. A farmer sold 3 of his hay for \$195.60. What was the value of his entire crop of hay?

\$ 195.60
$$+\frac{3}{7} = \frac{7}{3} \times$$
\$ $195.69 =$ \$ 456.40. Ans.

6. 213 is 14 of what number?

$$21\frac{3}{3} \div \frac{18}{17} = \frac{17}{13} \times \frac{\cancel{65}}{3} = \frac{85}{3} = 28\frac{1}{3}$$
. Ans.

7. 62 is 14 of what number?

$$6\frac{3}{5} \div \frac{1}{2} = \frac{3}{14} \times \frac{4}{56} = 12$$
. Ans.

8. $2\frac{13}{12}$ is $\frac{19}{11}$ of what number?

$$2\frac{18}{22} \div \frac{19}{11} = \frac{11}{19} \times \frac{\frac{3}{57}}{\frac{22}{2}} = \frac{3}{2} = 1\frac{1}{2}$$
. Ans.

9. If \$ of an acre of land is worth \$32, what is the value of an acre?

$$\$32 \div \frac{3}{7} = \frac{7}{3} \times \$32 = \$\frac{224}{3} = \$74\frac{2}{3}$$
. Ans.

10. If $\frac{4}{7}$ of a bushel of wheat is worth 48 cents, what is the value of $2\frac{7}{12}$ bushels of wheat?

$$48 \div \frac{4}{5} = \frac{5}{4} \times \overset{12}{\cancel{4}} = 60.$$
 $2\frac{7}{12} \times 60 = \frac{31}{\cancel{12}} \times \overset{5}{\cancel{9}} = 155.$ $155 \text{ cents} = \$1.55.$ Ans.

11. If $\frac{1}{7}$ of a ton of hay is worth \$15, what is the value of $7\frac{1}{3}$ tons of hay?

\$15 +
$$\frac{5}{7} = \frac{7}{5} \times \$ \stackrel{3}{15} = \$ 21.$$
 7\frac{1}{5} \times \\$21 = \\$154. Ans.

12. If § of a cord of wood is worth \$4, find the value of 7 cords of wood.

$$\$4 \div \frac{5}{6} = \frac{6}{5} \times \$4 = \$\frac{24}{5} = \$4\frac{4}{5}.$$
 $7 \times \$4\frac{4}{5} = \$33\frac{4}{5} = \$33.60.$ Ans.

13. If $\frac{4}{11}$ of a barrel of apples is worth 44 cents, what is the value of 12 barrels of apples?

$$44 + \frac{4}{11} = \frac{11}{4} \times \cancel{44} = 121.$$
 $12 \times 121 = 1452.$ $1452 \text{ cents} = \$14.52.$ Ans.

14. \$125 is 1 more than (that is, 5 of) what sum of money?

\$125 ÷
$$\frac{5}{4}$$
 = $\frac{4}{5}$ × \$125 = \$100. Ans.

15. \$132 is \(\frac{1}{4} \) less than what sum of money?

$$\$132 + \frac{3}{4} = \frac{4}{8} \times \$132 = \$176$$
. Ans.

16. 495 is \(\frac{1}{2} \) more than what number?

$$495 + \frac{9}{8} = \frac{8}{9} \times \cancel{495} = 440$$
. Ans.

17. 217 is \(\frac{1}{2}\) less than what number?

$$217 \div \frac{7}{8} = \frac{8}{7} \times \frac{31}{217} = 248$$
. Ans.

18. 495 is $\frac{2}{18}$ less than what number?

$$495 \div \frac{11}{13} = \frac{13}{11} \times \cancel{495} = 585$$
. Ans.

19. 495 is 18 more than what number?

$$495 + \frac{15}{13} = \frac{13}{15} \times \frac{33}{495} = 429$$
. Ans.

20. If § of a yard of silk is worth \$1, find the value of 4 yards of silk.

$$\$1 \div \frac{4}{5} = \frac{5}{4} \times \$1 = \$\frac{5}{4}.$$
 $\cancel{4} \times \$\frac{5}{\cancel{4}} = \$5.$ Ans.

21. If $\frac{2}{3}$ of a yard of linen is worth 60 cents, what is the value of $2\frac{1}{3}$ yards of linen?

$$60 \div \frac{2}{3} = \frac{3}{2} \times \cancel{60} = 90.$$
 $2\frac{1}{3} \times 90 = 210.$ 210 cents = \$2.10. Ans.

22. If a man who owned \(\frac{1}{2} \) of a schooner sold \(\frac{1}{2} \) of his share for \(\frac{1}{2} \) 1200, what was the value of the schooner?

$$\frac{3}{4} \times \frac{1}{3} = \frac{1}{4}$$
. \$1200 ÷ $\frac{1}{4}$ = 4 × \$1200 = \$4800. Ans.

23. One fourth of one third of three sevenths of a number is 60. What is the number?

$$\frac{1}{4} \times \frac{1}{3} \times \frac{3}{7} = \frac{1}{28}$$
. $60 + \frac{1}{28} = 28 \times 60 = 1680$. Ans.

24. Three fourths of two ninths of six sevenths of a number is 125. What is the number?

$$\frac{3}{4} \times \frac{2}{9} \times \frac{9}{7} = \frac{1}{7}$$
. $12\frac{5}{7} \div \frac{1}{7} = 7 \times 12\frac{5}{7} = 89$. Ans.

25. If $\frac{5}{16}$ of the goods in a store were sold for \$1000, what was the value of the whole stock of goods?

$$$1000 + \frac{5}{16} = \frac{16}{5} \times $1999 = $3200. Ans.$$

26. If $\frac{5}{32}$ of a farm is worth \$1200, what is the value of the whole farm?

\$ 1200 +
$$\frac{5}{32}$$
 = $\frac{32}{5}$ × \$ 1200 = \$ 7680. Ans.

Exercise 57. Page 125.

1. Change 1, 3, 5 to similar fractions.

The L. C.
$$D = 30$$
.

$$\therefore \frac{1}{2}, \frac{2}{5}, \frac{5}{6} = \frac{15}{30} \frac{12}{30}. Ans.$$

2. Change $\frac{2}{3}$, $\frac{5}{3}$, $\frac{7}{10}$ to similar fractions.

The L. C. D. =
$$360$$
.

$$\therefore \frac{2}{3}, \frac{5}{9}, \frac{7}{8}, \frac{9}{10} = \frac{240 \quad 200 \quad 315 \quad 324}{360}. \quad Ans.$$

3. Change $\frac{5}{5}$, $\frac{5}{1}$, $\frac{5}{21}$, $\frac{19}{15}$ to similar fractions.

The L. C.
$$D_{\cdot} = 840$$
.

$$\therefore \frac{5}{6}, \frac{1}{8}, \frac{5}{21}, \frac{19}{35} = \frac{700 \quad 105 \quad 200 \quad 456}{840}. \quad Ans.$$

4. Change $\frac{2}{15}$, $\frac{7}{20}$, $\frac{3}{25}$, $\frac{4}{45}$ to similar fractions.

The L. C.
$$D = 900$$
.

$$\therefore \frac{2}{15}, \frac{7}{20}, \frac{3}{25}, \frac{8}{45} = \frac{120 \quad 315 \quad 108 \quad 160}{900}. \quad Ans.$$

5. Change 12, 17, 18, 18 to similar fractions.

The L. C. D.
$$= 600$$
.

$$\therefore \frac{12}{25}, \frac{17}{40}, \frac{13}{60}, \frac{19}{75} = \frac{288}{600} \frac{255}{600} \frac{130}{152}. Ans.$$

6. Change $\frac{3}{8}$, $\frac{7}{80}$, $\frac{4}{85}$, $\frac{8}{28}$, $\frac{19}{24}$ to similar fractions.

The L. C. D.
$$= 840$$
.

$$\therefore \frac{3}{8}, \frac{7}{30}, \frac{4}{35}, \frac{3}{28}, \frac{19}{24} = \frac{315}{840} \frac{196}{840} \frac{96}{840} \frac{90}{840} \frac{665}{840}. Ans.$$

7. Change $\frac{1}{16}$, $\frac{7}{18}$, $\frac{13}{20}$, $\frac{33}{50}$, $\frac{17}{54}$ to similar fractions.

The L. C.
$$D. = 2160$$
.

$$\therefore \frac{11}{16}, \frac{7}{18}, \frac{13}{20}, \frac{23}{30}, \frac{17}{54} = \frac{1485}{2160} \frac{840}{2160} \frac{1404}{1656} \frac{1656}{680}. Ans.$$

8. Change 4, 5, 11, 15 to similar fractions.

The L. C.
$$D = 180$$
.

$$\therefore \frac{4}{5}, \frac{8}{9}, \frac{11}{12}, \frac{13}{15} = \frac{144}{180} \frac{160}{180} \frac{165}{180}. Ans.$$

9. Change $\frac{5}{6}$, $\frac{5}{18}$, $\frac{13}{24}$, $\frac{19}{10}$ to similar fractions.

The L. C.
$$D = 360$$
.

$$\therefore \frac{5}{6}, \frac{5}{18}, \frac{13}{24}, \frac{19}{30} = \frac{300 \quad 100 \quad 195 \quad 228}{360}. \quad Ans.$$

10. Change $\frac{7}{4}$, $\frac{17}{24}$, $\frac{19}{32}$, $\frac{11}{48}$ to similar fractions.

The L. C.
$$D = 96$$
.

$$\therefore \frac{7}{8}, \frac{17}{24}, \frac{19}{32}, \frac{11}{48} = \frac{84}{96} \frac{68}{96} \frac{57}{22}. Ans.$$

11. Change $\frac{2}{3}$, $\frac{5}{6}$, $\frac{7}{12}$, $\frac{15}{16}$ to similar fractions.

The L. C.
$$D = 48$$
.

$$\therefore \frac{2}{3}, \frac{5}{6}, \frac{7}{12}, \frac{15}{16} = \frac{32 \quad 40 \quad 28 \quad 45}{48}. \quad Ans.$$

12. Change $\frac{2}{7}$, $\frac{3}{14}$, $\frac{5}{18}$, $\frac{7}{9}$, $\frac{2}{21}$ to similar fractions.

The L. C.
$$D = 126$$
.

$$\therefore \frac{2}{7}, \frac{3}{14}, \frac{5}{18}, \frac{7}{9}, \frac{2}{21} = \frac{36}{126} \frac{27}{126} \frac{35}{126} \frac{98}{12}. Ans.$$

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13. Change $\frac{3}{6}$, $\frac{3}{4}$, $\frac{3}{16}$, $\frac{3}{64}$, $\frac{3}{156}$ to similar fractions.

The L. C. D. = 256.

$$\therefore \frac{3}{8}, \frac{3}{4}, \frac{3}{16}, \frac{3}{64}, \frac{3}{256} = \frac{96}{256} = \frac{98}{256} = \frac{9$$

14. Change $\frac{2}{5}$, $\frac{7}{15}$, $\frac{2}{5}$, $\frac{11}{25}$, $\frac{7}{4}$, $\frac{17}{45}$ to similar fractions.

The L. C. D. = 360.

$$\therefore \frac{3}{5}, \frac{7}{15}, \frac{2}{9}, \frac{11}{24}, \frac{7}{8}, \frac{17}{45} = \frac{216}{360} \frac{168}{360} \frac{80}{360} \frac{165}{315} \frac{315}{136}. Ans.$$

15. Change $\frac{2}{3}$, $\frac{3}{4}$, $\frac{5}{7}$, $\frac{7}{12}$, $\frac{18}{8}$, $\frac{4}{27}$ to similar fractions.

The L. C. D. = 756.

$$\therefore \frac{2}{3}, \frac{3}{4}, \frac{5}{7}, \frac{7}{12}, \frac{13}{18}, \frac{4}{27} = \frac{504}{756} \frac{540}{756} \frac{441}{756} \frac{546}{112}. Ans.$$

16. Change $\frac{11}{12}$, $\frac{9}{10}$, $\frac{14}{15}$, $\frac{4}{5}$, $\frac{17}{20}$, $\frac{39}{30}$ to similar fractions.

The L. C. D. = 60.

$$\therefore \frac{11}{12}, \frac{9}{10}, \frac{14}{15}, \frac{5}{6}, \frac{17}{20}, \frac{29}{30} = \frac{55}{60} \frac{54}{60} \frac{56}{60} \frac{51}{60} \frac{58}{60}. Ans.$$

17. Change $\frac{1}{2}$, $\frac{3}{4}$, $\frac{5}{8}$, $\frac{6}{11}$, $\frac{7}{44}$, $\frac{9}{22}$ to similar fractions.

The L. C. D. = 88.

$$\therefore \frac{1}{2}, \frac{3}{4}, \frac{5}{8}, \frac{6}{11}, \frac{7}{44}, \frac{9}{22} = \frac{44}{88} \frac{66}{88} \frac{55}{88} \frac{48}{14} \frac{14}{36}. Ans.$$

18. Change $\frac{9}{14}$, $\frac{7}{10}$, $\frac{13}{28}$, $\frac{17}{7}$, $\frac{3}{4}$, $\frac{31}{86}$ to similar fractions.

The L. C. D. = 280.

$$\therefore \frac{9}{14}, \frac{7}{10}, \frac{13}{28}, \frac{17}{70}, \frac{3}{4}, \frac{31}{56} = \frac{180}{280} \frac{196}{280} \frac{130}{280} \frac{68}{210} \frac{210}{155}. Ans.$$

19. Which is the greater, $\frac{1}{2}$ or $\frac{1}{4}$? $\frac{1}{5}$ or $\frac{7}{4}$?

The L. C. D. = 100.

The L. C. D.
$$= 60$$

$$\frac{13}{20} = \frac{65}{100},$$

$$\frac{17}{100} = \frac{68}{100}.$$

$$\frac{5}{6} = \frac{15}{18},$$

$$\frac{7}{9} = \frac{14}{18}.$$

$$\frac{3}{5} = \frac{36}{60}$$

$$\frac{17}{25} = \frac{68}{100}$$
. $\frac{7}{9}$:

$$\frac{7}{12} = \frac{35}{60}$$

:. 13 is the greater.

... § is the greater.

: \frac{2}{3} is the greater.

20. Arrange the fractions $\frac{7}{12}$, $\frac{1}{12}$, $\frac{1}{24}$ in order of magnitude.

The L. C. D. =
$$72$$
.

$$\frac{7}{12}$$
, $\frac{11}{18}$, $\frac{13}{24} = \frac{42}{72} = \frac{44}{72} = \frac{39}{24}$, $\frac{13}{12}$, $\frac{7}{12}$, $\frac{11}{18}$. Ans.

21. Arrange the fractions $\frac{5}{12}$, $\frac{8}{15}$, $\frac{4}{11}$, $\frac{7}{18}$ in order of magnitude.

The L. C. D.
$$= 1980$$
.

$$\frac{5}{12}, \frac{8}{15}, \frac{4}{11}, \frac{7}{18} = \frac{825}{1980} \frac{1056}{1980} \frac{720}{1980}.$$

$$\frac{4}{11}, \frac{7}{18}, \frac{5}{12}, \frac{8}{15}. Ans.$$

22. Arrange the fractions $\frac{3}{7}$, $\frac{4}{5}$, $\frac{9}{19}$, $\frac{10}{2}$ in order of magnitude.

The L. C. D.
$$= 27,531$$
.

$$\frac{3}{7}$$
, $\frac{4}{9}$, $\frac{9}{19}$, $\frac{10}{23} = \frac{11799}{27531}$ $\frac{12236}{27531}$ $\frac{13041}{7}$ $\frac{11970}{23}$, $\frac{3}{7}$, $\frac{10}{23}$, $\frac{4}{9}$, $\frac{9}{19}$. Ans.

Exercise 58. Page 127.

Find the sum of:

1.
$$\frac{1}{2} + \frac{3}{2}$$
. $\frac{1}{2} + \frac{3}{2} = \frac{4}{2} = 2$.

2.
$$\frac{1}{3} + \frac{2}{3} + \frac{1}{8}$$
.
 $\frac{1}{3} + \frac{2}{3} + \frac{1}{3} = \frac{4}{3} = 1\frac{1}{8}$.

3.
$$\frac{1}{4} + \frac{1}{4} + \frac{3}{4} = \frac{5}{4} = 1\frac{1}{4}$$
.

4.
$$1\frac{1}{2} + 2\frac{1}{2}$$
.
 $1\frac{1}{2} + 2\frac{1}{2} = 3\frac{1+1}{2} = 4$.

5.
$$1\frac{1}{8} + 2\frac{2}{8}$$
. $1\frac{1}{3} + 2\frac{2}{8} = 3\frac{1+2}{8} = 4$.

6.
$$3\frac{1}{4} + \frac{3}{4}$$
. $3\frac{1}{4} + \frac{3}{4} = 3\frac{1+8}{4} = 4$.

7.
$$2\frac{3}{5} + 3\frac{4}{5}$$
.
 $2\frac{3}{5} + 3\frac{4}{5} = 5\frac{3+4}{5} = 6\frac{3}{5}$.

8.
$$1\frac{7}{8} + \frac{8}{8}$$
. $1\frac{7}{8} + \frac{8}{8} = 1\frac{7+8}{8} = 2\frac{1}{4}$.

9.
$$\frac{9}{17} + \frac{3}{17} + \frac{14}{17} + \frac{14}{17}$$

$$\frac{9}{17} + \frac{3}{17} + \frac{14}{17} + \frac{11}{17} = \frac{37}{17} = 2\frac{3}{17}.$$

10.
$$8\frac{9}{17} + 6\frac{8}{17} + 5\frac{14}{17} + \frac{11}{17}$$
. $8\frac{9}{17} + 6\frac{3}{17} + 5\frac{14}{17} + \frac{11}{17} = 19\frac{87}{17} = 21\frac{8}{17}$.

11.
$$\frac{4}{5} + \frac{5}{6}$$
.

The L. C. D. = 30.

$$\frac{4}{5} + \frac{5}{6} = \frac{24 + 25}{30} = \frac{49}{30} = 1\frac{19}{30}.$$

12.
$$\frac{3}{4} + \frac{7}{8}$$
.

The L. C. D. = 8.

$$\frac{3}{4} + \frac{7}{8} = \frac{6+7}{8} = \frac{13}{8} = 1\frac{5}{8}.$$

13.
$$\frac{1}{3} + \frac{1}{6}$$
.

The L. C. D. = 6.

$$\frac{1}{2} + \frac{1}{6} = \frac{3+1}{6} = \frac{4}{6} = \frac{2}{3}$$

14.
$$\frac{4}{15} + \frac{11}{15}$$
.

The L. C. D. = 60.

$$\frac{4}{15} + \frac{11}{20} = \frac{16 + 33}{60} = \frac{49}{60}$$

15.
$$\frac{1}{16} + \frac{11}{24}$$
.

The L. C. D. = 48.

$$\frac{5}{16} + \frac{11}{24} = \frac{15 + 22}{48} = \frac{37}{48}$$

16.
$$12\frac{5}{1} + 7\frac{3}{16}$$
.

The L. C. D. = 16.

$$12\frac{5}{8} + 7\frac{3}{16} = 19\frac{10+3}{16} = 19\frac{3}{16}.$$

17.
$$85\frac{7}{12} + 27\frac{11}{13}$$
.

The L. C. D. = 36.

$$85\frac{7}{13} + 27\frac{1}{18} = 112\frac{21+22}{86} = 112\frac{48}{36} = 113\frac{7}{86}.$$

18.
$$\frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5}$$
.

The L. C. D. = 60.

$$\frac{1}{2} + \frac{1}{3} + \frac{1}{4} + \frac{1}{5} = \frac{30 + 20 + 15 + 12}{60} = \frac{77}{60} = 1\frac{17}{60}.$$

19. $\frac{1}{2} + \frac{2}{3} + \frac{1}{4} + \frac{1}{5}$.

The L. C. D. = 60.

$$\frac{1}{2} + \frac{2}{3} + \frac{3}{4} + \frac{4}{5} = \frac{30 + 40 + 45 + 48}{60} = \frac{163}{60} = 2\frac{3}{60}.$$

20. $\frac{5}{8} + \frac{1}{12} + \frac{4}{15} + \frac{7}{20} + \frac{18}{88}$.

The L. C. D. = 60.

$$\frac{5}{6} + \frac{11}{12} + \frac{8}{15} + \frac{7}{20} + \frac{13}{30} = \frac{50 + 55 + 32 + 21 + 26}{60} = \frac{184}{60} = 3\frac{1}{15}.$$

21. $5\frac{1}{2}\frac{7}{6} + 11\frac{1}{3}\frac{8}{6} + 24\frac{21}{6}\frac{1}{6} + \frac{9}{10} + 17\frac{4}{15} + 14 + 11\frac{5}{12}$

The L. C. D. = 600.

$$5\frac{1}{2}$$
7 + $11\frac{1}{3}$ 8 + $24\frac{2}{4}$ 1 + $\frac{9}{50}$ + $17\frac{4}{15}$ + 14 + $11\frac{5}{12}$

$$=82\frac{510+880+815+108+820+250}{600}=82\frac{1883}{600}=85\frac{88}{600}$$

22.
$$9\frac{1}{7} + 15\frac{1}{2}\frac{1}{7} + 163\frac{1}{6}\frac{7}{7} + 1\frac{1}{2}\frac{1}{7} + 10\frac{1}{7}$$
.

The L. C. D. = 252.

$$9\frac{1}{7} + 15\frac{1}{2}\frac{1}{8} + 163\frac{1}{6}\frac{1}{7} + 1\frac{1}{2}\frac{1}{2} + 10\frac{1}{2} = 198\frac{1}{2}\frac{4}{5}\frac{4}{2}\frac{1}{2}\frac{9}{5}\frac{1}{2}\frac{1}{5}\frac{1}{2} + 66\frac{1}{6}\frac{1}{6}\frac{1}{6}$$
$$= 198\frac{1}{2}\frac{1}{2}\frac{9}{2} = 199\frac{1}{6}\frac{7}{6}.$$

23.
$$3\frac{3}{5} + 4\frac{7}{5} + 1\frac{5}{6} + 2$$
. The L. C. D. = 30.

$$3\frac{3}{5} + 4\frac{7}{6} + 1\frac{5}{6} + 2 = 10\frac{18 + 20 + 25}{30} = 10\frac{3}{30} = 12\frac{3}{10} = 12\frac{1}{10}$$

24.
$$1\frac{3}{20} + 2\frac{3}{15} + 5\frac{7}{10} + \frac{4}{15}$$
.

The L. C. D. = 300.

$$1_{\frac{3}{20}} + 2_{\frac{2}{25}} + 5_{\frac{7}{30}} + \frac{4}{13} = 8_{\frac{4}{30}} + \frac{24}{300} + \frac{70}{300} = 8_{\frac{73}{300}} = 8_{\frac{73}{300}} = 8_{\frac{73}{300}}.$$

25.
$$\frac{2}{3} + 1\frac{4}{9} + 2 + 3\frac{8}{8} + 4\frac{5}{12}$$
.

The L. C. D. = 504.

$$\frac{3}{7} + 1\frac{4}{9} + 2 + 3\frac{3}{8} + 4\frac{5}{12} = 10\frac{144 + 224 + 189 + 210}{504} = 10\frac{767}{504} = 11\frac{262}{504}$$

26.
$$4\frac{4}{9} + 3\frac{9}{8} + 2\frac{7}{7} + 1\frac{1}{8} + \frac{9}{14}$$
.

The L. C. D. = 504.

$$4\frac{1}{6} + 3\frac{1}{6} + 2\frac{1}{6} + 1\frac{1}{6} + \frac{1}{14} = 10^{224+189+144+84+324} = 10\frac{265}{504} = 11\frac{261}{504}$$

27.
$$\frac{11}{85} + \frac{7}{40} + 10 + \frac{25}{80}$$
.

The L. C. D. = 840.

$$\frac{11}{85} + \frac{7}{40} + 10 + \frac{28}{85} = 10^{264 + 147 + 322} = 10^{283}$$

28.
$$\frac{27}{80} + \frac{20}{80} + \frac{81}{80} + \frac{83}{100} + \frac{87}{240}$$
.

The L. C. D. = 1200.

$$\frac{27}{50} + \frac{29}{60} + \frac{31}{80} + \frac{33}{100} + \frac{37}{240} = \frac{648 + 580 + 465 + 396 + 185}{1200} = \frac{2274}{1200} = 1\frac{179}{266}.$$

29.
$$2 + \frac{2}{5} + 1\frac{3}{5} + 4\frac{5}{5} + 5\frac{13}{2}$$
.

The L. C. D. = 72.

$$2 + \frac{2}{3} + 1\frac{3}{4} + 4\frac{3}{5} + 5\frac{13}{24} = 12\frac{48+54+64+89}{72} = 12\frac{205}{72} = 14\frac{61}{72}$$

30.
$$3\frac{5}{8} + 6 + \frac{4}{11} + 2\frac{3}{10} + 5\frac{5}{16} + \frac{9}{20}$$
.

The L. C. D. = 880.

$$3\frac{5}{8} + 6 + \frac{4}{11} + 2\frac{3}{10} + 5\frac{5}{16} + \frac{9}{20} = 16\frac{550 + 320 + 264 + 275 + 896}{880} = 16\frac{1805}{880} = 18\frac{45}{880} = 18\frac{45}{176}.$$

31.
$$\frac{8}{15} + \frac{7}{18} + 3\frac{17}{26} + 1\frac{13}{24} + 2\frac{19}{120}$$
.

The L. C. D. = 360.

$$\frac{8}{15} + \frac{7}{18} + 3\frac{17}{20} + 1\frac{19}{24} + 2\frac{19}{120} = 6\frac{192 + 140 + 306 + 285 + 57}{860} = 6\frac{980}{860} = 8\frac{18}{260} = 8\frac{18}{18}.$$

32.
$$\frac{1}{14} + \frac{4}{11} + 9\frac{1}{2}$$
.

The L. C. D. = 154.

$$\frac{5}{14} + \frac{6}{11} + 9\frac{1}{2} = 9\frac{55 + 84 + 77}{154} = 9\frac{1}{154} = 10\frac{62}{154} = 10\frac{63}{154} = 10\frac{63}{154}$$

33.
$$20\frac{5}{12} + 11\frac{7}{20} + 5\frac{1}{1} + 305$$
.

The L. C. D. = 120.

$$20\frac{5}{12} + 11\frac{7}{20} + 5\frac{1}{8} + 305 = 341\frac{50 + 42 + 15}{120} = 341\frac{107}{120}.$$

34.
$$\frac{11}{11} + \frac{14}{14} + \frac{17}{16}$$
.

The L. C. D. = 228.

$$\frac{11}{38} + \frac{14}{57} + \frac{17}{76} = \frac{66 + 56 + 51}{228} = \frac{173}{228}$$

35. $\frac{5}{17} + \frac{11}{11} + \frac{11}{11} + \frac{11}{11}$

The L. C. D. \doteq 204.

$$\frac{5}{17} + \frac{11}{34} + \frac{14}{51} + \frac{19}{68} = \frac{60 + 66 + 56 + 57}{204} = \frac{239}{204} = 1_{\frac{85}{204}}.$$

36.
$$317\frac{2}{5} + 17\frac{3}{51} + 4\frac{9}{10} + \frac{7}{15} + 6\frac{2}{5} + \frac{5}{17}$$
.

The L. C. D. = 510.

$$317\frac{2}{5} + 17\frac{3}{51} + 4\frac{9}{10} + \frac{7}{15} + 6\frac{2}{5} + \frac{5}{17} = 344204 + 80 + 459 + 288 + 840 + 150$$

$$= 3441431 = 346491.$$

37.
$$4\frac{7}{13} + 8\frac{5}{21} + 4\frac{7}{11} + 5\frac{2}{7} + 5\frac{4}{7} + \frac{2}{7}$$

The L. C. D. = 1155.

$$4\frac{7}{15} + 8\frac{5}{21} + 4\frac{7}{11} + 5\frac{2}{7} + 5\frac{4}{7} + 5\frac{4}{7} + \frac{2}{7} = 26\frac{589 + 275 + 785 + 380 + 924 + 770}{1155} = 26\frac{578}{1155} = 29\frac{108}{1155} = 29\frac{35}{385}.$$

38. $3\frac{2}{3} + 5\frac{3}{40} + 8\frac{7}{340} + \frac{58}{68} + 1\frac{2}{2880}$.

The L. C. D. = 2880.

 $8\frac{3}{8} + 5\frac{3}{40} + 8\frac{7}{240} + \frac{39}{60} + 1\frac{23}{2880} = 17\frac{1920 + 216 + 84 + 1872 + 29}{2880} = 17\frac{1320}{2880} = 18\frac{121}{280}.$

39. $4\frac{5}{18} + 7\frac{5}{18} + 5\frac{1}{28} + 275\frac{3}{18} + 2\frac{5}{2}$.

The L. C. D. = 1092.

 $4\frac{5}{13} + 7\frac{5}{89} + 5\frac{7}{18} + 275\frac{37}{186} + 2\frac{57}{186} = 293\frac{420+140+658+259+684}{1092} = 293\frac{7}{18}\frac{5}{18} = 294\frac{7}{18}\frac{5}{18}\frac{5}{2}.$

40. $\frac{17}{13} + 7\frac{1}{13} + 6\frac{1}{13} + 400\frac{1}{13} + 51\frac{25}{25}$.

The L. C. D. = 1848.

 $\frac{17}{18} + 7\frac{5}{12} + 6\frac{2}{11} + 400\frac{3}{18} + 51\frac{25}{88} = 464\frac{952 + 770 + 886 + 198 + 825}{1848} = 464\frac{324}{1848} = 465\frac{1}{1848}.$

41. $3\frac{2}{3} + 1\frac{1}{4} + 2\frac{1}{5} + 3\frac{5}{5} + 107\frac{5}{18} + 2\frac{7}{36}$.

The L. C. D. = 36.

 $3\frac{2}{3} + 1\frac{1}{4} + 2\frac{1}{5} + 3\frac{5}{5} + 107\frac{5}{15} + 2\frac{7}{56} = 118\frac{24+9+4+30+10+7}{36} = 118\frac{54}{36} = 120\frac{1}{3}$

42. $5\frac{1}{14} + 5\frac{3}{5} + 2\frac{1}{7} + 7\frac{3}{21} + 12\frac{4}{15}$.

The L. C. D. = 210.

 $5\frac{1}{14} + 5\frac{3}{5} + 2\frac{1}{7} + 7\frac{8}{21} + 12\frac{4}{15} = 31\frac{15+126+80+56}{210} = 31\frac{307}{210}.$

43. $4\frac{3}{4} + 2\frac{1}{3} + 3\frac{3}{6} + 7\frac{1}{6} + 8\frac{1}{6}$.

The L. C. D. = 48.

 $4\frac{3}{4} + 2\frac{1}{8} + 3\frac{3}{8} + 7\frac{1}{8} + 8\frac{15}{18} = 24\frac{36+6+18+8+45}{48} = 24\frac{113}{48} = 26\frac{17}{48}$

44. $6\frac{1}{2} + 7\frac{2}{3} + 8\frac{3}{4} + 9\frac{5}{5} + 8\frac{1}{13}$.

The L. C. D. = 36.

 $6\frac{1}{2} + 7\frac{2}{8} + 8\frac{2}{4} + 9\frac{5}{8} + 8\frac{11}{18} = 38\frac{18+24+27+80+22}{36} = 38\frac{121}{86} = 41\frac{1}{18}$

45. $7\frac{5}{6} + 8\frac{3}{4} + 5\frac{15}{16} + 7\frac{11}{12} + 9\frac{1}{2}$.

The L. C. D. = 48.

 $7\frac{1}{6} + 8\frac{1}{4} + 5\frac{1}{1}\frac{1}{6} + 7\frac{1}{1}\frac{1}{2} + 9\frac{1}{2} = 36\frac{40+86+45+44+24}{48} = 36\frac{189}{48} = 39\frac{1}{18} = 39\frac{1}{18}$

46.
$$5\frac{1}{4} + 6\frac{3}{4} + 7\frac{1}{4} + 9\frac{1}{4} + 3\frac{1}{1} + 2\frac{1}{4}$$
.

The L. C. D. = 48.

$$5\frac{1}{2} + 6\frac{2}{3} + 7\frac{1}{2}\frac{1}{4} + 9\frac{1}{2}\frac{1}{3} + 3\frac{1}{16} + 2\frac{1}{6} = 32\frac{24+82+22+17+88+8}{48} = 32\frac{186}{48}$$

= $34\frac{1}{2}\frac{1}{8} = 34\frac{1}{5}$.

47.
$$9\frac{4}{5} + 10\frac{4}{5} + 11\frac{2}{5} + 5\frac{17}{25} + 7\frac{4}{25} + 18\frac{4}{5}$$
.

The L. C. D. = 84.

$$9\frac{3}{4} + 10\frac{3}{4} + 11\frac{3}{4} + 5\frac{17}{4} + 7\frac{4}{21} + 7\frac{4}{21} + 18\frac{5}{6} = 60\frac{68 + 72 + 56 + 84 + 82 + 70}{84} = 60\frac{827}{64} = 63\frac{25}{64} = 63\frac{25}{26}.$$

The L. C. D. = 2205.

$$\frac{13}{21} + \frac{3}{49} + \frac{16}{35} + \frac{11}{63} + \frac{4}{7} + \frac{4}{15} + \frac{17}{45}$$

$$= \frac{1365 + 135 + 1008 + 385 + 1260 + 588 + 833}{2205}$$

$$= \frac{5574}{2205} = 2\frac{1164}{2205} = 2\frac{165}{785}.$$

Exercise 59. Page 129.

Find the value of:

1.
$$52\frac{1}{6} - 46 = 6\frac{1}{6}$$
.

2.
$$\frac{6}{9} - \frac{3}{9} = \frac{6-3}{9} = \frac{3}{9} = \frac{1}{3}$$
.

3.
$$\frac{3}{4} - \frac{2}{3} = \frac{9-8}{12} = \frac{1}{12}$$
.

4.
$$\frac{8}{15} - \frac{5}{12} = \frac{32 - 25}{60} = \frac{7}{60}$$
.

5.
$$\frac{11}{18} - \frac{3}{14} = \frac{77 - 27}{126} = \frac{50}{126} = \frac{25}{63}$$
.

6.
$$4-\frac{1}{2}=3\frac{1}{2}$$

7.
$$7 - \frac{2}{3} = 6\frac{1}{3}$$
.

8.
$$3-\frac{1}{4}=2\frac{1}{4}$$
.

9.
$$8 - \frac{1}{7} = 7\frac{1}{7}$$
.

10.
$$5-\frac{4}{5}=4\frac{1}{5}$$
.

11.
$$5 - \frac{7}{9} = 4\frac{3}{9}$$

12.
$$6\frac{1}{6} - 5\frac{1}{6} = 1\frac{2-1}{6} = 1\frac{1}{6}$$
.

13.
$$4\frac{3}{5} - 3\frac{3}{7} = 1\frac{14-15}{35}$$

= $\frac{49-15}{35} = \frac{34}{35}$.
14. $7\frac{1}{3} - 2\frac{3}{10} = 5\frac{10-9}{30} = 5\frac{1}{30}$.

14.
$$7\frac{1}{3} - 2\frac{8}{10} = 5\frac{10-9}{80} = 5\frac{1}{30}$$
.

15.
$$7\frac{2}{5} - 4\frac{8}{5} = 3\frac{18-40}{45}$$

= $2\frac{63-40}{45} = 2\frac{23}{45}$.

16.
$$6\frac{2}{3} - 2\frac{3}{4} = 4\frac{3-9}{12}$$

= $3\frac{2}{1}\frac{9-9}{2} = 3\frac{11}{12}$.

17.
$$9\frac{4}{5} - 4\frac{5}{6} = 5\frac{24-25}{80}$$

= $4\frac{54-25}{80} = 4\frac{29}{80}$.

18.
$$4\frac{2}{8} - \frac{1}{2} = 4\frac{4-8}{6} = 4\frac{1}{6}$$
.

19.
$$6\frac{3}{4} - 4\frac{3}{3} = 2\frac{9-8}{12} = 2\frac{1}{12}$$
.

20.
$$7\frac{1}{2} - 2\frac{3}{4} = 5\frac{2}{4} = 4\frac{6-8}{4} = 4\frac{3}{4}$$
.

21.
$$8\frac{1}{5} - 4\frac{4}{7} = 47 - \frac{20}{85}$$

= $342 - 20$ = $3\frac{2}{85}$

22.
$$85\frac{7}{18} - 27\frac{1}{18} = 58\frac{6}{198} - 121 = 57\frac{26}{198} - 57\frac{1}{198} = 57\frac$$

23.
$$8\frac{7}{10} - 2\frac{11}{16} = 6\frac{56-55}{80} = 6\frac{1}{10}$$

24.
$$10-3\frac{5}{8}=6\frac{5}{8}$$
.

25.
$$120\frac{21}{32} - 110\frac{1}{24} = 10\frac{63-52}{96} = 10\frac{1}{36}$$
.

. **26.**
$$5\frac{17}{28} - \frac{27}{85} = 5\frac{85-108}{140} = 4\frac{225-108}{140} = 4\frac{117}{140}$$
.

27.
$$13\frac{3}{40} - 2\frac{15}{44} = 11\frac{33-150}{440} = 10\frac{473-150}{440} = 10\frac{323}{460}$$

28.
$$2\frac{151}{240} - 1\frac{163}{102} = 1\frac{604 - 815}{960} = \frac{1564 - 815}{960} = \frac{749}{960}$$

29.
$$4 - 1\frac{2817}{4000} = 2\frac{4000 - 2317}{4000} = 2\frac{1688}{4000}$$

30.
$$1473 - 279\frac{1}{12} = 1193\frac{1}{12}$$
.

31.
$$1473\frac{5}{13} - 279\frac{1}{12} = 1194\frac{60 - 148}{156} = 1193\frac{216 - 148}{156} = 1193\frac{78}{156}$$
.

32.
$$1473\frac{7}{18} - 279\frac{11}{12} = 1194\frac{14-38}{36} = 1193\frac{59-38}{36} = 1193\frac{17}{36}$$

33.
$$278\frac{15}{16} - 30\frac{5}{12} = 248\frac{45-20}{48} = 248\frac{25}{48}$$
.

34.
$$125\frac{5}{22} - 10\frac{17}{88} = 115\frac{15-34}{66} = 114\frac{81-34}{66} = 114\frac{47}{66}$$

35.
$$118\frac{5}{11} - 17\frac{3}{14} = 101\frac{70-33}{154} = 101\frac{37}{154}$$
.

36.
$$94\frac{5}{11} - 91\frac{18}{14} = 3\frac{70-148}{154} = 2\frac{224-148}{154} = 2\frac{81}{154}$$
.

37.
$$7\frac{5}{21} - 2\frac{11}{14} = 5\frac{10}{42} = 4\frac{52}{42} = 4\frac{12}{42} = 4\frac{12}{42}$$

38.
$$\frac{235}{357} - \frac{13}{51} = \frac{235 - 91}{357} = \frac{144}{357} = \frac{48}{119}$$
.

39.
$$\frac{17}{63} - \frac{29}{108} = \frac{204 - 203}{756} = \frac{1}{756}$$
.

40.
$$\frac{9}{38} - \frac{43}{209} = \frac{99 - 86}{418} = \frac{13}{418}$$
.

41.
$$\frac{146}{273} - \frac{268}{637} = \frac{1022 - 804}{1911} = \frac{218}{1911}$$
.

42.
$$\frac{359}{360} - \frac{199}{200} = \frac{1795 - 1791}{1800} = \frac{4}{1800} = \frac{1}{450}$$
.

Exercise 60. Page 130.

- 1. Simplify $3\frac{2}{8} 2\frac{5}{8} + 4\frac{8}{10} + 1\frac{7}{6} 5\frac{8}{15}$. $3\frac{2}{8} + 4\frac{8}{10} + 1\frac{7}{9} = 8\frac{36 + 27 + 70}{90} = 8\frac{188}{90} = 9\frac{18}{10}.$ $2\frac{5}{8} + 5\frac{8}{15} = 7\frac{75 + 64}{120} = 7\frac{189}{120} = 8\frac{19}{120}.$ $9\frac{18}{120} - 8\frac{19}{120} = 1\frac{172 - 57}{860} = 1\frac{185}{800} = 1\frac{23}{72}. Ans.$
- 2. Simplify $1\frac{5}{11} \frac{11}{12} + 7\frac{3}{8} 2\frac{1}{3} 1\frac{11}{16}$. $1\frac{5}{11} + 7\frac{3}{8} = 8\frac{40 + 83}{88} = 8\frac{73}{88}.$ $\frac{11}{12} + 2\frac{1}{3} + 1\frac{11}{16} = 3\frac{44 + 16 + 83}{48} = 3\frac{23}{48} = 4\frac{15}{48} = 4\frac{15}{16}.$ $8\frac{73}{18} 4\frac{15}{16} = 4\frac{146 165}{76} = 3\frac{322 165}{76} = 3\frac{157}{6}. \text{ Ans.}$
- 3. Simplify $12 3\frac{2}{7} 1\frac{3}{10} 4\frac{5}{28} + 2\frac{13}{20} 4\frac{3}{8}$. $12 + 2\frac{13}{20} = 14\frac{13}{20}.$ $3\frac{2}{7} + 1\frac{3}{10} + 4\frac{5}{28} + 4\frac{3}{8} = 12\frac{40 + 42 + 25 + 84}{140} = 12\frac{121}{140} = 13\frac{51}{140}.$ $14\frac{13}{20} 13\frac{51}{140} = 1\frac{91 51}{140} = 1\frac{40}{140} = 1\frac{3}{7}. \text{ Ans.}$
- 4. Simplify $43\frac{7}{15} 1\frac{1}{8} 1\frac{1}{48} 1\frac{1}{28} 2\frac{1}{18} 2\frac{7}{12} 2\frac{48}{48} 3\frac{5}{12}$. $1\frac{1}{8} + 1\frac{21}{24} + 2\frac{1}{18} + 2\frac{7}{12} + 2\frac{48}{48} + 3\frac{5}{12} = 12\frac{16+81+46+18+28+48+20}{48} = 12\frac{197}{48} = 16\frac{5}{48}$. $43\frac{7}{15} - 16\frac{5}{48} = 27\frac{112-25}{240} = 27\frac{87}{240} = 27\frac{29}{80}$. Ans.
 - 5. Simplify $\frac{1}{2} + \frac{4}{13} + 7\frac{9}{40} + 8\frac{14}{36} + 7\frac{1}{4} + 8\frac{8}{10} + 4\frac{1}{13} 36\frac{1}{40}$. $\frac{1}{2} + \frac{4}{13} + 7\frac{9}{40} + 8\frac{1}{36} + 7\frac{1}{4} + 8\frac{3}{10} + 4\frac{1}{12}$ $= 34\frac{780 + 480 + 851 + 560 + 390 + 468 + 180}{1560} = 34\frac{1560}{1560} = 36\frac{1}{1560} = 36\frac{1}{40}.$ $36\frac{1}{40} 36\frac{1}{40} = 0. \text{ Ans.}$
 - 6. Simplify $(8\frac{5}{18} + 1\frac{1}{2}\frac{9}{7} + 17\frac{1}{3}\frac{1}{6} + 40) (30\frac{1}{4}\frac{3}{6} + 11\frac{1}{2}\frac{1}{6})$. $8\frac{5}{18} + 1\frac{1}{2}\frac{9}{7} + 17\frac{1}{3}\frac{1}{6} + 40 = 66\frac{80 + 40 + 88}{108} = 66\frac{108}{108}$. $30\frac{1}{4}\frac{3}{6} + 11\frac{1}{2}\frac{1}{6} = 41\frac{13 + 22}{40} = 41\frac{25}{40} = 41\frac{7}{6}$. $66\frac{1}{108} - 41\frac{7}{8} = 25\frac{20}{2}\frac{6 - 1}{16}\frac{89}{6} = 25\frac{17}{216}$. Ans.

7. Simplify
$$(172\frac{1}{8} + 93\frac{1}{14}) + (172\frac{1}{8} - 93\frac{1}{14})$$
.

$$(172\frac{1}{8} + 93\frac{1}{14}) + (172\frac{1}{8} - 93\frac{1}{14})$$

$$= 172\frac{1}{8} + 93\frac{1}{14} + 172\frac{1}{8} - 93\frac{1}{14}$$

$$= 172\frac{1}{8} + 172\frac{1}{8} = 344\frac{1}{78} + 198\frac{1}{8}$$
Ans.

8. Simplify
$$(172\frac{1}{3} + 93\frac{1}{14}) - (172\frac{1}{3} - 93\frac{1}{14})$$
.

$$(172\frac{1}{3} + 93\frac{1}{14}) - (172\frac{1}{3} - 93\frac{1}{14})$$

$$= 172\frac{1}{3} + 93\frac{1}{14} - 172\frac{1}{3} + 93\frac{1}{14}$$

$$= 93\frac{1}{14} + 93\frac{1}{14} = 186\frac{1}{14}$$
. Ans.

9. Simplify
$$(\frac{3}{15} - \frac{3}{39}) + (\frac{3}{75} + \frac{7}{155})$$
.

$$\frac{3}{15} - \frac{3}{59} = \frac{9-2}{59} = \frac{7}{59}.$$

$$\frac{5}{75} + \frac{7}{156} = \frac{10+7}{156} = \frac{17}{156}.$$

$$\frac{7}{15} + \frac{17}{156} = \frac{28+17}{156} = \frac{43}{156} = \frac{13}{15}. Ans.$$

10. Simplify
$$\frac{1}{8} - \frac{1}{11} - 2\frac{3}{4} + 3\frac{1}{4} + 7\frac{1}{13} - 1\frac{3}{4} - \frac{1}{14}$$
.
$$\frac{1}{8} + 3\frac{3}{8} + 7\frac{7}{13} = 10^{1.6 + \frac{3}{3}\frac{4}{6} + 21} = 10\frac{1}{16} = 11\frac{1}{3}\frac{1}{6}$$

$$\frac{1}{11} + 2\frac{3}{4} + 1\frac{3}{8} + \frac{3}{13} = 3\frac{60 + 16}{2}\frac{5 + 1}{2}\frac{32 + 30}{2} = 3\frac{1}{12}\frac{1}{6} = 4\frac{1}{12}\frac{1}{6}$$

$$11\frac{25}{16} - 4\frac{1}{12}\frac{1}{6} = 7\frac{187}{1980} = 6\frac{885}{1980} = 6\frac{185}{1980} = 6\frac{185}{1980} = 6\frac{1}{18}\frac{1}{6}$$
. Ans.

11. Simplify
$$\frac{8}{10} - \frac{7}{100} - \frac{9}{1000} - \frac{5}{10000}$$
.
$$\frac{7}{100} + \frac{9}{1000} + \frac{5}{10000} = \frac{700 + 90 + 5}{100000} = \frac{795}{10000} = \frac{159}{1000}$$

$$\frac{8}{10} - \frac{159}{2000} = \frac{600 - 159}{2000} = \frac{441}{1000}$$
. Ans.

12. Simplify
$$9\frac{1}{6} - 7 - \frac{3}{4} - \frac{5}{6}$$
.
$$7 + \frac{3}{4} + \frac{5}{6} = 7\frac{9+10}{12} = 7\frac{10}{12} = 8\frac{7}{12}.$$

$$9\frac{5}{6} - 8\frac{7}{12} = 1\frac{15-14}{24} = 1\frac{1}{12}. \text{ Ans.}$$

13. Simplify
$$5\frac{2}{3} + 8\frac{3}{4} - 1\frac{3}{5} - 4\frac{7}{6}$$
.
$$5\frac{3}{4} + 8\frac{3}{4} = 13\frac{5+9}{12} = 13\frac{7}{12} = 14\frac{5}{13}.$$

$$1\frac{3}{5} + 4\frac{7}{6} = 5\frac{2\cdot7+3\cdot5}{4\cdot5} = 5\frac{2\cdot3}{4\cdot5} = 6\frac{17}{13}.$$

$$1\frac{4\cdot5}{12} - 6\frac{17}{13} = 8\frac{7\cdot5-6\cdot8}{1\cdot80} = 8\frac{7}{1\cdot80}. \text{ Ans.}$$

- 14. Simplify $6\frac{3}{4} 5\frac{2}{3} + 4\frac{2}{5} 4\frac{5}{13}$. $6\frac{3}{4} + 4\frac{2}{5} = 10\frac{15+8}{20} = 10\frac{23}{20} = 11\frac{3}{20}.$ $5\frac{2}{3} + 4\frac{5}{12} = 9\frac{8+5}{12} = 9\frac{13}{12} = 10\frac{1}{12}.$ $11\frac{3}{10} - 10\frac{1}{12} = 1\frac{9-5}{60} = 1\frac{4}{60} = 1\frac{1}{15}. \text{ Ans.}$
- 15. Simplify $14\frac{7}{18} + 9\frac{3}{5} 6\frac{3}{4} 12\frac{4}{5} 3\frac{3}{5}$. $14\frac{7}{18} + 9\frac{3}{5} = 23\frac{3}{5}\frac{5+5}{9}\frac{4}{0} = 23\frac{3}{9}\frac{5}{0}.$ $6\frac{3}{4} + 12\frac{4}{5} + 3\frac{3}{5} = 21\frac{15+1}{2}\frac{6+1}{0} = 21\frac{4}{2}\frac{3}{0} = 23\frac{3}{20}.$ $23\frac{5}{9}\frac{9}{0} 23\frac{3}{20} = \frac{178-27}{180} = \frac{151}{80}. Ans.$
- 16. Simplify $20\frac{2}{3} 2\frac{5}{8} 9\frac{5}{9} + 10\frac{3}{16} 14\frac{7}{12}$. $20\frac{2}{3} + 10\frac{3}{10} = 30\frac{2}{3}\frac{9}{0} + 9 = 30\frac{29}{30}.$ $2\frac{5}{8} + 9\frac{5}{9} + 14\frac{7}{12} = 25\frac{4}{5} + \frac{4}{9}\frac{9}{4} + 42 = 25\frac{127}{72} = 26\frac{5}{72}.$ $30\frac{29}{30} - 26\frac{5}{72} = 4\frac{34}{36}\frac{8-275}{6} = 4\frac{73}{360}. \text{ Ans.}$
- 17. Simplify $95\frac{2}{3} 9\frac{7}{20} 8\frac{3}{7} 14\frac{2}{5} + 74\frac{2}{5}$. $95\frac{2}{3} + 74\frac{2}{5} = 169\frac{6}{9} + 2 = 169\frac{5}{9}.$ $9\frac{7}{20} + 8\frac{3}{7} + 14\frac{2}{5} = 31\frac{4}{9} + \frac{6}{1}\frac{0}{4} + \frac{5}{9} = 31\frac{6}{140} = 32\frac{25}{140} = 32\frac{5}{28}.$ $169\frac{2}{9} 32\frac{5}{28} = 137\frac{2}{2}\frac{2}{5}\frac{4}{2} = 137\frac{1}{2}\frac{7}{5}\frac{2}{3}. \quad Ans.$
- 18. Simplify $12\frac{3}{4} + 23\frac{3}{8} (4\frac{3}{10} + 12\frac{2}{5} + 7\frac{14}{15})$. $12\frac{3}{4} + 23\frac{3}{8} = 35\frac{6}{8} = 36\frac{1}{8}.$ $4\frac{3}{10} + 12\frac{3}{8} + 7\frac{14}{15} = 23\frac{9+1}{80} + 24\frac{9}{80} = 24\frac{19}{30}.$ $36\frac{1}{8} - 24\frac{19}{30} = 12\frac{15-76}{120} = 11\frac{135-76}{120} = 11\frac{59}{120}. Ans.$
- 19. Simplify $16\frac{2}{15} + 18\frac{5}{14} (5\frac{2}{5} + 9\frac{9}{40} + 14\frac{5}{24})$. $16\frac{2}{15} + 18\frac{5}{24} = 34\frac{16+25}{120} = 34\frac{41}{120}$. $5\frac{2}{5} + 9\frac{9}{40} + 14\frac{5}{24} = 28\frac{48+27+25}{120} = 28\frac{100}{120}$. $34\frac{41}{120} - 28\frac{100}{120} = 64\frac{1-100}{120} = 5\frac{161-100}{120} = 5\frac{61}{120}$. Ans.
- **20.** Simplify $97\frac{1}{8} (20 + 9\frac{1}{4} + 18\frac{2}{15} + 24\frac{19}{50})$. $20 + 9\frac{1}{4} + 18\frac{2}{15} + 24\frac{19}{50} = 71\frac{75+8+98}{100} = 71\frac{181}{100} = 72\frac{81}{100}$. $97\frac{1}{8} - 72\frac{81}{100} = 25\frac{800-729}{900} = 25\frac{71}{900}$. Ans.

21. Simplify
$$2\frac{1}{16} + 3\frac{1}{16} - (1\frac{1}{76} + 1\frac{1}{3}\frac{1}{2} + \frac{49}{56})$$
.
 $2\frac{1}{16} + 3\frac{1}{16} = 2\frac{3}{4} + 3\frac{3}{7} = 5\frac{21+12}{28} = 5\frac{3}{28} = 6\frac{5}{28}$.
 $1\frac{3}{76} + 1\frac{3}{12} + \frac{4}{16} = 2\frac{848+1085+980}{1120} = 2\frac{2913}{1120} = 4\frac{678}{1120}$.
 $6\frac{5}{28} - 4\frac{678}{1120} = 2\frac{200-678}{1120} = 1\frac{1320-678}{1120} = 1\frac{647}{1120}$. Ans.

22. Simplify
$$\frac{148}{100} + \frac{2471}{1000} - \frac{82648}{100000}$$
.

$$\frac{148}{100} + \frac{2471}{1000} = \frac{1480 + 2471}{1000} = \frac{8901}{1000} = 3_{1000}^{901}$$
.

$$3_{1000}^{901} - \frac{82648}{100000} = 3_{100000}^{90100 - 82648} = 3_{100000}^{7457}$$
. Ans.

Exercise 61. Page 132.

1. Simplify
$$\frac{2\frac{1}{11}}{3\frac{3}{4}}$$
.
$$\frac{2\frac{3}{11}}{3\frac{3}{4}} = \frac{\frac{5}{25}}{11} \times \frac{4}{\frac{15}{3}} = \frac{20}{33}$$
.

2. Simplify
$$\frac{3}{7\frac{1}{8}}$$
.
$$\frac{3}{7\frac{1}{8}} = 3 \times \frac{8}{57} = \frac{8}{19}$$
.

3. Simplify
$$\frac{17\frac{1}{7}}{13\frac{1}{8}}$$
.
$$\frac{17\frac{1}{7}}{13\frac{1}{7}} = \frac{120}{7} \times \frac{3}{40} = \frac{9}{7} = 1\frac{3}{7}.$$

4. Simplify
$$\frac{5}{8\frac{1}{3}}$$
.
$$\frac{5}{8\frac{1}{3}} = \frac{5}{9} \times \frac{3}{25} = \frac{1}{15}$$
.

5. Simplify
$$\frac{5\frac{1}{6}}{8\frac{4}{11}}$$
.
$$\frac{5\frac{1}{6}}{8\frac{4}{11}} = \frac{46}{9} \times \frac{11}{92} = \frac{11}{18}$$
.

6. Simplify
$$\frac{1\frac{4}{3} \text{ of } \frac{3\frac{1}{7}}{4\frac{1}{3} \text{ of } \frac{3\frac{1}{7}}{70}}$$

$$\frac{\frac{1\frac{4}{3} \text{ of } \frac{3\frac{1}{7}}{70}}{\frac{4}{3} \text{ of } \frac{3\frac{1}{7}}{70}} = \frac{\frac{2}{3}}{\frac{3}{7}} \times \frac{\frac{2}{7}}{7} \times \frac{\frac{8}{33}}{\frac{3}{33}} \times \frac{\frac{19}{7}}{9}$$

$$= \frac{32}{21} = 1\frac{1}{21}.$$

7. Simplify
$$\frac{2\frac{1}{2} - 1\frac{5}{6}}{1\frac{5}{6} - 1\frac{5}{6}}$$
.

$$\frac{2\frac{1}{2} - 1\frac{5}{6}}{1\frac{5}{6} - 1\frac{5}{6}} = \frac{180 - 112}{132 - 117} = \frac{68}{15} = 4\frac{8}{15}.$$

8. Simplify
$$\frac{10\frac{2}{5} - 1\frac{5}{7}}{7\frac{1}{5} - 3\frac{5}{40}}$$
.
$$\frac{10\frac{2}{5} - 1\frac{5}{7}}{7\frac{1}{4} - 3\frac{5}{40}} = \frac{2912 - 480}{1995 - 861} = \frac{2432}{1134} = 2\frac{164}{1134} = 2\frac{82}{567}.$$

9. Simplify
$$\frac{\frac{3}{7} \text{ of } 2\frac{1}{17}}{1\frac{2}{3} \div 2\frac{3}{7}}$$
.
$$\frac{\frac{3}{7} \text{ of } 2\frac{1}{17}}{1\frac{3}{7} \div 2\frac{3}{7}} = \frac{3}{7} \times \frac{35}{17} \times \frac{3}{5} \times \frac{17}{7} = \frac{9}{7} = 1\frac{3}{7}.$$

10. Simplify
$$\frac{6\frac{3}{4} - 1\frac{5}{14}}{2\frac{1}{6} + 1\frac{5}{7}}$$
.
$$\frac{6\frac{3}{4} - 1\frac{5}{14}}{2\frac{1}{4} + 1\frac{5}{7}} = \frac{567 - 114}{182 + 120} = \frac{453}{302} = 1\frac{151}{302} = 1\frac{1}{2}.$$

11. Simplify
$$\frac{5\frac{4}{3} + 2\frac{3}{13}}{4\frac{2}{3} - 3\frac{1}{13}}$$
.
$$5\frac{4}{5} + 2\frac{3}{7} = 7\frac{28 + 15}{35} = 7\frac{3}{15} = 8\frac{3}{15}.$$

$$4\frac{2}{3} - 3\frac{1}{13} = 1\frac{26 - 38}{39} = \frac{65 - 33}{39} = \frac{32}{39}.$$

$$\frac{5\frac{4}{3} + 2\frac{3}{7}}{4^2 - 3^{1}} = \frac{8\frac{3}{15}}{\frac{3}{2}} = \frac{288}{35} \times \frac{39}{32} = \frac{351}{35} = 10\frac{1}{35}.$$

12. Simplify
$$\frac{8\frac{3}{4}}{14} - \frac{\frac{2}{11}}{11}$$
.
$$\frac{8\frac{3}{4}}{14} = \frac{\frac{3}{3}}{4} \times \frac{1}{14} = \frac{5}{8}.$$

$$\frac{\frac{3}{4}}{11} = \frac{2}{3} \times \frac{7}{8} = \frac{7}{12}.$$

$$\frac{8\frac{3}{4}}{14} - \frac{2}{11} = \frac{5}{8} - \frac{7}{12} = \frac{15 - 14}{24} = \frac{1}{24}.$$

13. Simplify
$$\frac{3\frac{3}{1}}{11\frac{1}{4}}$$
 of $\frac{3\frac{3}{1}}{2\frac{3}{5}}$.
$$\frac{3\frac{3}{11}}{11\frac{1}{4}} \text{ of } \frac{3\frac{3}{11}}{2\frac{3}{5}} = \frac{24}{7} \times \frac{4}{45} \times \frac{3}{2} \times \frac{5}{12} = \frac{3}{7}$$

14. Simplify
$$\frac{5\frac{8}{5} - 4\frac{11}{12}}{5\frac{8}{5} - 2\frac{17}{12}}$$
.
$$\frac{5\frac{8}{5} - 4\frac{11}{12}}{5\frac{4}{5} - 2\frac{17}{12}} = \frac{424 - 354}{387 - 212} = \frac{70}{175} = \frac{2}{5}$$

15. Simplify
$$\frac{2\frac{3}{4} + 2\frac{7}{4}}{4\frac{3}{4} - 3\frac{1}{4}}$$
.

$$\frac{2\frac{3}{4} + 2\frac{7}{4}}{4\frac{3}{4} - 3\frac{1}{4}} = \frac{154 + 161}{266 - 176} = \frac{315}{90} = 3\frac{45}{90} = 3\frac{1}{2}.$$

16. Simplify
$$\frac{2\frac{8}{3} \times \frac{9}{11}}{3\frac{5}{7} \div 4\frac{1}{3}}$$
.

$$\frac{2\frac{3}{5} \times \frac{3}{11}}{3\frac{5}{7} + 4\frac{1}{8}} = \frac{13}{5} \times \frac{9}{11} \times \frac{7}{26} \times \frac{33}{8} = \frac{189}{80} = 2\frac{29}{80}.$$

17. Simplify
$$\frac{\frac{17}{20} + \frac{11}{13} + \frac{7}{10} + \frac{4}{5}}{\frac{17}{20} - \frac{11}{13} + \frac{7}{10} - \frac{4}{5}}$$
$$\frac{\frac{17}{20} + \frac{11}{13} + \frac{7}{10} + \frac{4}{5}}{\frac{17}{20} - \frac{11}{13} + \frac{7}{10} - \frac{4}{5}} = \frac{51 + 44 + 42 + 48}{51 - 44 + 42 - 48} = 185.$$

18. Simplify
$$\frac{4\frac{1}{7} - 2\frac{1}{4}}{6\frac{1}{4} - 2\frac{1}{4}}$$
.

$$\frac{4\frac{1}{7} - 2\frac{1}{4}}{6\frac{1}{7} - 2\frac{1}{4}} = \frac{116 - 63}{182 - 60} = \frac{53}{122}$$
.

19. Simplify
$$\frac{2\frac{27}{45} - 4\frac{1}{7} + \frac{31}{8}}{5\frac{6}{7} - 4\frac{7}{8} + \frac{31}{8}} = \frac{749 - 1280 + 875}{1640 - 1365 + 112} = \frac{344}{387} = \frac{8}{9}$$

20. Simplify
$$\frac{1\frac{1}{4} \times 1\frac{2}{7} + \frac{1}{3} \text{ of } 2\frac{1}{4} - \frac{1}{2}\frac{2}{3} \times 2}{\frac{1}{3} \text{ of } 2 + \frac{1}{3} \text{ of } 2\frac{1}{4} - 1\frac{1}{4} \text{ of } 1\frac{2}{7}}$$

$$\frac{1\frac{1}{4} \times 1\frac{2}{4} + \frac{1}{4} \text{ of } 2\frac{1}{4} - \frac{1\frac{2}{4}}{2\frac{2}{4}} \times 2}{\frac{1}{4} \times \frac{1}{4} \text{ of } 2\frac{1}{4} - \frac{1}{4} \times \frac{1}{4}}{\frac{1}{4} + \frac{2}{4} - \frac{1}{4} \times \frac{1}{4}} = \frac{45 + 21 - 26}{26 + 21 - 45} = \frac{40}{2} = 20.$$

21. Simplify
$$2\frac{1}{4} \times \frac{10\frac{3}{4} - 4\frac{1}{12}}{6\frac{3}{16} + 7\frac{3}{8}} \times \frac{3\frac{5}{12}}{1\frac{2}{8} \times 9\frac{1}{11}}$$
.
 $10\frac{3}{4} - 4\frac{1}{12} = 6\frac{9-1}{12} = 5\frac{21-11}{12} = 5\frac{1}{12} = 5\frac{3}{8}$.
 $6\frac{3}{16} + 7\frac{2}{8} = 13\frac{9+3}{48} = 13\frac{1}{48}$.

$$2\frac{1}{4} \times \frac{10\frac{3}{4} - 4\frac{11}{12}}{6\frac{3}{16} + 7\frac{3}{3}} \times \frac{3\frac{5}{12}}{1\frac{2}{8} \times 9\frac{1}{11}} = 2\frac{1}{4} \times \frac{5\frac{5}{8}}{13\frac{1}{48}} \times \frac{3\frac{5}{12}}{1\frac{2}{8} \times 9\frac{1}{11}}$$

$$= \frac{9}{4} \times \frac{3\cancel{5}}{\cancel{6}} \times \frac{\cancel{48}}{\cancel{66\cancel{5}}} \times \frac{\cancel{3}\cancel{8}}{\cancel{11}} \times \frac{\cancel{5}}{7} \times \frac{\cancel{11}}{\cancel{100}} = \frac{9}{35}.$$

$$= \frac{9}{4} \times \frac{\cancel{3}\cancel{5}}{\cancel{6}} \times \frac{\cancel{4}\cancel{8}}{\cancel{6}\cancel{6}\cancel{5}} \times \frac{\cancel{3}\cancel{8}}{\cancel{11}} \times \frac{\cancel{5}}{7} \times \frac{\cancel{11}}{\cancel{100}} = \frac{9}{35}.$$

22. Simplify
$$\frac{8\frac{7}{4} - 7\frac{6}{7} + 5\frac{5}{6} - 4\frac{4}{5}}{9\frac{6}{10} - 8\frac{1}{15} + 7\frac{7}{6} - 6\frac{6}{7}}$$

$$\frac{8\frac{7}{4} - 7\frac{6}{7} + 5\frac{5}{6} - 4\frac{4}{5}}{9\frac{10}{10} - 8\frac{13}{5} + 7\frac{7}{4} - 6\frac{6}{5}} = \frac{7455 - 6600 + 4900 - 4032}{8316 - 7448 + 6615 - 5760} = \frac{1723}{1723} = 1.$$

23. Simplify
$$\frac{1}{8} \times \frac{1}{9\frac{1}{4}} \times \frac{7\frac{1}{9}}{\frac{1}{8}} \times \frac{4\frac{3}{4}}{7\frac{3}{4}} \times \frac{3}{27} \times 1\frac{1}{8}$$
.

$$\frac{1}{8} \times \frac{4}{9\frac{1}{4}} \times \frac{7\frac{1}{4}}{4} \times \frac{4\frac{4}{5}}{7\frac{1}{14}} \times \frac{3}{27} \times 1\frac{1}{8}$$

$$= \frac{1}{7} \times \frac{1}{8} \times \frac{8}{7} \times \frac{2}{19} \times \frac{8}{9} \times \frac{9}{8} \times \frac{19}{4} \times \frac{14}{101} \times \frac{3}{27} \times \frac{9}{8} = \frac{1}{707}.$$

24. Simplify
$$\frac{27}{374} \times \frac{873}{981} \times \frac{7}{21} \times \frac{895}{128}$$
.

$$\frac{27}{37\frac{4}{5}} \times \frac{87\frac{3}{5}}{98\frac{1}{5}} \times \frac{7}{2\frac{1}{2}} \times \frac{89\frac{5}{128}}{128} = 27 \times \frac{3}{189} \times \frac{783}{9} \times \frac{8}{785} \times \frac{7}{8} \times \frac{2}{5} \times \frac{984}{11} \times \frac{1}{128} = \frac{41}{264}$$

25. Simplify
$$\frac{4\frac{1}{17}}{6\frac{1}{19}} \times \frac{170}{399} \div \frac{12\frac{2}{17}}{7\frac{2}{19}}$$
.

$$\frac{417}{619} \times \frac{170}{399} \div \frac{123}{73} = \frac{\cancel{69}}{\cancel{17}} \times \frac{\cancel{19}}{\cancel{113}} \times \frac{\cancel{179}}{\cancel{399}} \times \frac{\cancel{19}}{\cancel{9}} \times \frac{\cancel{3}}{\cancel{38}} = \frac{10}{57}.$$

26. Simplify
$$\left(1 - \frac{426}{697} + \frac{2\frac{1}{4}}{8\frac{1}{4}}\right) \div \frac{3\frac{1}{4}}{5\frac{1}{4}}$$

$$1 - \frac{426}{697} + \frac{21}{81} = \frac{271}{697} + \frac{5}{17} = \frac{271 + 205}{697} = \frac{476}{697} = \frac{28}{41}.$$

$$\left(1 - \frac{426}{697} + \frac{2\frac{1}{4}}{8\frac{1}{2}}\right) \div \frac{3\frac{1}{4}}{5\frac{1}{4}} = \frac{28}{41} \div \frac{3\frac{1}{4}}{5\frac{1}{4}} = \frac{\frac{7}{28}}{41} \times \frac{\frac{7}{2}}{7} \times \frac{41}{\frac{8}{4}} = 1.$$

27. Simplify
$$\frac{\frac{1}{6} \text{ of } \frac{1+\frac{1}{16}+1+\frac{1}{6} \text{ of } \frac{6+}{1}-1+\frac{1}{6} \text{ of } \frac{5+}{6}}{\frac{1}{6} \text{ of } \frac{2+}{6} \text{ of } \frac{5+}{6}}$$

$$\frac{1}{6} \text{ of } \frac{1+\frac{3}{6}}{\frac{1}{6}} = \frac{1}{6} \times \frac{29}{16} = \frac{29}{96}.$$

$$\frac{1}{6} \text{ of } \frac{6+}{6} = \frac{7}{6} \times \frac{25}{4} = \frac{175}{24}.$$

$$\frac{1}{6} \text{ of } \frac{5+}{6} = \frac{4}{3} \times \frac{49}{9} = \frac{196}{27}.$$

$$\frac{1}{6} \text{ of } \frac{2+}{6} \text{ of } \frac{5+}{3} = \frac{1}{6} \times \frac{17}{6} \times \frac{17}{3} = \frac{289}{108}.$$

$$\frac{1}{6} \text{ of } \frac{1+\frac{1}{6}+1+\frac{1}{6} \text{ of } \frac{6+}{2}-1+\frac{1}{6} \text{ of } \frac{5+}{2} = \frac{29}{108} + \frac{175}{108} - \frac{125}{108}$$

$$= \frac{261+6300-6272}{2312} = \frac{289}{2312} = \frac{1}{5}.$$

28. Simplify $\frac{$7 \times 51 \times 157 \times 151}{51}$.

$$\frac{\frac{17}{11} \times \frac{11}{11}}{\frac{51}{11}} = \frac{37}{68} \times \frac{\frac{17}{51}}{\frac{51}{111}} \times \frac{\frac{2}{8}}{\frac{152}{187}} \times \frac{\frac{17}{153}}{\frac{171}{11}} \times \frac{2}{11} = \frac{4}{121}$$

29. Simplify $\frac{\frac{3}{17} \times 9\frac{3}{19} \times 3\frac{1}{1} \times 9\frac{1}{10}}{\frac{4}{17} \times 3\frac{9}{19} \times 12\frac{1}{7} \times 2\frac{10}{83} \times \frac{7}{20}}$

$$\frac{\frac{3}{11} \times 9_{13} \times 3_{1} \times 9_{10}}{\cancel{4}_{7} \times 3_{19}^{9} \times 12_{1} \times 2_{3}^{10} \times \cancel{2}_{3}^{1}}$$

$$= \frac{3}{11} \times \frac{\cancel{120}}{\cancel{13}} \times \frac{\cancel{22}}{\cancel{7}} \times \frac{\cancel{91}}{\cancel{10}} \times \frac{\cancel{17}}{\cancel{4}} \times \frac{\cancel{19}}{\cancel{99}} \times \frac{\cancel{7}}{\cancel{85}} \times \frac{\cancel{33}}{\cancel{79}} \times \frac{\cancel{29}}{\cancel{7}} = 9.$$

30. Simplify $\frac{2\frac{3}{4} \times 7\frac{7}{11}}{\frac{1}{4} \times \frac{3}{4} \times 18\frac{3}{4}}$.

$$\frac{2\frac{3}{4} \times 7\frac{7}{11}}{\frac{1}{4} \times \frac{3}{4} \times 18\frac{3}{4}} = \frac{11}{4} \times \frac{34}{11} \times 2 \times \frac{4}{3} \times \frac{3}{36} = 3.$$

Exercise 62. Page 133.

1. What fraction of 8 is 3?

$$\frac{3}{8}$$
. Ans.

2. What fraction of 3 is 8?

$$\frac{8}{3}$$
 Ans.

3. What fraction of 9 is 7?

$$\frac{7}{9}$$
. Ans.

4. What fraction of 7 is 9?

$$\frac{9}{7}$$
. Ans.

5. What fraction of 8 is 12?

$$\frac{12}{8} = \frac{3}{2}$$
. Ans.

6. What fraction of 12 is 8?

$$\frac{8}{12} = \frac{2}{3}$$
. Ans.

7. What fraction of 2½ is §?

$$\frac{1}{21} = \frac{3}{11}$$
. Ans.

8. What fraction of $\frac{1}{2}$ is $2\frac{1}{2}$?

$$\frac{2\frac{1}{4}}{4} = \frac{11}{3}$$
. Ans.

9. What fraction of 2‡ is 1‡?

$$\frac{1\frac{1}{2}}{2\frac{3}{4}} = \frac{5}{11}$$
. Ans.

10. What fraction of $1\frac{1}{4}$ is $2\frac{\pi}{4}$?

$$\frac{24}{11} = \frac{11}{5}$$
 Ans.

11. What fraction of 21 is 71?

$$\frac{7\frac{1}{1}}{2\frac{1}{1}} = \frac{171}{56}$$
. Ans.

12. What fraction of 71 is 21?

$$\frac{2\frac{1}{1}}{7\frac{1}{4}} = \frac{51}{176}$$
. Ans.

13. What fraction of $3\frac{1}{2}$ is $8\frac{1}{2}$?

$$\frac{8\frac{1}{3}}{3\frac{1}{8}} = \frac{171}{70}$$
. Ans.

14. What fraction of \$2 is \$1\frac{1}{2}?

$$\frac{$1\frac{1}{2}}{$2} = \frac{3}{4}$$
 Ans.

15. What fraction of \$2\frac{1}{4} is \$5?

$$\frac{$5}{$21} = \frac{2}{1}$$
 Ans.

16. What fraction of \$\frac{1}{4}\$ is \$\frac{1}{4}\$?

$$\frac{\$ \frac{1}{4}}{\$ \frac{1}{4}} = \frac{1}{3}$$
 Ans.

17. What fraction of \$4 is \$4?

$$\frac{\$}{\$} = \frac{3}{10}$$
. Ans.

18. What fraction of \$2\frac{1}{2} is \$\frac{1}{2}\$?

$$\frac{\$1}{\$2\$} = \frac{4}{33}$$
. Ans.

19. What fraction of $\$\frac{1}{4}$ is $\$\frac{1}{10}$?

$$\frac{8}{8}\frac{1}{10} = \frac{1}{5}$$
 Ans.

20. What fraction of \$1 is \$7?

$$\frac{87}{81} = \frac{7}{8}$$
. Ans.

21. What fraction of \$10 is \$3? | 23. What fraction of \$100 is \$41?

$$\frac{\$\,\$}{\$\,10} = \frac{1}{15}$$
. Ans.

22. What fraction of \$100 is \$6?

$$\frac{86}{200} = \frac{3}{50}$$
. Ans.

$$\frac{\$4\frac{1}{1}}{\$100} = \frac{9}{200}$$
. Ans.

24. What fraction of \$4 is \$25?

$$\frac{$25}{$4} = \frac{25}{4}$$
 Ans.

25. What fraction of 1004 is 84?

$$\frac{8\frac{4}{5}}{100\frac{5}{5}} = \frac{76}{905} \cdot Ans.$$

26. What fraction of 21 is $\frac{15}{15}$ of $3\frac{4}{5}$?

$$\frac{\frac{15}{5} \times 3\frac{4}{5}}{21} = \frac{\cancel{15}}{\cancel{19}} \times \frac{\cancel{19}}{\cancel{5}} \times \frac{\cancel{1}}{\cancel{21}} = \frac{1}{7} \quad Ans.$$

27. What fraction of $18\frac{1}{12}$ is $\frac{\pi}{1}$ of $33\frac{\pi}{2}$?

$$\frac{\frac{5}{3} \times 33\frac{5}{4}}{18\frac{1}{2}\frac{17}{5}} = \frac{5}{8} \times \frac{135}{4} \times \frac{\frac{256}{32}}{\frac{256}{32}} = \frac{8}{7} \quad Ans.$$

28. What fraction of $3\frac{1}{2}$ is $\frac{3}{4} \times 1\frac{1}{4}$?

$$\frac{\frac{1}{3} \times 1}{3\frac{1}{3}} = \frac{2}{3} \times \frac{4}{3} \times \frac{3}{10} = \frac{4}{15}$$
 Ans.

29. What fraction of $3\frac{1}{11} \times 5\frac{1}{27}$ is 1720?

$$\frac{1720}{3\frac{1}{11} \times 5\frac{1}{27}} = \cancel{1720} \times \frac{11}{34} \times \frac{27}{\cancel{130}} = \frac{63855}{578}. \quad Ans.$$

30. What fraction of $3\frac{1}{4} \times \frac{8}{5}$ of $\frac{4}{18}$ is $1\frac{8}{5}$?

$$\frac{\frac{18}{3\frac{1}{4} \times \frac{8}{5} \times \frac{4}{7}}{3\frac{1}{4} \times \frac{8}{5} \times \frac{4}{7}} = \frac{8}{5} \times \frac{7}{7} \times \frac{9}{8} \times \frac{7}{4} = \frac{9}{10} \quad Ans.$$

31. What part of $\frac{25}{3} \times \frac{52}{63}$ is $\frac{1}{6} \times 4 \times \frac{3}{2}$?

$$\frac{\frac{1}{3} \times 4 \times \frac{1}{3}}{\frac{2}{3} \times \frac{5}{3} \times \frac{5}{3}} = \frac{1}{g} \times 4 \times \frac{2}{3} \times \frac{59}{28} \times \frac{63}{59} = \frac{1}{1}. \quad Ans.$$

32. What part of $13\frac{5}{8} \times \frac{2}{8} \times \frac{9}{65}$ is $\frac{2}{8}$ of $1\frac{4}{8}$ of $1\frac{1}{8}$?

$$\frac{\frac{3}{4} \times \frac{144}{134} \times \frac{11}{4}}{134 \times 4 \times 2} = \frac{2}{3} \times \frac{\cancel{109}}{\cancel{63}} \times \frac{\cancel{9}}{\cancel{8}} \times \frac{\cancel{8}}{\cancel{109}} \times \frac{\cancel{3}}{\cancel{2}} \times \frac{\cancel{63}}{\cancel{9}} = \frac{1}{1}. \quad Ans.$$

33. What part of $\frac{17}{20} + \frac{1}{15} + \frac{7}{10} + \frac{4}{5}$ is $\frac{17}{20} - \frac{11}{15} + \frac{7}{10} - \frac{4}{5}$?

$$\frac{\frac{17}{10} - \frac{11}{13} + \frac{7}{10} - \frac{4}{3}}{\frac{17}{10} + \frac{11}{13} + \frac{7}{10} + \frac{4}{3}} = \frac{51 - 44 + 42 - 48}{51 + 44 + 42 + 48} = \frac{1}{185}$$
 Ans.

34. What part of $4\frac{1}{7} - 2\frac{1}{7}$ is $6\frac{1}{7} - 2\frac{1}{7}$?

$$\frac{6\frac{1}{4}-2\frac{1}{7}}{4\frac{1}{7}-2\frac{1}{7}}=\frac{182-60}{116-63}=\frac{122}{53}$$
 Ans.

35. What part of $17\frac{2}{3} - 12\frac{4}{3}$ is $5 - \frac{1}{12} - \frac{4}{12} - \frac{1}{12}$?

$$\frac{5 - \frac{1}{13} - \frac{4}{10} - \frac{1}{25}}{173 - 123} = \frac{34125 - 525 - 700 - 273}{120575 - 87750} = \frac{32627}{32825}.$$
 Ans.

36. What part of $24 - 17\frac{4}{15}$ is $7 + \frac{2}{15} - \frac{5}{81} - \frac{11}{45}$?

$$\frac{7 + \frac{2}{15} - \frac{5}{11} - \frac{11}{12}}{24 - 17\frac{1}{12}} = \frac{36855 + 702 - 325 - 1287}{126360 - 91125} = \frac{35945}{35235} = \frac{7189}{7047}.$$
 Ans.

37. What part of $\frac{3}{7}$ of $2\frac{1}{17}$ is $1\frac{2}{8} + 2\frac{3}{7}$?

$$\frac{\frac{13}{3} \div 2\frac{3}{7}}{\frac{3}{7} \times 2\frac{1}{17}} = \frac{7}{17} \times \frac{5}{3} \times \frac{7}{3} \times \frac{17}{35} = \frac{7}{9} \cdot Ans.$$

38. What part of

$$\left(\frac{7}{4-\frac{5}{8}} - \frac{5}{6-\frac{3}{8}}\right) \div \left(\frac{4}{7-\frac{4}{7}} + \frac{2}{4-\frac{2}{8}}\right) \text{ is}$$

$$\left(14 - \frac{1}{\frac{1}{2} - \frac{6}{51}}\right) \div \left(\frac{1}{\frac{1}{2} - \frac{27}{55}} - 13\right)?$$

$$\left(14 - \frac{1}{\frac{1}{2} - \frac{6}{51}}\right) \div \left(\frac{1}{\frac{1}{2} - \frac{27}{55}} - 13\right)$$

$$\left(\frac{7}{4-\frac{5}{8}} - \frac{5}{6-\frac{3}{8}}\right) \div \left(\frac{4}{7-\frac{4}{7}} + \frac{2}{4-\frac{2}{5}}\right)$$

$$\frac{4 - \frac{62}{15} \div (\frac{118}{5} - 13)}{(\frac{12}{3} + \frac{13}{5})} = \frac{\frac{204}{19} \times \frac{5}{53}}{\frac{20}{3} + \frac{1}{3}} = \frac{102}{19}. \quad A$$

$$=\frac{(14-\frac{62}{19})\div(\frac{118}{5}-13)}{(\frac{12}{19}-\frac{8}{9})\div(\frac{23}{45}+\frac{5}{9})}=\frac{\frac{204}{19}\times\frac{5}{58}}{\frac{226}{11}\times\frac{45}{58}}=\frac{102}{113}. \ Ans.$$

Exercise 63. Page 134.

Reduce to a common fraction or to a mixed number:

- 1. $0.125 = \frac{125}{1000} = \frac{1}{1}$. Ans.
- 2. $0.625 = \frac{435}{1000} = \frac{4}{5}$. Ans.
- 3. $0.675 = \frac{675}{1000} = \frac{27}{20}$. Ans.
- 4. $10.864 = 10\frac{864}{1000} = 10\frac{11}{12}$. Ans.
- 5. $50.84 = 50\frac{84}{100} = 50\frac{21}{25}$. Ans.
- 6. $3.00025 = 3_{\overline{1000000}} = 3_{\overline{4000}}$. Ans.
- 7. $8.1075 = 8_{100000}^{10075} = 8_{4000}^{10075}$. Ans.
- **8.** $35.01024 = 35_{100000} = 35_{1200} = 35_{1250} = 35_{125}$. Ans.
- **9.** $7.015625 = 7\frac{155625}{100000} = 8\frac{1}{64}$. Ans.
- **10**. $20.100256 = 20\frac{100256}{1000000} = 20\frac{12582}{125000} = 20\frac{1133}{11250}$. Ans.
- **11.** $10.012575 = 10_{1000000} = 10_{40000}$. Ans.
- **12.** $104.235 = 104_{1000}^{23.5} = 104_{200}^{4.7}$. Ans.
- **13.** $50.0004 = 50_{\overline{10000}} = 50_{\overline{1500}}$. Ans.
- **14.** $100.001 = 100_{\overline{1000}}$. Ans.
- **15.** $8.00725 = 8_{10}^{7} \frac{25}{000} = 8_{4000}^{29}$. Ans.
- **16.** $20.018375 = 20_{1000000} = 20_{1000}^{147}$. Ans.
- **17.** $125.6048 = 125_{10000}^{6048} = 125_{1350}^{756} = 125_{135}^{75}$. Ans.
- **18.** $0.128 = \frac{1}{1000} = \frac{16}{125}$. Ans.
- **19.** $0.73125 = \frac{7}{100} \frac{1}{000} \frac{1}{000} = \frac{20}{1000} = \frac{117}{160}$. Ans.
- **20.** $1.1875 = 1_{100000}^{1.875} = 1_{100}^{75} = 1_{10}^{75} = 1_{10}^{8}$. Ans.
- **21.** $0.003125 = \frac{10000125}{1000000} = \frac{21125}{1000} = \frac{265}{1000} = \frac{125}{125}$. Ans.
- **22.** $0.03125 = 0.8333_0 = 0.25_0 = 0.1.$ Ans.
- **23.** $60.8125 = 60\frac{3}{10000} = 60\frac{3}{100} = 60\frac{3}{100}$. Ans.
- **24.** $7.0315 = 7_1 3 1 3_0 = 7_2 3_0$. Ans.
- **25.** $12.0025 = 12_{10000}^{625} = 12_{100}^{25} = 12_{10}^{25} = 12_{10}^{1}$. Ans.
- **26.** $4.7168 = 4_{170000}^{7100} = 4_{1230}^{800} = 4_{123}^{4}$. Ans.
- **27.** $0.0425 = \frac{1}{16660} = \frac{1}{400}$. Ans.
- **28.** $6.46875 = 6_{100000}^{4.6875} = 6_{100}^{7.5} = 6_{100}^{7.5} = 6_{100}^{7.5} = 6_{10}^{1.5}$. Ans.
- **29.** $0.00256 = \frac{256}{100000} = \frac{32}{12500} = \frac{8}{8125}$. Ans.
- 30. $0.000375 = \frac{1}{10000000} = \frac{15}{40000} = \frac{3}{1000}$. Ans.

Exercise 64. Page 135.

1. Reduce 7 to a decimal.

2. Reduce 15 to a decimal.

3. Reduce $\frac{9}{32}$ to a decimal.

4. Reduce $\frac{9}{25}$ to a decimal.

$$\frac{9}{25} = \frac{36}{100} = 0.36$$
. Ans.

5. Reduce 5 to a decimal.

6. Reduce $4\frac{11}{800}$ to a decimal.

7. Reduce 5_{33000} to a decimal.

8. Reduce $9_{\frac{1}{2}\frac{1}{2}\frac{1}{6}}$ to a decimal.

9. Reduce 11_{4000} to a decimal.

10. Reduce $\frac{9}{125}$ to a decimal.

11. Reduce $\frac{170}{4000}$ to a decimal.

12. Reduce 118 to a decimal.

13. Reduce $\frac{13}{625}$ to a decimal.

$$\begin{array}{r} 0.0208 \text{ Ans.} \\ 625)13.00 \\ \underline{1250} \\ \hline 5000 \\ 5000 \end{array}$$

14. Reduce $\frac{11}{256}$ to a decimal.

15. Reduce 180 to a decimal.

$$\begin{array}{r}
0.01875 \text{ Ans.} \\
169)0.30 \\
\underline{16} \\
140 \\
\underline{128} \\
120 \\
\underline{112} \\
80
\end{array}$$

16. Reduce $\frac{124}{16}$ to a decimal.

80

$$\frac{124}{16} = 7\frac{12}{16} = 7\frac{3}{4} = 7.75. \quad Ans.$$

17. Reduce $\frac{2}{3}$ of $1\frac{4}{3}$ to a decimal.

$$\frac{2}{3}$$
 of $1\frac{1}{5} = \frac{2}{3}$ of $\frac{3}{5} = \frac{6}{5} = \frac{12}{10} = 1.2$. Ans.

18. Reduce $\frac{3}{4}$ of $\frac{7}{10}$ to a decimal.

$$\frac{3}{4}$$
 of $\frac{5}{8}$ of $\frac{7}{10} = \frac{21}{64}$. Ans.

19. Reduce 3\footnote of 4\footnote to a decimal.

$$3\frac{1}{5}$$
 of $4\frac{1}{9} = \frac{\cancel{18}}{5} \times \frac{37}{\cancel{9}} = \frac{74}{5} = \frac{148}{10}$
= 14.8. Ans.

20. Reduce 33 of 42 to a decimal.

$$\frac{29}{32}$$
 of $\frac{49}{64} = \frac{1421}{2048}$.

0.69384765625 Ans.

10240

Exercise 65. Page 135.

Simplify by common fractions, then by reducing the common fractions to decimals, and show that the results in each example agree:

1.
$$7\frac{2}{5} + 4\frac{5}{5} + 9\frac{13}{25} + 11\frac{29}{25}$$
.
 $7\frac{2}{5} + 4\frac{5}{5} + 9\frac{13}{25} + 11\frac{29}{25} = 31\frac{135}{155} = 33\frac{25}{155} = 33.58125$.
 $7\frac{2}{5} + 4\frac{5}{5} + 9\frac{13}{25} + 11\frac{29}{25} = 7.4 + 4.625 + 9.65 + 11.90625 = 33.58125$.

2.
$$84\frac{18}{28} + 19\frac{1}{21} + \frac{41}{56}$$
.

$$84\frac{18}{26} + 19\frac{1}{21} + \frac{41}{36} = 103\frac{1865 + 1100 + 1722}{2100} = 103\frac{187}{2187} = 104\frac{2787}{2187} = 104.993809\frac{1}{21}.$$

$$84\frac{18}{25} + 19\frac{1}{25} + \frac{41}{25} = 84.65 + 19.523809\frac{1}{2} + 0.82 = 104.993809\frac{1}{2}$$

3.
$$4\frac{27}{64} + 13\frac{17}{64} + 42\frac{27}{64} + 2\frac{18}{64} + 1\frac{1}{2}$$
.

$$4\frac{27}{64} + 13\frac{17}{20} + 42\frac{87}{50} + 2\frac{18}{16} + 1\frac{1}{2} = 62\frac{675 + 1860 + 1864 + 1800 + 800}{1600} = 62\frac{819}{1600} = 65\frac{519}{1600} = 65.324375.$$

$$\frac{4\frac{2}{6}\frac{7}{4}+13\frac{1}{2}\frac{7}{6}+42\frac{2}{3}\frac{7}{6}+2\frac{1}{2}\frac{8}{6}+1\frac{1}{2}}{65.324375}=4.421875+13.85+42.74+2.8125+1.5$$

4.
$$5\frac{7}{8} + 13\frac{4}{5} + 19\frac{7}{16} + 7\frac{8}{20}$$
.

$$5\frac{7}{8} + 13\frac{4}{5} + 19\frac{7}{16} + 7\frac{3}{20} = 44\frac{70+6}{80}\frac{4+8}{80}\frac{5+12}{80} = 46\frac{21}{80} = 46\frac{21}{80} = 46.2625.$$

 $5\frac{7}{8} + 13\frac{4}{5} + 19\frac{7}{16} + 7\frac{3}{20} = 5.875 + 13.8 + 19.4375 + 7.15 = 46.2625.$

5.
$$5\frac{5}{10} + \frac{2}{3}$$
 of $1\frac{4}{5} + \frac{7}{8}$ of $2\frac{7}{7} + \frac{3}{4}$ of $\frac{5}{8}$.

$$5_{10}^{5} + \frac{2}{3} \times 1_{\frac{4}{5}} + \frac{7}{8} \times 2_{\frac{7}{7}} + \frac{2}{4} \times \frac{5}{8} = 5_{\frac{1}{7}}^{1} + 1_{\frac{1}{5}}^{1} + 2 + \frac{15}{32}^{1} = 8_{\frac{80 + 82 + 75}{160}}^{160} = 8_{\frac{1}{1}\frac{87}{60}}^{160} = 9_{\frac{1}{1}\frac{87}{60}}^{160} = 9.16875.$$

$$5\frac{5}{10} + \frac{2}{3} \times 1\frac{4}{5} + \frac{7}{6} \times 2\frac{2}{7} + \frac{3}{4} \times \frac{5}{8}$$

$$= 5.5 + 0.666\frac{2}{3} \times 1.8 + 0.875 \times 2.285714\frac{2}{7} + 0.75 \times 0.625$$

= $5.5 + 1.2 + 2 + 0.46875 = 9.16875$.

6. $1\frac{5}{12}$ of $2\frac{5}{3}$.

$$1_{\frac{5}{12}} \times 2_{\frac{5}{8}} = \frac{17}{12} \times \frac{21}{8} = \frac{119}{32} = 3_{\frac{33}{32}} = 3.71875.$$

$$1\frac{5}{18} \times 2\frac{5}{8} = 1.4166\frac{2}{8} \times 2.625 = 3.71875.$$

7.
$$3\frac{5}{16} + 2\frac{19}{20}$$
.

$$3\frac{5}{16} + 2\frac{19}{20} = 5\frac{2\cdot 5 + 7\cdot 6}{8\cdot 0} = 5\frac{101}{80} = 6\frac{21}{80} = 6.2625.$$

$$3\frac{5}{16} + 2\frac{19}{20} = 3.3125 + 2.95 = 6.2625.$$

8.
$$7\frac{2}{5} - 4\frac{5}{5}$$
.

$$7\frac{2}{8} - 4\frac{5}{8} = 3\frac{16-25}{40} = 2\frac{31}{40} = 2.775.$$
 $7\frac{2}{8} - 4\frac{5}{8} = 7.4 - 4.625 = 2.775.$

9.
$$82\frac{1}{3} - 37\frac{11}{16}$$
.

$$82\frac{1}{8} - 37\frac{1}{18} = 45\frac{16-55}{80} = 44\frac{1}{80} = 44.5125.$$

$$82\frac{1}{8} - 37\frac{1}{18} = 82.2 - 37.6875 = 44.5125.$$

10.
$$100 - 17\frac{18}{128}$$
.

$$100 - 17\frac{1}{6}\frac{1}{2}\frac{1}{5} = 82\frac{1}{2}\frac{1}{5} = 82.8192.$$

$$100 - 17\frac{1}{6}\frac{1}{2}\frac{1}{5} = 100 - 17.1808 = 82.8192.$$

11.
$$5\frac{1}{4} - 1\frac{1}{4}$$
 of $1\frac{1}{4}\frac{3}{4}$.

$$5\frac{1}{2} - 1\frac{1}{2} \times 1\frac{1}{2}\frac{3}{4} = 5\frac{1}{2} - 2\frac{5}{16} = 3\frac{3}{16} = 3.1875.$$

$$5\frac{1}{2} - 1\frac{1}{2} \times 1\frac{1}{2} = 5.5 - 1.5 \times 1.5416 = 5.5 - 2.3125 = 3.1875.$$

12.
$$\frac{14}{15} - \frac{11}{11}$$
.

$$\frac{14}{15} - \frac{11}{64} = \frac{896 - 275}{1600} = \frac{621}{1600} = 0.388125.$$

$$\frac{14}{15} - \frac{11}{64} = 0.56 - 0.171875 = 0.388125.$$

13.
$$8\frac{1}{3} - 1\frac{1}{2}$$
 of $\frac{3}{16}$.

$$8\frac{1}{5} - 1\frac{1}{2} \times \frac{8}{16} = 8\frac{1}{5} - \frac{9}{32} = 8\frac{8}{1}\frac{2-4}{6}\frac{5}{6} = 7\frac{147}{166} = 7.91875.$$

 $8\frac{1}{5} - 1\frac{1}{2} \times \frac{8}{16} = 8.2 - 1.5 \times 0.1875 = 8.2 - 0.28125 = 7.91875.$

14.
$$\frac{12}{12} \times 1000$$
.

$$\frac{12}{64} \times 1000 = \frac{2375}{8} = 2967 = 296.875.$$

 $\frac{12}{64} \times 1000 = 0.296875 \times 1000 = 296.875.$

Exercise 66. Page 137.

1. Reduce § to a decimal.

0.5. Ans.

2. Reduce 4 to a decimal.

0.45. Ans.

3. Reduce 3 to a decimal.

0.416

3.416. Ans.

4. Reduce 11 to a decimal.

0.183

0.183. Ans.

5. Reduce 317 to a decimal.

6. Reduce $2\frac{1}{87}$ to a decimal.

$$\begin{array}{r}
0.135 \\
37)5.0 \\
\underline{37} \\
130 \\
\underline{111} \\
190 \\
\underline{185} \\
5
\end{array}$$
2.135.. Ans.

7. Reduce $\frac{3}{3700}$ to a decimal.

$$0.00081$$
 $3799)0.0300$
 298
 $\overline{40}$
 37
 $\overline{3}$
 0.00081 . Ans.

8. Reduce 1111 to a decimal.

9. Reduce $9\frac{11}{108}$ to a decimal.

10. Reduce $11\frac{4}{35}$ to a decimal.

0.1142857
35)4.0
35
50
<u>35</u>
150
140
100
70
300
280
200
<u>175</u>
250
245
5
11.1142857. Ans.

11. Reduce 15 to a decimal.

0.267857142. Ans.

12. Reduce $\frac{4}{11}$ to a decimal. 0.380952

0.380952. Ans.

13. Reduce ## to a decimal.

14. Reduce \$7 to a decimal.

15. Reduce $2\frac{58}{255}$ to a decimal.

0.22745098039215686

2.22745098039215686. Ans.

16. Reduce 54 to a decimal.

$$5\frac{1}{100} = 5\frac{1}{100}$$
 $\frac{26}{40}$
 $\frac{39}{100}$
 $\frac{91}{90}$
 $\frac{78}{120}$
 $\frac{117}{3}$
 $\frac{117}{3}$
 $\frac{5.230769}{30769}$. Ans.

17. If $\frac{117}{5^7 \times 2^8}$ is expressed as a decimal, how many decimal places will the quotient contain?

As 7 is the highest power of 2 or 5 in the denominator, and as there are no other factors than 2 or 5, there will be seven decimal places in the quotient.

18. If $\frac{119}{2^5 \times 13}$ is expressed as a decimal, how many decimal places will precede the repetend?

As 5 is the highest power of 2 or 5 in the denominator, and as there is another factor than 2 or 5, five decimal places will precede the repetend.

19. If $\frac{57}{5^2 \times 7}$ is reduced to a decimal, how many decimal places will precede the repetend?

As 2 is the highest power of 2 or 5 in the denominator, and as there is another factor than 2 or 5, two decimal places will precede the petend.

Exercise 67. Page 138.

Reduce to a common fraction or to a mixed number:

1.
$$0.2\dot{4}\dot{5} = \frac{245-2}{990} = \frac{248}{990} = \frac{27}{110}$$

2.
$$0.4\dot{2}\dot{5} = \frac{425-4}{990} = \frac{121}{990}$$
.

3.
$$53.00\dot{2}4\dot{3} = 53_{9900}^{248} = 53_{9700}^{9}$$

4.
$$7.2011 = 72011-2 = 73009$$

5.
$$2.53\dot{0}\dot{6} = 2\frac{5806-58}{9900} = 2\frac{5358}{9800} = 2\frac{175}{8800}$$
.

6.
$$0.004\dot{2}\dot{6} = \frac{426-4}{99000} = \frac{422}{99000} = \frac{211}{49500}$$

7.
$$31.2\dot{0}\dot{3} = 31\frac{203-2}{990} = 31\frac{201}{990} = 31\frac{67}{830}$$
.

8.
$$0.35\dot{1} = \frac{451}{355} = \frac{15}{15}$$
.

9.
$$1.41\dot{6} = 1416-41 = 1875 = 15$$

10.
$$0.5\dot{5}7\dot{5} = \frac{5575-5}{9990} = \frac{557}{99} = \frac{557}{99}$$

11.
$$2.08\dot{1} = 2\frac{81}{990} = 2\frac{9}{110}$$
.

12.
$$5.12\dot{2}9\dot{7} = 5\frac{12297 - 12}{99900} = 5\frac{12285}{99900} = 5\frac{1}{740}$$

13.
$$0.35\dot{9}\dot{0} = \frac{3.590 - 3.5}{9.900} = \frac{3555}{9900} = \frac{79}{220}$$

14.
$$4.3\dot{1}6\dot{2} = 4\frac{3}{9}\frac{162-8}{9} = 4\frac{15}{9}\frac{15}{9} = 4\frac{1}{3}\frac{7}{7}$$

15.
$$0.7283 = \frac{7288-7}{9990} = \frac{7278}{9990} = \frac{288}{9990}$$

16.
$$5.1\dot{4}285\dot{7} = 5\frac{1}{9}\frac{4}{9}\frac{2}{9}\frac{5}{9}\frac{7}{9} = 5\frac{1}{9}\frac{4}{9}\frac{2}{9}\frac{5}{9}\frac{6}{9} = 5\frac{7}{4}\frac{1}{9}\frac{2}{9}\frac{6}{9}$$
.

17.
$$0.2368 = \frac{2368-2}{9990} = \frac{3888}{988} = \frac{1188}{1988}$$

18.
$$1.136 = 1\frac{136-1}{990} = 1\frac{135}{990} = 1\frac{27}{198} = 1\frac{3}{23}$$
.

19.
$$1.53\dot{1} = 153\dot{1} = 150$$

20.
$$3.28963 = 3\frac{28963 - 28}{99900} = 3\frac{28935}{9900} = 3\frac{648}{2220}$$
.

21.
$$5.878\dot{3} = 58788 - 878 = 57905 = 5527$$
.

22.
$$1.69408 = 1\frac{69498-6}{99990} = 169493 = 1\frac{15567}{16667}$$
.

23.
$$0.48\dot{3}2\dot{4} = \frac{48824-48}{99900} = \frac{48276}{99900} = \frac{447}{99900}$$

24.
$$0.00\dot{1}22\dot{1}\dot{3} = \frac{122\dot{1}3}{999900} = \frac{1357}{1111100}$$
.

Exercise 68. Page 140.

1. Find the G. C. M. and L. C. M. of 7, 14, 18.

$$\frac{14}{5} = \frac{2}{5}$$
.

The G. C. M. of 7, 14, 2 = 1.

The L. C. M. of 9, 27, 5 = 135.

 \therefore the G. C. M. required $= \frac{1}{15}$.

The L. C. M. of 7, 14, 2 = 14.

The G. C. M. of 9, 27, 5 = 1.

 \therefore the L. C. M. required = 14.

2. Find the G. C. M. and L. C. M. of $2\frac{2}{5}$, $2\frac{2}{5}$, $\frac{4}{10}$.

$$2\frac{3}{6} = \frac{20}{9}, \ 2\frac{3}{6} = \frac{12}{6}, \ \frac{4}{40} = \frac{1}{10}.$$

The G. C. M. of 20, 12, 1 = 1.

The L. C. M. of 9, 5, 10 = 90.

 \therefore the G. C. M. required $=\frac{1}{90}$.

The L. C. M. of 20, 12, 1 = 60.

The G. C. M. of 9, 5, 10 = 1.

 \therefore the L. C. M. required = 60.

3. Find the G. C. M. and L. C. M. of 33\$, 50\$.

$$33\frac{3}{4} = \frac{234}{1}$$
, $50\frac{5}{1} = \frac{495}{1}$.

The G. C. M. of 234, 405 = 9.

The L. C. M. of 7, 8 = 56.

 \therefore the G. C. M. required $=\frac{9}{56}$.

The L. C. M. of 234, 405 = 10,530.

The G. C. M. of 7, 8 = 1.

 \therefore the L. C. M. required = 10,530

4. Find the G. C. M. and L. C. M. of $\frac{7}{24}$, $\frac{35}{36}$, $\frac{49}{60}$.

The G. C. M. of 7, 35, 49 = 7.

The L. C. M. of 24, 36, 60 = 360.

 \therefore the G. C. M. required $= \frac{7}{860}$.

The L. C. M. of 7, 35, 49 = 245.

The G. C. M. of 24, 36, 60 = 12.

 $\therefore \text{ the L. C. M. required } = \frac{245}{12} = 20\frac{5}{12}.$

```
5. Find the G. C. M. and L. C. M. of 5\frac{1}{2}, 7\frac{1}{2}, 8\frac{1}{2}, 4\frac{3}{6}, 9\frac{1}{6}, 6\frac{5}{12}.
                                                                      5\frac{1}{2}, 7\frac{1}{3}, 8\frac{1}{4}, 4\frac{1}{3}, 9\frac{1}{3}, 6\frac{1}{12} = \frac{1}{2}, \frac{2}{3}, \frac{2}{3}, \frac{2}{3}, \frac{4}{3}, \frac{3}{3}, \frac{3
                                                                      The G. C. M. of 11, 22, 33, 44, 55, 77 = 11.
                                                                       The L. C. M. of 2, 3, 4, 9, 6, 12
                                                                                                                                                                                                                                                                                                                                                                                           = 36.
                                                                       ... the G. C. M. required
                                                                                                                                                                                                                                                                                                                                                                                                     = \frac{1}{11}.
                                                                      The L. C. M. of 11, 22, 33, 44, 55, 77
                                                                                                                                                                                                                                                                                                                                                                                                   = 4620.
                                                                      The G. C. M. of 2, 3, 4, 9, 6, 12
                                                                                                                                                                                                                                                                                                                                                                                                     = 1.
                                                                                                                                                                                                                                                                                                                                                                                                       = 4620.
                                                                       ... the L. C. M. required
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- 6. Find the G. C. M. and L. C. M. of $\frac{1}{2}$, $\frac{1}{4}$, $\frac{1}{5}$, $\frac{1}{6}$, $\frac{1}{10}$, $\frac{1}{12}$. The G. C. M. of 1, 1, 1, 1, 1, 1 =1.The L. C. M. of 2, 3, 4, 5, 6, 10, 12 = 60.... the G. C. M. required = %. The L. C. M. of 1, 1, 1, 1, 1, 1 = 1.The G. C. M. of 2, 3, 4, 5, 6, 10, 12 =1.... the L. C. M. required =1.
- 7. Find the G. C. M. and L. C. M. of $50\frac{1}{2}$, $67\frac{1}{2}$, $44\frac{1}{2}$, $84\frac{1}{2}$, 707. $50\frac{1}{4}$, $67\frac{1}{4}$, $44\frac{1}{8}$, $81\frac{1}{4}$, $707 = 12^{1}$, 22^{2} , 42^{4} , 52^{5} , 72^{7} . The G. C. M. of 101, 202, 404, 505, 707 = 101. The L. C. M. of 2, 3, 9, 6, 1 = 18.... the G. C. M. required = 49 = 511.The L. C. M. of 101, 202, 404, 505, 707 = 14,140. The G. C. M. of 2, 3, 9, 6, 1 = 1. ... the L. C. M. required = 14,140.
- 8. Find the G. C. M. and L. C. M. of $\frac{4}{5}$, $\frac{5}{6}$, $\frac{9}{7}$, $\frac{3}{5}$, $\frac{9}{10}$. The G. C. M. of 4, 5, 6, 7, 8, 9 = 1.The L. C. M. of 5, 6, 7, 8, 9, 10 = 2520.:. the G. C. M. required = 2520.The L. C. M. of 4, 5, 6, 7, 8, 9 = 2520.The G. C. M. of 5, 6, 7, 8, 9, 10 = 1.... the L. C. M. required = 2520.
- 9. Find the G. C. M. and L. C. M. of $1\frac{1}{14}$, $1\frac{1}{21}$, $4\frac{2}{7}$, $\frac{25}{2}$. 1_{14}^{1} , 1_{27}^{1} , 47, $\frac{25}{42} = \frac{15}{14}$, $\frac{47}{47}$, $\frac{89}{42}$. The G. C. M. of 15, 40, 30, 25 = 5.The L. C. M. of 14, 21, 7, 42 = 42.:. the G. C. M. required = 2The L. C. M. of 15, 40, 30, 25 = 600.The G. C. M. of 14, 21, 7, 42 = 7.= 490 = 854.

... the L. C. M. required

10. Find the G. C. M. and L. C. M. of 183, 571.

$$18\frac{2}{5} = \frac{92}{5}, \ 57\frac{1}{2} = \frac{115}{2}.$$

The G. C. M. of 92, 115 = 23.

The L. C. M. of 5, 2 = 10.

... the G. C. M. required $=\frac{23}{10}=2\frac{3}{10}$.

The L. C. M. of 92, 115 = 460.

The G. C. M. of 5, 2 = 1.

 \therefore the L. C. M. required = 460.

11. Find the G. C. M. and L. C. M. of 1342, 1281, 1151.

 $134\frac{3}{4}$, $128\frac{1}{8}$, $115\frac{1}{2} = \frac{539}{4}$, $\frac{335}{8}$, $\frac{231}{2}$.

The G. C. M. of 539, 385, 231 = 77.

The L. C. M. of 4, 3, 2 = 12.

... the G. C. M. required $=\frac{77}{4}=6\frac{6}{12}$.

The L. C. M. of 539, 385, 231 = 8085.

The G. C. M. of 4, 3, 2 = 1.

 \therefore the L. C. M. required = 8085.

12. Find the G. C. M. and L. C. M. of $2\frac{2}{3}$, $1\frac{2}{7}$, $\frac{68}{100}$.

$$2\frac{2}{2}\frac{2}{5}$$
, $1\frac{3}{7}\frac{7}{5}$, $\frac{63}{100} = \frac{72}{25}$, $\frac{112}{75}$, $\frac{68}{100}$.

The G. C. M. of 72, 112, 63 = 1.

The L. C. M. of 25, 75, 100 = 300.

 $\therefore \text{ the G. C. M. required } = \frac{1}{800}.$

The L. C. M. of 72, 112, 63 = 1008.

The G. C. M. of 25, 75, 100 = 25.

 $\therefore \text{ the L. C. M. required } = \frac{1008}{25} = 40\frac{8}{25}.$

13. A, B, and C start together to walk in the same direction round a circular island. It takes A 2½ days, B 2½ days, C 2½ days to walk round the island. They walk until they all meet at the point of starting. In how many days will they be together at the point of starting?

$$2\frac{1}{3}$$
, $2\frac{5}{6}$, $2\frac{7}{8} = \frac{7}{8}$, $\frac{17}{6}$, $\frac{23}{8}$.

The L. C. M. of 7, 17, 23 = 2737.

The G. C. M. of 3, 6, 8 = 1.

:. the L. C. M. required = 2737.

2737 days. Ans.

14. If the step of a man is 2\frac{1}{2} feet, and that of a horse is 2\frac{3}{4} feet, find the smallest number of feet which is an exact number of steps for a man and for a horse.

$$2\frac{1}{3}$$
, $2\frac{3}{4}$, $=\frac{7}{3}$, $\frac{11}{4}$.

The L. C. M. of 7, 11 = 77.

The G. C. M. of 3, 4 = 1.

.. the L. C. M. required = 77.

77 feet. Ans.

15. Find the largest number that is contained without remainder in $2\frac{5}{5}$, $6\frac{7}{18}$, $11\frac{1}{2}$, and $19\frac{1}{6}$.

25,
$$6\frac{7}{15}$$
, $11\frac{1}{2}$, $19\frac{1}{6} = \frac{28}{5}$, $\frac{115}{18}$, $\frac{23}{2}$, $\frac{115}{6}$.

The G. C. M. of 23, 115, 23, 115 = 23.

The L. C. M. of 9, 18, 2, $6 = 18$.

 \therefore the G. C. M. required $= \frac{23}{15} = 1\frac{5}{15}$. Ans.

Exercise 69. Page 141.

1. Simplify \$788, 48785, 587216, \$087.

$$\frac{2709}{6966} = \frac{301}{774} = \frac{7}{18} \cdot Ans. \qquad \frac{43785}{56835} = \frac{8757}{11367} = \frac{973}{1263} \cdot Ans.$$

$$\frac{2436}{567216} = \frac{203}{47268} \cdot Ans. \qquad \frac{4087}{5063} = \frac{67}{83} \cdot Ans.$$

2. Which is greater, and by how much, 7 or 12?

$$\frac{7}{9}$$
, $\frac{19}{24} = \frac{56}{72}$, $\frac{57}{72}$. $\therefore \frac{19}{24}$ is greater by $\frac{1}{72}$.

3. Find the sum of $3\frac{2}{5}$, $2\frac{4}{11}$, $5\frac{1}{2}$, $7\frac{7}{10}$, $1\frac{8}{23}$.

$$3\frac{2}{6} + 2\frac{4}{11} + 5\frac{1}{2} + 7\frac{7}{10} + 1\frac{3}{22} = 18\frac{44+40+55+77+15}{110} = 18\frac{23}{110} = 20\frac{11}{10} = 20\frac{1}{10}. Ans.$$

4. Simplify $5\frac{1}{2} - 3\frac{3}{7} + 2\frac{9}{10} - 1\frac{3}{5}$.

$$5\frac{1}{2} + 2\frac{9}{10} = 7\frac{5+9}{10} = 7\frac{14}{10} = 8\frac{4}{10} = 8\frac{3}{5}.$$

$$3\frac{3}{7} + 1\frac{3}{5} = 4\frac{15+21}{85} = 4\frac{3}{5} = 5\frac{1}{35}.$$

$$8\frac{2}{7} - 5\frac{1}{35} = 3\frac{14-1}{35} = 3\frac{13}{35}. \quad Ans.$$

5. Simplify $1\frac{4}{5} + 3\frac{5}{6} - 2\frac{7}{12} + 4\frac{3}{20} - 3\frac{7}{15}$.

$$1\frac{4}{5} + 3\frac{5}{6} + 4\frac{3}{20} = 8\frac{45 + 50 + 9}{60} = 8\frac{107}{60} = 9\frac{47}{60}.$$

$$2\frac{7}{12} + 3\frac{7}{15} = 5\frac{35 + 28}{60} = 5\frac{38}{60} = 6\frac{3}{60}.$$

$$9\frac{47}{60} - 6\frac{3}{60} = 3\frac{44}{60} = 3\frac{11}{15}. Ans.$$

6. Simplify
$$\frac{3\frac{1}{4} + 3\frac{5}{6}}{4\frac{1}{4} - 2\frac{7}{12}}$$
.
 $\frac{3\frac{1}{4} + 3\frac{5}{6}}{4\frac{1}{4} - 2\frac{7}{12}} = \frac{42 + 46}{52 - 31} = \frac{88}{21} = 4\frac{4}{21}$. Ans.

7. Simplify
$$7 + 2\frac{3}{4}$$
; $\frac{7}{1\frac{3}{8}}$; $\frac{95\frac{1}{4}}{8\frac{7}{17}}$; $15 + \frac{2}{3}$; $\frac{16}{5\frac{1}{4}}$; $7\frac{1}{11} + 9$; $43\frac{1}{4} + 37\frac{1}{3}$; $\frac{67}{18\frac{1}{4}}$; $5\frac{4}{5} + 4\frac{5}{6}$; $\frac{4}{11} \circ 6\frac{1}{4\frac{1}{4}}$; $106 + 8\frac{5}{6}$; $\frac{17}{4\frac{7}{17}}$
 $7 + 2\frac{3}{4} = \frac{4}{11} \times 7 = \frac{28}{11} = 2\frac{6}{11}$
 $43\frac{1}{4} + 37\frac{1}{3} = \frac{3}{112} \times \frac{173}{4} = \frac{519}{448} = 1\frac{71}{448}$.

 $\frac{7}{1\frac{3}{8}} = \frac{8}{11} \times 7 = \frac{56}{11} = 5\frac{1}{11}$
 $\frac{617}{18\frac{1}{4}} = \frac{4}{73} \times \frac{73}{11} = \frac{4}{11}$
 $\frac{95\frac{1}{4}}{8\frac{1}{11}} = \frac{11}{95} \times \frac{191}{2} = \frac{2101}{190} = 11\frac{11}{190}$
 $\frac{617}{18\frac{1}{4}} = \frac{4}{73} \times \frac{73}{11} = \frac{4}{11}$
 $\frac{15}{4} = \frac{3}{2} \times 15 = \frac{45}{2} = 22\frac{1}{2}$
 $\frac{1}{4} \circ 6\frac{41}{4} = \frac{3}{8} \times \frac{9}{2} \times \frac{4}{7} \times \frac{2}{3} = \frac{9}{14}$
 $\frac{16}{5\frac{1}{4}} = \frac{3}{16} \times 16 = 3$
 $\frac{9}{7^{1}} + 9 = \frac{1}{9} \times \frac{81}{11} = \frac{9}{11}$
 $\frac{17}{47} = \frac{17}{75} \times 17 = \frac{289}{75} = 3\frac{4}{5}$

8. Simplify $7\frac{1}{3} \times 8$; $43\frac{1}{3} \times 6\frac{1}{3}$; $6\frac{1}{5} \div 8\frac{1}{3}$; $5\frac{1}{14} \times 51$; $\frac{1}{14}$ of $\frac{1}{14}$; $\frac{1}{2}$ of $\frac{1}{4}$ of \frac

$$7\frac{1}{1}\frac{1}{1} \text{ of } \frac{7}{1}\text{ of } \frac{2}{3}\text{ of } \frac{2}{3}\text{ of } \frac{2}{3}\frac{2}{6}\frac{2}{3}; \frac{1}{2} \times \frac{2}{4} \times \frac{7}{11} \times \frac{2}{3} \times \frac{2}{3}.$$

$$7\frac{1}{3}\frac{2}{4} \times 8 = \frac{243}{32} \times 8 = \frac{243}{4} = 60\frac{2}{4}.$$

$$43\frac{1}{6}\frac{2}{3} \times 6\frac{2}{3} = \frac{2292}{53} \times \frac{33}{8} = \frac{573}{2} = 286\frac{1}{2}.$$

$$6\frac{1}{6}\frac{1}{6} + 8\frac{1}{6} = \frac{5}{6}.$$

$$5\frac{1}{17} \times 51 = \frac{86}{17} \times \frac{3}{5}I = 258.$$

$$\frac{17}{19} \text{ of } \frac{228}{56I} = \frac{4}{11}.$$

$$\frac{11}{12} \text{ of } \frac{11}{13} = \frac{121}{156}.$$

$$\frac{2}{39} \text{ of } \frac{7}{15} \text{ of } \frac{7}{8} \text{ of } \frac{2}{3} \text{ of } \frac{2}{5} = \frac{1}{15}.$$

$$\frac{1}{2} \times \frac{3}{4} \times \frac{7}{11} \times \frac{8}{9} \times \frac{3}{7} = \frac{1}{11}.$$

9. By what must \(\frac{1}{2}\) be multiplied to obtain \(\frac{1}{2}\)? \(\frac{1}{2}\) to obtain \(\frac{1}{2}\)? \(\frac{1}{2}\) to obtain \(\frac{1}{2}\)? \(\frac{1}{2}\) to obtain \(\frac{1}{2}\)?

$$\frac{1}{2} + \frac{1}{6} = \overset{3}{\cancel{6}} \times \frac{1}{\cancel{2}} = 3. \quad Ans.$$

$$\frac{5}{6} + \frac{1}{2} = \cancel{2} \times \frac{5}{\cancel{6}} = \frac{5}{3} = 1\frac{3}{3}. \quad Ans.$$

$$\frac{2}{3} + \frac{1}{6} = \overset{2}{\cancel{6}} \times \frac{2}{\cancel{3}} = 4. \quad Ans.$$

$$\frac{5}{6} + \frac{2}{3} = \overset{3}{\cancel{2}} \times \frac{5}{\cancel{6}} = \frac{5}{4} = 1\frac{1}{4}. \quad Ans.$$

$$\frac{7}{8} + \frac{3}{5} = \overset{5}{\cancel{3}} \times \frac{7}{8} = \frac{35}{24} = 1\frac{11}{24}. \quad Ans.$$

10. By what must $\frac{1}{6}$ be divided to obtain $\frac{1}{2}$? $\frac{2}{3}$ to obtain $\frac{1}{6}$?

$$\frac{1}{6} + \frac{1}{2} = 2 \times \frac{1}{6} = \frac{1}{3}. \quad Ans.$$

$$\frac{7}{8} + \frac{4}{5} = \frac{5}{4} \times \frac{7}{8} = \frac{35}{32} = 1\frac{3}{12}. \quad Ans.$$

$$\frac{2}{3} + \frac{1}{6} = \cancel{2} \times \frac{2}{3} = 4. \quad Ans.$$

$$\frac{3}{5} + \frac{7}{8} = \frac{8}{7} \times \frac{3}{5} = \frac{24}{35}. \quad Ans.$$

$$8 + 7\frac{19}{32} = \frac{32}{243} \times 8 = \frac{256}{243} = 1\frac{13}{243}. \quad Ans.$$

11. What number exceeds 5% by 4%?

$$5\frac{2}{9} + 4\frac{7}{8} = 9\frac{1.6 + 6.8}{7.2} = 9\frac{79}{72} = 10\frac{7}{72}$$
. Ans.

12. From what must 6 be subtracted to leave 1 of 31?

$$\frac{1}{2} \text{ of } 8\frac{1}{9} = \frac{1}{2} \times \frac{\frac{14}{28}}{9} = \frac{14}{9} = 1\frac{5}{9}.$$

$$6\frac{5}{8} + 1\frac{5}{9} = 7\frac{27 + 25}{45} = 7\frac{52}{45} = 8\frac{7}{45}. \text{ Ans.}$$

13. What fraction falls short of $\frac{7}{12}$ by $\frac{3}{10}$?

$$\frac{7}{12} - \frac{3}{20} = \frac{35 - 9}{60} = \frac{26}{60} = \frac{13}{30} \cdot Ans.$$

14. What fraction must be added to $\frac{5}{76}$ to make $\frac{1}{3}$?

$$\frac{11}{57} - \frac{5}{76} = \frac{44 - 15}{228} = \frac{29}{228} \cdot Ans.$$

13. Reduce to decimals: \(\frac{1}{4}\);

$$\frac{3)1.0}{0.3}$$

2)1.
$$4)1.$$
 $3)1.0$ $4)3.$ $8)1.$ 0.125 $1 = 0.5.$ $1 = 0.5.$ $1 = 0.25.$ $1 = 0.3.$ $1 = 0.75.$ $1 = 0.125.$

$$\therefore \ \ \frac{1}{2} = 0.25.$$

$$\therefore 1 = 0.8.$$

$$\therefore = 0.75$$

$$-1 = 0.125$$

8)3. 8)5. 8)7. 16)1. 0.0625

$$0.375$$
 0.625 0.875 0.0625 $\frac{3}{0.1875}$
 $\therefore \frac{1}{8} = 0.375$. $\therefore \frac{1}{4} = 0.625$. $\therefore \frac{1}{16} = 0.0625$.

$$\therefore \ \S=0.625.$$

$$1 = 0.875$$

$$1_{6} = 0.0625$$

$$\therefore \frac{3}{16} = 0.1875.$$

0.0625

$$\therefore \frac{5}{16} = 0.3125. \quad \therefore \frac{7}{16} = 0.4375. \quad \therefore \frac{9}{16} = 0.5625. \quad \therefore \frac{11}{16} = 0.6875.$$

$$\frac{7}{16} = 0.4375.$$

0.4375.

$$\therefore \frac{9}{16} = 0.5625.$$

$$H = 0.687$$

$$\frac{0.0625}{1875}$$

$$\therefore \ \S = 0.83$$

$$\therefore \frac{18}{18} = 0.8125.$$
 $\therefore \frac{18}{18} = 0.9375.$

$$7)3.$$
 $9)5.$ $11)3.$ $49)0.7$ 0.428571 0.5 0.27 0.175

$$\therefore \ \ \ \, \mathbf{3} = \mathbf{0.5}.$$

$$\therefore \ \mathbf{4} = 0.\dot{2}\dot{7}.$$

$$\therefore \Lambda_{\pi} = 0.175$$

16. Reduce to common fractions: 0.16; 0.016; 0.125; 0.13; 0.725; 0.625; 0.00625; 0.8125; 0.03125; 0.08; 0.54; 0.016; 0.5437; 0.027; $0.27\dot{7}$; $0.68\dot{4}9\dot{4}$; $1.3\dot{4}\dot{5}$.

$$0.16 = \frac{16}{100} = \frac{4}{25}$$

$$0.725 = \frac{725}{1000} = \frac{29}{40}.$$

$$0.016 = \frac{16}{1000} = \frac{2}{125}.$$

$$0.625 = \frac{625}{1000} = \frac{25}{45} = \frac{5}{8}.$$

$$0.125 = \frac{125}{1000} = \frac{1}{8}.$$

$$0.00625 = \frac{625}{100000} = \frac{25}{4000} = \frac{1}{160}.$$

$$0.13 = \frac{18}{100}$$
.

$$0.8125 = \frac{1125}{10000} = \frac{125}{400} = \frac{13}{10}.$$

$$0.03125 = \frac{3125}{100000} = \frac{125}{100} = \frac{1}{100} = \frac{1}{12}.$$

$$0.08 = \frac{1}{100} = \frac{2}{15}.$$

$$0.5\dot{4} = \frac{34}{900} = \frac{1}{10}.$$

$$0.01\dot{6} = \frac{16-1}{900} = \frac{15}{900} = \frac{1}{60}.$$

$$0.5\dot{4}3\dot{7} = \frac{5437-5}{9990} = \frac{3432}{9990} = \frac{2716}{4995}.$$

$$0.0\dot{2}\dot{7} = \frac{277-27}{900} = \frac{259}{900} = \frac{5}{18}.$$

$$0.68\dot{4}9\dot{4} = \frac{68494-68}{99900} = \frac{3426}{99900} = \frac{34313}{99900}.$$

$$1.3\dot{4}\dot{5} = 1\frac{345-3}{9900} = 1\frac{342}{990} = 1\frac{171}{175} = 1\frac{19}{15}.$$

17. Simplify $\frac{2.8 \text{ of } 2.\dot{2}\dot{7}}{1.1\dot{3}\dot{6}}$.

$$2.\dot{2}\dot{7} = 2\frac{27}{69} = 2\frac{8}{11}; \quad 1.\dot{3}\dot{6} = 1\frac{186-1}{990} = 1\frac{185}{190} = 1\frac{1}{110} = 1\frac{3}{22}.$$

$$\therefore \quad \frac{2.8 \text{ of } 2.\dot{2}\dot{7}}{1.\dot{3}\dot{6}} = \frac{24}{1\frac{3}{11}} \times \frac{25}{11} \times \frac{25}{25} = \frac{28}{5} = 5\frac{3}{5} = 5.6. \quad Ans.$$

18. Multiply 6.954 by 5.303, and express the result as a whole number and common fraction.

$$6.9\dot{5}\dot{4} = 6\frac{9}{9}\frac{5}{9}\frac{4-9}{9} = 6\frac{9}{9}\frac{45}{9} = 6\frac{1}{1}\frac{15}{16} = 6\frac{1}{2}\frac{1}{3};$$

$$5.3\dot{0}\dot{3} = 5\frac{3}{9}\frac{9}{9}\frac{3-3}{0} = 5\frac{9}{9}\frac{9}{9} = 5\frac{1}{3}\frac{9}{3};$$

$$\vdots \quad 6.9\dot{5}\dot{4} \times 5.3\dot{0}\dot{3} = 6\frac{1}{2}\frac{1}{2} \times 5\frac{1}{3}\frac{9}{3} = \frac{15\cancel{3}}{22} \times \frac{175}{\cancel{3}\cancel{3}} = \frac{8925}{242} = 36\frac{1}{2}\frac{1}{3}\frac{9}{3}. \quad Ans.$$

$$11$$

19. Simplify $1\frac{1}{2}$ of $2\frac{4}{5} + 6\frac{7}{5} + 2\frac{5}{4}$ and reduce the result to a decimal.

$$1\frac{1}{3} \text{ of } 2\frac{1}{5} + 6\frac{7}{3} \div 2\frac{3}{4} = \frac{3}{2} \times \frac{\cancel{14}}{5} + \frac{\cancel{4}}{\cancel{11}} \times \frac{\cancel{5}\cancel{5}}{\cancel{5}} = \frac{21}{5} + \frac{5}{2}$$
$$= 4\frac{1}{5} + 2\frac{1}{2} = 6\frac{2+5}{10} = 6\frac{7}{10} = 6.7. \text{ Ans.}$$

20. From what number can 417 be taken 9 times and leave no remainder?

$$9 \times 4\frac{17}{86} = 9 \times \frac{161}{36} = \frac{161}{4} = 40\frac{1}{4}$$
. Ans.

21. Of what fraction is 17 the 7th part?

$$17\frac{1}{8} \div \frac{1}{7} = \frac{52}{3} \times 7 = \frac{364}{3}$$
. Ans.

22. Add $\frac{4}{5}$, 0.35, $\frac{5}{5}$, $\frac{3}{5}$, 0.112, 45.28. $\frac{4}{5} + 0.35 + \frac{5}{5} + \frac{3}{5} + 0.112 + 45.28 = 0.8 + 0.35 + 0.625 + 0.75 + 0.112 + 45.28 = 47.917. Ans.$

23. Reduce to decimals $\frac{13}{13}$; $\frac{3}{11}$; $\frac{4}{35}$; $\frac{17}{60}$; $\frac{14}{13}$; $\frac{5}{13}$.

24. What part of $\frac{15}{18}$ is $\frac{3}{1241}$?

$$\frac{3}{1241} \div \frac{15}{73} = \frac{73}{15} \times \frac{3}{1241} = \frac{1}{85} \cdot Ans.$$

25. Divide 0.0015 by 0.012, and express the result as a common fraction in lowest terms.

$$012)1.5 \\ 0.125 0.125 = \frac{1}{8}. Ans.$$

26. Reduce to decimals: $\frac{3}{32}$; $\frac{3}{32000}$; $\frac{17}{4}$; $\frac{1}{7}$.

$$\frac{8}{82000} = 0.00009375.$$

$$\therefore \frac{17}{4} = 0.2297.$$

27. The product of two factors is $\frac{1}{2}$, and one factor is $1\frac{1}{4}$; find the other factor.

$$\frac{5}{8} \div 1\frac{1}{4} = \frac{4}{5} \times \frac{5}{8} = \frac{1}{2} \cdot Ans.$$

28. The dividend is $\frac{1}{12}$, the quotient $6\frac{1}{2}$; find the divisor.

$$\frac{11}{12} \div 6\frac{1}{2} = \frac{2}{13} \times \frac{11}{12} = \frac{11}{78} \cdot Ans.$$

29. The dividend is $12\frac{1}{4}$, quotient 3, remainder $1\frac{1}{12}$; find the divisor.

$$(12\frac{17}{12} - 1\frac{5}{12}) \div 3 = 10\frac{5}{12} \div 3 = \frac{1}{3} \times \frac{779}{72} = \frac{779}{218} = 3\frac{1}{218}$$
. Ans.

30. Find the G. C. M. and the L. C. M. of 833, 1127, 1421, 343.

The G. C. M. = $7 \times 7 = 49$. Ans.

The L. C. M. =
$$78 \times 17 \times 23 \times 29 = 3,889,277$$
. Ans.

31. Arrange in order of magnitude $\frac{9}{11}$, $\frac{23}{15}$, $\frac{19}{27}$, $\frac{17}{20}$, $\frac{29}{32}$.

$$\frac{2}{11} = \frac{4560}{5540}. \quad \frac{22}{45} = \frac{4324}{5540}. \quad \frac{12}{27} = \frac{4150}{5940}. \quad \frac{17}{20} = \frac{3040}{5940}. \quad \frac{20}{33} = \frac{8600}{5940}.$$

$$\frac{17}{20}, \quad \frac{9}{11}, \quad \frac{22}{45}, \quad \frac{19}{27}, \quad \frac{29}{33}. \quad Ans.$$

32. Find the L. C. M. of 15, 25, 25, 103.

The L. C. M. of 15, 26, 65 = 390.

The G. C. M. of 17, 51, 102 = 17.

 \therefore the L. C. M. required $=\frac{380}{12}=22\frac{15}{2}$.

33. Find the G. C. M. of $\frac{65}{68}$, $\frac{89}{2}$, $\frac{81}{6}$, and $6\frac{1}{2}$.

The G. C. M. of 65, 39, 91, 13 = 13.

The L. C. M. of 68, 2, 64, 2 = 1088.

 \therefore the G. C. M. required $= \frac{1}{1088}$

34. Reduce to common fractions: 7.2011; 6.954.

$$7.2011 = 7\frac{2011-2}{9990} = 7\frac{200}{500}. \qquad 6.954 = 6\frac{54-9}{990} = 6\frac{45}{500} = 6\frac{105}{100} = 6\frac{1}{100}.$$

35. Simplify
$$\frac{3\frac{7}{6} \times 1\frac{1}{17} + 4\frac{1}{12} - 3\frac{9}{16}}{5\frac{1}{9} - 7\frac{7}{8} \div 28\frac{7}{20} + \frac{1}{3}}.$$

$$3\frac{7}{8} \times 1\frac{1}{17} = \frac{\frac{2}{34}}{9} \times \frac{\frac{1}{18}}{17} = 4;$$
 $7\frac{7}{8} + 28\frac{7}{20} = \frac{63}{8} \times \frac{\frac{5}{20}}{\frac{567}{2}} = \frac{5}{18}$

$$\frac{3\frac{7}{6} \times 1_{17} + 4_{12} - 3_{16}}{5\frac{1}{9} - 7\frac{7}{8} \div 28_{20} + \frac{1}{3}} = \frac{4 + 4_{12} - 3_{16}}{5\frac{1}{9} - \frac{5}{18} + \frac{1}{8}} = \frac{4\frac{25}{48}}{5\frac{1}{8}} = \frac{7}{8}. Ans.$$

36. Simplify $\frac{6\frac{3}{4} + 5\frac{1}{2} \times 3\frac{1}{4} - 7\frac{1}{4}}{3\frac{1}{8} + 2\frac{1}{2} - 4\frac{1}{10}}$

$$5\frac{1}{2} \times 3\frac{1}{7} = \frac{11}{2} \times \frac{22}{7} = \frac{121}{7} = 17\frac{3}{7}.$$

$$\frac{6\frac{1}{4} + 5\frac{1}{4} \times 3\frac{1}{4} - 7\frac{1}{4}}{3\frac{1}{5} + 2\frac{1}{2} - 4\frac{1}{10}} = \frac{6\frac{3}{4} + 17\frac{3}{4} - 7\frac{1}{4}}{3\frac{1}{5} + 2\frac{1}{4} - 4\frac{1}{10}} = \frac{945 + 2420 - 1015}{448 + 350 - 574}$$
$$= \frac{2350}{224} = 10\frac{1}{2}\frac{10}{2} = 10\frac{55}{112}. \quad Ans.$$

37. Simplify $\frac{2\frac{4}{3}-1\frac{1}{2}+9\frac{1}{11}}{4\frac{1}{4}-2\frac{1}{2}+13\frac{7}{12}}$

$$\frac{2\frac{4}{5} - 1\frac{1}{2} + 9\frac{1}{11}}{4\frac{1}{5} - 2\frac{1}{4} + 13\frac{7}{11}} = \frac{616 - 330 + 2000}{924 - 495 + 3000} = \frac{2286}{3429} = \frac{2}{3} \cdot Ans.$$

38. Simplify $\frac{(3.71-1.908)\times7.03}{2.2-74}$.

$$\frac{(3.71-1.908)\times7.03}{2.2-\frac{74}{333}} = \frac{1.802\times7.03}{2\frac{2}{9}-\frac{2}{9}} = \frac{12.66806}{2} = 6.33403. \text{ Ans.}$$

39. Simplify
$$\frac{5\frac{5}{8} \div \frac{3}{4}}{1\frac{1}{8} \text{ of } \frac{5}{8} \div 10\frac{1}{8}} \times \frac{2}{8} \text{ of } \frac{1\frac{1}{4} \text{ of } 4\frac{1}{9}}{13\frac{7}{8} \text{ of } 5\frac{1}{8}}.$$

$$\frac{5\frac{1}{4} \div \frac{3}{4}}{1\frac{1}{8} \text{ of } \frac{5}{8} \div 10\frac{1}{8}} \times \frac{2}{8} \text{ of } \frac{1\frac{1}{4} \text{ of } 4\frac{1}{8}}{13\frac{7}{8} \text{ of } 5\frac{1}{8}}$$

$$= \frac{45}{8} \times \frac{3}{2} \times \frac{3}{6} \times \frac{9}{5} \times \frac{31}{3} \times \frac{2}{5} \times \frac{3}{2} \times \frac{37}{9} \times \frac{8}{111} \times \frac{3}{16} = \frac{279}{64} = 4\frac{23}{64}.$$

40. Simplify
$$1\frac{1}{2}$$
 of $2\frac{4}{5} + 6\frac{7}{5} \div 2\frac{3}{4} + \left(5\frac{1}{4} + \frac{0.24 + 0.53}{2.2 - 0.64}\right)$.

$$1\frac{1}{2} \text{ of } 2\frac{4}{5} = \frac{3}{2} \times \frac{14}{5} = \frac{21}{5} = 4\frac{1}{5}; \qquad 6\frac{7}{5} \div 2\frac{3}{4} = \frac{5}{3} \times \frac{4}{11} = \frac{5}{2} = 2\frac{1}{2};$$

$$\frac{0.24 + 0.53}{2.2 - 0.64} = \frac{24}{2\frac{1}{5} - \frac{13}{5}} = \frac{6}{2\frac{1}{5} + \frac{15}{15}} = \frac{54 + 120}{495 - 145} = \frac{174}{350} = \frac{87}{175}.$$

$$1\frac{1}{2} \text{ of } 2\frac{4}{5} + 6\frac{7}{5} \div 2\frac{3}{4} + \left(5\frac{1}{2} + \frac{0.24 + 0.53}{2.2 - 0.64}\right) = 4\frac{1}{5} + 2\frac{1}{4} + 5\frac{1}{2} + \frac{57}{175}$$

$$= 11\frac{70 + 175 + 175 + 174}{350} = 12\frac{344}{350} = 12\frac{344}{350} = 12\frac{345}{350} = 12\frac{345}{350}. \text{ Ans.}$$

41. Simplify 0.9 of § of 4 of 15§.

0.9 of
$$\frac{5}{8}$$
 of $\frac{4}{7}$ of $15\frac{3}{4} = \frac{9}{10} \times \frac{5}{8} \times \frac{4}{7} \times \frac{63}{4} = \frac{81}{16} = 5\frac{1}{16}$. Ans.

42. What part of $\frac{1}{3}$ is $\frac{1}{2}$?

$$\frac{1}{2} \div \frac{2}{3} = \frac{1}{2} \times \frac{3}{2} = \frac{3}{4}$$
. Ans.

43. What part of 0.390625 is 0.05?

$$\frac{0.05}{0.390625} = \frac{3}{100} \times \frac{10000}{1000000} = \frac{16}{125}. \quad Ans.$$

44. What fraction of 0.2045 is 0.09?

raction of 0.2045 is 0.09?
$$\frac{0.09}{0.2045} = \frac{9}{3000} = \frac{9}{3000} \times \frac{9999}{2925} = \frac{4}{9}. Ans.$$

45. Reduce to decimals: 49; 14; 13.

0.731343283582089552238805970149253

67)49.0		0.94091508
469		0.84931506
210		73)62.0
201_		584
90		360
67		292
$\overline{230}$		680
201		657
290	-	230
268		219
22	_	110
20		73
	- 90	370
	34	365
-		
	560 536	500 438
		
	240 201	62
		$\therefore \$ = 0.84931506.$
	390	7,
	335	
	550 540	
	536 536	
	140 400	
	<u>134</u> <u>335</u>	
•	600 650	
	<u>536</u> <u>603</u>	_
	640 47	
	<u>603</u> <u>46</u>	
A 978		100
0.378	<u>335 </u>	<u>67</u>
37)14.0	350	330
111	<u>335</u>	268_
290	150	620
259	<u>134</u>	603
310	160	170
<u>296</u>	<u>134</u>	<u>134</u>
14	260	360
$\therefore \frac{14}{37} = 0.378.$	<u>201</u>	335_
$\frac{1}{37} = 0.310.$	590	250
	<u>536</u>	201
	540	49
	• 49 - 0 721242222	58908Q559938805070140959

46. The G. C. M. of three numbers is 15, and their L. C. M. is 450. What are the numbers?

The G. C. M. = $15 = 3 \times 5$.

The L. C. M. =
$$450 = 2 \times 3^2 \times 5^2 = (3 \times 5) \times 2 \times 3 \times 5$$
.

- \therefore the numbers are $15 \times 2 = 30$, $15 \times 3 = 45$, $15 \times 5 = 75$.
- 47. A merchant, after selling 5½ yards and 3½ yards from a remnant of calico, found that he had 7½ yards left. What was the entire length of the remnant?

$$5\frac{1}{6} + 3\frac{1}{2} + 7\frac{3}{6} = 15\frac{5+1}{80} = 15\frac{3}{80} = 16\frac{3}{80} = 16\frac{4}{10}$$
.
 $16\frac{4}{15}$ yards. Ans.

48. If 3½ yards of cloth are required for a coat, how many coats can be made from 56½ yards of cloth?

$$56\frac{1}{4} \div 3\frac{3}{4} = \frac{225}{4} \times \frac{4}{15} = 15$$
. Ans.

49. A grocer bought a hogshead of sugar weighing 744 pounds at 47 cents per pound, and sold it at 51 cents per pound. How much did he gain?

$$5\frac{1}{4} - 4\frac{7}{8} = \frac{10 - 7}{8} = \frac{3}{8}$$
. $744 \times \frac{3}{8}$ cents = 279 cents = \$2.79. Ans.

50. A man, after selling $\frac{2}{3}$ of his field, sold $\frac{3}{4}$ of the remainder and then had $13\frac{1}{4}$ acres left. How many acres did he own at first?

$$1 - \frac{2}{9} = \frac{7}{9}; \quad \frac{2}{7} \text{ of } \frac{7}{9} = \frac{2}{9}; \quad \frac{2}{9} + \frac{2}{9} = \frac{4}{9}; \quad 1 - \frac{4}{9} = \frac{5}{9}.$$

$$13\frac{1}{3} \text{ acres} \div \frac{5}{9} = \frac{9}{5} \times \frac{\cancel{40}}{\cancel{3}} \text{ acres} = 24 \text{ acres. } Ans.$$

51. A railroad train passed over $\frac{7}{12}$ of its route in $3\frac{1}{2}$ hours. In how many hours would it pass over the entire route? In how many hours over $\frac{2}{3}$ of the route? $\frac{7}{3}$?

$$3\frac{1}{4} + \frac{7}{12} = \frac{7}{2} \times \frac{12}{7} = 6. \text{ Ans.} \qquad \frac{7}{8} \text{ of } \overset{3}{\%} = \frac{21}{4} = 5\frac{1}{4}. \text{ Ans.}$$

$$\frac{2}{5} \text{ of } 6 = \frac{12}{5} = 2\frac{2}{5}. \text{ Ans.} \qquad \frac{9}{14} \text{ of } \overset{3}{\%} = \frac{27}{7} = 3\frac{2}{7}. \text{ Ans.}$$

33 The meter is some it by feet, very nearly. Express in name meters the value of 4 , feet.

$$\frac{1}{2\pi} - \frac{1}{2\pi} = \frac{12}{24} + \frac{12}{24} = \frac{1}{4} = \frac{1}{4}$$
. $\frac{1}{2}\pi = \frac{125m}{2}$. And

58. For a passio cover a lady bought 24 yeards of panel, at \$15 year panel the same and our of living flather at \$5 per yeard, 15 yeards of sunge at \$15 per yeard. If the meaning our \$5, what was the ours of the passio cover?

25 A maker built of yards of wall on Monday, 45 yards on Thescay 65 yards on Wellsewist, and 75 yards on Thursday. If he is your 41 St per yard, h. w much has be earned in the four days

$$40.90 = 8\frac{4}{5}$$

$$40.90 = 8\frac{4}{5}$$

$$20.33 \times 8\frac{4}{5} = \frac{27.97}{12.9} \times 8\frac{4}{5} = 8\frac{27.97}{12.0} = 818.35$$
And

56. A coal dealer sold 100 tons of coal. If he shipped by six cars $14\frac{1}{2}$, $14\frac{1}{10}$, $14\frac{3}{14}$, $14\frac{3}{16}$, $14\frac{7}{16}$, $14\frac{1}{70}$ tons respectively, how many tons must he load on the seventh car to complete his shipment?

$$14\frac{1}{2} + 14\frac{1}{10} + 14\frac{3}{14} + 14\frac{3}{15} + 14\frac{7}{16} + 14\frac{7}{70}$$

$$= 84^{280+56+1}20+128+245+8$$

$$= 84\frac{387}{560} = 85\frac{277}{560}. 100-85\frac{277}{360} = 14\frac{388}{368}. Ans.$$

57. The moon's diameter is $\frac{8}{11}$ that of the earth, and the sun's diameter is 110 times that of the earth. What fraction of the sun's diameter is the moon's diameter?

$$\frac{3}{11} + 110 = \frac{3}{11} \times \frac{1}{110} = \frac{3}{1210}$$
. Ans.

58. If a silver rupee in Calcutta is worth \$ \frac{1}{2}\frac{2}{5}\$, what is the value in dollars and cents of a fan costing 4\frac{7}{4} rupees?

$$4\frac{7}{8} \times 8\frac{12}{25} = \frac{39}{8} \times 8\frac{12}{25} = 8\frac{117}{50} = 82.34$$
. Ans.

59. If a man can do $\frac{2}{11}$ of a piece of work in 25 days, what fraction of the work can he do in 624 days?

25 days +
$$\frac{2}{11} = \frac{11}{2} \times 25$$
 days = $\frac{275}{2}$ days.
 $\frac{8}{11} = \frac{440}{7} \times \frac{2}{275} = \frac{16}{35}$. Ans.

60. I paid a tailor \$3\frac{1}{2}\$ a yard for 5\frac{1}{4}\$ yards of broadcloth. On measuring it, I found that there were only 4\frac{1}{4}\$ yards. How much money ought the tailor to return?

$$5\frac{1}{4} - 4\frac{7}{8} = 1\frac{2-7}{8} = \frac{10-7}{8} = \frac{3}{8}$$

 $\frac{3}{8}$ of $3\frac{1}{2} = \frac{3}{8} \times 3\frac{7}{2} = 3\frac{21}{16} = 31.31$. Ans.

61. From a tank full of water 3 of the water was drawn off. Then 35 gallons were added, and the tank was just half full. What is the capacity of the tank?

$$\frac{2}{3} - \frac{1}{2} = \frac{1}{6}$$

35 gallons $\div \frac{1}{6} = 6 \times 35$ gallons = 210 gallons. Ans.

62. What number exceeds the sum of its fourth, fifth, sixth, and seventh parts by 101?

$$\frac{1}{4} + \frac{1}{5} + \frac{1}{6} + \frac{1}{7} = \frac{105 + 84 + 70 + 60}{420} = \frac{319}{420}$$

$$1 - \frac{319}{420} = \frac{101}{420}$$

$$101 \div \frac{101}{420} = 191 \times \frac{420}{191} = 420. \text{ Ans.}$$

63. A trader bought wheat at 75 cents a bushel, and sold it at 71 cents a bushel. How many cents did he lose on every dollar he paid? He lost 75 cents - 71 cents = 4 cents on every 75 cents.

Therefore, he lost $\frac{4}{75}$.

$$\frac{4}{75} \text{ of } 199 \text{ cents} = \frac{1}{3} \text{ cents} = 5\frac{1}{3} \text{ cents. } Ans.$$

64. How many bushels of potatoes at \$ \frac{2}{3} per bushel will pay for 16 bushels of wheat at \$ \frac{1}{3} per bushel?

$$\begin{array}{c}
 4 \\
 \hline{18} \times \$ \frac{13}{29} = \$ \frac{52}{5} \\
 \hline
 8 \frac{52}{5} \div \$ \frac{2}{5} = \frac{52}{5} \times \frac{5}{2} = 26. \quad Ans.
\end{array}$$

65. From a piece of calico containing $35\frac{7}{8}$ yards, there have been sold at different times $12\frac{5}{4}$ yards, $2\frac{1}{4}$ yards, $2\frac{5}{16}$ yards, and $8\frac{5}{8}$ yards. How many yards remain?

$$12\frac{3}{4} + 2\frac{1}{2} + 2\frac{3}{16} + 8\frac{5}{8} = 24\frac{12+8+8+10}{16} = 24\frac{38}{16} = 26\frac{1}{16}.$$
$$35\frac{7}{8} - 26\frac{1}{16} = 9\frac{14-1}{16} = 9\frac{18}{16}. Ans.$$

66. If gun metal is composed of 90½ parts of copper to 9½ parts of tin by weight, how many ounces of tin are there in one pound (16 ounces) of gun metal? how many ounces of copper in one pound?

$$\frac{9\frac{1}{2}}{90\frac{1}{2} + 9\frac{1}{2}} = \frac{9\frac{1}{2}}{100} = \frac{19}{200}.$$

$$\frac{19}{299} \times 19 \text{ ounces} = \frac{38}{25} \text{ ounces} = 1\frac{13}{25} \text{ ounces, tin. } Ans.$$

$$25$$

$$16 \text{ ounces} - 1\frac{1}{25} \text{ ounces} = 14\frac{1}{25} \text{ ounces, copper. } Ans.$$

67. One man mows $\frac{1}{3}$ of a field, a second $\frac{3}{4}$ of it, and a third $\frac{5}{21}$ of it. What fraction of the field remains to be mowed?

$$\frac{1}{3} + \frac{2}{7} + \frac{5}{21} = \frac{7+6+5}{21} = \frac{18}{21} = \frac{6}{7}$$
$$1 - \frac{6}{7} = \frac{1}{7} \cdot Ans.$$

68. Bell metal by weight consists of 4 parts of copper to 1 part of tin. What is the cost of a bell weighing 12,400 pounds, if the copper costs 19 cents per pound, the tin 22½ cents per pound, and the cost of making is \$500?

$$\frac{4}{1+4} = \frac{4}{5}$$
, copper. $\frac{1}{1+4} = \frac{1}{5}$, tin. $\frac{4}{5} \times 12499$ pounds = 9920 pounds, copper. $\frac{1}{5} \times 12499$ pounds = 2480 pounds, tin.

69. If an ore loses $\frac{17}{10}$ of its weight in roasting, and $\frac{8}{10}$ of the remainder in smelting, how many tons of ore must be mined to obtain 466 tons of pure metal?

$$1 - \frac{17}{40} = \frac{23}{40}. \qquad \frac{8}{19} \times \frac{23}{40} = \frac{23}{95}. \qquad \frac{23}{40} - \frac{23}{95} = \frac{437 - 184}{760} = \frac{253}{760}.$$
$$466 + \frac{253}{760} = 466 \times \frac{760}{253} = \frac{354160}{253} = 1399\frac{213}{253}. \quad Ans.$$

70. The amount of starch in potatoes is $\frac{11}{10}$ of their weight, but the amount that can usually be extracted is only $\frac{2}{10}$. How many pounds of starch can be obtained from 100 pounds of potatoes, and how many pounds of starch will be left in the potatoes?

ounds of starch will be left in the potatoes?
$$\frac{2}{15} \times 100 = \frac{40}{3} = 13\frac{1}{3}. \quad Ans.$$

$$\frac{11}{50} \times 100 = 22.$$

$$22 - 13\frac{1}{3} = 8\frac{1}{3}. \quad Ans.$$

71. How many pairs of trousers, each pair requiring 2[§] yards, can be made from 33[‡] yards of cloth?

$$33\frac{1}{4} + 2\frac{3}{8} = \frac{133}{4} \times \frac{2}{8} = 14$$
. Ans.

72. If 3½ yards of cloth are required for a shirt, how many shirts can be made from 12 pieces of cloth, each piece measuring 47½ yards?

$$\frac{12 \times 47\frac{1}{4}}{3\frac{1}{4}} = \frac{3}{12} \times \frac{27}{189} \times \frac{2}{7} = 162. \text{ Ans.}$$

73. Green coffee when roasted loses $\frac{1}{6}$ of its weight. If a dealer buys green coffee at 22 $\frac{1}{4}$ cents a pound, and sells it roasted at 30 cents a pound, what will be his gain in selling 1000 pounds of roasted coffee, the cost of roasting the whole quantity being \$2.25?

$$1000 \times \$0.22\frac{1}{2} = \$225$$
. $\$225 + \$2.25 = \$227.25$, cost. $\frac{5}{6} \times 1000 \times \$9.39 = \$250$, selling price. $\$250 - \$227.25 = \$22.75$. Ans.

74. If an iron bar, when heated 1 degree, expands $\frac{1}{143460}$ of its length, what is the length at 212 degrees of a bar whose length at 32 degrees is 10 \S feet?

$$212 - 32 = 180. 180 \times \frac{1}{143460} \times 108 = 189 \times \frac{1}{143469} \times \frac{65}{6} = \frac{65}{4782}.$$

$$108 + 4982 = 10\frac{3985 + 65}{4782} = 10\frac{4959}{782} = 10\frac{75}{787}. 10\frac{75}{97} \text{ feet. } Ans.$$

75. If a horse eats $\frac{7}{16}$ of a ton of hay in 30 days, how long will $4\frac{9}{10}$ tons of hay last 5 horses?

1 horse in 1 day eats
$$\frac{1}{30} \times \frac{7}{16}$$
 tons $= \frac{7}{480}$ tons.
5 horses in 1 day eat $3 \times \frac{7}{480}$ tons $= \frac{7}{96}$ tons.

$$4\frac{9}{10} \div \frac{7}{96} = \frac{\frac{49}{49}}{\frac{49}{5}} \times \frac{\frac{48}{96}}{\frac{7}{6}} = \frac{336}{5} = 67\frac{1}{5}.$$
 67\frac{1}{3} days. Ans.

76. If 4 is added to both terms of the fraction 11, by how much is the value of the fraction increased?

$$\frac{11+4}{16+4} = \frac{15}{20} = \frac{3}{4}. \qquad \frac{3}{4} - \frac{11}{16} = \frac{12-11}{16} = \frac{1}{16}. \quad Ans.$$

77. If 4 is subtracted from both terms of the fraction $\frac{1}{16}$, by how much is the value of the fraction decreased?

$$\frac{11-4}{16-4}=\frac{7}{12}.\qquad \qquad \frac{11}{16}-\frac{7}{12}=\frac{33-28}{48}=\frac{5}{48}. \ Ans.$$

78. Find the least number of apples that arranged in groups of 8, 9, 10, or 12 will have just 6 over in each case.

The L. C. M. of 8, 9, 10, and 12 is 360.

79. The diameter of a bicycle wheel is 2\frac{1}{2} feet, and the circumference is 3\frac{1}{2} times the diameter. How many times does the wheel turn in going 1 mile (5280 feet)?

$$\frac{5280}{3\frac{1}{7}\times2\frac{1}{3}} = 5289 \times \frac{7}{22} \times \frac{3}{7} = 720. Ans.$$

80. What is the least number of yards of carpet in a roll that can be cut into lengths of exactly 13\frac{1}{2} yards, 8 yards, or 11\frac{1}{2} yards?

13
$$\frac{1}{3}$$
, 8, 11 $\frac{1}{7} = \frac{40}{3}$, $\frac{8}{1}$, $\frac{80}{7}$.

The L. C. M. of 40, 8, 80 = 80.

The G. C. M. of 3, 1, 7 = 1.

... the L. C. M. of the fractions = 80.
80 yards. Ans.

81. What is the length of the longest chain that will exactly measure the sides of a field whose lengths are respectively 135½ yards, 118¾ yards, 152 yards, and 202¾ yards?

82. Find the least multiplier of $\frac{7}{4}$, $\frac{14}{2}$, and $\frac{24}{4}$ that will make each product an integral number.

The least multiplier that will make 3 an integer is 3.

The least multiplier that will make 14 an integer is 17.

The least multiplier that will make 25 an integer is 45.

The L. C. M. of 9, 27, 45 = 135.

The G. C. M. of 7, 14, 28 = 7.

... the L. C. M. of the multipliers = $\frac{135}{5}$.

$$\frac{135}{9} = 193$$
. Ans.

83. Find the least integral number that is exactly divisible by 51, 31, and 7.

$$5\frac{1}{4}$$
, $3\frac{1}{2}$, $7 = \frac{21}{4}$, $\frac{7}{2}$, $\frac{7}{1}$.

The L. C. M. of 21, 7, 7 = 21.

The G. C. M. of 4, 2, 1 = 1

 \therefore the L. C. M. of the fractions = 21.

Since 21 is integral, 21 is the number required.

84. Four bells commence tolling together, and toll at intervals of 1, $1\frac{1}{1}$, $1\frac{1}{12}$, and $1\frac{3}{10}$ seconds, respectively. In how many seconds will all four toll again at the same instant?

1,
$$1\frac{1}{3}$$
, $1\frac{1}{12}$, $1\frac{3}{10} = \frac{1}{1}$, $\frac{9}{8}$, $\frac{13}{12}$, $\frac{13}{10}$.

The L. C. M. of 1, 9, 13, 13 = 117.

The G. C. M. of 1, 8, 12, 10 = 1.

 \therefore the L. C. M. of the fractions = 117.

117 seconds. Ans.

85. What number multiplied by 7_1 of 9_2 will give 102_2 for the product?

$$\frac{102\frac{3}{11}}{\frac{7}{11}} = \frac{\frac{77}{308}}{\frac{9}{11}} = \frac{\frac{2}{308}}{\frac{3}{3}} \times \frac{11}{7} \times \frac{\frac{14}{9}}{\frac{9}{9}} \times \frac{\frac{3}{88}}{\frac{9}{8}} = \frac{77}{9} = 8\frac{5}{9}. \quad Ans.$$

86. How many miles an hour must a man walk to go 28 miles in $7\frac{7}{15}$ hours?

$$28 \div 7\frac{7}{15} = 28 \times \frac{15}{112} = \frac{15}{4} = 3\frac{3}{4}$$
. Ans.

87. If the rent of $5\frac{5}{12}$ acres of land is \$21\frac{2}{3}\$, what will be the rent of $19\frac{9}{16}$ acres at the same rate?

$$19\frac{9}{16} \times \$\frac{21\frac{3}{4}}{5\frac{5}{12}} = \frac{313}{\cancel{16}} \times \$\frac{\cancel{65}}{\cancel{3}} \times \frac{\cancel{12}}{\cancel{65}} = \$\frac{313}{4} = \$78\frac{1}{4}.$$
 Ans.

88. If the English acre is $\frac{31\frac{1}{49}}{49}$ of an Irish acre, how many English acres are there in 218 $\frac{1}{49}$ Irish acres?

$$218\frac{3}{4} \div \frac{31\frac{1}{4}}{49} = \frac{\cancel{875}}{\cancel{4}} \times \frac{\cancel{4}}{\cancel{125}} \times \cancel{49} = \cancel{343}. \quad Ans.$$

89. Resolve the denominator of $\frac{25}{4}$ into its prime factors; from the result state the number of figures the equivalent decimal will have, and the number that will precede the repetend.

$$48 = 2^4 \times 3$$
.

Since the highest power of 2 or 5 in the denominator is the fourth, the repetend will be preceded by 4 figures. Since the only factor of the denominator besides 2 and 5 is 3, the repetend will consist of 1 figure. Therefore, the decimal will contain 5 figures.

90. Find the greatest common measure of 9083, 9207, 8897.

Exercise 70. Page 149.

1. Reduce 3 pk. 5 qt. 1 pt. to pints.

pk.	g t.	pt.
3	5	1
8		
2 9		
2		
 59	59 pt.	Ans.

2. Reduce 4234 pt. (dry measure) to higher units.

3. Reduce 24 gal. 2 qt. 1 pt. 2 gl. to gills.

790 gi. Ans.

4. Reduce 3047 gills to higher units.

5. Reduce 1715½ bu. to pints.

6. Reduce 508 dry quarts to higher units.

7. Reduce 1016 liquid pints to higher units.

127 gal. Ans.

8. Reduce 44 gal. 3 qt. 1 pt. to pints.

gal.	qt.	pt.
44	8	1
4		
179		
2		
359	359	pt An

9. Reduce 44 bu. 3 pk. 7 qt. 1 pt. to pints.

bu.	pk.	qt.	pt.
44	3	7	1
4			
179			
8			
1439			
2			
2879		2879 pt.	Ans.

10. Reduce 272 liquid quarts o dry quarts.

to dry quarts.
$$272 \times \frac{57\frac{3}{4}}{67\frac{1}{8}} = \frac{17}{272} \times \frac{\frac{11}{231}}{4} \times \frac{5}{336}$$

$$= \frac{935}{4} = 233\frac{3}{4}.$$

$$233\frac{3}{4} \text{ qt. } Ans.$$

11. Reduce 429 dry quarts to liquid quarts.

$$429 \times \frac{67\frac{1}{5}}{57\frac{3}{4}} = 429 \times \frac{39}{5} \times \frac{336}{5} \times \frac{4}{231} = \frac{2496}{5} = 499\frac{1}{5}.$$

$$499\frac{1}{5} \text{ qt. } Ans.$$

Exercise 71. Page 150.

1. Add 5 bu. 3 pk. 6 qt. 1 pt.; 6 bu. 2 pk. 7 qt.; 7 bu. 1 pk. 1 qt. 1 pt.; 1 pk. 7 qt.; 2 bu. 3 pk. 1 pt.

bu.	pk.	qt.	pt.
5	3	6	1
6	2	7	0
7	1	1	1
0	1	7	0
2	3	0	1
23	0	6	1
	23 bu.	6 qt. 1	pt. Ans.

3. Add 4 gal. 3 qt. 1 pt.; 3 gal. 2 qt. 1½ pt.; 12 gal. 3 qt.; 14 gal. 1½ pt.; 5 gal. 2 qt. 1 pt.

2. Add 50 gal. 3 qt. 1 pt. 3 gi.; 12 gal. 1 qt. 1 pt. 1 gi.; 5 gal. 2 qt. 1 pt. 2 gi.; 75 gal. 3 qt. 1 pt. 3 gi.; 80 gal. 3 qt. 1 gi.; 17 gal. 1 qt. 1 pt. 3 gi.

gal.	qt.	pt.	gi.
50	8	1	3
12	1	1	1
5	2	1	2
75	3	1	3
80	3	0	1
17	1	_ 1	3
243	1	0	1
	243 gal.	1 qt.	1 gi. Ans.

4. Subtract 5 bu. 1 pk. 6 qt. 1 pt. from 5 bu. 3 pk. 3 qt.

1 pk. 4 qt. 1 pt. Ans.

5 Substant 22 8 11 1 1 arman fra the

78 29 11 m

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1 bar o par 2 quarter 220 220 50 bar 2 xm 7 at 1 1 2 A.

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Exercise 72 Page 151.

1 Multip v 19 g... 1, q. 1 p. 4 Multip v 26 g... 2 q. 1 V 107 70

ga.	qt.	pt	
110	:,		
		70	
1.;		t)	
	lata gal	1 63	Au

1 1 1

5 g. by 12

220 gail 2 q 1 T: Ak

5 Multiply 12 bu 3 pa - - ' 147. FV 2 .

bil	t ill	Ç,	j.
12	:.	7	•
			<u> </u>
	<u>:</u>	:.	•

324 b... 2 jih 3 or 1 ja 🔏🖦

6 Divine 34 gal 8 of 1 z. t/7

7. Divide 147 gal. 2 qt. 1 pt. 2 gi. by 17.

8. Divide 54 bu. 3 pk. 2 qt. 1 pt. by 11.

9. Divide 34 bu. 3 pk. 5 qt. 1 pt. by 15.

2 bu. 1 pk. 2 qt. 1 pt. Ans.

Exercise 73. Page 152.

1. Reduce 27,587 gr. to higher troy units.

4 lb. 9 oz. 9 dwt. 11 gr. Ans.

2. Reduce 34,652 pounds avoirdupois to long tons, etc.

3. Reduce 136,851 ounces avoirdupois to higher units.

4. Reduce 864,205 gr. to higher troy units.

5. Reduce 864,205 gr. to higher avoirdupois units.

864,205 gr. =
$$\frac{864205}{7000}$$
 lb.
= $123\frac{641}{1400}$ lb.
= 123 lb. $7\frac{57}{175}$ oz. Ans.

6. Reduce 5 lb. 7 oz: 6 dwt. 12 gr. to grains.

6613 35 lb. Aus.

224

ADVANCED ARITHMETIC.

7. Reduce 745 lb. avoirdupois to troy measures.

745 lb. avoir. = 745×7000 gr. = 5,215,000 gr.

	5215000				
	217291				
12	10864	oz	•		11 dwt.
,					4 oz.

905 lb. 4 oz. 11 dwt. 16 gr. Ans.

8. Reduce 745 lb. troy to avoirdupois measures.

745 lb. troy = $745 \times \frac{144}{5769} \times \frac{5769}{7999}$ lb. avoir.

= 579}} 1b. = 579 | b. 14}} oz. 1/ns.

9. Reduce 1,440,445 oz. avoirdupois to higher units.

16	1440445	OZ.			
100	90027	lb	•		13 oz.
20	900	cwt.	•	•	27 lb.
•	45				

45 t. 27 lb. 13 oz. Ans.

10. Reduce 5,640,773 oz. avoirdupois to higher units.

16	5640773	oz.			
100	352548	lb			5 oz.
20	3525	cwt.	•	•	48 lb.
,	176	t	•		5 cwt.

176 t. 5 cwt. 48 lb. 5 oz. Ans.

11. Add 48 t. 13 cwt. 75 lb. 6 oz.; 25 t. 12 cwt. 27 lb. 8 oz.; 51 t. 10 cwt. 44 lb.; 80 t. 5 cwt. 6 oz.; 19 cwt. 27 lb.; 25 lb. 8 oz.; 5 t. 5 cwt. 5 lb.

t.	cwt.	lb.	0Z.
48	13	7 5	6
25	12	27	8
51	10	44	0
80	5	0	6
	19	27	0
		25	8
5	5	` 5	0
212	ť	4	12
212	t. 6 cwt. 4	lb. 12 oz	. Ans

12. Add 13 lb. 4 oz. 8 dwt. 6 gr.; 25 lb. 8 oz. 13 dwt. 20 gr.; 8 lb. 11 oz. 14 gr.; 20 lb. 16 dwt. 8 gr.; 15 lb. 9 oz. 12 dwt.; 4 oz. 3 dwt.

lb.	oz.	dwt.	gr.
13	4	8	6
25	8	13	20
8	11	0	14
20	0	16	8
15	9	12	0
	4	3	0
84	2	14	U
	84 lb. 2	oz. 14 dv	vt. Ans.

13. Subtract 23 lb. 8 oz. 19 dwt. 10 gr. from 58 lb. 6 oz. 17 dwt. 21 gr.

lb.	oz.	dwt.	gr.
58	6	17	21
23	8	19	10
34	9	18	11
34 lh	9.07	18 dwt 11 o	T Ans

14. Subtract 17 t. 7 cwt. 17 lb. 6 oz. from 25 t. 13 cwt. 15 lb. 12 oz.

t.	cwt.	lb.	OZ.
25	13	15	12
17	7	17	6
8	5	98	6
	8 t. 5 cwt.	98 lb. 6 o	z. Ans.

15. Multiply 3 lb. 4 oz. 8 dwt. 10 gr. by 10.

lb. 3	o z. 4	dwt. 8	gr. 10
			10
33	8	4	4

33 lb. 8 oz. 4 dwt. 4 gr. Ans.

16. Multiply 5 t. 10 cwt. 67 lb. 4 oz. by 15.

17. Divide 17 t. 19 cwt. 79 lb. 8 oz. by 8.

18. Divide 60 lb. 6 oz. 10 dwt. 20 gr. by 7.

19. How many bags each holding 2 bu. 1 pk. 3 qt. are required to hold 234 bu. 1 pk. 4 qt. of corn?

 $7500 \div 75 = 100$. Ans.

20. What is the value at 4½ cents a pound of a calf weighing 184 lb. 6 oz.?

184 lb. 6 oz. = 184_{16}^6 lb. = 184_{8}^{8} lb. $184_{8}^{3} \times \$0.045 = 0.045 \times \184_{8}^{8} .

\$8.30. Ans.

21. How many tablespoons each weighing 2 oz. 17 dwt. 12 gr. can be made from 155 oz. 5 dwt. of silver?

54. Ans.

Exercise 74. Page 155.

1. Reduce 3 yd. 2 ft. to inches.

yd.	ft.	
3	2	
3		
11		
12		
132	132 in.	Ans.

2. Reduce 4 mi. 124 rd. 3 yd. 2 ft. to feet.

mi.	rd.	yd.	ft.
4	124	3	2
320			
$\overline{1404}$			
$5\frac{1}{4}$			
7725			
3			
23177		23,177	ft. Ans.

3. Reduce 27 rd. 4 yd. 9 in. to inches.

rd. yd. ft. in.
$$27$$
 4 0 9 $\frac{5\frac{1}{2}}{152\frac{1}{2}}$ $\frac{3}{457\frac{1}{2}}$ $\frac{12}{5499}$ 5499 in. Ans.

4. Reduce 290 leagues to feet.

leagues.	knots.	ft.
290	0	0
3		
870		
6086		
5294820	5,294,820	ft. Ans

5. Reduce 82,976,432 in. to higher units.

1309 mi. 192 rd. 4 yd. 2 ft. 8 in. Ans.

6. Reduce 7 mi. 3 yd. 1 ft. 6 in. to inches.

mi. rd. yd. ft. in.
7 0 3 1 6
$$\frac{320}{2240}$$

$$\frac{5\frac{1}{2}}{12323}$$

$$\frac{3}{36970}$$

$$\frac{12}{443646}$$
443,646 in. Ans.

7. Reduce 22 mi. 222 rd. 4 ft. 8 in. to inches.

8. Reduce 712 mi. to feet.

mi.
712
5280
3759360
3,759,360 ft. *Ans*.

9. Reduce 540,451 ft. to higher units.

102 mi. 114 rd. 3 yd. 1 ft. Ans.

10. Reduce 271,256 in. to higher units.

12 | 271256 in. 22604 ft. 8 in. 3 51 7534 yd. 2 ft. 2 11 15068 half yd. $[=4\frac{1}{2}]$ yd. 320 1369 rd. 9 half yd. 4 mi. . . . 89 rd. rd. yd. mi. ft. in. 4 89 **4**¥ 2 8 в 1 4 89 5 1 4 mi. 89 rd. 5 yd. 1 ft. 2 in. Ans.

11. Reduce 723,964 ft. to higher units.

 $3 \mid 723964 \text{ ft.}$ $5\frac{1}{2} \mid 241321 \text{ yd.} \dots 1 \text{ ft.}$ 2 $11 \mid 482642 \text{ half yd.} \mid = 3 \text{ yd.}$ $320 \mid 43876 \text{ rd.} \dots 6 \text{ half yd.}$ $137 \text{ mi.} \dots 36 \text{ rd.}$ 137 mi. 36 rd. 3 yd. 1 ft. Ans.

12. Reduce 233,205 in. to higher units.

3 mi. 217 rd. 4 yd. 1 ft. 3 in. Ans.

13. How many feet high is a horse 16 hands high?

1 hand = 4 in. =
$$\frac{1}{3}$$
 ft.
16 × $\frac{1}{3}$ ft. = $\frac{16}{3}$ ft. = $5\frac{1}{3}$ ft. Ans.

14. Add 6 mi. 120 rd. 3 yd. 2 ft. 2 in.; 18 mi. 15 rd. 1 yd. 1 ft. 6 in.; 3 mi. 215 rd. 2 yd. 2 ft. 3 in.; 7 mi. 95 rd. 1 yd. 1 ft. 8 in.

mi.	rd.	yd.	ft.	in.
6	120	3	2	2
18	15	1	1	6
3	215	2	2	3
7	95	1	1	8
35	126	31/	1	7
		,-	1	6
35	126	4	0	

35 mi. 126 rd. 4 yd. 1 in. Ans.

15. Subtract 3 mi. 217 rd. 4 yd. 1 ft. 3 in. from 4 mi. 100 rd. 3 yd. 2 in.

mi.	rd.	yd.	ft.	in.	
4	100	3	0	2	
3	217	4	1	3	
	202	31/	1	11	
		_	1	8	
	202	4	U	5	
	202 r	d. 4 vd	. 5 iı	n. Ans	:

16. Multiply 5 mi. 126 rd. 9 ft. 6 in. by 7125.

\mathbf{mi} .	rd.	ft.	in.
5	126	8	6
			7125
38443	92	4	6
38.443 n	ni. 92 rd	. 4 ft. 6	in. Ans.

How much does he build per day?

17. Divide 54 mi. 124 rd. 1 yd. 2 ft. 6 in. by 33.

1 mi. 207 rd. 2 yd. 8 in. Ans.

18. If a man builds 1 rd. 1 yd. 1 ft. 6 in. of stone wall in one day, how much will he build in 26 days?

19. A man builds 25 rd. 2 yd. 1 ft. 6 in. of wall in 20 days.

1 rd. 1 yd. 1 ft. 6 in. Ans.

Exercise 75. Page 156.

1. Reduce 92,638 sq. yd. to square inches.

120,058,848 sq. in. Ans.

2. Reduce 1,223,527 sq. in. to higher units.

31 sq. rd. 6 sq. yd. 2 sq. ft. 139 sq. in. Ans

3. Reduce 721 sq. mi. to square rods.

73,830,400 sq. rd. *Ans*.

4. Reduce 34,729 sq. yd. to higher units.

7 A. 28 sq. rd. 2 sq. yd. Ans.

sq. in.

23

5. Reduce to square inches 3 A. 107 sq. rd. 27 sq. yd. 7 sq. ft. 23 sq. in.

 $\frac{144}{23048771}$

23,048,771 eq. in. Ans.

6. Reduce 99,894,712 sq. in. to higher units.

15 A. 148 sq. rd. 2 sq. yd. 2 sq. ft. 40 sq. in. Ans.

7. Reduce 15,376 sq. yd. to higher units.

160 508 sq. rd. . . . 36 quarter sq. yd. = 9 sq. yd. 3 A. 28 sq. rd.

3 A. 28 sq. rd. 9 sq. yd. Ans.

8. Reduce 562,934 sq. in. to higher units.

121 1736 quarter sq. yd.

14 sq. rd. . . . 42 quarter sq. yd. = $10\frac{1}{2}$ sq. yd.

14 sq. rd. 10 sq. yd. 7 sq. ft. 110 sq. in. Aus.

9. Add 74 A. 21 sq. rd. 5 sq. yd. 4 sq. ft. 100 sq. in.; 123 A. 23 sq. rd. 13 sq. yd. 5 sq. ft. 83 sq. in.; 112 A. 106 sq. rd. 17 sq. yd. 8 sq. ft. 7 sq. in.; 541 A. 50 sq. rd. 23 sq. yd. 24 sq. in.

sq. mi.	A.	sq. rd.	sq. yd.	sq. ft.	sq. in.
	74	21	5	4	100
	123	23	13	5	83
	112	106	17	8	7
	541	50	23	0	24
1	·211	41	291/	0	70
			~	8	108
1	211	41	29	7	34

1 sq. mi. 211 A. 41 sq. rd. 29 sq. yd. 7 sq. ft. 34 sq. in. Ans.

10. From 20 A. take 13 A. 150 sq. rd. 98 sq. ft. 10 sq. in.

A.	sq. rd.	sq. ft.	sq. in
20	0	0	0
13	150	98	10
6	9	173¥	134
		, -	36
6	9	174	26

6 A. 9 sq. rd. 174 sq. ft. 26 sq. in. Ans.

11. Multiply 27 A. 76 sq. rd. 22 sq. yd. 5 sq. ft. by 90.

3 sq. mi. 553 A. 27 sq. rd. 3 sq. yd. 2 sq. ft. 36 sq. in. Ans.

12. Divide 74,128 sq. mi. 517 A. 80 sq. rd. by 10,000.

7 sq. mi. 264 A. 39 sq. rd. Ans.

Exercise 76. Page 157.

- 1. Reduce 10 ch. to inches. 1 ch. = 100×7.92 in. = 792 in. 10 ch. = 10×792 in. = 7920 in. Ans.
 - 2. Reduce 3168 in. to chains.

3. How many acres are there in a township?

4. Reduce 6400 sq. ch. to acres; to square miles.

640 A.; 1 sq. mi. Ans.

5. Reduce 82,426 sq. ch. to higher units.

12 sq. mi. 562 A. 6 sq. ch. Ans.

6. Add 4 sq. mi. 412 A. 6 sq. ch. 8 sq. rd.; 7 sq. mi. 88 A. 2 sq. ch. 11 sq. rd.; 3 sq. mi. 367 A. 7 sq. ch. 2 sq. rd.; 11 sq. mi. 344 A. 9 sq. ch. 15 sq. rd.

sq. mi.	A.	sq. ch.	sq. rd.
4	412	6	8
7	88	2	11
3	367	7	2
11	344	8	15
26	573	6	4

26 sq. mi. 573 A. 6 sq. ch. 4 sq. rd.

Ans.

7. Subtract 1 mi. 75 ch. 85 l. from 4 mi. 44 ch. 38 l.

8. What is the area of a field if it can be divided into 12 lots each containing 2 sq. ch. 7 sq. rd.?

2 A. 9 sq. ch. 4 sq. rd. Ans.

9. Multiply 3 sq. mi. 172 A. 5 sq. ch. 7 sq. rd. by 11.

35 sq. mi. 617 A. 9 sq. ch. 13 sq. rd. Ans.

10. Divide 6 sq. mi. 422 A. 2 sq. ch. 13 sq. rd. by 5.

1 sq. mi. 212 A. 4 sq. ch. 9 sq. rd.

Ans.

11. A field is divided into 47 gardens each containing 1 sq. ch. 9 sq. rd. What is the area of the field?

7 A. 3 sq. ch. 7 sq. rd. Ans.

12. A field containing 5 A. 4 sq. ch. 11 sq. rd. is divided into 25 equal lots. What is the area of each lot?

2 sq. ch. 3 sq. rd. Ans.

13. Find the rent of 8 sq. ch. 10 sq. rd. at \$2 an acre.

8 sq. ch. 10 sq. rd. = $\frac{188}{180}$ A.

$$\frac{138}{169} \times \$2 = \$\frac{69}{40} = \$1.73. \ Ans.$$
89
40

14. If a field contains 3 A. 6 sq. ch. 12 sq. rd., what is it worth at 14 cents a square foot?

Exercise 77. Page 158.

1. Reduce 25 cu. yd. 5 cu. ft. 143 cu. in. to cubic inches.

1,175,183 cu. in. Ans.

2. Reduce 921,730 cu. in. to higher units.

19 cu. yd. 20 cu. ft. 706 cu. in. Ans.

3. Wood cut in lengths of 4 ft. is piled 3½ ft. high. How long must the pile be to contain 2 cords?

$$\frac{2 \times 128}{4 \times 3\frac{1}{4}} = 2 \times 128 \times \frac{1}{4} \times \frac{2}{7}$$
$$= \frac{128}{7} = 18\frac{3}{4}.$$
$$18\frac{3}{4} \text{ ft. } Ans.$$

4. How many cords in a pile of 4-ft. wood 43 ft. long and 6 ft. high?

$$\frac{\cancel{4} \times \cancel{43} \times \cancel{6}}{\cancel{128}} = \frac{129}{16} = 8\frac{1}{16}.$$

$$\cancel{32}$$

$$\cancel{16}$$

$$\cancel{81}_{16} \text{ cd. } Ans.$$

5. Add 130 cu. yd. 5 cu. ft. 820 cu. in.; 56 cu. yd. 20 cu. ft. 304 cu. in.; 37 cu. yd. 4 cu. ft. 86 cu. in.; 8 cu. yd. 10 cu. ft. 129 cu. in.; 12 cu. yd. 19 cu. ft. 175 cu. in.

cu. yd.	cu. ft.	cu. in.
130	5	820
56	20	304
37	4	86
8	10	129
12	19	175
245	4	1514

245 cu. yd. 4 cu. ft. 1514 cu. in.

Ans.

6. Subtract 32 ca. yd. 13 ca. ' 7. Muitiply 12 cd. 4 cd. ft. by st. 1600 ca. in. from 39 ca. yd. 17 ca. ft. 1400 ca. in.

cu. yd.	cal fil	cu in.
39	17	1400
32	13	1600
7	3	1528

14

cd.	cd. ft.
12	4
	14
175	0
	175 cd. Ans.

7 cu. yd. 3 cu. ft. 1528 cu. in. Ans.

8. Divide 5 cu. yd. 10 cu. ft. 371 cu. in. by 6.

Exercise 78. Page 160.

1. Reduce £ 583 6 s. 8 d. to pence.

ciice.			
£	8.	d.	
583	6	8	
20			
11666			
12			
140000	140,	000 d. Ans	•

2. Reduce £79 18 s. 114 d. to farthings.

3. Reduce 28,572 d. to higher units.

4. Reduce 27,281 crowns to guineas.

21 | 136405 s.

6495 guineas . . . 10 s.

6495 guineas 10 shillings. Ans.

5. Reduce 1,716,114 guineas to pounds.

$$\begin{array}{r}
 1716114 \\
 \hline
 21 \\
 \hline
 1716114 \\
 3432228 \\
 \hline
 36038394
 \end{array}$$

20|36038394 s.

£ 1801919 . . . 14 s.

£1,801,919 14 s. Ans.

6. Reduce 706,126 d. to higher units.

7. Add £35 2s. 6\(\frac{1}{4}\)d.; £18
5s. 4d.; £27 3s. 10d.; £12
5d.; £6 7s. 8d.; £14 19s.
11d.; £29 16s. 2d.

£	s.	d.
35	2	63
18	5	4
27	3	10
12	0	5
6	7	8
14	19	11
29	16	2
143	15	104
	£ 143 15 g	108 d. A

£ 143 15 s. 104 d. Ans.

8. Subtract £92 15s. 1\fmathred{1}d. from £120 13s. 4d.

9. Multiply £312s. 61 d. by 8.

10. Divide £394 2s. 10\frac{1}{2} d. by £5 2s. 4\frac{1}{2} d.

77. Ans.

11. Divide £108 15s. 4d. by 13.

£87s. 4d. Ans.

12. Find the value in United States money of the money in a box containing 35 sovereigns, 27 half-sovereigns, 13 crowns, 41 half-crowns, and 85 shillings.

35 sovereigns
 =
$$35 \times 20 \, s. = 700 \, s.$$

 27 half-sovereigns
 = $27 \times 10 \, s. = 270 \, s.$

 13 crowns
 = $13 \times 5 \, s. = 65 \, s.$

 41 half-crowns
 = $41 \times 2.5 \, s. = 102.5 \, s.$

 85 shillings
 = $85 \, s.$

 1222.5 s.

\$297.4648\ \$297.46. Ans.

Exercise 79. Page 163.

1.	Reduce 6 hr	17 min. 25 tec.
to se	vinia.	

hr.	min.	sec.	
6	17	25	
(1)			
3.7			
60			
20,1.	22.64	ec.	Ans.

2. Reduce 1 yr. 13 dy. 8 hr. 4 m.n. to minutes.

ÿr.	dy.	hr.	min.
1	13	8	4
282,			
378			
24			
(diffil)			
6/1)			
એક્સ	544,	894 m	in. Ans.

- 3. Reduce 48,567 min. to higher units.
 - 60 18567 min.

33 dy. 17 hr. 27 min. Ans.

4. Reduce 7,423,922 sec. to higher units.

85 dy. 22 hr. 12 min. 2 sec. Ans.

5. How many minutes are there from midnight of March 7 to midght of June 20?

6. Find the number of seconds from eight o'clock Monday morning till six o'clock the next Saturday evening.

y even.	ماتين	br.
M m.	16 hr.	130
Tues.	24	60
WedL	24	7800
Thu.	24	60
Fri.	24	468000
Sat	18	
	1:30 hr.	

464,000 sec. Ans.

- 7. Which of the years 1600, 1656, 1700, 1734, 1800, 1818, 1880, 1900, 1924, 2000 are leap years? 1600; 1656; 1880; 1924; 2000.

 Ans.
- 8. Add 8 dy. 14 hr. 21 min. 37 sec.; 44 dy. 17 hr. 13 min. 32 sec.; 208 dy. 9 hr. 47 min. 43 sec.; 161 dy. 12 hr. 53 min. 54 sec.; 88 dy. 22 hr. 17 min. 50 sec.

yr.	dу.	hr.	min.	sec.
	8	14	21	37
	44	17	13	32
	208	9	47	4 3
	161	12	53	54
	88	22	17	50
1	147	4	34	36

1 yr. 147 dy. 4 hr. 34 min. 36 sec.

9. Subtract 2 yr. 213 dy. 17 hr. 48 min. 48 sec. from 3 yr. 147 dy. 14 hr. 14 min. 32 sec.

yr.	dy.	hr.	min.	80C.
3	147	14	14	32
2	213	17	48	48
	298	20	25	44

298 dy. 20 hr. 25 min. 44 sec.

Ans.

10. Multiply 34 dy. 10 hr. 13 min. 12 sec. by 108.

10 yr. 67 dy. 23 hr. 45 min. 36 sec. Ans.

11. Divide 16 yr. 357 dy. 17 hr. 20 min. 48 sec. by 18.

344 dy. 7 hr. 37 min. 491 sec. Ans.

12. Divide 22 wk. 2 dy. by 11 hr. 31 min. 12 sec.

325. Ans.

Exercise 80. Page 164.

1. Napoleon was born Aug. 15, 1769, and died at the age of 51 yr. 8 mo. 20 dy. What was the date of his death?

yr.	mo.	dy.
1769	8	15
51	8	20
1821	5	5
	May 5	. 1821. A

2. Daniel Webster was born Jan. 18, 1782, and died Oct. 24, 1852. How old was he when he died?

yr.	mo.	dy.	
1852	10	24	
1782	1	18	
70	9	8	
	70 yr. 9 mo.	6 dy.	Ans.

3. A note dated July 14, 1897 has 63 days to run. When is the note due?

The number of days in July = 17 The number of days in Aug. = 31 The number of days in Sept. = $\frac{15}{63}$

Sept. 15, 1897. Ans.

4. A note dated Feb. 11, 1896 has 93 days to run. When is the note due?

The number of days in Feb. = 18
The number of days in Mar. = 31
The number of days in Apr. = 30
The number of days in May = $\frac{14}{93}$

May 14, 1896. Ans.

5. A note dated Feb. 11, 1897 has 63 days to run. When is the note due?

The number of days in Feb. = 17 The number of days in Mar. = 31 The number of days in Apr. = $\frac{15}{63}$

Apr. 15, 1897. Ans.

6. In the morning of July 5 a man went into the country for his vacation, and returned in the evening of Sept. 26. Express in weeks and days the length of his vacation.

July 5 and Sept. 26 are both included in the vacation.

The number of days in July = 27
The number of days in Aug. = 31
The number of days in Sept. = $\frac{26}{84}$

84 dy. = 12 wk. Ans.

7. Find the difference in time between Oct. 12, 1492, and July 4, 1776.

yr.	mo.	dy
1776	7	4
1492	10	12
283	8	22

283 yr. 8 mo. 22 dy. Ans.

8. Jan. 1, 1859, fell on Saturday. What day of the week was Jan. 1, 1860? Jan. 1, 1861?

The year from Jan. 1, 1859, to Jan. 1, 1860, contained 365 days; that is, 52 wk. 1 dy.

Therefore, Jan. 1, 1860, fell one day later, or on Sunday.

The year from Jan. 1, 1860, to Jan. 1, 1861, contained 366 days; that is, 52 wk. 2 dy.

Therefore, Jan. 1, 1861, fell two days later, or on Tuesday.

Sunday; Tuesday. Ans.

Exercise 81. Page 166.

1. Reduce 2° 30′ 25″ to seconds.

2. Reduce 15° 3' 22" to seconds.

3. Reduce 56,760" to higher units.

4. Reduce 212,221" to higher units.

5. Add 60° 50′ 50″; 20° 41′ 52″; 30° 25′ 20″; 20° 32′ 43″.

	132° 3	0′ 45″.	Ans.
132	30	45	
20	32	43	
30	25	20	
20	41	52	
60	50	50	
0	1	"	
•			

6. Subtract 58° 33′ 36″ from 90° 11′ 21″.

0	,	"
90	11	21
58	33	36
31	37	45

31° 37′ 45″. Ans.

7. Multiply 12° 14′ 32″ by 48.

0	1	"	
12	14	32	
		48	
587	37	36	
	587° 3	7′ 36″. <i>2</i>	lns.

8. Divide 321° 49′ 24″ by 22.

9. Divide 38° 37′ 42″ by 5° 31′ 6″.

7 Ans. 19866)139062 139062

Exercise 82. Page 168.

1. Find the value of \$ of a mile.

‡ mi. = ‡ of 320 rd. = 256 rd. Ans.

2. Find the value of $\frac{3}{16}$ of an acre.

$$_{16}^{3}$$
 A. = $_{16}^{3}$ of 160 sq. rd. = 30 sq. rd. Ans.

3. Find the value of \(\frac{1}{2} \) of a hundredweight.

$$\frac{1}{2}$$
 cwt. = $\frac{1}{2}$ of 100 lb. = $62\frac{1}{2}$ lb. $\frac{1}{2}$ lb. = $\frac{1}{2}$ of 16 oz. = 8 oz. 62 lb. 8 oz. Ans.

4. Find the value of 3 of a pound sterling.

£
$$\frac{1}{3} = \frac{1}{3}$$
 of 20 s. = 13 $\frac{1}{3}$ s.
 $\frac{1}{3}$ s. = $\frac{1}{3}$ of 12 d. = 4 d.
13 s. 4 d. Ans.

5. Find the value of ? of a mile.

$$\frac{9}{11} \text{ mi.} = \frac{9}{11} \text{ of } 320 \text{ rd.} = 261 \frac{9}{11} \text{ rd.}$$
 $\frac{9}{11} \text{ rd.} = \frac{9}{11} \text{ of } 5\frac{1}{2} \text{ yd.} = 4\frac{1}{2} \text{ yd.}$
 $\frac{1}{2} \text{ yd.} = \frac{1}{2} \text{ of } 3 \text{ ft.} = 1\frac{1}{2} \text{ ft.}$
 $\frac{1}{2} \text{ ft.} = \frac{1}{2} \text{ of } 12 \text{ in.} = 6 \text{ in.}$
261 rd. 4 vd. 1 ft. 6

261 rd. 4 yd. 1 ft. 6 in. Ans.

6. Find the value of $\frac{7}{11}$ of an acre.

$$\frac{7}{11} A. = \frac{7}{11} \text{ of } 160 \text{ sq. rd.} = 101 \frac{9}{11} \text{ sq. rd.}$$
 $\frac{9}{11} \text{ sq. rd.} = \frac{9}{11} \text{ of } 30\frac{1}{4} \text{ sq. yd.} = 24\frac{3}{4} \text{ sq. yd.}$
 $\frac{3}{4} \text{ sq. yd.} = \frac{3}{4} \text{ of } 9 \text{ sq. ft.}$
 $\frac{3}{4} \text{ sq. ft.} = \frac{3}{4} \text{ of } 144 \text{ sq. in.} = 108 \text{ sq. in.}$
 $101 \text{ sq. rd. } 24 \text{ sq. yd. 6 sq. ft. } 108 \text{ sq. in.}$
 $Ans.$

7. Find the value of 4 of a degree.

$$\frac{4}{3}^{\circ} = \frac{4}{3} \text{ of } 60' = 26\frac{2}{3}'.$$
 $\frac{2}{3}' = \frac{2}{3} \text{ of } 60'' = 40''.$
 $26' \ 40''. Ans.$

8. Find the value of $\frac{1}{3}$ of a year.

$$\frac{1}{3}$$
 yr. = $\frac{1}{3}$ of 365 dy. = 121 $\frac{2}{3}$ dy. $\frac{1}{3}$ dy. = $\frac{2}{3}$ of 24 hr. = 16 hr. 121 dy. 16 hr. Ans.

9. Find the value of 0.15625 of a bushel.

$$\begin{array}{r}
0.15625 \\
 \underline{4} \\
0.62500 \\
 \underline{8} \\
5.000
\end{array}$$
5 qt. Ans.

10. Find the value of 0.625 of a gallon.

11. Find the value of 0.875 of a leap year.

$$\begin{array}{r}
0.875 \\
\underline{366} \\
5250 \\
5250 \\
\underline{2625} \\
320.250 \\
\underline{24} \\
100 \\
\underline{50} \\
6.00
\end{array}$$

320 dy. 6 hr. Ans.

12. Find the value of 0.325 of a pound troy.

3 oz. 18 dwt. Ans.

13. Find the value of $6\frac{1}{3}$ of 3 A. $101\frac{1}{3}$ sq. rd.

A. sq. rd. sq. yd. sq. ft. sq. in.

3 1011
2

427

A. sq. rd. sq. yd. sq. ft. sq. in. 3 1011

$$\frac{6}{21}$$

7

23 A. 40 sq. rd. 16 sq. yd. 1 sq. ft. 284 sq. in. Ans.

14. Find the value of 13 of 7 hr. 21 min. 27 sec.

hr.	min.	sec.
7	21	27
7 22	4	$\frac{3}{21}$
3	9	11 4
7	21	27
10	30	384

10 hr. 30 min. 384 sec. Ans.

15. Find the value of 10.0175 of 1 dy. 13 hr.

370 hr. 38 min. 51 sec. = 15 dy. 10 hr. 38 min. 51 sec. Ans.

60

16. Find the value of $17\frac{7}{12}$ of 10 yd. 2 ft. $3\frac{1}{3}$ in.

•	•	
yd.	ft.	in.
10	2	31
		7
12 75	0	103
6	0	913
yd.	ft.	in.
10	2	3 1
		17
182	2	63
6	0	913
189	0	414

189 yd. $4\frac{4}{15}$ in. = 34 rd. 2 yd. $4\frac{4}{15}$ in. Ans.

17. Find the value of 0.01284 of 14 mi.

57 rd. 2 yd. 2 ft. 7.5936 in. Ans.

18. Find the value of 0.42776 of 12 t. 10 cwt.

12 t. 10 cwt. = 12.5 t.

5 t. 6 cwt. 94 lb. Ans.

19. Find the value of $\frac{3}{5}$ of 1 lb. $+3\frac{3}{5}$ oz. $+5\frac{3}{5}$ dwt.

 $\frac{2}{3}$ of 1 lb. = $\frac{2}{3}$ lb. = $\frac{2}{3}$ of 12 oz. = $\frac{44}{3}$ oz.

 $4\frac{4}{3}$ oz. $+3\frac{1}{3}$ oz. $=8\frac{1}{45}$ oz.

 $\frac{1}{45}$ oz. = $\frac{1}{45}$ of 20 dwt. = $\frac{4}{9}$ dwt.

 $\frac{4}{3}$ dwt. $+5\frac{2}{3}$ dwt. $=6\frac{1}{3}$ dwt.

 $\frac{1}{2}$ dwt. = $\frac{1}{2}$ of 24 gr. = 2 $\frac{1}{2}$ gr.

8 oz. 6 dwt. 23 gr. Ans.

20. Find the value of 0.35 of 4 lb. 5 oz. 6 dwt. 16 gr.

1 lb. 6 oz. 13 dwt. 8 gr. Ans.

21. Find the value of 3.726 mi. - 33.57 rd.

$$\begin{array}{r}
3.726 \\
320 \\
\hline
14520 \\
2178 \\
\hline
232.320
\end{array}$$

mi. rd.
$$3$$
 232.32 33.57 $\overline{3}$ 198.75 $\underline{5.5}$ 375 $\underline{4.125}$ $\underline{3}$ 0.375 $\underline{12}$ 4.500

3 mi. 198 rd. 4 yd. 4.5 in. Ans.

22. Find the value of $\frac{3}{75}$ of a year $+\frac{9}{55}$ of a week $+\frac{7}{12}$ of an hour.

 $\frac{3}{73}$ yr. = $\frac{3}{73}$ of 365 dy. = 15 dy. $\frac{9}{56}$ wk. = $\frac{9}{56}$ of 7 dy. = $\frac{1}{8}$ dy. $\frac{1}{8}$ dy. = $\frac{1}{8}$ of 24 hr. = 3 hr. $\frac{7}{12}$ hr. = $\frac{7}{12}$ of 60 min. = 35 min.

16 dy. 3 hr. 35 min. Ans.

23. Find the value of 5.268 of 2 dy. +2.829 of 16 hr. +0.9528 of 25 min.

5.268	2.829	0.9528
2	16	25
10.536	16974	47640
24	2829	19056
2144	45.264	23.8200
1072	12.864	7.68
12.864	58.128	$\overline{31.50}$
	60	60
	7.680	30.0

10 dy. 58 hr. 31 min. 30 sec. =12 dy. 10 hr. 31 min. 30 sec. Ans.

24. Find the value of $\frac{3}{16}$ of a mile $+\frac{2}{3}$ of 40 rd. $+\frac{3}{8}$ of a yard.

 $\frac{8}{16}$ mi. = $\frac{8}{16}$ of 320 rd. = 60 rd. $\frac{3}{2}$ of 40 rd. = 26 $\frac{3}{4}$ rd. 60 rd. + 26 $\frac{3}{8}$ rd. = 86 $\frac{3}{8}$ rd. $\frac{3}{8}$ rd. = $\frac{3}{5}$ of $5\frac{1}{2}$ yd. = $3\frac{3}{5}$ yd. $3\frac{7}{2}$ yd. + $\frac{3}{8}$ yd. = $4\frac{1}{24}$ yd. $\frac{1}{24}$ yd. = $\frac{1}{24}$ of 3 ft. = $\frac{1}{2}$ ft. $\frac{1}{8}$ ft. = $\frac{1}{8}$ of 12 in. = $1\frac{1}{2}$ in. 86 rd. 4 yd. $1\frac{1}{2}$ in. Ans. 25. Find the value of \$\frac{1}{4}\$ of 2 cwt. 84 lb. + \$\frac{1}{7}\$ of 5 cwt. 98 lb. + \$\frac{1}{7}\$ of 7\$\frac{1}{2}\$ lb. \$\frac{1}{4}\$ of 2 cwt. 84 lb. \$\frac{1}{4}\$ of 2 cwt. 84 lb. \$\frac{1}{4}\$ of 5 cwt. 98 lb. \$\frac{1}{4}\$ of 598 lb. \$\frac{1}{2}\$ of 598 lb. \$\frac{1}{2}\$ of 7\$\frac{1}{2}\$ lb. \$\frac{1}{2}\$ lb. + 256\$\frac{1}{2}\$ lb. + 3 lb. = 472\$\frac{1}{2}\$ lb. \$\frac{1}{4}\$ lb. = \$\frac{1}{4}\$ of 16 oz. \$\frac{1}{4}\$ oz. 472 lb. 4\$\frac{1}{4}\$ oz.

26. Find the value of $\frac{3}{2}$ of 21 ft. 7 in. + 0.855 of 16 ft. 2 in. + 0.365 of 1 ft.

= 4 cwt. 72 lb. 44 oz. Ans.

21 ft. 7 in. = 259 in.; 16 ft. 2 in. = 194 in.; 1 ft. = 12 in.

259	194	0.365
0.375	0.855	12
1295	970	730
1813	970	365
777	1552	4.380
97.125	165.870	

97.125 in.
165.87
4.38
12 267.375 in.
3 22 ft. . . . 3.375 in.
7 yd. . . . 1 ft.
7 yd. 1 ft. 3\frac{3}{8} in. Ans.

27. Find the value of 0.9 of 4 A. 17 sq. rd. $-\frac{11}{12}$ of 3 A. 15 sq. rd.

187 sq. rd. 16 sq. yd. 5 sq. ft. 106.2 sq. in. Ans.

28. Find the value of 0.652 of 2 cu. yd. 7 cu. ft. — 0.888 of 1 cu. yd. 2 cu. ft.

2 cu. yd. 7 cu. ft. = 61 cu. ft. 1 cu. yd. 2 cu. ft. = 29 cu. ft.

$$\begin{array}{ccc}
\mathbf{0.652} & \mathbf{0.888} \\
\underline{\mathbf{61}} & \mathbf{29} \\
\hline
\mathbf{652} & \mathbf{7992} \\
\underline{\mathbf{3912}} & \mathbf{1776} \\
\underline{\mathbf{39.772}} & \mathbf{25.752}
\end{array}$$

14 cu. ft. 34.56 cu. in. Ans.

29. Find the value of 0.456 of 12 bu. 3 pk. — 0.654 of 5 bu. 2 pk.

0.456	0.654	23.256
51	22	14.388
456	1308	8.868
2 280	1308	8
23.256	14.388	6.944
		2
		1.888

8 pk. 6 qt. 1.888 pt. = 2 bu. 6 qt. 1.888 pt. Ans.

Exercise 83. Page 169.

1. Express a pound avoirdupois as the fraction of a pound troy.

1 lb. av. = 7000 gr. 1 lb. troy = 5760 gr.
$$\frac{7000}{5760} = \frac{175}{144}$$
. Ans.

2. Express an ounce avoirdupois as the fraction of an ounce troy.

1 oz. av.
$$= \frac{1}{16}$$
 of 7000 gr. $= 437\frac{1}{2}$ gr.
1 oz. troy $= \frac{1}{12}$ of 5760 gr. $= 480$ gr.
 $\frac{437\frac{1}{4}}{480} = \frac{875}{960} = \frac{175}{192}$. Ans.

3. Express 363 sq. yd. as the fraction of an acre.

$$\frac{363}{160 \times 30\frac{1}{4}} = 333 \times \frac{1}{139} \times \frac{4}{121} = \frac{3}{40}. Ans.$$

4. Express $\frac{3}{4}$ of £2 1s. 3d. $+\frac{5}{11}$ of £1 4s. 9d. as the fraction of £2 14s.

£	s.	d.	£	8.	· d.
2	1	3	1	4	9
		3			5
5 6.	3	9	11 6	3	8
1	4	8	\	11	3
£	8.	d.	£	s.	
1	4	8	2	14	
	11	3	20		
1	16	0	20 54		
20					
20 36		<u>36</u> _	$\frac{2}{3}$. Ans.		
		54 —	<i></i> 1/•••. 3		

5. Express 2 mi. 138 rd. 1 yd. as the fraction of 3 mi. 265 rd. 3 yd. 1 ft. 6 in.

3 mi. 265 rd. 3 yd. 1 ft. 6 in. = 3 mi. 265 rd. $3\frac{1}{2}$ yd.

mi. rd. yd. mi. rd. yd.
$$\frac{320}{778}$$
 $\frac{320}{1225}$ $\frac{5\frac{1}{2}}{4280}$ $\frac{5\frac{1}{2}}{6741}$ $\frac{4280}{63}$ $\frac{40}{63}$ Ans.

6. Express 7 of 560 lb. as the fraction of 5 long tons.

$$\frac{\frac{3}{5} \text{ of } 560}{5 \times 2240} = \frac{2}{7} \times 560 \times \frac{1}{5} \times \frac{1}{2240} = \frac{1}{70} \cdot Ans.$$

7. Express 3 of 200 rd. as the fraction of 4 mi.

$$\frac{3 \text{ of } 200}{4 \times 320} = \frac{2}{3} \times \cancel{200} \times \frac{1}{4} \times \frac{1}{320} = \frac{5}{48}. \text{ Ans.}$$

8. Express 19 of 2 dy. 2 hr. 24 min. as the fraction of 2 wk. 1 dy.

$$\frac{\frac{19}{21600} \text{ of } 3024}{21600} = \frac{\cancel{10}}{\cancel{27}} \times \cancel{\cancel{3024}} \times \frac{1}{\cancel{21600}} = \frac{7}{135}. \text{ Ans.}$$

9. Express 4 of the difference between 3 yd. 2 ft. 11 in. and 10 yd. 7 in. as the fraction of 8 yd.

yd. ft. in. 10 0 7
$$\frac{3}{6}$$
 $\frac{2}{6}$ $\frac{11}{8}$ 6 yd. 8 in. = $6\frac{5}{36}$ yd. = $6\frac{2}{3}$ yd.

$$\frac{\frac{4}{5} \text{ of } 6\frac{3}{5}}{8} = \frac{4}{5} \times \frac{\frac{5}{5}}{9} \times \frac{1}{8} = \frac{28}{45} \cdot Ans.$$

10. Express $\frac{10}{21}$ of the difference between $\frac{5}{8}$ of 7 hr. and $\frac{7}{25}$ of 15 min. as the fraction of 12 hr. 18 min.

 $\frac{5}{8}$ of 7 hr. = $\frac{85}{8}$ hr. = $\frac{48}{8}$ hr.

 $\frac{7}{25}$ of 15 min. = $\frac{7}{25}$ of $\frac{1}{4}$ hr. = $\frac{7}{100}$ hr. 12 hr. 18 min. = $12\frac{18}{60}$ hr. = $12\frac{8}{10}$ hr.

$$4\frac{3}{8}$$
 hr. $-\frac{7}{100}$ hr. $=4\frac{61}{200}$ hr.

$$\frac{\frac{10}{21} \frac{\text{of } 4\frac{61}{2000}}{12\frac{3}{10}} = \frac{\cancel{10}}{\cancel{21}} \times \frac{\cancel{801}}{\cancel{200}} \times \frac{\cancel{10}}{\cancel{123}} = \frac{1}{6} \cdot Ans.$$

11. Express $\frac{2}{5}$ pt. as the fraction of a gallon.

$$1 \text{ gal.} = 8 \text{ pt.}$$

$$\frac{\frac{2}{8}}{8} = \frac{2}{5} \times \frac{1}{8} = \frac{1}{20}$$
. Ans.

12. Express 16 s. 3\frac{3}{4} d. as the decimal of a pound.

13. Express 233 rd. 9 ft. 10.8 in. as the decimal of a mile.

14. Express 71 sq. rd. 54 sq. ft. 64.8 sq. in. as the decimal of an acre.

15. Express 15 hr. 14 min. 6 sec. as the decimal of 2 days.

16. Express 38 sq. rd. 21 sq. yd. 5 sq. ft. 108 sq. in. as the decimal of an acre.

17. Express 3 mi. 242 rd. 2 yd. 2 ft. 3 in. as the decimal of 7 mi. 160 rd.

12 | 3. in. 320 | 160 rd.
3 | 2.25 ft., 7.5 mi.
5\frac{1}{2} | 2.75 yd.
320 | 242.5 rd.
3.7578 mi.

$$\frac{3.7578}{7.5} = 0.501. Ans.$$

18. Express 5 hr. 13 min. 30 sec. as the decimal of a week.

19. Express 27° 14′ 45″ as the decimal of 90°.

$$60 \begin{vmatrix} 45. \\ 60 \end{vmatrix} \frac{14.75'}{27.246}$$

$$\frac{27.246}{90} = 0.303. \ Ans.$$

20. Express 54 dy. 2 hr. 40 min. as the decimal of 3651 days.

2 hr. 40 min. =
$$2\frac{2}{3}$$
 hr. = $\frac{2\frac{2}{3}}{24}$ dy.
= $\frac{4}{72}$ dy. = $\frac{1}{5}$ dy.

$$\frac{54\frac{1}{5}}{365\frac{1}{4}} = \frac{487}{9} \times \frac{4}{1461} = \frac{4}{27} = 0.148.$$
3 Ans.
0.148
27)4.0

$$\frac{27}{130}$$

$$\frac{108}{220}$$
216

Express 44,920.9025 hr. as mal of a year.

$$\frac{805}{9925} = \frac{8984.1805}{1752} = 5.128.$$
Ans.

Express 14.52 sq. yd. as the of a square chain.

sq. ch. = 16 sq. rd.
= 484 sq. yd.
$$\frac{14.52}{494} = 0.08. Ans.$$

26. What part of 2 mi. is § 6 rd. 3 yd. 2 in.?

2 in. =
$$\frac{2}{16}$$
 yd. = $\frac{1}{18}$ yd.
3 $\frac{1}{18}$ yd. = $\frac{3}{18}$ rd. = $\frac{5}{9}$ rd.

$$\frac{\frac{2}{3} \text{ of } 6\frac{5}{5}}{2 \times 320} = \frac{2}{3} \times \frac{59}{9} \times \frac{1}{2} \times \frac{1}{320} = \frac{6}{86}$$

27. What part of a bushe 1 pk. 2 qt. 1 pt.?

1 bu.
$$= 64$$
 pt.

29. What part of 5 tons is 3 t. 240 lb.?

$$3 \text{ t. } 240 \text{ lb.} = 6240 \text{ lb.}$$

$$\frac{\cancel{6249}}{5 \times \cancel{2999}} = \frac{78}{125} \cdot Ans.$$

30. What part of an acre is 38 sq. rd. 194 sq. ft. 108 sq. in.?

38 sq. rd. 194 sq. ft. 108 sq. in. = 38 sq. rd. 1943 sq. ft.

$$\begin{array}{ccc}
sq. rd. & sq. ft. \\
38 & 194\frac{1}{4} \\
\underline{272\frac{1}{4}} \\
10540\frac{1}{4} & \underline{42161} \\
\underline{42560} & \underline{42161} \\
\end{array}$$

31. Express 2 lb. 9 oz. 21 dwt. as the decimal of 4 lb. 7 oz. 19 dwt.

32. Express 17 wk. 6 dy. 22 hr. 39 min. as the decimal of 35 wk. 3 dy. 15 hr. 25 min.

wk. dy. hr. min. wk. dy. hr. min.

17 6 22 39 35 3 15 25

7 7

125 248

24 24

3022 5967

60 60

181359 358045

33. What part of 61 ft. 3 in. is 8 ft. 7 in.?

Exercise 84. Page 172.

Find the difference in longitude between two cities, if the difference in time is:

1. 1 hr. 15 min.

1 hr. 15 min.

	15
18°	45'

2. 2 hr. 11 min.

2 hr. 11 min.

3. 5 hr. 10 min. 10 sec.

5 hr. 10 min. 10 sec.

4. 3 hr. 25 min. 35 sec.

3 hr. 25 min. 35 sec.

5. 6 hr. 12 min. 30 sec.

6 hr. 12 min.

30 sec.

6. 4 hr. 8 min. 12 sec.

4 hr. 8 min. 12 sec.

7. 18 hr. 10 min.

18 hr. 10 min.

8. 15 hr. 15 min. 15 sec.

15 hr. 15 min. 15 sec.

Find the difference in time between two cities, if the difference in longitude is:

9. 9° 20′.

15 9° 20′ 37 min. 20 sec.

10. 70° 30′.

15 70° 30′ 4 hr. 42 min.

11. 56° 36′ 12″.

15 56° 36' 12"
3 hr. 46 min. 24.8 sec.

12. 108° 32′ 36″.

15 108° 32' 36" 7 hr. 14 min. 10,4 sec. **13**. 120° 14′ 30″.

15 120° 14′ 30″ 8 hr. 0 min. 58 sec.

14. 100° 45′ 54″.

15 100° 45' 54" 6 hr. 43 min. 3.6 sec.

15. 2° 2' 2".

 $\frac{15 \ 2^{\circ} \qquad 2' \qquad 2''}{8 \text{ min.} \qquad 8\frac{2}{15} \text{ sec.}}$

16. 75° 10′.

15 75° 10'
5 hr. 0 min. 40 sec.

17. Find the difference in time between New York, longitude 74° 0′ 3″ west, and San Francisco, longitude 122° 26′ 15″ west.

18. The difference in time between Berlin and New York is 5 hr. 49 min. 35 sec. What is the difference in longitude?

Exercise 85. Page 174.

The longitude of some public building in:

- (1) Berlin is 13° 23′ 43″ E.
- (2) Rome, 12° 27′ 14″ E.
- (3) Constantinople, 28° 59' E.
- (4) Pekin, 116° 23′ 45″ E.
- (5) San Francisco, 122° 26′ 15″ W.
- (6) St. Louis, 90° 15′ 15″ W.

- (7) Jerusalem, 35° 32' E.
- (8) Bombay, 72° 54′ E.
- (9) Calcutta, 88° 19′ 2″ E.
- (10) Chicago, 87° 35' W.
- (11) New York, 74° 0′ 3″ W.
- (12) Montreal, 73° 25' W.

What is the clock-time at each of the above cities:

1. When is it noon at Greenwich?

53 min. 3418 sec. past 12 p.m. Ans.

49 min. 4814 sec. past 12 р.м. Ans.

55 min. 56 sec. past 1 P.M. Ans.

45 min. 35 sec. past 7 p.m. Ans.

50 min. 15 sec. past 3 A.M. Ans.

58 min. 59 sec. past 5 A.M. Ans.

	(7)	
15 35°	32'	
2 hr.	22 min.	8 sec.
22 min 8	sec past 2	PW. Ans.

51 min. 36 sec. past 4 P.M. Ans.

53 min. $16\frac{2}{15}$ sec. past 5 p.m. Ans.

9 min. 40 sec. past 6 A.M. Ans.

3 min. 59 sec. past 7 A.M. Ans.

2. When it is half-past 4 P.м. at Chicago?

13 min. 5418 sec. past 11 P.M. Ans.

10 min. 814 sec. past 11 P.M. Ans.

16 min. 16 sec. past 12 A.M. of the following day. Ans.

	(4)	
87°	35′	0" W.
116°	23'	45" E.
15 203°	58′	45"
13 hr.	35 min.	55 sec.
hr.	min.	8ec.
4	30	
13	35	55
18	5	55
12	0	0
6	5	5 5

5 min. 55 sec. past 6 A.M. of the following day. Ans.

	(5)	
122°	26′	15" W.
87°	351	W .
15 34°	51'	15"
2 hr.	19 min.	25 sec.
hr.	min.	sec.
4	30	
2	19	25
2	10	35

10 min. 35 sec. past 2 P.M. Ans.

	(6)	
90°	15'	15" W.
87°	351	W.
15 2°	40'	15"
-	10 min.	41 sec.
hr.	min.	sec.
4	30	
	10	41
4	19	19

19 min. 19 sec. past 4 P.M. Ans.

	(7)	
87°	35' W.	
35°	32' E.	
15 123°	7'	
8 hr.	12 min.	28 sec.
hr.	min.	sec.
4	30	
8	12	28
12	42	28

42 min. 28 sec. past 12 A.M. of the following day. Ans.

11 min. 56 sec. past 3 A.M. of the following day. Ans.

	(9)	
87°	35′	0" W.
88°	19'	2" E.
15 175°	54'	211
11 hr.	43 min.	36_{13}^{2} sec.
hr.	min.	sec.
4	30	
11	43	36.2
16	13	3613
12	0	0
4	13	362

13 min. 36_{13}^{2} sec. past 4 A.M. of the following day. Ans.

	(10)	
30 min.	past 4 P.M.	Ans.

U	O MAINI.	Person z r.m.	21/60.
		(11)	
	87°	35′	0" W.
	74°	0'	3" W.
15	13°	34′	57''
_		54 min.	19 4 sec.
	hr.	min.	sec.
	4	30	
		54	194
	5	24	194

24 min. 194 sec. past 5 p.m. Ans.

hr.	min.	sec.
4	30	
	56	40
5	26	40

26 min. 40 sec. past 5 P.M. Ans.

3. When it is eight o'clock A.M. at Constantinople?

	(1)	
28°	59 ′	0" E.
13°	23'	43" E.
15 15°	35'	17"
1 hr.	2 min.	$21\frac{2}{15}$ sec.
hr.	min.	sec.
8	0	0
1	2	$21\frac{2}{15}$
6	57	3818

57 min. 3818 sec. past 6 A.M. Ans.

hr. min. sec.
$$8 0 0$$
 $\frac{1}{6} \frac{6}{53} \frac{52}{13}$

53 min. 5214 sec. past 6 A.M. Ans.

49 min. 39 sec. past 1 P.M. Ans.

		(5)	
	28°	591	0" E.
	122°	26′	15" W.
15	151°	25′	15"
	10 hr.	5 min.	41 sec.
	hr.	min.	sec.
	8	0	0
	10	5	41
	9	54	19

54 min. 19 sec. past 9 P.M. of the previous day. Ans.

•	(6)	
28°	59/	0" E.
80 °	15'	15" W.
15 119°	14'	15"
7 hr.	56 min.	57 sec.
hr.	min.	sec.
8	0	0
7	56	57
	3	3

3 min. 3 sec. past 12 A.M. Ans.

		(7)	
	3 5°	32′ E.	
	28°	59' E.	
15	6°	33'	
• · · · · · · · · · · · · · · · · · · ·		26 min	. 12 sec.
	hr.	min.	sec.
	8	0	0
		26	12
	8	26	12
OA.	i 10		0 4.

26 min. 12 sec. past 8 A.M. Ans.

55 min. 40 sec. past 10 A.M. Ans.

		(9)	
	88° 28°	19'	2" E.
	28°	59′	E.
15	59°	20′	2"
•	3 hr.	57 min.	2013 sec.
	hr.	min.	sec.
	8	0	0
	3	57	$20_{\frac{2}{15}}$
	11	57	2013
57 1	min. $20\frac{2}{15}$	sec. past 1	1 A.M. Ans.

(10)
28° 59' E.
87° 35' W.
15 116° 34'
7 hr. 46 min. 16 sec.

hr. min. sec. 8 0 0 7 46 16 13 44

13 min. 44 sec. past 12 A.M. Ans.

(11) 28° 0" E. 59' 3" W. 74° 0' 15 102° 591 311 6 hr. 51 min. 561 sec. min. hr. sec. 8 0 0 в 561 51 1 8 34 8 min. $3\frac{4}{5}$ sec. past 1 A.M. Ans.

(12)28° 59' E. 73° 25′ W. 15 102° 24' 6 hr. 49 min. 36 sec. hr. min. sec. 8 0 0 6 49 36

1

10 min. 24 sec. past 1 A.M. Ans.

24

10

When it is noon at Greenwich the time at:

- (1) Boston, Mass., is 7 hr. 15 min. 46 sec. A.M.
- (2) Columbia, S.C., 6 hr. 35 min. 32 sec. A.M.
- (3) Salt Lake, 4 hr. 30 min. A.M.
- (4) Albany, N.Y., 7 hr. 5 min. 1 sec. A.M.
- (5) Harrisburg, Penn., 6 hr. 52 min. 40 sec. A.M.

- (6) New Orleans, La., 6 hr. A.M.
- (7) Columbus, O., 6 hr. 27 min. 48 sec. A.M.
- (8) Washington, D.C., 6 hr. 51 min. 44 sec. A.M.
- (9) Springfield, Ill., 6 hr. 1 min. 48 sec. A.M.

4. What is the longitude of each of the above cities?

	(1)		
hr.	min.	sec.	
12	0	0	
7	15	46	
4	44	14	
		15	
71°	3′	30"	
	71° 3′	30" W.	Ans.

81° 7' W. Ans.

112° 30' W. Ans.

	(5)	
hr.	min.	sec
12	0	0
6	52	10
5	7	<u> </u>
		15
76°	50′	

76° 50′ W. Ans.

90° W. Ans. (8)

	(7)	
hr.	min.	sec.
12	0	0
6	27	48
5	32	12
		15
83°	3'	

83° 3' W. Ans.

	(8)	
hr.	min.	sec.
12	0	0
6	51	44
5	8	16
		15
770	4'	

7724' W. Ans.

	(9)	
hr.	min.	sec
12	0	0
6	1	48
5	58	12
		15
89°	33'	

89° 33' W. Ans.

Exercise 86. Page 175.

1. Reduce 7 gal. 3 qt. 1 pt. to gallons and the decimal of a gallon.

2. Reduce £ 4.375 to pounds, shillings, and pence.

£
$$4.375$$
 $\frac{20}{7.5 \text{ s.}}$
 $\frac{12}{6 \text{ d.}}$

£4 7s. 6d. Ans.

3. Reduce 7.6875 gal. to gallons, quarts, and pints.

$$\begin{array}{r}
 7.6875 \\
 \underline{4} \\
 2.75 \\
 \underline{2} \\
 1.5
 \end{array}$$

7 gal. 2 qt. 1.5 pt. Ans.

4. If \$4.85 is equal to a pound, reduce to pounds, shillings, and pence \$5.875; \$7.38; \$17.85; \$21.75.

$$\begin{array}{r}
1.2\frac{1}{67} \\
485)587.5 \\
\underline{485} \\
1025 \\
\underline{970} \\
55 \\
0.2\frac{1}{67} = \frac{41}{104}.
\end{array}$$

$$\begin{array}{r}
0.2\frac{1}{67} = \frac{41}{104}. \\
\cancel{2} \text{ for } 20 \text{ s.} = 4\frac{27}{67} \text{ s.} \\
\cancel{3} \text{ s.} = \cancel{3} \text{ of } 12 \text{ d.} = 2\cancel{7} \text{ d.}
\end{array}$$

$$\begin{array}{r}
1\frac{258}{485} \\
485)738 \\
\underline{485} \\
253
\end{array}$$

£ 1 4 s. 279 d. Ans.

£
$$\frac{258}{185} = \frac{258}{185}$$
 of 20 s. = 10 $\frac{1}{9}$ s. $\frac{47}{19}$ s. = $\frac{47}{19}$ of 12 d. = $\frac{5}{19}$ d. £ 1 10 s. $\frac{5}{19}$ d. Ans.

$$\begin{array}{r}
 389 \\
 \hline
 485)1785 \\
 \hline
 1455 \\
 \hline
 330
 \end{array}$$

£
$$\frac{6}{97}$$
 = $\frac{6}{97}$ of 20 s. = $13\frac{5}{97}$ s.
 $\frac{5}{97}$ s. = $\frac{5}{97}$ of 12 d. = $7\frac{2}{97}$ d.
£ 3 13 s. $7\frac{2}{97}$ d. Ans.

$$4\frac{4}{4}$$

$$485)2175$$

$$1940$$

$$235$$

£
$$\frac{47}{57} = \frac{47}{57}$$
 of 20 s. = 9 $\frac{47}{57}$ s. $\frac{47}{57}$ s. = $\frac{47}{57}$ of 12 d. = 8 $\frac{47}{57}$ d. £ 4 9 s. 8 $\frac{44}{57}$ d. Ans.

5. How many square yards in 3.7156 A.?

6. If 2 qt. of linseed oil are mixed with 1 pt. spirits of turpentine, what fraction of the mixture is turpentine? How much turpentine in one pint of the mixture?

2 qt.
$$+\frac{1}{2}$$
 pt. $=4\frac{1}{2}$ pt. $\frac{1}{4\frac{1}{2}} = \frac{2}{9} \times \frac{1}{2} = \frac{1}{9}$. Ans. $\frac{1}{9}$ of 1 pt. $=\frac{1}{9}$ pt. Ans.

7. Reduce 5.1732 mi. to yards, feet, and inches.

9104 yd. 2 ft. 5.952 in. Ans.

8. If a man walks 88 mi. in 26 hr., how many feet does he walk in a second?

11

$$\frac{\cancel{88} \times \cancel{5280}}{\cancel{20} \times \cancel{00} \times \cancel{00}} \text{ ft.} = \frac{968}{195} \text{ ft.}$$

$$= 4188 \text{ ft.} \quad 4ns.$$

= 4188 ft. Ans.

9. Of a mixture of sand and lime 0.27 of the weight is lime. How many ounces of lime in a pound of the mixture? many troy grains of lime in an avoirdupois pound of the mixture?

10. A gill of water is put into a quart measure, and the measure then filled with milk. What part of the mixture is water?

1 gi. =
$$\frac{1}{3}$$
 qt.
 $\therefore \frac{1}{3}$ is water.

11. Reduce 555 ft. to the decimal of a mile.

0.1051136 mi. Ans.

12. Reduce 1 mi. 13 rd. 2 yd. 2 ft. 6 in. to inches.

66,036 in. Ans.

13. How many cubic inches in 2½ cu. ft.?
1728 cu. in.

14. How many pounds avoirdupois does a cubic yard of water weigh if a cubic foot weighs 1000 oz.?

15. Express the weight of a cubic yard of water as the decimal of a ton.

1687½ lb. =
$$\frac{1687.5}{2000}$$
t.
= 0.84375 t. Ans.

16. What is the weight of 7 bu. 3½ pk. of potatoes?

3\frac{1}{2} pk. =
$$\frac{3\frac{1}{4}}{4}$$
 bu. = $\frac{7}{8}$ bu. $\frac{7\frac{7}{8}}{52\frac{1}{4}}$ \frac{420}{472\frac{1}{4}} lb. Ans.

17. A farmer sowed 5 bu. 1 pk. 1 qt. of seed, and harvested from it 103 bu. 3 pk. 5 qt. How much did he raise from a bushel of seed?

bu.	pk.	qt.	bu.	pk.	qt.
5	1	1	103	3	5
4			4		
2 1			415		
8			8		
169			3325		

$$\frac{8335}{169}$$
 of 1 bu. $= \frac{8325}{169}$ bu. $= 19\frac{14}{169}$ bu. $\frac{114}{169}$ bu. $= \frac{114}{169}$ of 4 pk. $= 2\frac{118}{169}$ pk. $\frac{118}{169}$ pk. $= \frac{118}{169}$ of 8 qt. $= 5\frac{99}{169}$ qt. $= 5.6$ qt. 19 bu. 2 pk. 5.6 qt. Ans.

18. How many bushels in 5 tons of oats?

$$\frac{5 \times 2000}{32} = \frac{625}{2} = 312\frac{1}{2}. Ans.$$

19. How many bottles, each holding 1 pt. 3 gi., can be filled from a barrel of cider?

1 pt. 3 gi. =
$$\frac{18}{4}$$
 pt. = $\frac{7}{32}$ gal.

$$\frac{16}{31\frac{1}{2}} = \frac{32}{7} \times \frac{63}{2} = 144. Ans.$$

20. If a steamer makes 13 mi. 6 rd. an hour, how far will she go between 6 A.M. and 6 P.M.? How many hours will she require to make 113 miles?

156 mi. 72 rd. Ans.

13 mi. 6 rd. = 13_{160} mi.

$$\frac{113}{13_{180}} = \frac{160}{2083} \times 113$$

$$= \frac{18080}{2083} = 8\frac{1418}{2083}. Ans.$$

21. If a train runs at the average rate of 111 rd. a minute, how many hours will it require to run from Boston to Buffalo, **498 miles?**

$$\frac{166}{498 \times 320} = \frac{2656}{111} = 23_{111}^{103}.$$

$$\frac{103}{8} \text{ hr.} = \frac{103}{111} \text{ of 60 min.}$$

$$= 56 \text{ min. nearly.}$$
23 hr. 56 min. nearly. Ans.

22. What is the cost of 12 A. 146 sq. rd. of land at \$16.25 an acre?

$$146 \text{ sq. rd.} = \frac{73}{16} \text{ A.}$$

$$12\frac{73}{10} \times \$16\frac{1}{4} = \frac{1033}{80} \times \$\frac{65}{4}$$

$$= \$\frac{13429}{64} = \$209.83. \text{ Ans.}$$

23. What is the cost of 8 t. 3 cwt. 27 lb. of coal at \$5.75 a ton?

\$46.94. Ans.

24. What is the cost of 7 t. 1560 lb. of hay at \$15.50 a ton?

1560 lb. =
$$\frac{1560}{2000}$$
 t. = $\frac{78}{100}$ t.
\$15.50
 $\frac{7.78}{12400}$
 $\frac{10850}{120.59}$ Ans.

25. What is the cost of a car load of wheat weighing 20,000 lb., at \$1.05 a bushel?

\$ 1.05 = \$
$$1\frac{1}{20}$$
 = \$ $\frac{21}{20}$.

$$\frac{50}{1999} \qquad 7 \\
\frac{29999}{69} \times $ \frac{21}{29} = $350. Ans.$$

26. Reduce 5 rd. 4 yd. 2½ ft. to the decimal of a mile.

27. Reduce 9 sq. ch. 11.25 sq. rd. to the decimal of an acre.

28. Reduce 0.09375 bu. to quarts.

29. Reduce 7560 chains to miles.

30. How many gross are 2000 pens?

$$\frac{\cancel{5000}}{\cancel{5000}} = \frac{\cancel{125}}{\cancel{9}} = \cancel{138}. \quad Ans.$$

31. Find the cost of 27.248 A., at \$93.75 an acre.

32. Which is the greater, 2.8 of 3 ft. 11 in. or 3.11 of 2 ft. 8 in., and by how much?

3 ft. 11 in. = 47 in.;

2 ft. 8 in. = 32 in.
47 in. 32 in.

$$\frac{2.8}{376}$$
 $\frac{3.11}{32}$
 $\frac{94}{131.6}$ in. $\frac{96}{99.52}$ in.

131.6 in. -99.52 in. =32.08 in. =2 ft. 8.08 in.

Therefore, 2.8 of 3 ft. 11 in. is the greater by 2 ft. 8.08 in. Ans.

33. Reduce 171 lb. 6 oz. troy to the decimal of a ton avoirdupois.

171 lb. 6 oz. =
$$171\frac{1}{2}$$
 lb.

$$\frac{171\frac{1}{2} \times 5760}{7000} = \frac{\cancel{3\cancel{4}\cancel{3}}}{\cancel{\cancel{2}}} \times \frac{\cancel{\cancel{57\cancel{9}\cancel{9}}}}{\cancel{\cancel{7}\cancel{9}\cancel{9}\cancel{9}}} = 141.12.$$

34. Express 14.52 sq. yd. as the decimal of a square chain.

14.52 sq. yd. =
$$\frac{14.52}{30\frac{1}{4}}$$
 sq. rd.
= $\frac{14.52}{16 \times 30\frac{1}{4}}$ sq. ch.
= $\frac{14.52}{484}$ sq. ch.
= 0.03 sq. ch. Ans.

25. If a sovereign is equal to 25.22 francs, or to \$4.85, what decimal of a dollar is a franc?

36. If 0.327 of some work is done in 3 hr. 38 min., how long will the whole work require?

3 hr. 38 min. = 218 min.

218 min.
$$\neq 0.327 = \frac{1000}{327}$$
 of 218 min.
= $\frac{2000}{3}$ min. = 6663 min.

 $=\frac{1}{3}$ min. = 0004 min. = 11 hr. 6 min. 40 sec. Ans.

37. A can run a mile in 7.68 min.; B can run at the rate of 7.68 mi. an hour. Which is the faster runner?

Therefore, A is the faster runner.

38. How many miles an hour does a person walk who takes 2 steps a second and 1900 steps in mile?

$$\frac{6}{69 \times 69 \times 2} = \frac{72}{19} = 3\frac{11}{19}. \text{ Ans.}$$

$$\frac{190}{19}$$

39. If an ounce troy of gold is worth \$20, what is the value of a pound avoirdupois?

$$\frac{175}{7000} \times \$ 249 = \$ \frac{875}{3} = \$ 291.67.$$

$$\frac{144}{3}$$
Ans.

40. Two stars cross the meridian at 6 hr. 4 min. 42.3 sec. and 7 hr. 2 min. 57.21 sec., respectively. What is the interval between the observations?

hr.	min.	8eC.
7	2	57.21
6	4	42.3
	58	14.91

58 min. 14.91 sec. Ans.

41. How long will it take to fill \(\frac{12}{25}\) of a cistern, when the whole requires 6 hr. 10 min.?

42. The circumference of a circle is 6 yd. 1 ft. 5.1 in. What is the length of 55°?

$$\frac{55}{360} \text{ of } 233.1 = \frac{11}{\cancel{55}} \times \frac{259}{\cancel{2331}}$$

$$\frac{72}{8}$$

$$= \frac{2849}{80} = 35\frac{49}{80}.$$

 $35\frac{48}{85}$ in. = 2 ft. $11\frac{48}{85}$ in. Ans.

43. Multiply 2 t. 16 cwt. 633 lb. by 14.

t. cwt. lb.
2 16
$$63\frac{2}{5}$$

4

9 11 6 $53\frac{2}{5}$

1 5 $17\frac{1}{15}$

2 16 $63\frac{2}{5}$

4 1 $80\frac{7}{15}$

4 t. 1 cwt. $80\frac{7}{15}$ lb. Ans.

44. Into how many shares has £ 120 been divided when each share is £3 8s. 6\$ d.

$$6\frac{4}{9} d. = \frac{6\frac{9}{7}}{12} s. = \frac{4}{9} s.$$

$$8\frac{4}{9} s. = \cancel{2} \frac{8\frac{4}{7}}{20} = \cancel{2} \frac{4}{9} s.$$

$$\frac{120}{3\frac{3}{7}} = \frac{7}{2\cancel{4}} \times \cancel{120} = 35. \quad Ans.$$

45. If \(\frac{1}{6} \) of one line is equal to \(\frac{1}{6} \) of another line, which is the greater? What fraction of the greater is the less?

$$\frac{14}{15}$$
, $\frac{8}{9} = \frac{42, 40}{45}$.

... the second line is the greater.

Ans.

$$\frac{\frac{1}{8}}{\frac{1}{15}} = \frac{\frac{4}{8}}{\frac{8}{9}} \times \frac{\frac{5}{15}}{\frac{15}{14}} = \frac{20}{21} \cdot Ans.$$

46. Multiply 5 mi. 206 rd. 2 ft. 2 in. by 786.

4436 mi. 99 rd. 3 ft. 6 in. Ans.

47. The returns of a gold mine are 241 t. of ore yielding 2 oz. 1 dwt. 15 gr. of fine gold a ton, and 193 t. yielding 1 oz. 12 dwt. 9 gr. a ton. Find the value of the whole yield, at \$19.45 an ounce.

67 lb. 10 oz. = 814 oz.

48. Divide 93 long tons 56 lb. by 23 lb. 5 oz.

t.	lb.	lb.	02.	
93	56	23	5	
2240		16		
205576	•			
16				
3334016				
	.8938]44 Ans.			

49. Telegraph poles on railroads are generally erected at intervals of 88 yd. Show that if a passenger counts the number of poles which the train passes in three minutes, that number will express the number of miles an hour the train is going.

Since 1 mi. = 1760 yd., 88 yd. = $\frac{1}{20}$ of a mile, and there are 20 poles to the mile. Since 1 hr. = 60 min., 3 min. = $\frac{1}{20}$ of an hour. Hence, the number of poles passed by in 3 min. expresses the rate of the train in miles per hour.

50. If Greenwich time is 5 hr. 8 min. 16 sec. later than Washington time, and Chicago is 87° 35′ W., what is the difference between Washington time and Chicago time?

15 87°	357			
5 hr.	50 min.	20 sec.		
hr.	min.	sec.		
5	50	20		
5	8	16		
	42	4	42 min. 4 sec.	Ans.

51. What fraction of 21 cu. yd. 11 cu. ft. 1215 cu. in. is 3 cu. yd. 1 cu. ft. 1161 cu. in.?

cu. yd.	cu. ft.	cu. in.	cu. yd.	cu. ft.	cu. in.
21	11	1215	3	1	1161
27			27		
578			82		
1728			1728		
999999			142857	14285	$abla = \frac{1}{2}$. Ans.

52. How many minutes in the first three months of 1895? How many in the first three months of 1896?

Jan. 31 dy.Jan. 31 dy.Feb. 28Feb. 29Mar.
$$\frac{31}{90}$$
 dy.Mar. $\frac{31}{91}$ dy. $\frac{24}{60}$ $\frac{60}{1440}$ $\frac{90}{129600}$ $\frac{91}{1440}$ $\frac{12960}{131040}$

129,600 min.; 131,040 min. Ans.

53. A knot is $\frac{1}{60}$ of a degree, and a mile is 0.01477 of a degree. Find in miles the value of a knot to five decimals.

1 knot =
$$\frac{1}{60}^{\circ}$$
 = 0.01 $\dot{6}^{\circ}$.
1 mi. = 0.01477°.
1.12841
01477)01666.66666
1477
1896
1477
4196
2954
12426
11816
6106
5908
1986
1477
509

1.12841 mi. Ans.

54. The captain of a steamer, sailing from Liverpool, found on taking an observation that the sun crossed his meridian at 42 min. 5 sec. past one o'clock P.M. by Greenwich time. Find his longitude.

Time on the steamer was 1 hr. 42 min. 5 sec. later than Greenwich time.

55. If a walk 6 ft. wide is made round a park 600 ft. square within the enclosure, how many square yards will the walk contain?

600 ft. = 200 yd.; 6 ft. = 2 yd.

$$2(200 + 196) \times 2 = 1584$$
.
1584 sq. yd. *Ans*.

56. How many pickets 3 in. wide, placed 3 in. apart, will be required to fence a rectangular lot 231 ft. long and 99 ft. wide? What will they cost at \$3.25 per hundred?

Each picket occupies with its space 3 in. + 3 in. = 6 in. $= \frac{1}{2}$ ft.

Perimeter =
$$2 \times (231 + 99)$$
 ft. = 660 ft.

$$660 + \frac{1}{2} = 2 \times 660 = 1320. \ Ans.$$

$$\begin{array}{r} 3.25 \\ \underline{13.2} \\ 650 \\ \underline{975} \\ \underline{325} \\ 842.90 \ Ans. \end{array}$$

57. The length of a year is 365.242218 mean solar days. Express the length of a year in days, hours, minutes, and seconds.

365 dy. 5 hr. 48 min. 47.6352 sec. Ans.

58. The Flying Dutchman Express runs from London to Exeter, a distance of 1931 mi., in 41 hr., making one stop of 10 min., two of 5 min. each, and one of 3 min. What is its average speed per hour when in motion?

The time lost at stations = $1 \times 10 \text{ min.} + 2 \times 5 \text{ min.} + 1 \times 3 \text{ min.} = 23 \text{ min.}$

Actual running time = $4\frac{1}{4}$ hr. -23 min. = 4 hr. 15 min. -23 min. = 3 hr. 52 min.

59. The Scotch Express runs from London to Edinburgh, a distance of 393\frac{1}{2}\$ mi., in 9 hr., making one stop of 30 min., three of 5 min. each, and one of 3 min. What is its average speed per hour when in motion?

The time lost at stations = 1×30 min. $+ 3 \times 5$ min. $+ 1 \times 3$ min. = 48 min.

Actual running time = 9 hr. - 48 min. = 8 hr. 12 min. = $8\frac{1}{8}$ hr.

$$393\frac{3}{5} + 8\frac{1}{5} = \frac{1968}{5} \times \frac{5}{41} = 48.$$
 48 mi. Ans.

60. The Empire State Express runs from New York to Buffalo, a distance of 439 mi., in 8 hr. 15 min., making two stops of 3 min. each, and two stops of 2 min. each. What is its average speed per hour when in motion?

The time lost at stations = $2 \times 3 \text{ min.} + 2 \times 2 \text{ min.} = 10 \text{ min.}$ Actual running time= $8 \text{ hr. } 15 \text{ min.} -10 \text{ min.} = 8 \text{ hr. } 5 \text{ min.} = 8\frac{1}{12} \text{ hr.}$

$$439 + 8\frac{1}{12} = 439 \times \frac{13}{13} = \frac{5335}{13} = 54\frac{1}{13} = 54.31.$$

54.31 mi. Ans.

61. How many dollars worth 4s. 2d. each will pay a bill of £11 17s. 6d.?

s. d.
$$\pounds$$
 s. d. $2850 \div 50 = 57$.

4 2 11 17 6

20 237

12 2850

62. The lunar month is 29.53059 days. Express the length of a lunar month in days, hours, minutes, and seconds.

29 dy. 12 hr. 44 min. 2.976 sec. Ans.

Exercise 87. Page 179.

1. If 15 yards of silk cost \$18.75, what will be the cost of 201 yards?

If 15 yd. of silk cost \$18\frac{3}{4}\$, 1 yd. will cost $\frac{1}{15}$ of \$18\frac{3}{4}\$, and 20\frac{1}{3}\$ yd. will cost $20\frac{1}{8} \times \frac{1}{15} \times \$18\frac{3}{4}$.

$$20\frac{1}{3} \times \frac{1}{15} \times \$ 18\frac{3}{4} = \frac{61}{3} \times \frac{1}{15} \times \$ \frac{75}{4} = \$ \frac{305}{12} = \$ 25.42$$
. Ans.

2. If 3\frac{2}{3} pounds of tea cest \\$3.80, how many pounds can be bought for \\$21.89?

If $3\frac{2}{5}$ lb. of tea cost \$3\frac{4}{5}\$, 1 lb. costs \$\frac{3\frac{4}}{3\frac{2}{5}}\$, and as many pounds can be bought for \$21.89 as $21.89 \div \frac{3\frac{4}{5}}{3\frac{2}{5}}$.

\$21.89 ÷
$$\frac{34}{32}$$
 = $\frac{5}{19}$ × $\frac{17}{5}$ × \$ $\frac{2189}{100}$ = \$ $\frac{37213}{1900}$ = \$19.59. Ans.

3. If $\frac{8}{14}$ of a ton of coal costs \$1.12, what is the price of $5\frac{1}{4}$ cwt.?

$$5\frac{1}{2}$$
 cwt. $=\frac{5\frac{1}{2}}{20}$ t. $=\frac{11}{40}$ t.

If $\frac{3}{14}$ t. of coal costs \$1.12, 1 t. costs \$1.12 ÷ $\frac{3}{14}$ and $\frac{11}{10}$ t. costs $\frac{11}{10} \times (\$1.12 \div \frac{3}{14})$.

$$\frac{11}{40} \times \left(\$1.12 \div \frac{3}{14}\right) = \frac{11}{40} \times \frac{14}{3} \times \$1.12 = \$\frac{21.56}{15} = \$1.44. \text{ Ans.}$$

4. If $_{11}^{2}$ of a piece of work is done in 25 days, what fraction of the work will be done in 112 days?

If $\frac{2}{11}$ of the work is done in 25 dy., the fraction that can be done in $11\frac{2}{3}$ dy. is $\frac{11\frac{2}{3}}{25} \times \frac{2}{11}$.

$$\frac{11\frac{2}{3}}{25} \times \frac{2}{11} = \frac{35}{3} \times \frac{1}{25} \times \frac{2}{11} = \frac{14}{165}. \quad Ans.$$

5. A bankrupt's debts are \$2520, and the value of his property is \$1890. How much can he pay on a dollar?

He can pay on each dollar \$ \frac{1}{2} \frac{2}{2} \frac{2}{2} \frac{1}{2}.

$$\frac{1899}{2529} \text{ of } \$1.99 = \$0.75. Ans.}$$

6. If a bankrupt's debts are \$4264, and he pays 62½ cents on a dollar, what are his assets?

$$\$0.62\frac{1}{3} = \$\frac{1}{6}$$
. $\frac{5}{8}$ of $\$4264 = \2665 . Ans.

7. If an ounce of gold is worth \$20.67, what is the value of 0.04 of a pound?

0.04 lb. troy =
$$0.04$$
 of 12 oz. = 0.48 oz.

\$9.92. Ans.

8. A man spent § of his money for dry goods, 7 of the remainder for groceries, and had \$15 left. How much had he at first?

After spending $\frac{3}{6}$ of his money he had $\frac{5}{6}$ left. After spending $\frac{7}{6}$ of $\frac{5}{8}$ of his money he had left $\frac{2}{6}$ of $\frac{5}{8} = \frac{5}{36}$. Then, $\frac{5}{8} \cdot 15 = \frac{5}{36}$ of the money he had at first.

$$\$15 \div \frac{5}{36} = \frac{36}{5} \times \$15 = \$108$$
. Ans.

9. Sampson & Reed and ; it a not if wheat to one man, } of the remainder to another, and had shall manual left. How much had they at first?

After seiling $\frac{1}{4}$ if the wheat they had $\frac{1}{4}$ left. After seiling $\frac{1}{4}$ of $\frac{1}{4}$ they had left $\frac{1}{4}$ if $\frac{1}{4} = \frac{1}{12}$. Then, if $m_1 = \frac{1}{12}$ if the lot.

33
$$m_L - \frac{3}{32} = \frac{22}{3} < 23 m_L = 392 m_L$$
 Ana.

10. In a sertain school $\frac{1}{12}$ of the scholars are pris. * of the boys are over 16 years old, and 4 hove are under 16. How many girls and how many scholars are there in the school.

Since $\frac{1}{12}$ if the scholars are prist $\frac{1}{12}$ are boys. Since $\frac{1}{2}$ of the boys are over 16 yr. not $\frac{1}{12}$ if the boys are under 16; that is, $\frac{1}{2}$ of $\frac{1}{12} = \frac{1}{12}$ of the scholars.

Therefore, d is $\frac{1}{\sqrt{2}}$ if the number if scholars.

$$6 - \frac{3}{16} = \frac{16}{3} < \frac{2}{3} = 32$$

$$\frac{9}{16} < \frac{2}{32} = 18.$$

18 ; 32. **4ns.**

II. In a zertain school $\frac{17}{14}$ of the scholars are boys; $\frac{1}{12}$ of the girls are under 16, and 13 girls are over 16. How many boys and how many girls are there in the school?

Since $\frac{1}{14}$ of the scholars are boys, $\frac{1}{14}$ are girls. Since $\frac{3}{14}$ of the girls are under 16, $\frac{1}{14}$ of the girls are over 16, that is,

$$\frac{13}{22} \text{ if } \frac{11}{24} = \frac{13}{48} \text{ if the scholars.}$$

Therefore, 13 is 👯 of the number of scholars.

$$13 - \frac{13}{48} = \frac{48}{13} \times 13 = 48.$$

Hence, the number of boys is $\frac{13}{14}$ of 48 = 26. Ans.

Hence, the number of girls is $\frac{11}{24}$ of 48 = 22. Ans.

12. If from a certain number $\frac{1}{4}$ of it is subtracted, then $\frac{1}{3}$ of the remainder, then $\frac{1}{3}$ of that remainder, 6 still remains. What is the number?

After ‡ of the number is subtracted ‡ is left.

After $\frac{1}{3}$ of $\frac{1}{4}$ is subtracted $\frac{4}{3}$ of $\frac{1}{4} = \frac{1}{3}$ is left.

After $\frac{1}{2}$ of $\frac{1}{3}$ is subtracted $\frac{6}{3}$ of $\frac{1}{3} = \frac{6}{35}$ is left.

Therefore, the number =
$$6 + \frac{6}{35} = \frac{35}{\cancel{g}} \times \cancel{g} = 35$$
. Ans.

13. A ship's cargo sold for \$45,000 belongs to three partners. A owns $\frac{7}{4}$ of $\frac{3}{4}$ of it, B's share is equal to $3\frac{3}{14}$ of $\frac{3}{4}$ of A's share, and C owns the remainder. What does each receive from the sale?

$$\frac{7}{9}$$
 of $\frac{3}{5} = \frac{7}{15}$. $\frac{7}{15}$ of $\frac{3000}{45999} = 21,000$, A's. Ans.

$$3_{14}^{*}$$
 of $\frac{2}{9}$ of \$21,000 = $\frac{45}{14} \times \frac{2}{9} \times $21,000 = $15,000$, B's. Ans.

$$$45,000 - $21,000 - $15,000 = $9000$$
, C's. Ans.

14. A man bequeathed $\frac{5}{12}$ of his property to A, $\frac{1}{4}$ of it to B, $\frac{1}{6}$ to C, $\frac{1}{4}$ to D, and the remainder, \$550, to E. What was the value of his whole property?

$$\frac{5}{12} + \frac{1}{4} + \frac{1}{6} + \frac{1}{8} = \frac{10 + 6 + 4 + 3}{24} = \frac{23}{24}$$

Therefore, \$550 is $\frac{1}{24}$ of the property.

$$$550 \div \frac{1}{14} = 24 \times $550 = $13,200$$
. Ans.

15. A farmer raised 321 bu. 3 pk. of corn from 9 acres of land. At the same rate, what would be the yield from 25 acres?

321 bu. 3 pk. =
$$321\frac{3}{4}$$
 bu.

If 9 A. yield $321\frac{3}{4}$ bu., 1 A. will yield $\frac{1}{3}$ of $321\frac{3}{4}$ bu., and 25 A. will yield $25 \times \frac{1}{3} \times 321\frac{3}{4}$ bu.

$$25 \times \frac{1}{9} \times 321\frac{3}{4}$$
 bu. = $25 \times \frac{1}{9} \times \frac{1287}{4}$ bu. = $\frac{3575}{4}$ bu. = $893\frac{3}{4}$ bu. Ans.

16. If 7 horses eat 21 bushels of oats in 16 days, how many days will 99 bu. 3 pk. last them?

99 bu.
$$3 \text{ pk.} = 99\frac{3}{4} \text{ bu.}$$

If 21 bu. of oats last 16 days, 99\frac{3}{4} bu. will last $\frac{99\frac{3}{4}}{21} \times 16$ days.

$$\frac{99\frac{8}{4}}{21} \times 16 \text{ days} = \frac{\frac{19}{399}}{\frac{84}{4}} \times \frac{4}{19} \text{ days} = 76 \text{ days. } Ans.$$

17. If 12 horses can plow 96 acres in 6 days, how many horses will plow 64 acres in 8 days?

In 6 days 96 acres can be plowed by 12 horses.

In 1 day 96 acres can be plowed by 6×12 horses.

In 1 day 1 acre can be plowed by $\frac{6 \times 12}{96}$ horses.

In 8 days 1 acre can be plowed by $\frac{6 \times 12}{8 \times 96}$ horses.

In 8 days 64 acres can be plowed by $\frac{64 \times 6 \times 12}{8 \times 96}$ horses.

$$\frac{\cancel{64} \times \cancel{6} \times \cancel{12}}{\cancel{8} \times \cancel{96}} = 6. \text{ Ans.}$$

18. If 40 acres of grass is moved by 8 men in 7 days, how many acres will be moved by 24 men in 28 days?

24 men will mow three times as much as 8 men in the same time; the same number of men will mow four times as much in 28 days as in 7 days. Hence, 24 men in 28 days will mow 3×4 or 12 times as much as 8 men in 7 days.

$$12 \times 40 \text{ A.} = 480 \text{ A.}$$
 Ans.

19. How many bushels of wheat will serve 72 people 8 days when 4 bushels serve 6 people 24 days?

72 people require 12 times as much wheat as 6 people for the same time; the same number of people require \(\frac{1}{4} \) as much wheat for 8 days as for 24 days. Hence for 8 days 72 people require

$$\frac{4}{12} \times \frac{1}{3} \times 4$$
 bu. = 10 bu. Ans.

20. If 2 horses eat 8 bushels of oats in 16 days, how many horses will eat 3000 bushels in 24 days?

In 16 dy. 8 bu. will be eaten by 2 horses.

In 1 dy. 8 bu. will be eaten by 16×2 horses.

In 1 dy. 1 bu. will be eaten by $\frac{16 \times 2}{8}$ horses.

In 24 dy. 1 bu. will be eaten by $\frac{16 \times 2}{24 \times 8}$ horses.

In 24 dy. 3000 bu, will be eaten by $\frac{3000 \times 16 \times 2}{24 \times 8}$ horses.

$$\frac{125}{8999} \times 19 \times 2 = 500. Ans.$$

21. If a man travels 150 miles in 5 days of 12 hours, in how many days of 10 hours will he travel 500 miles?

In 1 day of 12 hr. he travels 150 mi.

In 1 day of 10 hr. he travels $\frac{10}{12} \times \frac{150}{2}$ mi.

Hence, to travel 500 mi., the number of days he will require is

$$500 \div (\frac{14}{14} \times \frac{14}{3}).$$

$$500 + (\frac{19}{12} \times \frac{150}{3}) = 500 \times \frac{4}{10} \times \frac{5}{150} = 20. \text{ Ans.}$$

22. If 939 soldiers consume 351 bu. of wheat in 21 days, how many soldiers will consume 1404 bu. in 7 days?

1404 bu. will last the same number of men 4 times as long as 351 bu.; the same number of bushels will last three times the number of men for 7 days as for 21 days. Hence, 1404 bu. will last 3×4 times the number of men for 7 days that 351 bu. will last 939 men for 21 days.

$$3 \times 4 \times 939 = 11,268$$
. Ans.

23. If 5 men, working 16 hours a day, can reap a field of 12½ acres in 3½ days, in how many days can 7 men, working 12 hours a day, reap a field of 15 acres?

5 meń can reap 121 A. in 31 days of 16 hr. = 56 hr.

1 man can reap 121 A. in 5×56 hr.

1 man can reap 1 A, in $\frac{5 \times 56}{12\frac{1}{4}}$ hr.

1 man can reap 15 A. in $\frac{15 \times 5 \times 56}{12\frac{1}{2}}$ hr.

7 men can reap 15 A. in $\frac{15 \times 5 \times 56}{7 \times 121}$ hr.

7 men can reap 15 A. in $\frac{15 \times 5 \times 56}{12 \times 7 \times 12\frac{1}{4}}$ days of 12 hr.

$$\frac{15 \times 5 \times 56}{12 \times 7 \times 12\frac{1}{4}} = \frac{\cancel{15} \times \cancel{5} \times \cancel{56} \times 2}{\cancel{12} \times \cancel{7} \times \cancel{25}} = 4. \text{ Ans.}$$

- 24. If 7 men in 8 days of 11 hours mow 22 acres, in how many days of 10 hours will 12 men mow 360 acres?
 - \sim 7 men can mow 22 A. in 8 days of 11 hr. = 88 hr.

1 man can mow 22 A. in 7×88 hr.

1 man can mow 1 A. in $\frac{7 \times 88}{22}$ hr.

12 men can mow 1 A. in $\frac{7 \times 88}{12 \times 22}$ hr.

12 men can mow 360 A. in $\frac{360 \times 7 \times 88}{12 \times 22}$ hr.

12 men can mow 360 A. in $\frac{360 \times 7 \times 88}{10 \times 12 \times 22}$ days of 10 hr.

$$\frac{3}{36} \frac{4}{360 \times 7 \times 88} = 84. Ans.$$

$$\frac{10 \times 12 \times 22}{10 \times 12 \times 22} = 84. Ans.$$

25. If 44 cannon, firing 30 rounds an hour for 3 hours a day, use 300 barrels of powder in 5 days, how many days will 400 barrels last 66 cannon, firing 40 rounds an hour for 5 hours a day?

TEACHERS' EDITION.

- 44 cannon firing 30 rounds for 3 hr. consume 300 bbl. in 5 days.
- 44 cannon firing 30 rounds for 1 hr. consume 300 bbl. in 3×5 days.
- 44 cannon firing 1 round for 1 hr. consume 300 bbl. in $30 \times 3 \times 5$ days.
 - 1 cannon firing 1 round for 1 hr. consumes 300 bbl. in $44 \times 30 \times 3 \times 5$ days.
- 1 cannon firing 1 round for 1 hr. consumes

 1 bbl. in $\frac{44 \times 30 \times 3 \times 5}{300}$ days.
- 66 cannon firing 1 round for 1 hr. consume 1 bbl. in $\frac{44 \times 30 \times 3 \times 5}{300 \times 66}$ days.
 - 66 cannon firing 40 rounds for 1 hr. consume 1 bbl. in $\frac{44 \times 30 \times 3 \times 5}{40 \times 300 \times 66}$ days.
 - 66 cannon firing 40 rounds for 5 hr. consume 1 bbl. in $\frac{44 \times 30 \times 3 \times 5}{5 \times 40 \times 300 \times 66}$ days.
 - 66 cannon firing 40 rounds for 5 hr. consume

 400 bbl. in $\frac{400 \times 44 \times 30 \times 3 \times 5}{5 \times 40 \times 300 \times 66}$ days.

$$\frac{10}{490 \times 44 \times 30 \times 3 \times 5} = 2. \text{ Ans.}$$

$$\frac{5 \times 40 \times 300 \times 50}{10} = 22$$

Exercise 88. Page 182.

1. Find the area of a floor 16 ft. 3 in. long and 12 ft. 6 in. wide.

16 ft. 3 in. =
$$16\frac{1}{4}$$
 ft.; 12 ft. 6 in. = $12\frac{1}{2}$ ft.

$$16\frac{1}{4} \times 12\frac{1}{4} = \frac{65}{4} \times \frac{25}{2} = \frac{1625}{8} = 203\frac{1}{8}$$
. 203\frac{1}{8} sq. ft. Ans.

2. A rectangle contains 672 sq. ft. 108 sq. in., and is 19 ft. 6 in. wide. Find its length.

672 sq. ft. 108 sq. in. = 672 $\frac{3}{4}$ sq. ft.; 19 ft. 6 in. = 19 $\frac{1}{4}$ ft.

$$672\frac{3}{4} + 19\frac{1}{4} = \frac{2}{39} \times \frac{2691}{4} = \frac{69}{2} = 34\frac{1}{4}$$
. $34\frac{1}{4}$ ft. Ans.

3. What length of board 15 in. wide will contain 11 sq. ft. 36 sq. in. ? 11 sq. ft. 36 sq. in. = 11 $\frac{1}{2}$ sq. ft.; 15 in. = 1 $\frac{1}{2}$ ft.

$$11\frac{1}{4} + 1\frac{1}{4} = \frac{4}{5} \times \frac{43}{4} = 9.$$
 Oft. Ans.

4. What length of road 44 ft. wide will contain an acre?

$$1 \text{ A.} = 43,560 \text{ sq. ft.}$$

 $43,560 \div 44 = 990.$ 990 ft. = 60 rd. Ans.

5. Find the area of a rectangular field 13.12 chains long, 10.35 chains broad.

$$\begin{array}{r}
13.12 \\
\underline{10.35} \\
6560 \\
3936 \\
\underline{1312} \\
135.7920
\end{array}$$

135.792 sq. ch. = 13 A. 5.792 sq. ch. Ans.

- 6. A path 216 ft. long measures 72 sq. yd. Find its breadth. 216 ft. = 72 yd. $72 \div 72 = 1$. 1 yd. Ans.
- 7. A rectangular field of 21.66 A. is 250.8 yd. broad. Find its length. 1 A. = 4840 sq. yd.

418 yd. Ans.

8. What is the area of a table, if its length and breadth are 4 ft. 33 in. and 2 ft. 93 in., respectively?

4 ft. 3\$ in. = 4\$ ft.; 2 ft. 9\$ in. = 2\$ ft.

$$\frac{6}{4} \times 2$ = \frac{30}{7} \times \frac{14}{3} = 12.$$
12 sq. ft. Ans.

9. From each corner of a square, each side of which is 2 ft. 5 in. long, a square measuring 5 in. on a side is cut out. Find the area of the remainder of the figure.

2 ft. 5 in. =
$$2\frac{5}{12}$$
 ft. $2\frac{5}{12} \times 2\frac{5}{12} = \frac{29}{12} \times \frac{29}{12} = \frac{541}{12} = 5\frac{21}{12}$. $5\frac{121}{12}$ sq. ft. = 5 sq. ft. 121 sq. in. $5 \times 5 = 25$. 4×25 sq. in. = 100 sq. in. $5 \times 5 = 25$. $5 \times 5 \times 5 = 25$.

10. The length and breadth of a map are 4½ ft. and 3½ ft. respectively. If the map represents 77,760 sq. mi. of country, how many square miles are there to a square inch?

$$4\frac{1}{2}$$
 ft. = 54 in.; $3\frac{1}{2}$ ft. = 40 in.

$$\frac{36}{40} \frac{36}{2160} \frac{2169)7776}{648} \frac{648}{1296} \frac{1296}{1296} \frac{36 \text{ sq. mi. } Ans.}$$

11. In rolling a grass plot that is 24 yd. long, and contains 400 sq. yd., how many times must a roller 3 ft. 4 in. wide be drawn over it lengthwise that the whole plot may be rolled?

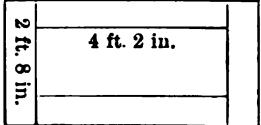
$$400 \div 24 = 16\frac{2}{3}$$
. 3 ft. 4 in. = $3\frac{1}{3}$ ft. = $1\frac{1}{3}$ yd.
$$16\frac{2}{3} \div 1\frac{1}{3} = \frac{50}{3} \times \frac{3}{10} = 15$$
. Ans.

12. How many sods, each 2 ft. 31 in. long and 81 in. broad, will be required to turf an acre of ground?

2 ft.
$$3\frac{1}{2}$$
 in. $= 2\frac{7}{24}$ ft.; $8\frac{1}{4}$ in. $= \frac{11}{16}$ ft. 1 A. $= 43,560$ sq. ft.
$$\frac{72}{3960} = \frac{3960}{232 \times 11} = 43360 \times \frac{24}{35} \times \frac{16}{11} = 27,648.$$
 Ans.

13. Find the area of a picture frame 2½ in. broad, if the outside measurement is 4 ft. 6½ in. in length and 2 ft. 8 in. in width.

$$2 \times 2\frac{1}{4}$$
 in. $= 4\frac{1}{4}$ in. $= 4$ ft. 2 in. $= 6$ ft. $= 10$ in. $= 13\frac{1}{4}$ ft. $= 13\frac{1$



$$13\frac{2}{3} \times \frac{3}{16} = \frac{41}{3} \times \frac{3}{16} = \frac{41}{16} = 2\frac{9}{16}$$
. $2\frac{9}{16}$ sq. ft. = 2 sq. ft. 81 sq. in. Ans.

14. Find the expense of glazing four windows, each containing 12 panes, if the panes are each 1 ft. long and 10 in. wide, and the price of the glass is 38 cents per square foot.

10 in. =
$$\frac{3}{6}$$
 ft. $4 \times 12 \times 1 \times \frac{5}{6} \times \$0.38 = \$15.20$. Ans.

15. A field 76 yd. long and 56 yd. broad, enclosed by a wall, has a border 4 ft. wide within the wall, and within this a path 5 ft. wide. If the remainder of the field is grass, find the area of the border, of the path, and of the grass.

4 ft. =
$$1\frac{1}{3}$$
 yd. $2 \times 1\frac{1}{3}$ yd. $= 2\frac{2}{3}$ yd. $2 \times (76 \text{ yd.} + 53\frac{1}{3} \text{ yd.}) = 258\frac{2}{3}$ yd. $2 \times (76 \text{ yd.} + 53\frac{1}{3} \text{ yd.}) = 258\frac{2}{3}$ yd. $258\frac{2}{3} \times 1\frac{1}{3} = \frac{776}{2} \times \frac{4}{2} = \frac{3104}{2} = 344\frac{2}{3}$.

Area of border = 344 sq. yd. Ans.

5 ft. =
$$1\frac{2}{3}$$
 yd.
2 × 3 yd. = 6 yd.
2 × $(70 \text{ yd.} + 53\frac{1}{3} \text{ yd.}) = 246\frac{2}{3}$ yd.
2 × $(70 \text{ yd.} + 53\frac{1}{3} \text{ yd.}) = 246\frac{2}{3}$ yd.
246 $\frac{2}{3}$ × $1\frac{2}{3}$ = $\frac{740}{3}$ × $\frac{5}{3}$ = $\frac{3700}{9}$ = 411 $\frac{1}{3}$.

Area of path = $411\frac{1}{9}$ sq. yd. Ans.

Field is 70 yd. long and 50 yd. wide.

Area of field = (70×50) sq. yd. = 3500 sq. yd. Ans.

16. A square plot of land 127 yd. long has a path 1 yd. wide running round the inside of it. Find the cost of graveling this path at 15 cents per square yard.

127 yd.
$$-(2 \times 1 \text{ yd.}) = 125 \text{ yd.}$$
 $2 \times (127 \text{ yd.} + 125 \text{ yd.}) = 504 \text{ yd.}$
 $(504 \times 1) \text{ sq. yd.} = 504 \text{ sq. yd.}$
 $504 \times 75.60 \text{ Ans.}$

17. A street \(\frac{1}{4} \) of a mile long has on each side a sidewalk $7\frac{1}{4}$ ft. wide. What will it cost to pave the sidewalks with stones, each measuring 2 ft. 9 in. by 1 ft. 8 in., if the stones are worth 75 cents each?

$$\frac{3}{4}$$
 mi. $=\frac{3}{4} \times 3280$ ft. = 3960 ft. $\frac{2 \times 7\frac{1}{2} \text{ ft.}}{3960} = \frac{15}{19800} = \frac{15}{59400}$

2 ft. 9 in. = $2\frac{3}{4}$ ft.; 1 ft. 8 in. = $1\frac{3}{4}$ ft.

$$2\frac{3}{4} \times 1\frac{3}{3} = \frac{11}{4} \times \frac{5}{3} = \frac{55}{12}.$$

$$59400 \div \frac{55}{12} = \frac{12}{55} \times \frac{1080}{59499} = 12,960.$$

$$12,960 \times \$0.75 = \frac{3240}{12999} \times \$\frac{3}{4} = \$9720. Ans.$$

18. How many planks 11 ft. by 9 in. are needed to cover a platform 27 ft. 6 in. long and 8 yd. wide? What will be the cost at 20 cents a square foot?

9 in. =
$$\frac{3}{4}$$
 ft.; 8 yd. = 24 ft.; 27 ft. 6 in. = $27\frac{1}{4}$ ft.

$$\frac{27\frac{1}{4} \times 24}{11 \times \frac{3}{4}} = \frac{55}{2} \times \cancel{24} \times \cancel{1}{\cancel{11}} \times \cancel{\frac{4}{3}} = 80. \text{ Ans.}$$

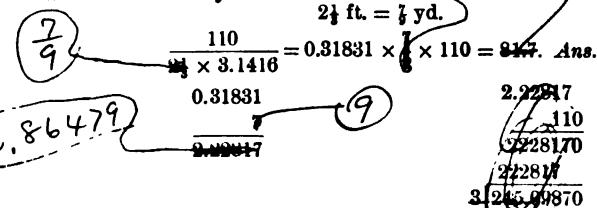
$$\frac{4}{\cancel{20}} \times \cancel{11} \times \cancel{\frac{3}{4}} \times \cancel{3} = \cancel{3} \times \cancel{132}. \text{ Ans.}$$

19. How many tiles 9 in. long and 4 in. wide will be required to pave a walk 8 ft. wide that surrounds a rectangular court 60 ft. long and 36 ft. wide?

86 ft.
$$+ (2 \times 8 \text{ ft.}) = 52 \text{ ft.}$$
 $2 \times (60 \text{ ft.} + 52 \text{ ft.}) = 224 \text{ ft.}$ $(8 \times 224) \text{ sq. ft.} = 1792 \text{ sq. ft.}$ $9 \text{ in.} = \frac{3}{4} \text{ ft.}$; $4 \text{ in.} = \frac{1}{3} \text{ ft.}$ $\frac{3}{4} \times \frac{1}{3} = \frac{1}{4}$ $1792 \div \frac{1}{4} = 4 \times 1792 = 7168$. Ans.

45. ADVANCED ARITHMETIC.

20. How many times will a wheel 21 ft. in diameter/turn in going a distance of 110 yards?



21. What distance will a wheel $\frac{5}{11}$ yd. in diameter pass over in making 4½ revolutions?

$$\begin{array}{c}
0.1428 \\
9.2856 \\
4\frac{1}{4} \times 3.1416 \times \frac{5}{11} \text{ yd.} = \frac{9}{2} \times \cancel{3.1416} \times \frac{5}{11} \text{ yd.} = 6.426 \text{ yd.} \text{ Ans.}
\end{array}$$

22. Find the diameter of a wheel that makes 9 revolutions in going 7½ yards.

$$7\frac{1}{5}$$
 yd. $\div 9 = \frac{1}{9} \times \frac{36}{5}$ yd. $= \frac{4}{5}$ yd.
0.31831 $\times \frac{4}{5}$ yd. $= \frac{1.27324}{5}$ yd. $= 0.25465$ yd. $= 9.1674$ in. *Ans.*

23. If the circumference of a wheel is 3/2 of 1 yd. 11/2 ft., how many times will the wheel turn in going 34 miles?

$$\frac{3\frac{3}{7} \times 5280}{\frac{3}{7} \times 4\frac{1}{7}} = \frac{8}{7} \times \frac{240}{5280} \times \frac{7}{22} \times \frac{8}{33} = \frac{15360}{11} = 1396\frac{4}{11}. Ans.$$

24. If the wheel of a locomotive is 31 times 5.52 ft. in circumference, how many times does it turn in a minute when the locomotive is running at the rate of 13.34 mi. an hour?

13.34 mi. an hour =
$$\frac{13.34 \times 5280}{60}$$
 ft. a minute.

$$\frac{13.34 \times 5280}{60} \div (3) \times 5.52) = \frac{29}{1834} \times \frac{240}{5280} \times \frac{7}{22} \times \frac{100}{532} = \frac{203}{3} = 673. \text{ Ans.}$$

25. Find the area of a circle that has a radius of 3 feet.

$$3.1416 \times (3 \times 3)$$
 sq. ft. = 28.2744 sq. ft. Ans.

3.1416 3 9 - 28.2744

26. What is the area of a circular field that has a radius of 400 yards?

 $8.1416 \times (400 \times 400)$ sq. yd. = 502,656 sq. yd. Ans.

27. The radius of the rotunda of the Pantheon at Rome is 71 ft. 6 in. Find the area of the floor.

$$3.1416 \times 71\frac{1}{2} \times 71\frac{1}{2} = 16,060.6446.$$

3.1416	224.6244
71.5	71.5
157080	11231220
31416	2246244
219912	15723708
224.62440	16060.64460

16,060.6446 sq. ft. Ans.

28. The diameter of a cylindrical cistern is 13 ft. What is the area of the bottom?

$$0.7854 \times (13 \times 13)$$
 sq. ft. = 132.7326 sq. ft. Ans.

13	0.7854
13	169
39	70686
13	47124
169	7854
	132.7326

29. The two dials of the clock of St. Paul's, London, are each 18, ft. in diameter. What is the area of each in square feet?

$$0.7854 \times (18) \times 18$$
) sq. ft. = 258.5248 sq. ft. Ans. 0.1122 $9.7854 \times \frac{127}{7} \times \frac{127}{7} = \frac{1809.6738}{7} = 258.5248$.

30. At 20 cents a square yard, what will it cost to gravel a walk 6 ft. wide running round a circular fish pond 70 yd. in diameter?

Area of pond = $0.7854 \times (70 \times 70)$ sq. yd. = 3848.46 sq. yd.

Area of pond and walk = $0.7854 \times (74 \times 74)$ sq. yd. = 4300.8504 sq. yd.

4300.85 sq. yd. - 3848.46 sq. yd. = 452.39 sq. yd., area of walk.

$$452.39 \times \$0.20 = \$90.48$$
. Ans.

31. How many square inches on the surface of a ball 3 inches in diameter?

$$3.1416 \times 3 \times 3 = 28.2744$$
. 28.2744 sq. in. Ans.

32. How many square inches of surface on a spherical blackboard 12 inches in diameter?

$$3.1416 \times 12 \times 12 = 452.3904.$$

$$3.1416$$

$$144$$

$$125664$$

$$125664$$

$$31416$$

452.3904 sq. in. Ans.

33. What is the interior surface of a hemispherical vase whose interior diameter is 20 inches?

452,3904

$$\frac{1}{4} \times 3.1416 \times (20 \times 20)$$
 sq. in. = 628.32 sq. in. = 4 sq. ft. 52.32 sq. in. Ans.

34. Find the external and the internal surface of a spherical shell whose external and internal diameters are 8 in. and 5 in., respectively.

$$3.1416 \times (8 \times 8)$$
 sq. in. = 201.0624 sq. in. Ans.

$$3.1416 \times (5 \times 5)$$
 sq. in. = 78.54 sq. in. Ans.

3.1416	3.1416
64	25
125664	157080
188496	62832
201.0624	78.5400

35. How many square feet of tin are required to make 16 hemispherical bowls, each 2 ft. 4 in. in diameter?

$$2 \text{ ft. 4 in.} = 2\frac{1}{4} \text{ ft.}$$

 $16 \times \frac{1}{4} \times 3.1416 \times (2\frac{1}{4} \times 2\frac{1}{4})$ sq. ft. = 136.8341 sq. ft. Ans.

36. Find the lateral surface of a right cylinder if its height is 10 in. and the radius of its base is 7 in.

$$(10 \times 2 \times 3.1416 \times 7)$$
 sq. in. = 439.824 sq. in. Ans.

37. Find the lateral surface of a right cylinder if its height is 12 ft. and the diameter of its base is 9 ft. 4 in.

9 ft. 4 in.
$$= 9\frac{1}{4}$$
 ft.

 $(12 \times 3.1416 \times 9\frac{1}{2})$ sq. ft. = 351.8592 sq. ft. Ans.

12	3.1416
91	112
112	62832
	31416
	31416
	351 8592

38. At 32 cents a square foot, what is the cost of cementing a cylindrical cistern 20 ft. deep and 18 ft. in diameter?

Lateral area = $(20 \times 3.1416 \times 18)$ sq. ft. = 1130.976 sq. ft.

Area of bottom = $3.1416 \times (9 \times 9)$ sq. ft. = 254.4696 sq. ft.

3.1416	3.1416
360	81
1884960	31416
94248	251328
1130.9760	254.4698
1130.976 sq. ft.	1385.4456
254.4696	0.32
1385.4456 sq. ft.	27708912
	41563368
	443.342592

\$ 443.34. Ans.

39. The diameters of two right cylinders of the same height are as 6 to 1. Compare the lateral surfaces.

$$\frac{\text{Lateral area of larger}}{\text{Lateral area of smaller}} = \frac{\text{height} \times 3.1416 \times 6}{\text{height} \times 3.1416 \times 1} = \frac{6}{1}.$$

That is, the lateral areas are as 6 to 1.

Exercise 89. Page 186.

1. How many yards of carpeting 27 in. wide will be required for a floor 26 ft. long, 15\frac{1}{4} ft. wide, if the strips run lengthwise? How many if the strips run across the room? How much will be turned under in each case?

27 in. = 21 ft.
$$15\frac{3}{4} + 2\frac{1}{4} = \frac{4}{9} \times \frac{63}{4} = 7.$$

Hence 7 strips will be required.

7 × 26 ft. = 182 ft. =
$$60\frac{2}{3}$$
 yd. Ans.
26 ÷ $2\frac{1}{4} = \frac{4}{9} \times 26 = \frac{104}{9} = 11\frac{5}{3}$.

Hence 12 strips will be required.

$$12 \times 15\frac{3}{4}$$
 ft. = $12 \times 5\frac{1}{4}$ yd. = 63 yd. Ans.

In the first case nothing will be turned under; in the second a strip of 86 in. = 16 in. wide.

TEACHERS' EDITION.

2. How many yards of carpeting $\frac{7}{4}$ yd. wide will be required for a room $8\frac{1}{4}$ yd. by 17 ft., if the strips run lengthwise, and if there is a waste of $\frac{1}{16}$ yd. a strip?

17 ft. = 5
$$\frac{3}{8}$$
 yd. $5\frac{3}{8} + \frac{7}{8} = \frac{8}{7} \times \frac{17}{3} = \frac{136}{21} = 6\frac{19}{21}$.

Hence 7 strips will be required.

$$8\frac{1}{2}$$
 yd. $+\frac{1}{16}$ yd. $= 8\frac{9}{16}$ yd. $= 59\frac{1}{16}$ yd. $= 59\frac{1}{16}$ yd. Ans.

3. How many square yards of oilcloth will be required for a hall floor 51 yd. long and 10 ft. wide?

10 ft. =
$$3\frac{1}{4}$$
 yd.
$$5\frac{1}{4} \times 3\frac{1}{3} = \frac{7}{21} \times \frac{5}{2} = \frac{35}{2} = 17\frac{1}{2}.$$
2 17\frac{1}{2} sq. yd. Ans.

4. At \$0.92 a yard, what is the cost of a carpet 27 in. wide for a room 281 ft. by 181 ft., if the strips run lengthwise?

27 in. = 2½ ft.; 28½ ft. = 9½ yd.
$$18\frac{3}{4} \div 2\frac{1}{4} = \frac{25}{4} \times \frac{4}{9} = \frac{25}{3} = 8\frac{1}{3}.$$
 Hence, 9 strips will be required.

$$9 \times 9\frac{1}{2} \text{ yd.} = 85\frac{1}{2} \text{ yd.}$$

$$\begin{array}{r} \$0.92 \\ \hline 85\frac{1}{2} \\ \hline 46 \\ \hline 460 \\ \hline \hline 736 \\ \hline \$78.66 \text{ Ans.} \end{array}$$

5. Find the cost of carpet 30 in. wide, at \$1.25 per yard, for a room 18 ft. by 14 ft., if the strips run lengthwise.

30 in. =
$$2\frac{1}{5}$$
 ft.; 18 ft. = 6 yd. $14 \div 2\frac{1}{2} = \frac{2}{5} \times 14 = \frac{28}{5} = 5\frac{1}{5}$.

Hence, 6 strips will be required.

$$\frac{3}{9} \times \frac{3}{9} \times \frac{5}{4} = \$45$$
. Ans.

Find the cost of carpeting 27 in. wide, at \$1.121 per yard, for a room 29 ft. 9 in. by 23 ft. 6 in., if the strips run across the room.

27 in. =
$$2\frac{1}{4}$$
 ft.; 29 ft. 9 in. = $29\frac{1}{4}$ ft.; 23 ft. 6 in. = $7\frac{1}{6}$ yd.

$$20\frac{1}{4} \div 2\frac{1}{4} = \frac{119}{4} \times \frac{4}{9} = \frac{119}{9} = 13\frac{1}{4}.$$

Hence, 14 strips will be required.

$$14 \times 7\frac{1}{2} \times 81\frac{1}{1} = 14 \times \frac{47}{6} \times \frac{9}{8} = 8\frac{987}{8} = 8123.38. \text{ Ans.}$$

7. Find the cost of carpeting 27 in. wide, at \$2.75 per yard, for a room 34 ft. 8 in. by 13 ft. 3 in., if the strips run lengthwise, and if there is a waste of 1 yd. a strip.

27 in. =
$$2\frac{1}{4}$$
 ft.; 13 ft. 3 in. = $13\frac{1}{4}$ ft. $13\frac{1}{4} \div 2\frac{1}{4} = \frac{53}{4} \times \frac{4}{9} = \frac{53}{9} = 5\frac{1}{9}$.

$$13\frac{1}{4} \div 2\frac{1}{4} = \frac{53}{4} \times \frac{4}{9} = \frac{53}{9} = 5\frac{4}{9}.$$

Hence, 6 strips will be required.

34 ft. 8 in. =
$$11\frac{1}{2}$$
 yd.

$$11\frac{5}{9}$$
 yd. $+\frac{7}{4}$ yd. $=11\frac{7}{3}\frac{5}{4}$ yd.

$$6 \times 11\frac{23}{36} \times \$2\frac{3}{4} = 6 \times \frac{425}{36} + \frac{11}{4} = \$\frac{4675}{24} = \$194.79$$
. Ans.

8. Which way must the strips of carpet 27 in. wide run to carpet most economically a room 201 ft. by 191 ft.?

27 in. =
$$2\frac{1}{4}$$
 ft. $20\frac{1}{4} \div 2\frac{1}{4} = \frac{41}{2} \times \frac{4}{9} = \frac{82}{9} = 9\frac{1}{4}$.

Hence, if the strips run across the room, 10 strips will be required.

$$10 \times 19\frac{1}{2}$$
 ft. = 195 ft. = 65 yd. $19\frac{1}{2} \div 2\frac{1}{4} = \frac{13}{\cancel{2}} \times \frac{\cancel{2}}{\cancel{2}} = \frac{26}{\cancel{3}} = 8\frac{1}{\cancel{3}}$.

Hence, if the strips run lengthwise, 9 strips will be required.

$$9 \times 20\frac{1}{2}$$
 ft. = $184\frac{1}{2}$ ft. = $61\frac{1}{2}$ yd.

Hence, it takes 3½ yd. less if the strips run lengthwise.

9. How many double rolls of paper will be required for a room of ordinary height, 15 ft. long and 12 ft. wide, if the room has one door and three windows, each 3½ ft. wide?

> Perimeter of room = $2 \times (15 + 12)$ ft. = 54 ft. Width of door and windows = $4 \times 3\frac{1}{4}$ ft. = 14 ft.

> =40 ft. Perimeter less door and windows

40 + 7 = 54. Hence, 6 double rolls will be required.

10. At \$2.25 a double roll, put on, what is the cost of papering a room of ordinary height, 16 ft. by 14 ft., if the room has two doors each 4 ft. wide, and four windows each 3 ft. 6 in. wide?

Perimeter of room = $2 \times (16 + 14)$ ft. = 60 ft. Width of doors and windows

 $= 2 \times 4$ ft. $+ 4 \times 3\frac{1}{2}$ ft. = 8 ft. + 14 ft. $= \frac{22}{38}$ ft. Perimeter less doors and windows $= \frac{38}{38}$ ft.

 $38 \div 7 = 5$. Hence, 6 double rolls will be required.

 $6 \times \$2.25 = \13.50 . Ans.

11. At 75 cents a single roll, put on, what is the cost of papering a room of ordinary height, 20 ft. 6 in. long and 17 ft. 4 in. wide, if the room has two doors each 3 ft. 6 in. wide, and five windows each 3 ft. 3 in. wide?

Perimeter of room = $2 \times (20\frac{1}{2} + 17\frac{1}{8})$ ft. = $75\frac{2}{3}$ ft. Width of doors and windows

 $=2 \times 3\frac{1}{2}$ ft. $+5 \times 3\frac{1}{4}$ ft. =7 ft. $+16\frac{1}{4}$ ft. $=23\frac{1}{4}$ ft. Perimeter less doors and windows $=\overline{52\frac{5}{12}}$ ft.

$$52\frac{5}{12} \div 3\frac{1}{2} = \frac{2}{7} \times \frac{629}{12} = \frac{629}{42} = 14\frac{1}{42}.$$

Hence, 15 single rolls will be required. $15 \times \$0.75 = \11.25 . Ans.

12. What is the cost of the border for the room of Ex. 11 at \$0.45 a running yard?

Perimeter of room = $75\frac{2}{3}$ ft. = $25\frac{2}{3}$ yd.

13. At \$1.75 a double roll, put on, what is the cost of papering a room of ordinary height, 18 ft. 6 in. by 14 ft. 4 in., if the room has three doors 4 ft. wide, and three windows 3 ft. 9 in. wide?

Perimeter of room = $2 \times (18\frac{1}{2} + 14\frac{1}{3})$ ft. = $65\frac{2}{3}$ ft. Width of doors and windows

 $= 3 \times 4 \text{ ft.} + 3 \times 3\frac{3}{4} \text{ ft.} = 12 \text{ ft.} + 11\frac{1}{4} \text{ ft.} = \frac{23\frac{1}{4}}{42\frac{5}{12}} \text{ ft.}$ Perimeter less doors and windows $= \overline{42\frac{5}{12}} \text{ ft.}$ $42\frac{5}{12} + 7 = 6\frac{5}{14}.$ Hence, 7 double rolls will be required.

 $7 \times $1.75 = 12.25 . Ans.

14. Find at 20 cents a square yard the cost of plastering the walls and ceiling of a room 18 ft. by 16 ft. by 10 ft., if the room has two doors 7 ft. 6 in. by 4 ft., three windows 6 ft. 6 in. by 4 ft., and a base board of 10 in.

Perimeter of room = $2 \times (18 + 16)$ ft. = 68 ft. Height of room = 10 ft. - 10 in. = $9\frac{1}{6}$ ft. Area of walls = $9\frac{1}{6} \times 68$ sq. ft. = $623\frac{1}{6}$ sq. ft. Area of ceiling = 18×16 sq. ft. = 288 sq. ft. Total area = $623\frac{1}{6}$ sq. ft. + 288 sq. ft. = $911\frac{1}{6}$ sq. ft. Area of doors and windows = $2 \times (6\frac{1}{6} \times 4)$ sq. ft. + $3(6\frac{1}{6} \times 4)$ sq. ft. = $53\frac{1}{6}$ sq. ft. + 78 sq. ft. = $131\frac{1}{6}$ sq. ft. $\frac{1}{6}$ of $131\frac{1}{6}$ sq. ft. = $65\frac{1}{6}$ sq. ft. Net area = $911\frac{1}{6}$ sq. ft. - $65\frac{1}{6}$ sq. ft. = $845\frac{1}{6}$ sq. ft. = $93\frac{1}{6}$ sq. yd. $94 \times \$0.20 = \18.80 . Ans.

15. Find at 25 cents a square yard the cost of plastering the walls and ceiling of a room 16 ft. by 15 ft. by 10 ft., if the room has two doors 7 ft. by 3 ft. 9 in., three windows 5 ft. 6 in. by 3 ft. 6 in., and a base board of 10 in.

Perimeter of room $=2 \times (16+15)$ ft. =62 ft.

Height above base board = $10 \text{ ft.} - 10 \text{ in.} = 9\frac{1}{6} \text{ ft.}$

Total wall area = $9\frac{1}{6} \times 62$ sq. ft. = $568\frac{1}{6}$ sq. ft. Area of ceiling = 16×15 sq. ft. = 240 sq. ft. Total area = $808\frac{1}{6}$ sq. ft.

Height of doors above base board is 7 ft. -10 in. $=6\frac{1}{6}$ ft.

Area of 2 doors= $2 \times (6\frac{1}{6} \times 3\frac{3}{4})$ sq. ft. =46\frac{1}{4} sq. ft.

Area of 3 windows= $3 \times (5\frac{1}{2} \times 3\frac{1}{2})$ sq. ft. = $57\frac{3}{4}$ sq. ft.

Total area of openings =104 sq. ft.

Half area of openings = 52 sq. ft.Net area $= 756\frac{1}{8} \text{ sq. ft.}$ $= 84\frac{1}{17} \text{ sq. yd.}$

At \$0.25 a square yard, 84 sq. yd. will cost $84 \times $0.25 = 21 . Ans.

16. Find at 20 cents a square yard the cost of plastering the walls and ceiling of a room 15 ft. by 14 ft. by 9 ft. 6 in., if the room has two doors 7 ft. 4 in. by 4 ft., two windows 5 ft. 6 in. by 3 ft. 6 in., and a base board of 9 in.

```
Perimeter of room=2 \times (15+14) ft.=58 ft.
Height above base board = 9 ft. 6 in. -9 in. =8\frac{3}{2} ft.
     Total wall area = 84 \times 58 sq. ft.
                                                                =507\frac{1}{4} sq. ft.
     Area of ceiling=15 \times 14 sq. ft.
                                                                =210 \text{ sq. ft.}
          Total area
                                                                =717\frac{1}{4} sq. ft.
Height of doors above base board is 7 ft. 4 in. -9 in. =6\frac{7}{12} ft.
Area of 2 doors = 2 \times (6\frac{7}{12} \times 4) sq. ft. = 52\frac{3}{12} sq. ft.
Area of 3 windows = 3 \times (5\frac{1}{2} \times 3\frac{1}{2}) sq. ft. = 57\frac{2}{4} sq. ft.
                                                =110^{5}_{1} sq. ft.
     Total area of openings
                                                                 = 55\frac{5}{24} sq. ft.
     Half area of openings
                                                                 =662\frac{7}{24} sq. ft.
          Net area
                                                                 = 73\frac{1}{12} sq. yd.
At $0.20 a square yard, 74 sq. yd. will cost 74 \times $0.20 = $14.80. Ans.
  17. Find at 15 cents a square yard the cost of painting the outside
of the walls of a cottage-roofed house 36 ft. by 32 ft. by 13 ft., if the
house has three doors 7 ft. 6 in. by 4 ft., and eleven windows 6 ft. by
4 ft.
Perimeter of house = 2 \times (36+32) ft. = 136 ft.
     Total wall area = 13 \times 136 sq. ft.
                                                                  =1768 sq. ft.
Area of 3 doors=3 \times (71 \times 4) sq. ft.
                                                = 90 \text{ sq. ft.}
Area of 11 windows=11 \times (6 \times 4) sq. ft. = 264 sq. ft.
     Total area of openings
                                                =354 \text{ sq. ft.}
     Half area of openings
                                                                  = 177 sq. ft.
                                                                  =1591 sq. ft.
          Net area
                                                                  = 1767 \text{ sq. yd.}
At $0.15 a square yard, 177 sq. yd. will cost 177 \times $0.15 = $26.55. Ans.
   18. Find at 20 cents a square yard the cost of painting the walls
of a room 16 ft. by 15 ft. by 10 ft., if the room has two doors 7 ft.
6 in. by 4 ft., four windows 6 ft. by 3 ft. 9 in., and a base board of 9 in.
Perimeter of room =2 \times (16+15) ft. =62 ft.
Height above base board = 10 ft. -9 in. =91 ft.
     Total area = 91 \times 62 sq. ft.
                                                                   =573\frac{1}{4} sq. ft.
Height of doors above base board is 7 ft. 6 in. -9 in. =6\frac{5}{4} ft.
Area of 2 doors = 2 \times (6\frac{1}{2} \times 4) sq. ft. = 54 sq. ft.
Area of 4 windows=4 \times (6 \times 3\frac{3}{4}) sq. ft. = 90 sq. ft.
     Total area of openings
                                                =144 \text{ sq. ft.}
     Half area of openings
                                                                   = 72 \text{ sq. ft.}
                                                                   =501\frac{1}{4} sq. ft.
          Net area
                                                                   =55\frac{1}{1} sq. yd.
```

At \$0.20 a square yard, 56 sq. yd. will cost $56 \times $0.20 = 11.20 . Ans.

19. How many bricks 8 in. long and 4 in. wide will be needed to pave a rectangular court 60 ft. by 30 ft.?

Area of a brick = (8×4) sq. in.

Area of court =
$$(60 \times 30)$$
 sq. ft. = $(60 \times 30 \times 144)$ sq. in.

Hence, the number of bricks needed =
$$\frac{\cancel{50} \times \cancel{30} \times \cancel{144}}{\cancel{5} \times \cancel{4}} = 8100. \text{ Ans.}$$

20. How many bricks 8 in. long and 2½ in. thick, laid on edge, will be needed to pave the court of Ex. 19?

Area of a brick =
$$(8 \times 2\frac{1}{2})$$
 sq. in.

Hence, the number of bricks needed

$$=\frac{60\times30\times144}{8\times2\frac{1}{2}}=\frac{\cancel{60}\times30\times144}{\cancel{20}}=12,960. \text{ Ans.}$$

21. How many clapboards will be required for the front of a house 40 ft. long and 20 ft. high, allowing 120 sq. ft. for doors and windows?

Total area =
$$40 \times 20$$
 sq. ft. = 800 sq. ft.

Net area =
$$800 \text{ sq. ft.} - 120 \text{ sq. ft.} = 680 \text{ sq. ft.}$$

$$680 \div 1\frac{1}{6} = \frac{6}{7} \times 680 = \frac{4080}{7} = 5824.$$
 583. Ans.

22. How many clapboards will be required for a house 44 ft. long. 35 ft. wide, and 22 ft. high to the eaves, if the gables extend 14 ft. above the end walls, the two gables to be reckoned as one full wall, and 500 sq. ft. to be allowed for doors and windows?

Perimeter =
$$2 \times (44 + 35)$$
 ft. = 158 ft.
Area to eaves = 22×158 sq. ft. = 3476 sq. ft.

Area of gables = 14×35 sq. ft. = 490 sq. ft.

Total area = 3966 sq. ft.

Area of openings = 500 sq. ft.

Net area $= \overline{3466}$ sq. ft.

$$3466 \div 1\frac{1}{6} = \frac{6}{7} \times 3466 = \frac{20796}{7} = 2970\$.$$
 2971. Ans.

23. Allowing 1000 shingles for 120 sq. ft., how many thousand will be required for the pitched roof of a house 60 ft. long, if the width of each side of the roof is 24½ ft.?

Total area =
$$2 \times (24\frac{1}{2} \times 60)$$
 sq. ft.

Number of thousand =
$$\frac{2 \times 24\frac{1}{2} \times 60}{120} = 24\frac{1}{2}$$
. Ans.

24. Allowing 1000 shingles for 110 sq. ft., how many thousand will be required for the pitched roof of a barn 40 ft. long, if the width of each side of the roof is 24 ft.?

Total area = $2 \times (24 \times 40)$ sq. ft.

Number of thousand =
$$\frac{2 \times 24 \times 49}{119} = \frac{192}{11} = 17\frac{5}{11}$$
.

As shingles are put up in bundles of $\frac{1}{4}$ thousand, $17\frac{1}{4}$ M will be required.

25. Allowing 1000 shingles for 120 sq. ft., how many thousand will be required for the pitched roof of a house 28 ft. long, if the width of each side of the roof is 18 ft.?

Total area = $2 \times (18 \times 28)$ sq. ft.

Number of thousand =
$$\frac{2 \times 18 \times 28}{120} = \frac{42}{5} = 83$$
.

As shingles are put up in bundles of ‡ thousand, 8½ M will be required.

26. How many feet board measure in a board 18 ft. long, 9 in. wide, 7 in. thick?

$$18 \times \frac{3}{4} = \frac{27}{2} = 13\frac{1}{2}. Ans.$$

27. How many feet board measure in a board 16 ft. long, 11 in. wide, 1 in. thick?

$$16 \times \frac{11}{12} \times 1 = \frac{44}{3} = 14\frac{2}{3}. Ans.$$

28. How many feet board measure in twenty boards averaging 14 ft. long, 10 in. wide, $1\frac{1}{2}$ in. thick?

$$\begin{array}{c} 10 & 7 \\ 20 \times 14 \times \frac{5}{9} \times \frac{3}{2} = 350. \ Ans. \end{array}$$

29. How many feet board measure in three joists 13 ft. long, 8 in. wide, 3 in. thick?

$$3 \times 13 \times \frac{2}{3} \times 3 = 78$$
. Ans.

30. How many feet board measure in a stick of timber 8 in. by 9 in., and 27 ft. long?

$$27 \times \frac{3}{4} \times \stackrel{2}{8} = 162$$
. Ans.

31. How many feet board measure in two beams, each 6 in. by 9 in., and 23 ft. long?

$$2 \times 23 \times \frac{3}{4} \times \% = 207$$
. Ans.

32. How many feet board measure in three joists, each 3 in. by 4 in., and 11 ft. long?

$$3 \times 11 \times \frac{1}{3} \times 3 = 33$$
. Ans.

33. How many feet board measure in five joists, each 6 in. by 4 in., and 14 ft. long?

$$5 \times 14 \times \frac{1}{2} \times \stackrel{2}{\cancel{1}} = 140$$
. Ans.

34. How many feet board measure in a stick of timber 10 in. square, and 36 ft. long?

$$36 \times \frac{5}{6} \times 10 = 300. Ans.$$

35. How many feet board measure in ten planks, each 13 ft. long, 15 in. wide, 2 in. thick?

$$\begin{array}{c}
 5 \\
 \cancel{10} \times 13 \times \frac{5}{4} \times 2 = 325. \text{ Ans.} \\
 \cancel{2}
 \end{array}$$

36. Find the cost of nine joists, each 15 ft. long, 3½ in. by 5 in., at \$12 per M.

$$9 \times 13 \times \frac{3}{12} \times \frac{5}{2} \times \frac{7}{2} \times \frac{12}{1999} = \frac{189}{80} = 2.36$$
. Ans.

37. Find the cost of thirty planks, each 12 ft. long, 11 in. wide, 3 in. thick, at \$15 per M.

$$389 \times 12 \times \frac{11}{12} \times 3 \times 3 \times \frac{15}{1999} = 3297 = 314.85. Ans.$$

38. Find the cost of four sticks of timber, each 8 in. by 9 in., and 23 ft. long, at \$18 per M.

$$4 \times 23 \times \frac{3}{4} \times 8 \times \$ \frac{18}{1999} = \$ \frac{1242}{125} = \$ 9.94.$$
 Ans.

39. Find the cost of a board 24 ft. long, 23 in. wide at one end and 17 in. at the other, and 1½ in. thick, at \$30 per M.

Average width = $\frac{1}{4}(23 + 17)$ in. = 20 in.

$$\frac{3}{\cancel{5}}
\cancel{24} \times \frac{\cancel{5}}{\cancel{3}} \times \frac{\cancel{3}}{\cancel{2}} \times \cancel{3} \times \cancel{3} \times \cancel{3} \times \cancel{3} \times \cancel{3} = \cancel{5} = \cancel{5}$$

40. Find the cost of a stick of timber 29 ft. long, 10 in. by 12 in., at \$13.50 per M.

$$29 \times 1 \times 19 \times \$ \frac{\cancel{1339}}{\cancel{199999}} = \$ \frac{783}{200} = \$ 3.92. Ans.$$

41. Find the cost of the flooring for two floors, each 23 ft. by 17 ft., each floor double, and of boards 7 in. thick; the under floors at \$18, and the upper at \$24, per M.

The average price is $\frac{1}{4}$ (\$ 18 + \$ 24) = \$ 21.

$$4 \times 23 \times 17 \times \$ \frac{21}{1000} = \$ \frac{8211}{250} = \$ 32.84$$
. Ans.

42. Find the cost of the flooring timbers for a room 23 ft. by 17 ft., at \$18 per M, if they are 2 in. by 10 in., 17 ft. long, and are placed on edge, one close to each wall and the others with spaces \frac{32}{48} ft. wide between them.

Since the room is 17 ft. wide, and the timbers are 17 ft. long, the timbers must run across the room. When a timber is placed against the wall the remaining distance is 23 ft. -2 in. $=22\frac{1}{2}$ ft.

The distance taken up by a timber and its space = $\frac{1}{6}$ ft. + $\frac{39}{40}$ ft. = $\frac{137}{120}$ ft. The number of timbers required for the remaining space

$$=22\frac{5}{6}\div\frac{137}{120}=\frac{137}{6}\times\frac{120}{137}=20,$$

and the whole number of timbers is 21.

$$21 \times 17 \times \frac{5}{6} \times 2 \times 3 \times \frac{18}{100} = 31071 = 10.71$$
. Ans.

43. Find the number of feet board measure in a log 12 ft. long, and 20 in. in diameter at the smaller end.

$$20^{2} - 2 \times 20 = 400 - 40 = 360.$$

$$\frac{6}{12} \times \frac{21}{40} \times \frac{9}{300} = \frac{1134}{5} = 227. Ans.$$

44. Find the number of feet board measure in a log 14 ft. long, smallest diameter 17 in.

$$17^{2} - 2 \times 17 = 289 - 34 = 255.$$
 $\frac{7}{\cancel{19}} \times \frac{21}{40} \times \cancel{255} = 187.$ Ans.

45. Find the number of feet board measure in a log 11 ft. long, smallest diameter 13 in.

$$13^2 - 2 \times 13 = 169 - 26 = 143.$$
 $\frac{11}{10} \times \frac{21}{40} \times 143 = 83.$ Ans.

46. Find the number of feet board measure in a log 16 ft. long, smallest diameter 20 in.

$$20^2 - 2 \times 20 = 400 - 40 = 360.$$
 $\frac{8}{\cancel{10}} \times \frac{21}{\cancel{40}} \times \cancel{300} = 302.$ Ans.

47. Find the number of feet board measure in a log 12 ft. long, smallest diameter 15 in.

$$15^2 - 2 \times 15 = 225 - 30 = 195.$$
 $\frac{3}{12} \times \frac{21}{40} \times \frac{39}{195} = 123.$ Ans.

48. Find the value at \$9 per M of a log 15 ft. long, smallest diameter 11 in.

$$11^2 - 2 \times 11 = 121 - 22 = 99.$$
 $\frac{3}{\cancel{19}} \times \frac{21}{40} \times 99 = 78.$

$$78 \times \$0.009 = \$0.70$$
. Ans.

49. Find the value at \$9 per M of a log 16 ft. long, smallest diameter 13 in.

$$13^2 - 2 \times 13 = 169 - 26 = 143.$$

$$\frac{16}{10} \times \frac{21}{40} \times 143 = 120.$$
 $120 \times \$0.009 = \$1.08.$ Ans.

50. Find the value at \$9 per M of a log 13 ft. long, smallest diameter 16 in.

$$16^2 - 2 \times 16 = 256 - 32 = 224.$$

$$\frac{13}{10} \times \frac{21}{40} \times \frac{56}{224} = 153.$$

$$153 \times \$0.009 = \$1.38. Ans.$$

51. Find the value at \$9 per M of a log 14 ft. long, smallest diameter 12 in.

$$12^2 - 2 \times 12 = 144 - 24 = 120.$$

$$\frac{14}{10} \times \frac{21}{40} \times 120 = 88.$$
 88 × \$0.009 = \$0.79. Ans.

Exercise 90. Page 192.

1. Find the volume of a rectangular solid 7 ft. long, 2 ft. 6 in. wide, and 11 in. thick.

$$7 \times 2\frac{1}{2} \times \frac{11}{12} = 7 \times \frac{5}{2} \times \frac{11}{12} = \frac{385}{24} = 16\frac{1}{24}$$

 16_{24} cu. ft. = 16 cu. ft. 72 cu. in. Ans.

2. How many cubic feet of air in a hall 54 ft. long, 33 ft. wide, and 21 ft. 4 in. high?

$$54 \times 33 \times 21\frac{1}{2} = 54 \times \frac{11}{33} \times \frac{64}{3} = 38,016$$
. Ans.

3. Find the volume of a cube whose edge is 21 yd.

$$2\frac{1}{4} \times 2\frac{1}{4} \times 2\frac{1}{2} = \frac{5}{2} \times \frac{5}{2} \times \frac{5}{2} = \frac{125}{8} = 15\frac{5}{8}$$
. 15\frac{5}{6} cu. yd. Ans.

4. A cellar was dug 21 ft. long, 17 ft. 3 in. wide, and 9 ft. deep. How many cubic yards of earth were taken out?

$$\frac{\frac{7}{21 \times 17\frac{1}{4} \times 9}}{\frac{27}{3}} = 120\frac{3}{4}. Ans.$$

5. Find the volume of a brick 8 in. long, 3½ in. wide, and 2½ in. thick.

$$8 \times 3\frac{1}{4} \times 2\frac{1}{4} = 8 \times \frac{7}{2} \times \frac{9}{4} = 63.$$
 63 cu. in. Ans.

6. How many cubic feet of water will a rectangular cistern hold whose length, breadth, and height are 5 ft. 4 in., 3 ft. 6 in., and 2 ft. 10 in., respectively?

$$5\frac{1}{3} \times 3\frac{1}{3} \times 2\frac{5}{8} = \frac{\frac{16}{8}}{3} \times \frac{7}{2} \times \frac{17}{6} = \frac{476}{9} = 52\frac{5}{9}$$
. Ans.

7. Find the volume in cubic inches of a bar of iron 21 ft. long, 3 in. wide, and 2 in. thick.

21 ft. = 252 in.
$$252 \times 3 \times 2 = 1512$$
. 1512 cu. in. Ans.

8. What is the value at \$190 a cubic inch of a bar of gold 8 in. long and \ of an inch square?

$$\frac{2}{8} \times \frac{3}{4} \times \frac{3}{4} \times \$ 199 = \$ 855.$$
 Ans.

9. A rectangular reservoir 15 yd. long, 12 yd. wide, holds 330 cu. yd. of water. What is its depth?

$$\frac{\cancel{339}}{\cancel{15} \times \cancel{12}} = \frac{11}{6} = 1\frac{5}{6}.$$
1\frac{5}{6} \text{yd. Ans.}

10. What length must be cut off a beam 9 in. by 15 in. that the part cut off may contain 2½ cu. ft.?

$$\frac{2\frac{1}{4}}{\frac{3}{4} \times \frac{4}{4}} = \frac{\cancel{5}}{\cancel{2}} \times \frac{\cancel{4}}{\cancel{5}} \times \frac{\cancel{4}}{\cancel{5}} = \frac{\cancel{8}}{\cancel{3}} = 2\frac{\cancel{3}}{\cancel{5}}.$$

$$2\frac{\cancel{3}}{\cancel{5}} \text{ ft.} = 2 \text{ ft. 8 in. } Ans.$$

11. How high is a room, if it is 31 ft. 3 in. long, 24 ft. broad, and contains 10,000 cu. ft. of air?

$$\frac{10000}{31\frac{1}{4} \times 24} = \cancel{19999} \times \frac{4}{\cancel{125}} \times \frac{1}{\cancel{24}} = \frac{40}{3} = 13\frac{1}{3}.$$

$$13\frac{1}{4}$$
 ft. = 13 ft. 4 in. Ans.

12. A piece of wood 5 ft. long, 1 ft. broad, and 9 in. thick, is cut up into matches 2½ in. long and 0.1 of an inch square. How many matches will there be, if no allowance is made for waste in cutting?

Volume of the wood = $(60 \times 12 \times 9)$ cu. in.

Volume of a match = $(2\frac{1}{2} \times \frac{1}{10} \times \frac{1}{10})$ cu. in.

Therefore, the number of matches

$$= \frac{60 \times 12 \times 9}{2\frac{1}{4} \times \frac{1}{10} \times \frac{1}{10}} = 60 \times 12 \times 9 \times \frac{2}{5} \times \frac{2}{10} \times 10 = 259,200. Ans.$$

13. How long a wall 6 ft. high, 12\frac{1}{2} in. thick, can be built with the bricks forming a rectangular pile 17 ft. 6 in. long, 5 ft. wide, and 4 ft. 3 in. high?

$$12\frac{3}{4}$$
 in. $=1\frac{1}{16}$ ft.

Volume of pile of bricks = $(17\frac{1}{2} \times 5 \times 4\frac{1}{4})$ cu. ft.

$$\frac{17\frac{1}{1} \times 5 \times 4\frac{1}{4}}{6 \times 1\frac{1}{16}} = \frac{35}{2} \times 5 \times \frac{17}{4} \times \frac{1}{6} \times \frac{16}{17} = \frac{175}{3} = 58\frac{1}{3}.$$
 58\frac{1}{3} ft. Ans.

14. Find the surface of a cube whose edge is 3 ft. 53 in.

The surface of the cube consists of 6 squares 3 ft. $5\frac{2}{3}$ in., that is $3\frac{17}{3}$ ft., on a side.

$$6 \times 3\frac{17}{36} \times 3\frac{17}{36} = 6 \times \frac{125}{36} \times \frac{125}{36} = \frac{15625}{216} = 72\frac{73}{216}.$$

 $72\frac{73}{116}$ sq. ft. = 72 sq. ft. 481 sq. in. Ans.

15. Find the surface of a rectangular block of stone 4 ft. long, 2½ ft. broad, and 1½ ft. thick.

$$2 \times 4 \times 2\frac{1}{4} = 2 \times 4 \times \frac{5}{2} = 20.$$

$$2 \times 4 \times 1\frac{1}{4} = 2 \times 4 \times \frac{5}{4} = 10.$$

$$2 \times 2\frac{1}{4} \times 1\frac{1}{4} = 2 \times \frac{5}{2} \times \frac{5}{4} = \frac{25}{4} = 6\frac{1}{4}.$$

20 sq. ft. + 10 sq. ft. + 61 sq. ft. = 361 sq. ft. = 36 sq. ft. 36 sq. in. Ans.

16. A lake whose area is 45 A. is covered with ice 3 in. thick. Find the weight of the ice in tons, if a cubic foot of ice weighs 920 oz.

45 A. = 45 × 43,560 sq. ft. 920 oz. =
$$\frac{920}{16}$$
 lb. = $\frac{920}{16 \times 2000}$ t.

$$\begin{array}{c}
9 & 1089 \\
45 \times 43569 \times \frac{1}{4} \times \frac{\cancel{920}}{\cancel{16} \times \cancel{2000}} \text{ t.} = \frac{225423}{\cancel{16}} \text{ t.} = 14,088 \frac{1}{8} \text{ t.} \quad Ans. \\
\cancel{59} & \cancel{59} & \cancel{5}
\end{array}$$

17. How many bricks will be required to build a wall 75 ft. long, 6 ft. high, and 16 in. thick, if each brick is 8 in. long, 4 in. wide, and 21 in. thick?

Volume of wall = $75 \times 6 \times \frac{4}{3} \times 1728$ cu. in.

Volume of brick = $(8 \times 4 \times 2\frac{1}{4})$ cu. in.

$$\frac{75 \times 6 \times \frac{4}{5} \times 1728}{8 \times 4 \times 2\frac{1}{4}} = 75 \times \cancel{6} \times \cancel{4} \times \cancel{1728} \times \frac{1}{\cancel{8}} \times \frac{1}{\cancel{4}} \times \cancel{\frac{4}{\cancel{9}}} = 14,400. \text{ Ans.}$$

18. The ceiling of a room 27 ft. long, 24 ft. broad, and 10 ft. high, is to be raised so as to increase the space by 84 cu. yd. What will then be the height of the room?

27 ft. = 9 yd.; 24 ft. = 8 yd.
$$\frac{\frac{7}{28}}{\frac{84}{3} \times \frac{8}{2}} = \frac{7}{6} = 1\frac{1}{4}.$$

Hence, the ceiling must be raised 14 yd., or 31 ft.

10 ft.
$$+3\frac{1}{2}$$
 ft. $=13\frac{1}{2}$ ft. Ans.

19. Find the cost of making a road 110 yd. long and 18 ft. wide, if the soil is first removed to the depth of 1 ft. at a cost of 25 cents a cubic yard, rubble then laid 8 in. deep at 25 cents a cubic yard, and gravel placed on top 9 in. thick at 62½ cents a cubic yard.

The cost of removing the soil is

The cost of laying the rubble is

110 ×
$$\emptyset$$
 × $\frac{\frac{2}{8}}{\frac{8}{9}}$ × $\$\frac{1}{4}$ = $\$\frac{110}{3}$ = $\$36.67$.

The cost of laying the gravel is

$$\begin{array}{c}
55 \\
119 \\
4 \\
2
\end{array}
\times \frac{9}{39} \times \$ \frac{5}{8} = \$ \frac{825}{8} = \$ 103.12.$$

$$\$55 + \$36.67 + \$103.12 = \$194.79$$
. Ans.

20. If a rectangular block of wood 5 ft. 4.8 in. long, 1 ft. 9 in. wide and thick, weighs 7.56 cwt., find in pounds its weight per cubic foot.

5 ft.
$$4.8$$
 in. $= 5\frac{3}{5}$ ft.

Volume of block = $(5\frac{2}{5} \times 1\frac{3}{4} \times 1\frac{3}{4})$ cu. in.

$$7.56 \text{ cwt.} = 756 \text{ lb.}$$

$$\frac{756}{5\frac{2}{3} \times 1\frac{3}{4} \times 1\frac{3}{4}} = \frac{108}{756} \times \frac{5}{27} \times \frac{4}{7} \times \frac{4}{7} = \frac{320}{7} = 45\frac{5}{7}.$$
 45\frac{1}{7}\text{ lb. Ans.}

21. How many cords of wood in a pile 40 ft. long, 4 ft. wide, and 5 ft. 4 in. high?

$$\frac{40 \times 4 \times 51}{8 \times 4 \times 4} = \frac{\cancel{40} \times \cancel{4} \times \cancel{10}}{\cancel{8} \times \cancel{4} \times \cancel{4} \times 3} = \frac{20}{3} = 6\cancel{3}. \text{ Ans.}$$

22. A pile of wood containing 67½ cords is 270 ft. long and 4 ft. wide. How high is it?

$$\frac{67\frac{1}{2} \times 128}{270 \times 4} = \frac{\cancel{135} \times \cancel{128}}{\cancel{2} \times \cancel{279} \times \cancel{4}} = 8.$$

8 ft. Ans.

23. What will be the cost of a pile of wood 25 ft. long, 4 ft. wide, and 4 ft. 8 in. high, at \$3.75 a cord?

$$\frac{25 \times 4 \times 4\frac{7}{4}}{8 \times 4 \times 4} \times \$3\frac{3}{4} = \frac{25 \times 4 \times 14}{8 \times 4 \times 4 \times 3} \times \$\frac{5}{4} = \$\frac{875}{64} = \$13.67. Ans.$$

24. What must be the length of a load of wood 31 ft. high and 5 ft. wide to contain a cord?

$$\frac{128}{3\frac{1}{2} \times 5} = \frac{2 \times 128}{7 \times 5} = \frac{256}{35} = 7\frac{11}{35}.$$
 7\frac{11}{35} ft. Ans.

25. How high must manure be piled in a cart 6 ft. by 4 ft., that the load may contain half a cord?

$$\frac{\frac{1}{10}}{\frac{1}{6} \times 4} = \frac{\frac{128}{128}}{\frac{1}{2} \times \frac{1}{10} \times \frac{1}{10}} = \frac{8}{3} = 2\frac{1}{3}.$$

2**]** ft. *Ans*.

26. How many cords of wood in a pile 32 ft. long, 8 ft. wide, and 6 ft. high?

$$\frac{2}{8}$$

$$\frac{32 \times 8 \times 6}{8 \times 4 \times 4} = 12. Ans.$$

27. How many cords of wood in a pile 40 ft. long, 4 ft. wide, and 8 ft. high?

$$\frac{\cancel{40} \times \cancel{4} \times \cancel{8}}{\cancel{8} \times \cancel{4} \times \cancel{4}} = 10. \text{ Ans.}$$

28. Find the cost of the wood at \$3.75 a cord that can be piled in a shed 18 ft. long, 16 ft. wide, and 7 ft. high.

$$\frac{\cancel{18} \times \cancel{16} \times 7}{\cancel{8} \times \cancel{4} \times \cancel{4}} \times \cancel{\$} \frac{15}{4} = \cancel{\$} \frac{945}{16} = \cancel{\$} 59.06. \ Ans.$$

29. Find the number of cubic inches in a sphere 11 in. in diameter.

$$0.5236 \times (11 \times 11 \times 11)$$
 cu. in.

30. How many cubic inches of water can be poured into a hollow sphere whose inner diameter is 161 in.?

$$0.5236 \times (16\frac{1}{2} \times 16\frac{1}{2} \times 16\frac{1}{2})$$
 cu. in.

$$0.1309$$

$$9.2618$$

$$= 9.5236 \times \left(\frac{33}{2} \times \frac{33}{2} \times \frac{33}{2}\right) \text{ cu. in.}$$

$$\frac{33}{99} \qquad \frac{35937}{323433}$$

$$\frac{99}{107811}$$

$$\frac{33}{3267} \qquad \frac{35937}{24704.1533}$$

$$\frac{3267}{35937}$$

$$\frac{3267}{35937}$$

31. What is the volume of the ball on top of St. Paul's in London, which is 6 ft. in diameter?

$$\begin{array}{ccc}
6 & 0.5236 \\
\underline{6} & 216 \\
\hline
36 & 31416 \\
\underline{6} & 5236 \\
\underline{216} & 10472 \\
\hline
113.0976
\end{array}$$

113.0976 cu. ft. Ans.

32. If 30 cu. in. of powder weigh 1 lb., how many ounces of powder will just fill a shell, inner diameter 3 in.?

33. Find the volume of a cylinder whose height is 5 ft. and the radius of whose base is 1 ft. 2 in.

$$5 \times 3.1416 \times 1\frac{1}{6} \times 1\frac{1}{6}$$

$$0.2618$$

$$9.5236$$

$$5 \times 3.1416 \times \frac{7}{6} \times \frac{7}{6} = 4.2761.$$

\$1.3803 cu. ft. Ans.

34. Find the volume of a cylinder whose height is 4 ft. 6 in. and the diameter of whose base is 8 ft. 2 in.

$$4\frac{1}{2} \times 0.7854 \times 8\frac{1}{6} \times 8\frac{1}{6}$$

$$= \frac{9}{2} \times \cancel{9.7854} \times \frac{49}{\cancel{6}} \times \frac{49}{\cancel{6}} = 235.7182$$

$$\frac{49}{441} \qquad \frac{21609}{194481}$$

$$\frac{196}{2401} \qquad \frac{64827}{21609}$$

$$\frac{21609}{235.7182}$$

$$235.7182 \text{ cu. ft. } Ans.$$

35. How many cubic yards of earth must be excavated to make a well 3 ft. in diameter and 20 ft. deep?

$$(20 \times 0.7854 \times 3 \times 3) \text{ cu. ft.}$$

$$= \frac{0.2618}{27}$$

$$= \frac{20 \times 9.7834 \times 3 \times 3}{27} \text{ cu. yd.}$$

$$= 5.236 \text{ cu. yd.} \text{ Ans.}$$

36. How many cubic yards in a tunnel 800 ft. long, if a cross section is a semicircle with a radius of 10 ft.?

$$(800 \times \frac{1}{4} \times 3.1416 \times 10 \times 10) \text{ cu. ft.}$$

$$0.5236$$

$$1.9472$$

$$= \frac{800 \times \cancel{3}.1416 \times 10 \times 10}{\cancel{2} \times \cancel{27}} \text{ cu. yd.}$$

$$= \frac{41888}{9} \text{ cu. yd.} = 4654\frac{2}{9} \text{ cu. yd.}$$
Ans.

37. Find the number of cubic feet in a bushel.

1 bu. = 2150.42 cu. in.

1.24446 cu. ft. Ans.

38. Find the number of bushels a bin will hold that is 6 ft. long, 5 ft. wide, and 4 ft. deep.

$$\frac{4}{3}$$
 of $6 \times 5 \times 4 = 96$.
 $\frac{1}{4}$ of 0.01 of $96 = \frac{0.48}{96.48}$.

39. Find the number of cubic feet required for 1000 bu.

$$\frac{5}{4}$$
 of 1000 = 1250.
 $\frac{1}{2}$ of 0.01 of 1250 = $\frac{6.25}{1243.75}$ Ans.

40. Find the number of bushels a bin will hold that is 8 ft. long, 4 ft. wide, 3 ft. deep.

$$\frac{4}{5}$$
 of $8 \times 4 \times 3 = 76.8$
 $\frac{1}{2}$ of 0.01 of $76.8 = \frac{0.384}{77.184}$ Ans.

41. Find the number of bushels a bin will hold that is 9 ft. long, 6 ft. 6 in. wide, 3 ft. 4 in. deep.

$$\frac{4}{3}$$
 of $9 \times 6\frac{1}{2} \times 3\frac{1}{3} = 156$.
 $\frac{1}{2}$ of 0.01 of 156 = 0.78
 $\frac{1}{156.78}$ Ans.

42. Find the depth of a bin that will hold 360 bu., if its length is 12 ft. and its width 6 ft.

$$\begin{array}{rcl}
\frac{2}{1} & \text{of } 360 & = 450. \\
\frac{1}{2} & \text{of } 0.01 & \text{of } 450 = \underbrace{2.25}_{447.75} \\
199 & & & & & \\
\end{array}$$

$$\frac{447.75}{12 \times 6} = \frac{\cancel{1791}}{\cancel{4}} \times \frac{1}{\cancel{12}} \times \frac{1}{\cancel{6}} = \frac{199}{32} = 6\cancel{7}_{\cancel{12}}.$$

$$6\frac{7}{82}$$
 ft. = 6 ft. $2\frac{5}{8}$ in. Ans.

43. Find the length of a bin that is 6 ft. wide and 5 ft. deep, if it will hold 400 bu.

$$\frac{5}{4}$$
 of 400 = 500.
 $\frac{1}{2}$ of 0.01 of 500 = 2.5
 $\frac{497.5}{}$

$$\frac{497.5}{6 \times 5} = \frac{995}{2} \times \frac{1}{6} \times \frac{1}{5} = \frac{199}{12} = 16\frac{7}{12}.$$

$$16\frac{7}{12} \text{ ft.} = 16 \text{ ft. 7 in. } Ans.$$

44. Find the number of bushels that will fill a bin 8.5 ft. long, 4.5 ft. wide, 3.5 ft. deep.

$$\frac{4}{3}$$
 of $8\frac{1}{2} \times 4\frac{1}{2} \times 3\frac{1}{2} = 107.1$
 $\frac{1}{2}$ of 0.01 of 107.1 = $\frac{0.5355}{107.6355}$
Ans.

45. A bin 20 ft. long, 12 ft. wide, and 6 ft. deep is full of wheat. What is its value at \$0.75 a bushel?

46. If a ton of coal occupies 40 cu. ft., how many tons of coal will fill a bin 21 ft. long, 10 ft. wide, 5 ft. deep?

$$\frac{21 \times \cancel{10} \times 5}{\cancel{40}} = \frac{105}{4} = 26\frac{1}{4}. Ans.$$

47. If a ton of Lehigh coal occupies 35 cu. ft., how many tons of Lehigh coal will fill a bin 8 ft. long, 5 ft. 9 in. wide, 3 ft. 6 in. deep?

$$\frac{8 \times 5\frac{3}{4} \times 3\frac{1}{4}}{35} = \frac{2}{8} \times \frac{23}{4} \times \frac{7}{2} \times \frac{1}{35}$$
$$\frac{23}{5} = 4\frac{3}{5}. Ans.$$

48. How many bushels will a bin hold that is 22 ft. long, 12 ft. 6 in. wide, 9 ft. 9 in. deep?

$$\frac{4}{5}$$
 of $22 \times 12\frac{1}{2} \times 9\frac{3}{4} = 2145$.
 $\frac{1}{2}$ of 0.01 of 2145 = $\frac{10.725}{2155.725}$

Ans.

49. Find the number of gallons in a cubic foot.

50. Find the exact number of gallons a cistern will hold that is 5 ft. square, and 6 ft. deep.

$$\frac{5 \times 5 \times 6 \times 1728}{231} = 1122.078. \text{ Ans.}$$

$$\frac{5}{77} = \frac{1122.077}{77}$$

$$\frac{5}{25} = \frac{150}{28800} = \frac{77}{94}$$

$$\frac{6}{150} = \frac{576}{86400} = \frac{77}{170}$$

$$\frac{154}{160}$$

$$\frac{154}{600}$$

$$\frac{539}{610}$$

$$\frac{539}{71}$$

51. Find the exact number of gallons a cistern will hold that is 13 ft. long, 6 ft. wide, 7 ft. 4 in. deep.

52. Find the exact number of gallons a tank will hold that is 4 ft. long, 2 ft. 8 in. wide, 1 ft. 8 in. deep.

$$\frac{4 \times 2\frac{7}{4} \times 1\frac{7}{4} \times 1728}{231} = \frac{4 \times 8 \times 5 \times 1728}{3 \times 3 \times 231}$$

$$= 132.987. \quad Ans.$$

$$\frac{132.987}{77}$$

$$\frac{8}{32} \qquad \frac{77}{254}$$

$$\frac{5}{160} \qquad \frac{231}{230}$$

$$\frac{64}{640} \qquad \frac{154}{760}$$

$$\frac{960}{10240} \qquad \frac{693}{670}$$

$$\frac{616}{540}$$

$$\frac{539}{1029}$$

53. Find the capacity in cubic feet of a cistern that will hold 200 bbl. of water.

$$200 \times 31\frac{1}{4} + (1728 + 231)$$

$$= \stackrel{25}{\cancel{299}} \times \frac{\cancel{63}}{\cancel{2}} \times \frac{\cancel{231}}{\cancel{17\cancel{28}}} = 842.1875. \quad Ans.$$

$$\stackrel{192}{\cancel{64}}$$

$$\stackrel{64}{\cancel{8}}$$

54. Find the approximate number of gallons a cylindrical cistern will hold that is 6 ft. in diameter and 7 ft. deep.

 $\frac{1}{4}$ of 0.01 of 1484.406 = 3.711. 1484.406 - 3.711 = 1480.695. Ans.

55. Find the approximate number of gallons a cylindrical vessel will hold that is 12 in. in diameter and 10 in. deep.

$$\frac{5}{6} \times \cancel{9.7854} \times 1 \times 1 \times \frac{15}{2}.$$
15
0.1309
$$\frac{5}{75} \qquad \qquad \frac{75}{6545}$$
9163
$$2 \cancel{9.8175}$$
4.90875

 $\frac{1}{4}$ of 0.01 of 4.90875 = 0.01227.

4.90875 - 0.01227 = 4.89648. Ans.

56. How many quarts will a cylindrical vessel hold 51 in. in diameter and 6 in. deep?

$$\frac{6 \times 0.7854 \times 5\frac{1}{8} \times 5\frac{1}{8}}{\frac{1}{4} \times 231}$$

$$= \cancel{6} \times \cancel{9.7854} \times \frac{31}{\cancel{6}} \times \frac{31}{\cancel{6}} \times \frac{2}{\cancel{4}}$$
$$= 2.1783. \ Ans.$$

1922

57. How many quarts will a hollow sphere hold whose interior diameter is 12 in.?

$$\frac{0.5236 \times 12 \times 12 \times 12}{\frac{1}{4} \text{ of } 231}$$

$$= 0.0068 \quad 4$$

$$= 0.5236 \times 12 \times 12 \times 12 \times \frac{4}{231}$$

$$= 15.6672. \quad Ans.$$

$$\frac{12}{144} \qquad \frac{576}{2304}$$

58. What part of a bushel will a hemispherical bowl hold that is 13 in. in diameter?

$$\frac{\frac{1}{2} \times 0.5236 \times 13 \times 13 \times 13}{2150.42}$$

$$0.1309$$

$$0.2618$$

$$= \frac{9.5236 \times 13 \times 13 \times 13}{2 \times 2150.42}$$

$$= 0.267. Ans.$$

$$13$$

$$0.1309$$

$$\frac{13}{39}$$

$$\frac{0.1309}{19773}$$

$$\frac{13}{169}$$

$$\frac{2197}{287.5873}$$

$$\frac{169}{2197}$$

$$\begin{array}{r} 0.267 \\ 107521)28758.73 \\ \underline{215042} \\ \hline 725453 \\ \underline{645126} \\ \hline 803270 \\ \underline{752647} \\ \hline 50623 \\ \end{array}$$

59. If a cubical box 2 ft. on an edge contains a solid sphere 2 ft. in diameter, how many gallons of water can be poured into the box?

$$2 \times 2 \times 2 = 8.$$
 $0.5236 \times 2 \times 2 \times 2 = 4.1888.$
8 cu. ft. -4.1888 cu. ft. $=3.8112$ cu. ft.
 3.8112 cu. ft. $=3.8112 \times 1728$ cu. in.

$$= \frac{3.8112 \times 1728}{231} \text{ gal.}$$

$$= 28.5098 \text{ gal. } Ans.$$

3.8112	28.5097
576	77)2195.2512
228672	154
266784	655
190560	616
2195.2512	392
	385
	751
	693
	582
	539
	43

60. If 64 qt. of water are poured into a vessel that will hold 2 bu. of wheat, what part of the vessel will be filled?

64 qt. = 16 gal. =
$$16 \times 231$$
 cu. in.

2 bu. = 2×2150.42 cu. in.

231

2 bu. = 2×2150.42 cu. in.

360168

638320

537605

1007150

967689

1075.21

Exercise 91. Page 198.

- 1. Find the number of cubic inches in 1 oz. (av.) of water. 1 cu. ft. of water weighs 1000 oz. $1728 \div 1000 = 1.728$. Ans.
 - 2. Find the weight in ounces (av.) of 1 cu. in. of water.

1000 oz.
$$\div$$
 1728 = $\frac{1}{1728} \times 1999$ oz. = $\frac{125}{216}$ oz. Ans.

3. Find the weight in ounces (av.) of 1 pt. of water.

1 pt. =
$$\frac{231}{8}$$
 cu. in.
 $\frac{77}{231} \times \frac{125}{216} = \frac{9625}{576} = 16.71$ oz. Ans.

4. Find the number of pints in 1 lb. of water.

By Ex. 3, 1 pt. of water weighs 16.71 oz. 1 lb. = 16 oz.

$$16 \div 16.71 = 0.9575$$
. Ans.

$$\begin{array}{r}
 0.9575 \\
 \hline
 1671)1600. \\
 \underline{15039} \\
 \hline
 9610 \\
 \underline{8355} \\
 \overline{12550} \\
 \underline{11697} \\
 \underline{8530} \\
 \underline{8355} \\
 \overline{175}
\end{array}$$

5. Find the weight in grains of 1 cu. in. of water.

1 cu. in. of water weighs $\frac{125}{216}$ oz.=

$$\frac{125}{16 \times 216} \text{lb.} = \frac{125 \times 7999}{16 \times 216} \text{gr.} = \frac{109375}{432} \text{gr.} = 253.183 \text{ gr.} Ans.$$

6. A bar of iron 5 in. long and 2 in. square weighs 5 lb. What is the specific gravity of the iron?

$$(5 \times 2 \times 2)$$
 cu. in. = 20 cu. in.

If 20 cu. in. of iron weighs 5 lb., 4 cu. in. weighs 1 lb., and 1 cu. in. weighs 4 oz. But by Ex. 2, 1 cu. in. of water weighs $\frac{1}{2}$ oz.

Therefore, the specific gravity of the iron is

$$4 + \frac{125}{216} = \frac{216}{125} \times 4 = \frac{864}{125} = 6.912$$
. Ans.

7. If a bar of iron 18 in. long, 2\frac{1}{4} in. wide, 1\frac{1}{4} in. thick weighs 18 lb. 9 oz., what is the specific gravity of the iron?

$$(18 \times 2\frac{1}{3} \times 1\frac{3}{4}) \text{ cu. in.} = \begin{pmatrix} \frac{3}{3} \\ 18 \times \frac{7}{3} \times \frac{7}{4} \end{pmatrix} \text{ cu. in.}$$
$$= \frac{147}{2} \text{ cu. in.} = 73\frac{1}{2} \text{ cu. in.}$$

18 lb. 9 oz.
$$= 297$$
 oz.

Therefore, 1 cu. in. of the iron weighs $\frac{297}{73\frac{1}{2}}$ oz., and the specific gravity of the iron is

$$\frac{297}{73\frac{1}{2}} \div \frac{125}{216} = \frac{216}{125} \times \frac{99}{297} \times \frac{2}{147} = \frac{42768}{6125} = 6.98. \text{ Ans.}$$

8. If the specific gravity of iron is 7.48, find the number of cubic inches of iron to the pound.

1 cu. ft. of water weighs 62.5 lb.

Therefore, 1 lb. of water occupies $\frac{1728}{62.5}$ cu. in., and 1 lb. of iron, specific gravity 7.48, occupies

$$\frac{1728}{7.48 \times 62.5} \text{ cu. in} = 3.696 \text{ cu. in.} \quad Ans.$$

$$\frac{7.48}{62.5} = \underbrace{\frac{3.696}{4675}}{3740}$$

$$\frac{1496}{4488} = \underbrace{\frac{14025}{32550}}{467.500}$$

$$\frac{28050}{42075}$$

$$\frac{28050}{1200}$$

9. If the specific gravity of gold is 19.36, find the number of cubic inches in 2 lb. 61 oz. of gold.

2 lb.
$$6\frac{1}{2}$$
 oz. $(\text{troy}) = 2\frac{1}{2}\frac{3}{4}$ lb.

1 lb. av. of water occupies
$$\frac{1728}{62.5}$$
 cu. in.

1 lb. troy of water occupies
$$\frac{1728}{62.5 \times 7928}$$
 cu. in.

1 lb. troy of gold occupies
$$\frac{1728}{19.36 \times 62.5 \times \frac{7999}{5786}}$$
 cu. in.

213 lb. troy of gold occupies
$$\frac{2\frac{13}{24} \times 1728}{19.36 \times 62.5 \times \frac{7988}{1988}}$$
 cu. in.

$$\frac{2\frac{14}{19.36} \times 1728}{19.36 \times 62.5 \times \frac{7000}{1980}} = \frac{2\frac{14}{19} \times 1728}{19\frac{9}{15} \times 62\frac{1}{2} \times \frac{7000}{1980}}$$

$$= \frac{61}{24} \times 1728 \times \frac{432}{484} \times \frac{2}{125} \times \frac{5760}{7000}$$

$$= \frac{316224}{105875} = 2.987.$$
2.987 cu. in. Ans.

10. How many pounds does a boy lift in raising a cubic foot of stone under water, if its specific gravity is $2\frac{1}{2}$?

The boy lifts $2\frac{1}{2}$ times the weight of a cubic foot of water less the weight of a cubic foot of water; that is, he lifts $1\frac{1}{2}$ times the weight of a cubic foot of water.

$$1\frac{1}{4} \times 62.5$$
 lb. = 93.75 lb. Ans.

11. A square-built scow 12 ft. long, 6½ ft. wide, sinks 5 in. into the water. What does it weigh, and how many pounds will be required to sink it 7 in. deeper?

The weight of the scow is equal to the weight of the water it displaces.

$$12 \times 6\frac{1}{2} \times \frac{5}{12} \times 62\frac{1}{2} = 12 \times \frac{13}{2} \times \frac{5}{12} \times \frac{125}{2} = \frac{8125}{4} = 2031\frac{1}{4}.$$

$$2031\frac{1}{4} \text{ lb. } Ans.$$

$$\begin{array}{c}
3 \\
6 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text{ lb.} = 2843 \\
4875 \text{ lb.} - 2031 \\
4875 \text$$

12. A square-built scow 11 ft. long, 5½ ft. wide, weighs 320 lb. and is loaded with 750 lb. of stone. How deep will it sink in the water?

The total weight of the scow is 320 lb. + 750 lb. = 1070 lb.

The volume in cubic feet of the water displaced is $\frac{1070}{62\frac{1}{2}}$.

The area in square feet of the top of the scow is $11 \times 5\frac{1}{4}$.

Therefore, the depth in feet the scow will sink is $\frac{1070}{62\frac{1}{2}}$ ÷ (11 × 5\frac{1}{2}),

and the depth in inches the scow will sink is $12 \times \frac{1070}{62\frac{1}{4}} \div (11 \times 5\frac{1}{4})$.

$$12 \times \frac{1070}{62\frac{1}{2}} \div (11 \times 5\frac{1}{4}) = 12 \times 1979 \times \frac{214}{125} \times \frac{1}{11} \times \frac{4}{21}$$
$$= \frac{6848}{1925} = 3\frac{1973}{925} = 3.557. \qquad 3.557 \text{ in. } Ans.$$

13. How many tons of ice, specific gravity 0.93, can be packed in a building 50 ft. long, 40 ft. wide, 20 ft. high?

$$\frac{50 \times 40 \times 20 \times 0.93 \times 62\frac{1}{2}}{2000} = \frac{50 \times 40 \times 20}{2000} \times \frac{93}{100} \times \frac{125}{2} = \frac{2325}{2}$$
$$= 1162\frac{1}{2}. Ans.$$

14. If the specific gravity of an iceberg is 0.9, how many cubic yards does an iceberg contain that is 40 rd. long, 6 yd. wide, and rises 160 ft. out of the sea?

40 rd. = 220 yd.;
$$160$$
 ft. = $53\frac{1}{2}$ yd.

$$220 \times 6 \times 53\frac{1}{3} = 220 \times \cancel{6} \times \frac{160}{3} = 70,400.$$

Now, if the specific gravity of the iceberg is 0.9, only $\frac{1}{10}$ of the iceberg is above the water.

$$10 \times 70,400$$
 cu. yd. = $704,000$ cu. yd. Ans.

15. If a cubic foot of brick wall weighs 90 lb. and contains 22 bricks, with the mortar, what is the weight and the specific gravity of a brick and its share of mortar?

90 lb.
$$\div 22 = 4\frac{1}{11}$$
 lb. Ans.

The specific gravity =
$$\frac{90}{62\frac{1}{4}} = \frac{18}{99} \times \frac{2}{125} = \frac{36}{25} = 1.44$$
. Ans.

16. What is the weight of a brick wall 40 ft. long, 20 ft. high, and 1 ft. thick, if the specific gravity of a brick with its mortar is 1.46? How many thousand bricks will be required for the wall, allowing 22 for a cubic foot?

$$40 \times 20 \times 1 \times 1.46 \times 62\frac{1}{2} = \cancel{40} \times \cancel{20} \times \cancel{\frac{146}{100}} \times \cancel{\frac{25}{2}} = 73,000.$$

73,000 lb. =
$$36\frac{1}{2}$$
 t. Ans. $40 \times 20 \times 1 \times 22 = 17,600$. Ans.

17. If the specific gravity of iron is 7.48, what is the weight of a cylindrical iron shell 1 in. thick and 2 ft. long, whose inner radius is 7 in.?

The outer radius is 8 in. $= \frac{2}{3}$ ft.

$$3.1416 \times \frac{2}{3} \times \frac{2}{3} \times 2 = \frac{8.3776}{3} = 2.7925.$$

The inner radius is 7 in. = $\frac{7}{12}$ ft.

$$0.1309 \atop 0.2618 \atop 3.1416 \times \frac{7}{12} \times \frac{7}{12} \times 2 = \frac{6.4141}{3} = 2.1380.$$

The volume of the shell =2.7925 cu. ft. -2.1380 cu. ft. =0.6545 cu. ft. The weight of the shell = $0.6545 \times 7.48 \times 62.5$ lb. =305.97875 lb. Ans.

62.5	467.5
7.48	0.6545
5000	23375
2500	18700
4375	23375
487.500	28050
	305.97875

18. If a piece of marble weighs 37.78 oz. in air, and 23.89 oz. in water, what is its volume and its specific gravity?

The weight of the water displaced by the marble is

$$37.78 \text{ oz.} - 23.89 \text{ oz.} = 13.89 \text{ oz.}$$

By Ex. 1, the volume of 1 oz. of water is 1.728 cu. in. Therefore, the volume of the marble is

 13.89×1.728 cu. in. = 24.00192 cu. in. Ans.

The specific gravity of the marble

$$\begin{array}{r}
1.728 \\
\underline{13.89} \\
15552 \\
13824 \\
5184 \\
\underline{1728} \\
24.00192
\end{array}$$

$$= 37.78 + 13.89 = 2.72. Ans.$$

$$\begin{array}{r}
2.72 \\
1389)3778. \\
\underline{2778} \\
10000 \\
\underline{9723} \\
2770
\end{array}$$

19. If a mass of lead weighs 1986 lb. in air, and 1811 lb. in water, what is its volume and its specific gravity?

The weight of the water displaced by the lead is 1986 lb. — 1811 lb. = 175 lb.

Since 1 cu. ft. of water weighs 621 lb., the volume of the lead is

$$\frac{175}{62\frac{1}{2}}$$
 cu. ft. = $\frac{7}{175} \times \frac{2}{125}$ cu. ft. = $\frac{14}{5}$ cu. ft. = $\frac{24}{5}$ cu. ft. Ans.

The specific gravity of the lead

$$= 1986\frac{1}{4} + 175 = \frac{7945}{4} \times \frac{1}{175} = \frac{227}{20} = 11\frac{7}{20} = 11.35. Ans.$$

Exercise 92. Page 201.

Express:

1. 59° F. in Centigrade scale; in Réaumur's scale.

$$59^{\circ} - 32^{\circ} = 27^{\circ}.$$
 $\frac{1}{5}$ of $27^{\circ} = 15^{\circ}.$
 $\therefore 1^{\circ} F. = \frac{80}{180^{\circ}} R. = \frac{4}{5^{\circ}} R.$
 $\frac{1}{5}$ of $27^{\circ} = 12^{\circ}.$
 $\frac{1}{5}$ of $27^{\circ} = 12^{\circ}.$
 $\frac{1}{5}$ of $27^{\circ} = 12^{\circ}.$
 $\frac{1}{5}$ of $27^{\circ} = 12^{\circ}.$

2. 77° F. in Centigrade scale; in Réaumur's scale.

$$77^{\circ} - 32^{\circ} = 45^{\circ}.$$
 $\frac{1}{2}$ of $45^{\circ} = 25^{\circ}.$
 $\frac{1}{2}$ of $45^{\circ} = 20^{\circ}.$
 $\frac{1}{2}$ of 77° F. $\frac{1}{2}$ $\frac{1}{2}$ of $\frac{1}{2}$ $\frac{1}{2}$ $\frac{1}{2}$ of $\frac{1}{2}$ \frac

3. 950° F. in Centigrade scale; in Réaumur's scale.

$$950^{\circ} - 32^{\circ} = 918^{\circ}.$$
 $\frac{5}{9}$ of $918^{\circ} = 510^{\circ}.$
 $\frac{4}{9}$ of $918^{\circ} = 408^{\circ}.$
 $\frac{5}{9}$ of $918^{\circ} = 408^{\circ}.$
 $\frac{5}{9}$ of $918^{\circ} = 408^{\circ}.$
 $\frac{5}{9}$ of $918^{\circ} = 408^{\circ}.$

4. - 40° F. in Centigrade scale; in Réaumur's scale.

- 40° F. is 72° below the freezing point.
§ of 72° = 40°.

$$\cdot \cdot \cdot - 40^{\circ}$$
 F. = - 40° C.
• of 72° = 32°.
 $\cdot \cdot \cdot - 40^{\circ}$ F. = - 32° R.

5. - 4° F. in Centigrade scale; in Réaumur's scale.

6. 10° C. in Fahrenheit's scale; in Réaumur's scale.

$$\frac{2}{5}$$
 of $10^{\circ} = 18^{\circ}$. $\frac{4}{5}$ of $10^{\circ} = 8^{\circ}$. $18^{\circ} + 32^{\circ} = 50^{\circ}$. 10° C. 10° C

7. 22° C. in Fahrenheit's scale; in Réaumur's scale.

$$\frac{2}{3}$$
 of $22^{\circ} = 39.6^{\circ}$.
 $\frac{4}{3}$ of $22^{\circ} = 17.6^{\circ}$.

 $39.6^{\circ} + 32^{\circ} = 71.6^{\circ}$.
 $\therefore 22^{\circ}$ C. = 17.6° R.

 $\therefore 22^{\circ}$ C. = 71.6° F.

8. – 30° C. in Fahrenheit's scale; in Réaumur's scale.

$$\frac{9}{5}$$
 of $30^{\circ} = 54^{\circ}$.

54° below the freezing point in Fahrenheit's scale is - 22°.

$$... - 30^{\circ} \text{ C.} = -22^{\circ} \text{ F.}$$

f of $30^{\circ} = 24^{\circ}.$ $... - 30^{\circ} \text{ C.} = -24^{\circ} \text{ R.}$

9. – 114° C. in Fahrenheit's scale; in Réaumur's scale.

$$\frac{9}{5}$$
 of $11\frac{3}{7}^{\circ} = 20\frac{4}{7}^{\circ}$.

204° below the freezing point in Fahrenheit's scale is 114°.

...
$$-113^{\circ}$$
 C. $=113^{\circ}$ F.
4 of $113^{\circ} = 93^{\circ}$ -113° C. $=-93^{\circ}$ R.

Exercise 93. Page 201.

1. If one man can do a piece of work in 9 days and another man can do the same work in 8 days, in how many days can the men working together do the work?

If one man can do the work in 9 days, in 1 day he can do ; of it.

If another man can do the work in 8 days, in 1 day he can do 1 of it.

Both together can do $\frac{1}{6} + \frac{1}{6} = \frac{17}{2}$ of the work in 1 day.

Therefore, both together can do the work in $\frac{72}{17}$ days, or $4\frac{4}{17}$ days.

Ans.

- 2. A cistern can be filled by a water-pipe in 30 min., and emptied by a waste-pipe in 20 min. If the cistern is full and both pipes are opened, in how many minutes will the cistern be emptied?
 - If the water-pipe will fill the cistern in 30 min., in 1 min. it will fill $\frac{1}{30}$ of the cistern.
 - If the waste-pipe will empty the cistern in 20 min., in 1 min. it will empty $\frac{1}{20}$ of the cistern.

When both are opened $\frac{1}{20} - \frac{1}{30} = \frac{1}{60}$ will be emptied each minute.

- Therefore, when both are opened, the cistern will be emptied in $\frac{\beta_0}{r}$ min., or 60 min. Ans.
- 3. If A can mow a certain meadow in 4 days, and B in 3 days, how long will it take both together?

If A can mow the meadow in 4 days, in 1 day he can mow 1 of it.

If B can mow the meadow in 3 days, in 1 day he can mow $\frac{1}{3}$ of it.

Both together can mow $\frac{1}{4} + \frac{1}{3} = \frac{7}{12}$ of the meadow in 1 day.

Therefore, both together can mow the meadow in 1/2 days, or 15/4 days. Ans.

4. If A can lay a certain wall in 4½ days, and B in 5½ days, how long will it take both together?

If A can lay the wall in $4\frac{1}{4}$ days, in 1 day he can lay $\frac{1}{4\frac{1}{4}} = \frac{2}{6}$ of it.

If B can lay the wall in $5\frac{1}{2}$ days, in 1 day he can lay $\frac{1}{5\frac{1}{2}} = \frac{2}{11}$ of it. Both together can lay $\frac{2}{5} + \frac{2}{11} = \frac{4}{5}$ of it in 1 day.

Therefore, both together can lay the wall in 28 days, or 218 days. Ans.

5. If one pipe will fill a cistern in 4½ hr., and another pipe in 3½ hr., how long will it take both together to fill the cistern?

If one pipe will fill the cistern in $4\frac{1}{2}$ hr., in 1 hr. it will fill $\frac{1}{4\frac{1}{2}} = \frac{2}{3}$ of it.

If another pipe will fill the cistern in $3\frac{1}{2}$ hr., in 1 hr. it will fill $\frac{1}{3\frac{1}{2}} = \frac{3}{4}$ of it.

Both pipes together will fill $\frac{2}{5} + \frac{3}{7} = \frac{3}{5}\frac{2}{5}$ of the cistern in 1 hr.

Therefore, both pipes together will fill the cistern in $\frac{68}{32} = 1\frac{81}{32}$ hr. Δns .

6. If A can go from Boston to Albany in 9½ hr., and B from Albany to Boston in 11½ hr., and they start at the same time, in how many hours will they meet?

If A can go in $9\frac{1}{4}$ hr., in 1 hr. he can go $\frac{1}{9\frac{1}{4}} = \frac{4}{37}$ of the distance.

If B can go in 11½ hr., in 1 hr. he can go $\frac{1}{114} = \frac{3}{34}$ of the distance.

Both together can go $\frac{4}{37} + \frac{8}{84} = \frac{247}{1258}$ of the distance in 1 hr.

Therefore, they will meet in $\frac{1258}{247}$ hr. = $5\frac{23}{247}$ hr. Ans.

7. If it takes A working alone 4 days, B 3 days, and C 4½ days to do a piece of work, how long will it take to do the work if all three work together?

If A can do the work in 4 days, in 1 day he can do 1 of it.

If B can do the work in 3 days, in 1 day he can do 1 of it.

If C can do the work in $4\frac{1}{2}$ days, in 1 day he can do $\frac{1}{4\frac{1}{4}} = \frac{2}{3}$ of it.

All together can do $\frac{1}{4} + \frac{1}{3} + \frac{2}{3} = \frac{2}{3}$ of the work in 1 day.

Therefore, it will take them, all working together, $\frac{3}{2}$ days = $1\frac{7}{29}$ days. Ans.

8. A can mow § of a field in 3 days; B can mow § of it in 4 days. How long will it take both together to mow the field?

If A can mow the field in 53 days, in 1 day he can mow $\frac{1}{53} = \frac{5}{27}$ of it.

If B can mow the field in 6 days, in 1 day he can mow 1 of it.

Both together can mow $\frac{5}{27} + \frac{1}{6} = \frac{19}{54}$ of the field in 1 day.

Therefore, both together can mow the field in \$4 days = 214 days.

Ans.

9. One pipe can fill a cistern half full in \(\frac{1}{4} \) of an hour, and another can fill it three quarters full in \(\frac{1}{4} \) an hour. How long will it take both pipes together to fill the cistern?

$$\frac{3}{4}$$
 hr. $+\frac{1}{2} = \frac{1}{2}$ hr. $+\frac{3}{4} = \frac{3}{8}$ hr.

If one pipe can fill the cistern in $1\frac{1}{2}$ hr., in 1 hr. it can fill $\frac{1}{1\frac{1}{2}} = \frac{3}{2}$ of it.

If another pipe can fill the cistern in $\frac{3}{4}$ hr., in 1 hr. it can fill $\frac{1}{\frac{3}{4}} = \frac{3}{4}$ of it.

Both together can fill $\frac{2}{3} + \frac{3}{2} = \frac{13}{6}$ of the cistern in 1 hr.

Therefore, both together can fill the cistern in $6 \div 13 = \frac{6}{18}$ hr. Ans.

10. A pipe can fill a cistern one third full in \(\frac{1}{4} \) of an hour; a wastepipe can empty one fourth of the cistern in 20 minutes. If both pipes are opened, in what time will the cistern be filled?

$$3 \times \frac{1}{4} \text{ hr.} = \frac{3}{4} \text{ hr.} = 45 \text{ min.}$$
; $4 \times 20 = 80 \text{ min.}$

The water-pipe can fill 45 every minute.

The waste-pipe can empty 1 every minute.

When both are open, $\frac{1}{43} - \frac{1}{80} = \frac{7}{720}$ is gained every minute.

Therefore, the whole will be filled in 130 min. = 1024 min. Ans.

11. A cistern that will hold 100 gallons can be filled by a pipe in 25 minutes, and emptied by a waste-pipe in 45 minutes. If the cistern is empty and both pipes are opened, how long will it take to fill the cistern, and how much water will be wasted?

The water-pipe fills 1/25 every minute.

The waste-pipe empties $\frac{1}{45}$ every minute.

When both are open, $\frac{1}{25} - \frac{1}{45} = \frac{1}{225}$ is gained every minute.

Therefore, the whole will be filled in $\frac{325}{4}$ min. = 56\frac{1}{4} min. Ans.

If $\frac{1}{48}$ of the cistern is wasted every minute, the number of gallons

wasted =
$$56\frac{1}{4} \times \frac{1}{45}$$
 of $100 = \frac{225}{4} \times \frac{1}{45} \times \frac{25}{100} = 125$. 125 gal. Ans.

12. If water runs into a cistern by one pipe at the rate of 2 gal.' in 3 min., by another at the rate of 5 gal. in 4 min., and runs out by a third at the rate of 4 gal. in 5 min., how long will it take to gain 71 gal. in the cistern?

2 gal. $\div 3 = \frac{2}{3}$ gal. $\div 5 = \frac{4}{3}$ gal. $\div 5 = \frac{4}{3}$ gal. $\div 5 = \frac{4}{3}$ gal.

If one pipe pours in $\frac{2}{3}$ gal. per minute, another pours in $\frac{5}{4}$ gal. per minute, and another empties $\frac{4}{3}$ gal. per minute, the cistern gains $\frac{3}{4} + \frac{5}{4} - \frac{4}{5} = \frac{67}{65}$ gal. per minute.

Therefore, it will take as many minutes to gain 71 gal. as $71 \div \frac{67}{67} = 63\frac{27}{67}$.

63\frac{27}{67} \text{min. } Ans.

13. A can do a piece of work in 6 days, and B can do it in 7 days. If they work together 2 days, and A then leaves, how long will it take B to finish the work?

If A can do the work in 6 days, in 1 day he can do 1 of it.

If B can do the work in 7 days, in 1 day he can do 1 of it.

A and B together can do $\frac{1}{6} + \frac{1}{7} = \frac{13}{2}$ of the work in 1 day, and in 2 days can do $2 \times \frac{13}{2} = \frac{13}{4}$ of the work.

The part of the work then not done is $\frac{21}{21} - \frac{13}{21} = \frac{3}{21}$.

To do $\frac{8}{21}$ of the work, it will take B $(\frac{8}{21} \div \frac{1}{7})$ days = $2\frac{2}{3}$ days. Ans.

14. A cistern that will hold 200 gal. has two pipes; one will supply 0.15 gal. a second, the other 1\frac{1}{2} qt. a second. If the first is turned on for 10 minutes, and afterwards both run together, in what time will the cistern be filled?

0.15 gal. per sec. is 60×0.15 gal. = 9 gal. per min.

1 gt. per sec. is 60×1 gt. = 24 gal. per min.

In 10 min. the first pipe will supply 10×9 gal. = 90 gal.

There remains to be filled 200 gal. -90 gal. =110 gal.

Since the two pipes together supply 9 gal. +24 gal. =33 gal. per minute, to supply 110 gal. will require $\frac{110}{13}$ min. $=3\frac{1}{1}$ min. $=3\frac{1}{1}$ min. $=3\frac{1}{1}$ min.

15. A and B together can do a piece of work in 15 days. After working together 6 days, A leaves and B finishes the work in 30 days more. In how many days can each alone do the work?

A and B together can do $\frac{1}{15}$ of the work in 1 day, and in 6 days can do $6 \times \frac{1}{15} = \frac{2}{5}$ of the work.

There remains $\frac{3}{5} - \frac{3}{5} = \frac{3}{5}$ of the work to be done.

If B can do $\frac{1}{2}$ of the work in 30 days, B alone can do the work in $\frac{1}{2}$ of 30 days = 50 days. Ans.

B alone can do $\frac{1}{50}$ of the work in 1 day.

Therefore, A alone can do $\frac{1}{15} \div \frac{1}{50} = \frac{7}{150}$ of the work in 1 day.

Therefore, A alone can do the work in 150 days = 214 days. Ans.

16. A and B together can do a piece of work in 12 days. After working together 9 days, however, they call in C to help them, and the three finish the work in 2 days. In how many days can C alone do the work?

A and B together can do $\frac{1}{12}$ of the work in 1 day, and in 9 days can do $9 \times \frac{1}{12} = \frac{3}{4}$ of the work.

There remains $\frac{1}{4} - \frac{3}{4} = \frac{1}{4}$ of the work to be done.

If A, B, and C together can do $\frac{1}{4}$ of the work in 2 days, to do the whole work would require them 4×2 days = 8 days.

Therefore, C alone in 1 day can do $\frac{1}{3} - \frac{1}{12} = \frac{1}{24}$ of the work.

Therefore, C alone can do the work in 24 days. Ans.

17. A and B can do a piece of work in 2½ days; A and C in 3½ days; B and C in 3½ days. How long will it take the three working together to do the work, and how long will it take each alone?

If A and B can do the work in $2\frac{1}{2}$ days, they can do $\frac{1}{2\frac{1}{2}} = \frac{2}{5}$ of it in 1 day.

If A and C can do the work in $3\frac{1}{8}$ days, they can do $\frac{1}{3\frac{1}{8}} = \frac{3}{10}$ of it in 1 day.

If B and C can do the work in $3\frac{3}{4}$ days, they can do $\frac{1}{3\frac{3}{4}} = \frac{4}{15}$ of it in 1 day.

All together in 2 days can do $\frac{2}{5} + \frac{3}{10} + \frac{4}{15} = \frac{29}{30}$ of the work.

Hence, by working 1 day each they can do ½ of 3% or 3% of the work.

Therefore, all together can do the work in $\frac{9}{2}$ days= $2\frac{2}{19}$ days. Ans.

In 1 day A can do $\frac{28}{80} - \frac{4}{15} = \frac{18}{80}$ of the work.

Therefore, A can do the work in $\frac{60}{13}$ days = $4\frac{3}{13}$ days. Ans.

In 1 day B can do $\frac{29}{60} - \frac{3}{10} = \frac{11}{60}$ of the work.

Therefore, B can do the work in $\frac{60}{11}$ days = $5\frac{5}{11}$ days. Ans.

In 1 day C can do $\frac{29}{60} - \frac{2}{5} = \frac{1}{12}$ of the work.

Therefore, C can do the work in 12 days. Ans.

18. A and B together can do a piece of work in 48 days; A and C together in 30 days; B and C together in 26 days. How long will it take each alone to do the work?

If A and B can do the work in 48 days, they can do $\frac{1}{48}$ of it in 1 day.

If A and C can do the work in 30 days, they can do $\frac{1}{30}$ of it in 1 day.

If B and C can do the work in $26\frac{2}{3}$ days, they can do $\frac{1}{26\frac{2}{3}} = \frac{3}{50}$ of it in 1 day.

All together in 2 days can do $\frac{1}{48} + \frac{1}{80} + \frac{3}{80} = \frac{11}{120}$ of the work.

Hence, by working 1 day each, they can do $\frac{1}{4}$ of $\frac{11}{120}$ or $\frac{11}{240}$ of the work.

In 1 day A can do $\frac{11}{240} - \frac{3}{80} = \frac{1}{120}$ of the work.

Therefore, A can do the work in 120 days. Ans.

In 1 day B can do $\frac{11}{240} - \frac{1}{30} = \frac{1}{30}$ of the work.

Therefore, B can do the work in 80 days. Ans.

In 1 day C can do $\frac{11}{440} - \frac{1}{48} = \frac{1}{40}$ of the work.

Therefore, C can do the work in 40 days. Ans.

19. A cistern has three pipes. The first and second will fill it in 1 hr. 10 min.; the first and third in 1 hr. 24 min.; the second and third in 2 hr. 20 min. How long will it take each alone to fill the cistern?

1 hr. 10 min. = $1\frac{1}{6}$ hr.; 1 hr. 24 min. = $1\frac{2}{3}$ hr.; 2 hr. 20 min. = $2\frac{1}{3}$ hr.

If the 1st and 2d will fill the cistern in $1\frac{1}{6}$ hr., they will fill $\frac{1}{1\frac{1}{6}} = \frac{4}{7}$ of it in 1 hr.

If the 1st and 3d will fill the cistern in $1\frac{2}{3}$ hr., they will fill $\frac{1}{1\frac{2}{3}} = \frac{3}{7}$ of it in 1 hr.

If the 2d and 3d will fill the cistern in $2\frac{1}{3}$ hr., they will fill $\frac{1}{2\frac{1}{3}} = \frac{3}{7}$ of it in 1 hr.

All together in 2 hr. will fill \$ + \$ + \$ = 4 of the cistern.

Hence, in 1 hr. the three together will fill $\frac{1}{2}$ of $\frac{1}{2} = \frac{7}{7}$ or the whole cistern.

In 1 hr., the 1st will fill $\frac{7}{7} - \frac{3}{7} = \frac{4}{7}$ of the cistern.

Therefore, 1st will fill the cistern in $\frac{7}{4}$ hr. = 1 hr. 45 min. Ans.

In 1 hr., the 2d will fill $\frac{7}{4} - \frac{5}{4} = \frac{2}{4}$ of the cistern.

Therefore, 2d will fill the cistern in $\frac{7}{4}$ hr. =3 hr. 30 min. Ans.

In 1 hr., the 3d will fill 7-9=1 of the cistern.

Therefore, the 3d will fill the cistern in 7 hr. Ans.

- 20. A, B, and C together can do a piece of work in 10 days; A and B together in 12 days; B and C together in 20 days. How long will it take each alone to do the work?
 - If A, B, and C can do the work in 10 days, they can do $\frac{1}{10}$ of it in 1 day.

If A and B can do the work in 12 days, they can do $\frac{1}{12}$ of it in 1 day.

If B and C can do the work in 20 days, they can do $\frac{1}{20}$ of it in 1 day.

In 1 day C can do $\frac{1}{10} - \frac{1}{12} = \frac{1}{60}$ of the work.

Therefore, C can do the work in 60 days. Ans.

In 1 day B can do $\frac{1}{20} - \frac{1}{60} = \frac{1}{30}$ of the work.

Therefore, B can do the work in 30 days. Ans.

In 1 day A can do $\frac{1}{12} - \frac{1}{30} = \frac{1}{10}$ of the work.

Therefore, A can do the work in 20 days. Ans.

Exercise 94. Page 204.

1. A train travels 24 miles in 0.8 of an hour. Find its rate per hour.

24 mi.
$$\div$$
 0.8 = 30 mi. Ans.

2. A train runs from New York to Philadelphia, 90 miles, in 1 hr. 33 min. What is its rate per hour?

1 hr. 33 min. =
$$1\frac{11}{20}$$
 hr.

90 mi.
$$+ 1\frac{11}{20} = \frac{20}{31}$$
 of 90 mi. $= \frac{1800}{31}$ mi. $= 58\frac{3}{31}$ mi. Ans.

3. A train runs from New York to Philadelphia, 90 miles, in 2 hr. 5 min. What is its rate per hour?

2 hr. 5 min. =
$$2\frac{1}{12}$$
 hr.

90 mi.
$$+2\frac{1}{12} = \frac{12}{25}$$
 of 99 mi. $=\frac{216}{5}$ mi. $=43\frac{1}{5}$ mi. Ans.

4. Winlock, in 1869, found that electricity went through 7200 miles of wire in 3 of a second. What was its rate per second?

7200 mi.
$$\div \frac{2}{3} = \frac{3}{2}$$
 of 7299 mi. = 10,800 mi. Ans.

5. If the time required for a signal to pass through the cable from Brest to Duxbury, 3799 miles, is 0.816 of a second, what is the rate per second?

3799 mi. + 0.816 = 4655.637 mi. Ans.

6. If the report of a gun 1½ miles distant is heard in 5\{ \text{seconds} after the flash is seen, what is the velocity of sound in feet per second?

$$\frac{1\frac{1}{4} \times 5280}{5\frac{5}{8}} = \frac{5}{4} \times \frac{1760}{5289} \times \frac{\frac{2}{8}}{\frac{45}{3}} = \frac{3520}{3} = 1173\frac{1}{3}.$$
 1173\frac{1}{3} ft. Ans.

7. If a man walks 31 miles in 46 minutes, what is his rate per hour?

8. If a horse goes 48 miles in 10 hr. 40 min., what is his average rate per hour?

10 hr. 40 min. =
$$10\frac{2}{3}$$
 hr.

48 mi.
$$+ 10\frac{3}{3} = \frac{3}{32} \times \frac{3}{48}$$
 mi. $= \frac{9}{2}$ mi. $= 4\frac{1}{2}$ mi. Ans.

9. If a stone on a glacier is carried 95½ feet in 188 days, what is its rate in inches per day?

$$\frac{95\frac{1}{4} \times 12}{188} = \frac{191}{2} \times \frac{\cancel{12}}{\cancel{188}} = \frac{573}{94} = 6\frac{9}{\cancel{14}}. \qquad 6\frac{9}{\cancel{14}} \text{ in. } Ans.$$

10. If a horse went 5½ miles in 33 minutes, how long did it take him to go a mile?

33 min.
$$\div 5\frac{1}{2} = \frac{2}{11}$$
 of 33 min. = 6 min. Ans.

11. If a horse can trot $\frac{1}{2}$ of a mile in $2\frac{1}{2}$ minutes, in what time can he trot a mile?

$$2\frac{1}{3}$$
 min. $\div \frac{5}{6} = \frac{\cancel{6}}{5} \times \frac{7}{3}$ min. $= \frac{14}{5}$ min. $= 2\frac{4}{5}$ min. Ans.

12. If a train runs 18 miles in 39 minutes, how long does it take to run one mile?

39 min.
$$\div$$
 18 = $2\frac{1}{6}$ min. Ans.

13. If sound travels 1125 feet a second, how long will it take to travel one mile?

14. If a train requires 3 hours to run 1041 miles, find its average time for running a mile.

$$3 \text{ hr.} = 180 \text{ min.}$$

180 min.
$$+ 104\frac{1}{417} = \frac{4}{417} \times 189 \text{ min.} = \frac{240}{139} \text{ min.} = 1\frac{101}{139} \text{ min.}$$

= 1 min. 43.6 sec. Ans.

15. If a man cuts 7½ A. of grass in 3½ days, what part of a day will it take him to cut an acre? If 10 hr. makes a day, what part of an acre will he cut in an hour?

$$\frac{\frac{3\frac{1}{4}}{7\frac{1}{2}} = \frac{7}{15}}{\frac{3}{15}} = \frac{\frac{7}{15}}{\frac{3}{2}} \times \frac{2}{7} \times \frac{1}{10} = \frac{3}{14}.$$

$$\frac{\frac{7\frac{1}{4}}{3\frac{1}{2} \times 10}}{\frac{3}{2} \times \frac{2}{7}} \times \frac{2}{7} \times \frac{1}{10} = \frac{3}{14}.$$

$$\frac{\frac{3}{14}}{2} \text{ A. Ans.}$$

16. If a mower cuts 3½ square rods in ½ of an hour, how many acres will he cut in a day of 10 hours?

$$3\frac{1}{2}$$
 sq. rd. $\div \frac{1}{8} = 28$ sq. rd. 10×28 sq. rd. $= 280$ sq. rd. $= 1\frac{3}{4}$ A. Ans.

17. If a fountain yields 117½ gallons of water in ¾ of an hour, at what rate per hour is the water flowing?

117½ gal.
$$+\frac{3}{4} = \frac{\frac{2}{4}}{3} \times \frac{235}{2}$$
 gal. $=\frac{470}{3}$ gal. $=156$ 3 gal. Ans.

18. If a merchant's profits are \$3147 in 7½ months, what will be his profits at the same rate for a year?

$$12 \times \frac{\$3147}{7\frac{1}{2}} = \cancel{12} \times \frac{2}{\cancel{15}} \times \$3147 = \$\frac{25176}{5} = \$5035.20. \ Ans.$$

19. If a wheel turns 17° 30' in 35 minutes, in how many hours does it make a complete revolution?

$$17^{\circ} 30' \div 35 = \frac{1}{2}^{\circ}$$
.
 $360 \div \frac{1}{2} = 720$. $720 \text{ min.} = 12 \text{ hr. } Ans.$

20. If a man's expenditures are \$4358 in 13\frac{1}{4} months, what is his yearly rate of expenditure?

$$12 \times \frac{\$4358}{13\frac{1}{8}} = \cancel{12} \times \frac{3}{\cancel{40}} \times \cancel{\$\cancel{4358}} = \cancel{\$}\frac{19611}{5} = \cancel{\$}3922.20. \ Ans.$$

21. If a cistern loses by leakage 7 gal. 1 pt. in 49 hr. 40 min., what is its hourly rate of loss?

49 hr. 40 min. =
$$49\frac{2}{3}$$
 hr.
7 gal. 1 pt. = 57 pt.
57 pt. + $49\frac{2}{3} = \frac{2}{149} \times 57$ pt. = $\frac{171}{149}$ pt. = $1\frac{22}{149}$ pt. Ans.

22. If a man travels 33 miles in 72 minutes, how many miles will he travel in 50 minutes? How long will it take him to travel 50 miles?

7½ min. ÷ 3½ =
$$\frac{5}{18} \times \frac{15}{2}$$
 min. = $\frac{25}{12}$ min. = $2\frac{1}{12}$ min.
50 ÷ $2\frac{1}{12} = \frac{12}{25} \times \frac{2}{50} = 24$. 24 mi. Ans.
3½ mi. ÷ $7\frac{1}{2} = \frac{2}{15} \times \frac{15}{5}$ mi. = $\frac{12}{25}$ mi.
50 ÷ $\frac{12}{25} = \frac{25}{12} \times \frac{25}{50} = \frac{625}{6} = 104$.
6 104½ min. Ans.

Exercise 95. Page 206.

1. At what time between 5 and 6 o'clock do the hour and minute hands of a clock coincide?

Since in one hour the hour hand moves through 5 minute-spaces, and the minute hand through 60 minute-spaces, the minute hand moves 12 times as fast as the hour hand, and in moving through 12 minute-spaces gains 11 minute-spaces.

When the hour hand is at V, the minute hand, being at XII, is 25 minute-spaces behind. Since to gain 11 minute-spaces the minute hand must move through 12 minute-spaces, to gain 1 minute-space the minute hand must pass through $\frac{12}{11}$ of 1 minute-space, and to gain 25 minute-spaces, it must pass through $\frac{12}{11}$, or $\frac{27}{11}$ minute-spaces.

Hence, the hands coincide when the minute hand has moved through $27\frac{3}{11}$ minute-spaces; that is, at $27\frac{3}{11}$ minutes after 5 o'clock. Ans.

- 2. At what time between 10 and 11 o'clock do the hour and minute hands of a watch coincide?
 - At 10 o'clock the minute hand is 50 minute-spaces behind the hour hand.

$$50 \times \frac{12}{11} = \frac{600}{11} = 54\frac{6}{11}$$
. $54\frac{6}{11}$ minutes after 10 o'clock. Ans.

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- 3. At what time between 1 and 2 o'clock do the hour and minute hands of a clock coincide?
 - At 1 o'clock the minute hand is 5 minute-spaces behind the hour hand.

 $5 \times \frac{12}{12} = \frac{49}{12} = \frac{5}{12}$

5,5 minutes after 1 o'clock. Ans.

- 4. At what time between 8 and 9 o'clock are the hands of a clock exactly opposite each other?
 - At 8 o'clock the minute hand is 40 minute-spaces behind the hour hand, and should be 30 minute-spaces behind the hour hand.
 - Therefore, the minute hand must gain 40 30, or 10 minute-spaces on the hour hand.

 $10 \times \frac{12}{12} = \frac{120}{10} = 10\frac{1}{10}$. 10\frac{1}{2}\$ minutes after 8 o'clock. Ans.

- 5. At what time between 11 and 12 o'clock are the hands of a clock exactly opposite each other?
 - At 11 o'clock the minute hand is 55 minute-spaces behind the hour hand, and should be 30 minute-spaces behind the hour hand.
 - Therefore, the minute hand must gain 55 30, or 25 minute-spaces on the hour hand.

 $25 \times \frac{12}{11} = \frac{800}{11} = 27\frac{8}{11}$. $27\frac{8}{11}$ minutes after 11 o'clock. Ans.

- 6. At what time between 4 and 5 o'clock are the hands of a clock exactly opposite each other?
 - At 4 o'clock the minute hand is 20 minute-spaces behind the hour hand, and should be 30 minute-spaces ahead of the hour hand.
 - Therefore, the minute hand must gain 20 + 30, or 50 minute-spaces on the hour hand.

 $50 \times \frac{12}{11} = \frac{600}{11} = 54\frac{6}{11}$. $54\frac{6}{11}$ minutes after 4 o'clock. Ans.

- 7. At what time between 2 and 3 o'clock do the hands of a clock make right angles with each other?
 - At 2 o'clock the minute hand is 10 minute-spaces behind the hour hand, and should be 15 minute-spaces ahead of the hour hand.
 - Therefore, the minute hand must gain 10 + 15, or 25 minute-spaces on the hour hand.

 $25 \times \frac{1}{11} = \frac{300}{11} = 27\frac{3}{11}$

27 minutes after 2 o'clock. Ans.

- 8. At what times between 6 and 7 o'clock do the hands of a watch make right angles with each other?
 - At 6 o'clock the minute hand is 30 minute-spaces behind the hour hand, and should be 15 minute-spaces behind, or 15 minute-spaces ahead of the hour hand.
 - Therefore, the minute hand must gain 30 15, or 15 minute-spaces on the hour hand, or must gain 30 + 15, or 45 minute-spaces on the hour hand.

$$15 \times \frac{13}{13} = \frac{180}{11} = 16\frac{4}{11}$$
. $45 \times \frac{13}{12} = \frac{540}{11} = 49\frac{1}{11}$.

164 minutes after 6 o'clock, or 491 minutes after 6 o'clock.

Ans.

- 9. At what time between 7 and 8 o'clock do the hands of a watch make an angle of 120° with each other?
 - At 7 o'clock the minute hand is 35 minute-spaces behind the hour hand, and should be 20 minute-spaces behind.
 - Therefore, the minute hand must gain 35 20, or 15 minute-spaces on the hour hand.

$$15 \times \frac{12}{11} = \frac{180}{11} = 16\frac{4}{11}$$
. $16\frac{4}{11}$ minutes after 7 o'clock. Ans.

- 10. At what time between 12 and 1 o'clock do the hands of a watch make an angle of 60° with each other?
 - At 12 o'clock the hour and minute hands coincide, and the minute hand should be 10 minute-spaces ahead of the hour hand.
 - Therefore, the minute hand must gain 10 minute-spaces on the hour hand.

$$10 \times \frac{13}{11} = \frac{120}{11} = 10\frac{19}{11}$$
. $10\frac{19}{11}$ minutes after 12 o'clock. Ans.

TEACHERS' EDITION.

Exercise 96. Page 208.

Make out receipted bills for the following accounts, supplying dates:

1. James Hardy bought of C. H. Mills 275 bbl. flour, at \$6.75; 324 bbl. flour, at \$6.25; 300 bu. potatoes, at 48 cents; 1578 lb. butter, at 32 cents; 2000 bbl. apples, at \$1.25; a car-load (20,000 lb.) of oats, at 42 cents a bushel; a car-load (28,575 lb.) of corn, at 55 cents a bushel.

Mr. James Hardy,

Boston, Mass., March 1, 1898.

To C. H. MILLS, DR.

1898					
Jan.	5	To 275 bbl. Flour	@ \$6.75	₹ 1856	25
	12	To 324 bbl. Flour	@ 6.25	2025	00
	19	To 300 bu. Potatoes	@ 0.48	144	00
	26	To 1578 lb. Butter	@ 0.32	504	96
Feb. •	2	To 2000 bbl. Apples	@ 1.25	2500	00
	`	To 20,000 lb. Oats, 625 bu.	@ 0.42	262	50
	9	To 28,575 lb. Corn, 510.27 bu.	@ 0.55	280	65
				\$ 7573	36

1898, March 10.

Received Payment,

C. H. Mills.

2. James Harlow bought of John Pike 12 bales, 480 lb. each, Texas cotton, at 9½ cents; 7 bales, 502 lb. each, upland, at 10½ cents; 3 bales, 492 lb. each, low middling, at 9½ cents; 18 bales, 490 lb. each, good ordinary, at 9 cents.

Boston, Mass., March 1, 1898.

Mr. James Harlow,

To JOHN PIKE, DR.

1898						
Jan.	7	To 12 bales Texas Cotton, 5760 lb.	@	91 ¢	\$ 532	80
•	14	To 7 bales Upland, 3514 lb.		101 4	360	19
	21	To 3 bales Low middling, 1476 lb.	@	93 ¢	143	91
Feb.	14	To 18 bales Good ordinary, 8820 lb.	@	9¢	' 79 3	80
					\$ 1830	70

1898, March 10.

Received Payment,

John Pike.

3. Richard Rowe bought of John Doe 125 lb. sugar, at 5 cents; 1 bag coffee, 115 lb., at 32 cents a pound; 25 gal. molasses, at 38 cents; 8 lb. Japan tea, at 92 cents; 28 lb. crackers, at 8 cents; 2 bbl. flour, at \$7.50.

Mr. Richard Rowe,

Boston, Mass., March 1, 1898.

To JOHN DOE, DR.

1898					
${\it Feb}$.	3	To 125 lb. Sugar	@ 5 %	\$ 6	25
		To 1 bag Coffee, 115 lb.	@ 324	3 6	80
		To 25 gal. Molasses	@ 38 4	9	50
	10	To 8 lb. Japan Tea	@ 924	7	36
		To 28 lb. Crackers	@ 84	2	24
		To 2 bbl. Flour	@ # 7.50	15	00
			-	\$77	15

1898, March 10.

Received Payment,

John Doe.

4. William Litchfield bought of John Garvin 8 bags cracked corn, at 75 cents; 4 bags oats, at 80 cents; 16 lb. sweet potatoes, at 3½ cents; 2 bu. potatoes, at \$1.10; 100 lb. wire nails, at 2½ cents; 5 lb. coffee, at 35 cents.

Mr. William Litchfield,

Boston, Mass., March 1, 1898.

To JOHN GARVIN, DR.

1898	1					
Feb.	8	To 8 bags Cracked Corn	@	75 \$	\$ 6	00
		To 4 bags Oats	@	80 \$	3	20
		To 16 lb. Sweet Potatoes	@	31 4	0	5 2
	18	To 2 bu. Potatoes	@	1.10	2	20
		To 100 lb. Wire Nails	@	21 0	2	25
		To 5 lb. Coffee	@	35¢	1	75
					\$ 15	92

1898, March 10.

Received Payment,

John Garvin.

5. Amos Tuck sold to Aaron Young 11 lb. ham, at 15 cents; 22 lb. beefsteak, at 24 cents; 18 lb. mutton, at 13 cents; 14 lb. veal, at 11 cents; and took in exchange 5 doz. eggs, at 18 cents; 15 lb. butter, at 26 cents; 9 bu. potatoes, at 40 cents; and 2 bbl. apples, at \$1.35.

Mr. Amos Tuck,

Boston, Mass., March 1, 1898.

To AARON YOUNG, DR.

		Bala	nce due				#0	29
	22	By 14 lb. Veal	@	114	1	54	10	81
	8	By 18 lb. Mutton	@	134	2	34		
Feb.	1	By 22 lb. Beefsteak	@	249	5	28		
Jan.	25	By 11 lb. Ham	@	15 \$	# 1	65		
		Cr.						
	15	To 2 bbl. Apples	@	1.35	2	70	# 11	10
	7	To 9 bu. Potatoes	@	409	3	60	 	
Feb.	4	To 15 lb. Butter	@	26 %	3.	90		
1898 Jan .	25	To 5 doz. Eggs	@	18¢	# 0	90		

1898, March 10.

Received Payment,

Aaron Young.

6. W. G. Fernald sold to John Waldron 35 lb. sugar, at 5 cents; 18 lb. coffee, at 35 cents; 20 lb. rice, at 8 cents; 4 tons hay, at \$15.75; 3 cords pine wood, at \$2.75; 4 cords hard wood, at \$3.50; 8 tons furnace coal, at \$6.75; 5 tons stove coal, at \$7.25; 8 rolls wall paper, at 35 cents; and took in exchange 25 bbl. apples, at \$1.15; 32 bu. pears, at 60 cents; and 42 bu. blueberries, at 8 cents a quart.

Mr. John Waldron,

Boston, Mass., Aug. 1, 1898.

To W. G. FERNALD, DR.

		Balance de	ue				# 32	48
		1344 qt.	@	8 🕏	107	52	155	47
July	23	By 42 bu. Blueberries,						
1898				,				
		By 32 bu. Pears	<u>@</u>	60 \$	19	20		
Oct.	13	By 25 bbl. Apples	@	8 1.15	\$ 28	75		
1897		Cr.						
June	20	To 8 rolls Wall Paper	@	35 ¢	2	80	# 187	95
	İ	To 5 t. Stove Coal	@	7.25	3 6	25		
	14	To 8 t. Furnace Coal	@	6.75	54	00		
		To 4 cd. Hard Wood	@	3. 50	14	00		
Mar.	7	To 3 cd. Pine Wood	@	2.75	8	25		
		To 4 t. Hay	@	15.75	63	00		
Feb.	26	To 20 lb. Rice	@	84	1	60		
	18	To 18 lb. Coffee	@	35 g	6	30		
Jan.	10	To 35 lb. Sugar	@	5 ¢	# 1	75		
<i>1898</i>								ļ

1898, August 5.

Received Payment,

W G Fernald

7. C. A. Colton bought of Green, Fisk & Co. 4 doz. No. 7 teakettles, at 85 cents each; 2 safety ash barrels, at \$2.50; 3 doz. common scrapers, at 50 cents a dozen; 8 eagle shovels, at 10 cents; ½ doz. 8 by 12 black registers, at \$1.50 each; ½ doz. spice boxes, at 55 cents each; ½ doz. 14-qt. dish pans, at \$6.00 a dozen; 2 doz. common stove lifters, at 50 cents a dozen; ½ doz. 12 by 14 drip pans, at \$4.00 a dozen; ½ gross retinned teaspoons, at 25 cents a dozen; 1 doz. ash sifters, at \$1.00 each.

Mr. C. A. Colton,

Boston, Mass., March 1, 1898.

To GREEN, FISK & CO., Dr.

1898					
Mar.	1	To 4 doz. No. 7 Teakettles	@ 85 \$	# 40	80
		To 2 Safety Ash Barrels	@ # 2.50	5	00
		To 3 doz. Common Scrapers	@ 50%	1	50
		To 8 Eagle Shovels	@ 10 \$	0	80
		To $\frac{1}{4}$ doz. 8×12 Black Registers	@ # 1.50	9	00
		To 1 doz. Spice Boxes	@ 55¢	3	<i>30</i>
		To ½ doz. 14-qt. Dish Pans	@ # 6.00	3	00
•		To 2 doz. Common Stove Lifters	@ 50\$	1	00
		To $\frac{1}{4}$ doz. 12×14 Drip Pans	@ \$ 4.00	2	00
		To ½ gr. Retinned Teaspoons	@ 25 \$	1	<i>50</i>
:		To 1 doz. Ash Sifters	@ # 1.00	12	00
!	,			# 79	90

1898, March 7.

Received Payment,

Green, Fisk & Co.

8. R. M. Hanson bought of W. F. Fox & Co. 2 bbl. flour, at \$5.75; ½ bbl. fine sugar, 153 lb., at \$4.81 a cwt.; 25 lb. coffee, at 33 cents; 3 lb. Oolong tea, at 50 cents; 15 pint bottles olives, at 25 cents; 2 boxes graham wafers, at 40 cents; ½ doz. cans tomatoes, at \$1.20 a dozen; ½ doz. cans J. H. F. peaches, at \$3.50 a dozen; 4 Ferris hams, 48 lb., at 12½ cents a pound; 6 strips Ferris bacon, 19 lb. 9 oz., at 13 cents a pound; 3 lb. rice, at 9 cents; 3 lb. tapioca, at 5 cents; 40 lb. rye meal, at 2½ cents; 5 lb. boneless codfish, at 14 cents; ½ doz. cans plums, at \$2.90 a dozen.

Mr. R. M. Hanson,

Boston, Mass., July 14, 1898.

To W. F. FOX & CO., DR.

1898				li		
July	14	To 2 bbl. Flour	@	\$ 5.75	§ 11	50
		To \frac{1}{2} bbl. Fine Sugar, 153 lb.	@	4.81	7	36
		To 25 lb. Coffee	@	33 4	8	25
		To 3 lb. Oolong Tea	@	50 \$	1	50
		To 15 pint bottles Olives	(a)	25 %	3	75
		To 2 boxes Graham Wafers	@	40 \$	0	80
		To ½ doz. cans Tomatoes	@	\$ 1.20	0	60
		To ½ doz. cans J. H. F. Peaches	@	3.50	1	75
		To 4 Ferris Hams, 48 lb.	@	121 4	6	00
		To 6 strips Ferris Bacon, 19 16 lb.	@	13 %	2	54
		To 3 lb. Rice	@	99	0	27
		To 3 lb. Tapioca	@	5 %	0	15
		To 40 lb. Rye Meal	@	21/2	1	00
		To 5 lb. Boneless Codfish	@	149	0	70
		To ½ doz. cans Plums	@	\$ 2.90	1	45
					\$ 47	62

1898, July 23.

Received Payment,

W. F. Fox & Co.

9. G. B. Cook bought of Gray, Higginson & Co. 1 No. 8-20 Glenwood B range, at \$35.00; 1 No. 12 Rockford heater, at \$20.00; 4 lb. Eng. stovepipe, at 15 cents; 3 lb. Rus. stovepipe, at 25 cents; 8 lb. sheet zinc, at 8 cents; 1 stove board, at \$2.00; 1 set kitchen knives and forks, at \$1.50; 2 washtubs, at 85 cents; 1 washboard, at 25 cents; 1 set Mrs. Potts' nickel sad-irons, at 75 cents; 2 milk cans, at 35 cents; 1 hand lamp complete, at 30 cents; 1 stand lamp, at \$3.50; 1 granite iron washbowl, at 50 cents; 1 tea canister and 1 coffee canister, at 20 cents each; 1 carving knife and fork, at \$2.00; 1 corn popper, at 25 cents; 1 rolling-pin, at 20 cents; 2 8-qt. porcelain kettles, at 70 cents; 1 granite iron coffee-pot, at 75 cents.

Mr. G. B. Cook,

Boston, Mass., March 1, 1898.

To GRAY, HIGGINSON & CO., Dr.

1898]			1
Mar.	1	To 1 No. 8-20 Glenwood B Range	\$ 35	00
		To 1 No. 12 Rockford Heater	20	00
		To 4 lb Eng. Stovepipe @ 15 \$	0	60
		To 3 lb. Rus. Stovepipe @ 25 \$	0	75
		To 8 lb. Sheet Zinc @ 8 \$	0	64
		To 1 Stove Board	2	00
		To 1 set Kitchen Knives and Forks	1	50
		To 2 Washtubs @ 85 \$	1	70
		To 1 Washboard	0	25
	; !	To 1 set Mrs. Potts' Nickel Sad-irons	0	75
		To 2 Milk Cans @ 35 \$		70
	}	To 1 Hand Lamp complete	0	30
		To 1 Stand Lamp	3	50
	[To 1 Granite Washbowl		50
		To 1 Tea Canister	0	20
		To 1 Coffee Canister	0	20
	1	To 1 Carving Knife and Fork	2	00
	!	To 1 Corn Popper	0	25
	Ì	To 1 Rolling-pin	o	20
		To 2 8-qt. Porcelain Kettles @ 70 \$	1	40
		To 1 Granite Coffee-pot	0	1 .
			# 73	11

1898, March 10.

Received Payment,

Gray, Higginson & Co.

Exercise 97. Page 211.

1. Reduce 25.55kg to pounds avoirdupois.

$$\begin{array}{r}
25.55 \\
\underline{2.205} \\
12775 \\
5110 \\
\underline{5110} \\
56.33775
\end{array}$$

56.338 lb. Ans.

2. Reduce 5 sq. yd. 6 sq. ft. 108 sq. in. to square meters.

5 sq. yd. 6 sq. ft. 108 sq. in. =5 sq. yd. $6\frac{1}{4}$ sq. ft. =5.75 sq. yd.

$$0.836^{qm}$$
 $\frac{5.75}{4180}$
 5852
 $\frac{4180}{4.807^{qm}}$ Ans.

3. Reduce 24 gal. to liters.

24 gal. = 96 qt.

$$0.946^{1}$$

 96
 $\overline{5676}$
 8514
 $\overline{90.816^{1}}$ Ans.

4. Reduce 10 lb. troy to kilograms.

10 lb. = 120 oz.
$$\begin{array}{r}
31.1048 \\
\underline{120} \\
622080 \\
\underline{31104} \\
3732.4808
\end{array}$$

3732.48g = 3.732kg. Ans.

5. Reduce 50.5 cu. yd. to cubic meters.

6. Reduce $69\frac{17}{100}$ mi. to kilometers.

111.295km. Ans.

7. Reduce 12 A. 12 sq. rd. to hektars.

12 A. 12 sq. rd. =
$$12\frac{3}{40}$$
 A.
= 12.075 A.

$$\begin{array}{r}
12.075 \\
\underline{0.405} \\
60375 \\
\underline{48300} \\
4.890375
\end{array}$$
4.890ha. Ans.

8. Reduce 10 cd. to sters.

$$10 \times 3.624^{st} = 36.24^{st}$$
. Ans.

9. Reduce 4 cwt. 24 lb. to kilograms.

4 cwt. 24 lb. = 424 lb.
$$0.454^{kg}$$

$$\frac{424}{1816}$$

$$908$$

$$\frac{1816}{192.496^{kg}}$$
Ans.

10. Reduce 25 bu. 2 pk. to hektoliters.

25 bu. 2 pk. =
$$102$$
 pk. = 816 qt.
1 qt. = 1.101^1 = 0.0110^{hl} .
 $\frac{816}{0.011}$
 $\frac{816}{8.976}$
 $\frac{816}{8.976}$
 $\frac{8}{100}$

11. Express 15km in the common system.

9 mi. 100 rd. 13.2 ft. Ans.

12. Express 3ha in the common system.

7 A. 66 sq. rd. 2.4 sq. yd. Ans.

13. Express 12.125cbm in the common system.

$$\begin{array}{r}
12.125 \\
\underline{1.308} \\
97000 \\
36375 \\
\underline{12125} \\
15.8595 \\
\underline{27} \\
60165 \\
\underline{17190} \\
23.2065
\end{array}$$

15 cu. yd. 23.2 cu. ft. Ans.

14. Express 101.251 in the common system.

$$\begin{array}{cccc}
101.25 & 101.25 \\
\underline{1.057} & 0.908 \\
70875 & 81000 \\
\underline{50625} & 91125 \\
\underline{10125} & 91.935 \\
\underline{107.02125} & 2 \\
\underline{1.87}
\end{array}$$

26 gal. 3 qt.; 2 bu. 3 pk. 3 qt. 1.9 pt. Ans.

15. Reduce 20.25^{hl} to liquid quarts; to dry quarts.

$$1^{\rm hl} = 105.671$$
 liquid quarts = 90.810 dry quarts.

105.671	90.81
20.25	20.25
528355	45405
211342	18162
211342	18162
2139.83775	1838,9025

2139.838 liquid quarts; 1838.903 dry quarts. Ans.

16. Express 5^{kg} in troy weight. $1^{kg} = 15,432.35$ gr.

15432.35 gr.

13 lb. 4 oz. 15 dwt. 2 gr. Ans.

17. Express 24st in the common system.

$$0.276$$

$$-24$$

$$\overline{1104}$$

$$\underline{552}$$

$$6.624$$

$$-128$$

$$\overline{4992}$$

$$1248$$

$$\underline{624}$$

$$79.872$$

6 cd. 80 cu. ft. nearly. Ans.

18. Express 62.5^{qm} in the common system.

$$\begin{array}{r}
1.196 \\
\underline{62.5} \\
5980 \\
2392 \\
7176 \\
74.75
\end{array}$$

74 sq. yd. Ans.

19. Express 1001kg in avoirdupois weight.

$$2.205 \text{ lb.} \\ \frac{1001}{2205} \\ \frac{2205}{2207.205} \text{ lb.}$$

2207.2 lb. = 1 t. 207.2 lb. Ans.

20. Express 42 A. 100 sq. rd. in the metric system.

42 A. 100 sq. rd. = 42.625 A.

21. Find in acres, etc., the area of a rectangular field if it is 100^{m} long and 75^{m} broad.

 $100 \times 75 = 7500$.

$$7500^{qm} = 0.75^{ha}$$
.
$$\begin{array}{r}
2.471 \\
0.75 \\
12355 \\
17297 \\
\hline
1.85325 \\
160 \\
\hline
5119500 \\
85325 \\
\hline
136.52 \\
\hline
301 \\
\hline
13 \\
1560 \\
\hline
15.73 \\
\end{array}$$

- 1 A. 136 sq. rd. 16 sq. yd. neariy.

 Ans.
- 22. Find the number of cubic meters in a rectangular box 2 yd. long, 3 ft. wide, and 2½ ft. deep.

3 ft. = 1 yd.;
$$2\frac{1}{2}$$
 ft. = $\frac{5}{6}$ yd.
2 × 1 × $\frac{5}{6}$ = $1\frac{3}{6}$.
0.765cbm

$$\frac{1\frac{2}{6}}{510}$$

$$\frac{765}{1.275cbm}$$
 Ans.

23. Find the number of cubic yards in a rectangular box 2^m long, 75^{cm} wide, and 50^{cm} deep.

$$75^{\text{cm}} = \frac{1}{4}^{\text{m}}; 50^{\text{cm}} = \frac{1}{4}^{\text{m}}.$$
 $2 \times \frac{1}{4} \times \frac{1}{3} = \frac{3}{4} = 0.75.$

1.308 cu, yd.

0.75

6540

9158

0.981 cu. yd. Ans.

24. If a man walks 75^m a minute, what is his rate in miles per hour?

$$75^{m}$$
 a minute = 60×75^{m} per hour
= 4500^{m} per hour
= 4.5^{km} per hour.

25. If a cubic centimeter of cast iron weighs 7.113s, how many pounds does a cubic foot weigh?

1 cu. ft. =
$$\frac{1}{27}$$
 of 0.76453cbm
= 0.0283cbm = 28,300ccm.
7.113g
 $\frac{28300}{2133900}$
 $\frac{56904}{14226}$
 $\frac{14226}{201297.9g} = 201.2979kg$

26. How many steps 2 ft. 6 in. long will a man take in walking a kilometer?

$$1^{\text{km}} = 0.621 \text{ mi.}$$

$$\frac{0.621 \times 5280}{2\frac{1}{2}} = 0.621 \times 5280 \times \frac{2}{5}$$

$$= 1312 \text{ nearly.}$$

$$1312 \text{ steps. } Ans.$$

27. Find the value of a carboy (17 qt.) of sulphuric acid, specific gravity 1.841, at 4½ cents a kilogram.

\$ 1.41. Ans.

28. Find the value of a carboy $(17\frac{1}{2})$ of nitric acid, specific gravity 1.451, at 15 cents a pound.

171 of water weighs 17.5ks.

29. If the specific gravity of sea water is 1.026, and that of olive oil is 0.915, what is the weight of a hektoliter of each in pounds and in kilograms?

$$1^{hl} = 100^{l}$$
.

1001 of water weighs 100kg.

$$1.026 \times 100^{kg} = 102.6^{kg}$$
.

$$\begin{array}{c} 2.205 \text{ lb.} \\ \underline{102.6} \\ 13230 \\ \underline{4410} \\ \underline{2205} \\ \underline{226.233} \text{ lb.} \end{array}$$

$$0.915 \times 100^{\text{kg}} = 91.5^{\text{kg}}$$
.
 2.205 lb .

91.5 11025 2205 19845 201.7575 lb. Therefore, 1^{hl} of sea water weighs 226.23 lb., or 102.6^{kg}; 1^{hl} of olive oil weighs 201.76 lb., or 91.5^{kg}. Ans.

30. Find the weight in pounds and in kilograms of 31½ gal. of the best alcohol, specific gravity 0.792.

$$31\frac{1}{8}$$
 gal. = $124\frac{2}{3}$ qt.
 $124\frac{2}{3}$ $117.935^{\frac{1}{2}}$
 0.946 0.792
 $\overline{0.792}$
 $\overline{\phantom{$

205.958 lb. Ans.

31. Find the weight in pounds and in kilograms of the air, specific gravity 0.00129206, in a room 7^m long, 5^m wide, and 3.5^m high.

 $7 \times 5 \times 3.5 = 122.5$.

122.5^{cbm} of water weighs 122,500 ч.

•	
0.00129206	
122500	
64603000	
258412	
258412	
129206	
158.27735	
158.277 ≥ €.	Ans.
158.277	
2.205	
791385	
3165 54	
316554	
349.000785	
349 lb.	Ans

32. Find the weight in pounds and in kilograms of the air, specific gravity 0.00129206, in a room 23 ft. long, 16 ft. wide, and 10 ft. high.

$$23 \times 16 \times 10 \times 62.5$$
 lb. = 230,000 lb.

23	0.00129206
160	230000
$\overline{1380}$	3876180000
23	258412
3680	297.1738
62.5	297.17 lb. Ans.
18400	
736 0	297.1738
220 80	0.454
230000.	11886952
	14858690
	11886952
	134.9169052
	134.92ks. Ans.

33. What is the lifting force in kilograms and in pounds of a balloon that weighs 2^{kg}, and contains 10,000¹ of hydrogen gas, specific gravity 0.00008929?

The difference in weight between $10,000^{1}$ of air and $10,000^{1}$ of hydrogen is $(0.00129206 - 0.00008929) \times 10,000^{kg}$

 $= 0.00120277 \times 10,000$

= 12.0277kg.

The lifting force of the balloon is 12.0277 kg - 2 kg = 10.0277 kg. Ans.

22.111 lb. Ans.

34. What is the value at \$4.50 a cord of a pile of wood 1.2^m wide, 7^m long, and 2^m high?

 $1.2 \times 7 \times 2 = 16.8$. $16.8^{\text{cbm}} = 16.8^{\text{st}}$.

35. How many miles will a train run in 1 hr. 28 min. 21 sec., at the rate of 50km an hour?

36. Find the time it takes a train to run 31 mi. 180 yd. at the rate of 1 min. 25 sec. per kilometer.

31 mi. 180 yd. =
$$31\frac{9}{88}$$
 mi.
= $31\frac{9}{88} \times 1.609$ km = 50.044 km.

$$\frac{1.609}{1.65}$$

1 min. 25 sec. = $1\frac{5}{13}$ min. $50.044 \times 1\frac{5}{13}$ min. = 70.896 min. Ans. 37. What is the weight of 12 cu. yd. 16 cu. ft. 720 cu. in. of earth, if a cubic meter weighs 1 t. 17 cwt.?

1 t. 17 cwt. = 37 cwt.

12.608	9.64 512
0.765	37
63040	6751584
75648	2893536
38256	356.86944
9.64512	

356.87 cwt. = 17 t. 16 cwt. 87 lb.

Ans.

38. Find the weight in grams of a liter of mercury, if a cubic inch weighs 0.4925 of a pound avoirdupois.

$$1^1 = 1000^{\text{ccm}} = 61.03 \text{ cu. in.}$$

11 weighs 61.03×0.4925 lb. = $61.03 \times 0.4925 \times 453.59$ g.

39. How many yards of cloth, at \$3.12½ a meter, should be given in exchange for 15^m at \$2.75 a yard?

\$3.12\frac{1}{2} \text{ a meter}
=0.914 \times \frac{3}{3}.12\frac{1}{4} \text{ a yard.}
15\mathbf{m} = 15 \times 1.094 \text{ yd.}
\[\frac{15 \times 1.094 \times 2.75}{0.914 \times 3.125} \]
$$= \frac{3}{15} \times \frac{1094}{1000} \times \frac{11}{4} \times \frac{1000}{914} \times \frac{2}{25} \\
= \frac{36102}{2285} = 15\frac{1227}{25} = 15.8.
\]
15.8 yd. Ans.$$

40. If a wine merchant buys 3^{hl} of wine for 1600 francs, what does a gallon cost him in United States money, if 25 francs are equivalent to \$4.825?

$$3^{hl} = 300^{l}$$
.
1 fr. = $\frac{\$4.825}{25}$ = \\$0.193.

$$1^{1}$$
 costs $\frac{1600 \times \$0.193}{300}$.

1 gal. =4 qt. = 4×0.946^{1} . Therefore, 1 gal. costs

$$\begin{array}{r} 4 \times 0.946 \times 1600 \times \$0.193 \\ \hline 300 \\ \hline 0.946 & 6054.4 \\ \hline 4 & 0.193 \\ \hline 3.784 & 181632 \\ \hline 1600 & 544896 \\ \hline 2270400 & 60544 \\ \hline 3784 & 1168.4992 \\ \hline 6054.4 \\ \hline \end{array}$$

41. A mill wheel is turned by a stream of water running at the rate of a yard a second in a channel 5 ft. wide and 9 in. deep. Find the weight in metric tons and in tons avoirdupois of the water supplied in 12 hr., if a cubic foot of water weighs 1000 oz.

Volume of water each second = $(3 \times 5 \times \frac{3}{4})$ cu. ft.

Volume of water for 12 hr. = $(12 \times 60 \times 60 \times 3 \times 5 \times \frac{3}{4})$ cu. ft.

Weight of water for 12 hr. =
$$\left(12 \times 60 \times 60 \times 3 \times 5 \times \frac{3}{4} \times \frac{1000}{2000 \times 16}\right)$$
t.

1 lb. = 0.45359kg.

1 t. = $2000 \text{ lb.} = 2000 \times 0.45359 \text{kg} = 907 \text{kg} = 0.907 \text{t}$.

 $\begin{array}{r}
15187.5 \\
0.907 \\
\hline
1063125 \\
1366875 \\
\hline
13775.0625
\end{array}$

13,775.06t. Ans.

Exercise 98. Page 214.

1. When water is heated from the freezing point to the boiling point, it expands $\frac{1}{24}$ in volume. Find in kilograms the weight of a cubic foot of water at the freezing point and at the boiling point.

At the freezing point 1 cu. ft. of water weighs $62\frac{1}{2}$ lb.; at the boiling point $\frac{24}{25} \times 62\frac{1}{2}$ lb. = 60 lb. 1 lb. = $\frac{5}{11}$ kg.

$$62\frac{1}{2} \times \frac{5}{11}^{kg} = \frac{125}{2} \times \frac{5}{11}^{kg} = \frac{625}{22}^{5kg} = 28.41^{kg}.$$

$$60 \times \frac{5}{11}^{kg} = \frac{800}{11}^{0kg} = 27.27^{kg}.$$

At the freezing point 28.41kg; at the boiling point 27.27kg. Ans.

2. A circular plate of lead 8 in. in diameter and 2 in. thick is changed without loss into spherical shot, each 1.25^{mm} in radius. How many shot does it make?

The volume of the plate =
$$(2 \times 3.1416 \times 4 \times 4)$$
 cu. in.
= $(2 \times 3.1416 \times 4 \times 4 \times 16)^{ccm}$.

The volume of 1 shot =
$$\left(\frac{1}{6} \times 3.1416 \times \frac{1}{4^8}\right)^{\text{ccm}}$$
.
.: the number of shot = $\frac{2 \times 3.1416 \times 4 \times 4 \times 16}{\frac{1}{6} \times 3.1416 \times \frac{1}{4} \times \frac{1}{4} \times \frac{1}{4}}$
= $\frac{6 \times 2 \times 3.1416 \times 4 \times 4 \times 16 \times 4 \times 4 \times 4}{3.1416}$
= 196,608. Ans.

3. If \(\frac{1}{4}\) of a yard of velvet costs \(\frac{1}{4}\)3, how many francs will \(\frac{1}{4}\) of a meter cost?

$$\frac{3}{4}$$
 yd. = $\frac{3}{4}$ of $\frac{9}{10}$ ^m = $\frac{27}{40}$ ^m. 1 fr. = \$0.193.
∴ \$3 = $\frac{3}{0.193}$ fr. = $\frac{3000}{193}$ fr.

If $\frac{27}{40}$ cost $\frac{2000}{198}$ fr., $\frac{5}{7}$ will cost $\frac{5}{7} \times (\frac{2000}{198} + \frac{27}{40})$ fr.

$$= \frac{5}{7} \times \frac{40}{27} \times \frac{\cancel{3000}}{\cancel{193}} \text{ fr.} = \frac{200000}{12159} \text{ fr.} = 16.4 \text{ fr. } Ans.$$

4. Water expands $\frac{1}{10}$ in freezing, and a floating body displaces an amount of water equal in weight to the body. What is the volume in cubic meters, and the weight in metric tons, of an iceberg floating in the ocean, if the specific gravity of sea water is 1.026, and the part of the iceberg above the water is a rectangular solid 200 ft. long, 60 ft. wide, and 12 ft. high?

If water expands $\frac{1}{10}$ in freezing, the volume of ice is $\frac{11}{10}$ of the volume of the water. Hence, the specific gravity of ice is $\frac{19}{10}$. The difference between the specific gravity of sea water and that of the iceberg is $1.026 - \frac{19}{10} = 1.026 - 0.909 = 0.117$.

Volume of iceberg above water

=
$$(200 \times 60 \times 12)$$
 cu. ft. = $\frac{200 \times 60 \times 12}{27}$ cu. yd. = $\frac{200 \times 60 \times 12}{27} \times \frac{10^{\text{ebm}}}{13}$.

Volume of whole iceberg

$$= \frac{1.026 \times \left(\frac{200 \times 60 \times 12}{27} \times \frac{10}{13}\right)^{\text{cbm}}}{0.117}$$

$$= \frac{\cancel{114}}{\cancel{1999}} \times \frac{200 \times \cancel{99} \times \cancel{12}}{\cancel{27}} \times \frac{\cancel{1999}}{\cancel{117}} \times \frac{10^{\text{cbm}}}{13} = \frac{6080000^{\text{cbm}}}{169} = 35,976.33^{\text{cbm}}. Ans.$$

35,976.33cbm of ice weighs $\frac{10}{11}$ of 35,976.33t = $\frac{359763.3t}{11}$ = 32,705.75t. Ans.

5. How many hektoliters of wheat will a rectangular bin hold 14 ft. long, 10 ft. wide, and 6 ft. high?

Volume of bin =
$$(14 \times 10 \times 6)$$
 cu. ft. = $\frac{14 \times 10 \times 6}{27}$ cu. yd.
= $\frac{14 \times 10 \times 6}{27} \times \frac{10^{\text{cbm}}}{13} = \frac{14 \times 10 \times 6}{27} \times \frac{10}{13} \times 10^{\text{hl}}$
= $\frac{28000^{\text{hl}}}{117} = 239.3^{\text{hl}}$. Ans.

6. How many hektoliters of water will a cylindrical stand-pipe hold 70 ft. high and 35 ft. in diameter?

Volume of stand-pipe

$$= \left(70 \times \frac{22}{7} \times \frac{35}{2} \times \frac{35}{2}\right) \text{ cu. ft.} = \frac{70 \times 22 \times 35 \times 35}{27 \times 7 \times 2 \times 2} \text{ cu. yd.}$$

$$= \frac{70 \times 22 \times 35 \times 35}{27 \times 7 \times 2 \times 2} \times \frac{10^{\text{cbm}}}{13} = \frac{\cancel{10} \times \cancel{10} \times \cancel{10} \times \cancel{10} \times \cancel{10}}{\cancel{27} \times \cancel{10} \times \cancel{22} \times \cancel{20}} \times \frac{\cancel{10}}{\cancel{13}} \times 10^{\text{hl}}$$

$$= \frac{6737500^{\text{hl}}}{351} = 19,195.2^{\text{hl}}. \quad Ans.$$

7. How many bushels of wheat will a rectangular bin hold 4^m long, 3^m wide, and 2.5^m high?

Volume of bin

$$= (4 \times 3 \times 2\frac{1}{2})^{\text{cbm}} = (4 \times 3 \times 2\frac{1}{2} \times 10)^{\text{hl}} = 4 \times 3 \times 2\frac{1}{2} \times 10 \times 2\frac{5}{6} \text{ bu.}$$

$$4 \times 3 \times 2\frac{1}{2} \times 10 \times 2\frac{5}{6} = \cancel{4} \times \cancel{3} \times \cancel{5} \times 10 \times \cancel{\frac{17}{6}} = 850.$$
850 bu. Ans.

8. How many gallons of water in a well 1.2^m in diameter, if the depth of the water is 2^m ?

Volume of the water =
$$(2 \times \frac{2}{7} \times 0.6 \times 0.6)^{cbm} = 2 \times \frac{2}{7} \times \frac{2}{5} \times \frac{2}{5} \times 1000^{1}$$

= $2 \times \frac{2}{7} \times \frac{2}{5} \times \frac{2}{5} \times 1000 \times \frac{1}{16}$ qt.
= $2 \times \frac{2}{7} \times \frac{2}{5} \times \frac{2}{5} \times 1000 \times \frac{1}{16} \times \frac{1}{2}$ gal.

$$2 \times \frac{11}{7} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{1000}{100} \times \frac{17}{100} \times \frac{1}{4} = \frac{8415}{14} = 601.1.$$

$$2 \times \frac{22}{7} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{1000}{100} \times \frac{17}{100} \times \frac{1}{4} = \frac{8415}{14} = 601.1.$$

$$2 \times \frac{11}{7} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{3}{5} \times \frac{1000}{100} \times \frac{17}{100} \times \frac{1}{4} = \frac{8415}{14} = 601.1.$$

$$2 \times \frac{3}{7} \times \frac{3}{5} \times \frac{$$

9. If 1 lb. troy of silver is worth \$6.20, what is the value of a lump of silver weighing 2.64kg?

$$2.64^{\text{kg}} = 2.64 \times \frac{1}{3}$$
 lb. troy = $2\frac{1}{2}\frac{6}{5} \times \frac{1}{3}$ lb. troy.

$$2\frac{14}{5} \times \frac{13}{5} \times \$6.20 = 2\frac{14}{5} \times \frac{13}{5} \times \$6\frac{1}{5} = \frac{66}{25} \times \frac{13}{5} \times \$\frac{31}{5} = \$\frac{26598}{625} = \$42.56.$$
 Ans.

10. A pound of brass contains 3.3 cu. in., and a pound of antimony contains 6.27 cu. in. Find the weight in kilograms of a mass of 313½ cu. in. that contains equal volumes of the two metals.

The volume of each metal in the mass is $\frac{1}{2}$ of 313 $\frac{1}{2}$ cu. in. = 156.75 cu. in.

The weight of the mass =
$$\left(\frac{156.75}{3.3} + \frac{156.75}{6.27}\right)$$
 lb.
= $\left(\frac{156.75}{3.3} + \frac{156.75}{6.27}\right) \times \frac{5}{11}$ kg.

$$\frac{95}{14.23} \times \frac{5}{11} = \frac{\cancel{13673}}{\cancel{330}} \times \frac{5}{\cancel{11}} = \frac{475}{22} = 21.59.$$

$$\frac{25}{6.27} \times \frac{5}{11} = \frac{\cancel{13673}}{\cancel{11}} \times \frac{5}{\cancel{11}} = \frac{125}{11} = 11.36.$$

11. If 2 cu. in. of mercury weighs 1 lb., and 100 cu. in. of air weighs 31 gr., how many kilometers high must a column of air be to weigh as much as a column of mercury 29.388 in. high, standing on a base of the same area?

 $21.59^{\text{kg}} + 11.36^{\text{kg}} = 32.95^{\text{kg}}$. Ans.

If 2 cu. in. of mercury weighs 1 lb., or 7000 gr., 1 cu. in. of mercury weighs 1 of 7000 gr.; that is, 3500 gr.

If 100 cu. in. of air weighs 31 gr., 1 cu. in. of air weighs 0.31 gr.

Therefore, mercury weighs $\frac{3500}{0.31}$ times as much as air, and the column of air to weigh as much as a column of mercury 29.388 in. high must be $\frac{3500}{0.31} \times 29.388$ in. high.

$$\frac{3500}{0.31} \times 29.388 \text{ in.} = \frac{3500 \times 29.388}{0.31 \times 36} \text{ yd.} = \frac{3500 \times 29.388}{0.31 \times 36} \times 0.9^{\text{m}}$$
$$= \frac{3500 \times 29.388}{0.31 \times 36} \times 0.0009^{\text{km}}.$$

$$7 \atop 3599 \times \frac{7347}{1999} \times \frac{9}{19999} \times \frac{199}{31} \times \frac{1}{36} = \frac{1659}{200} = 8.295. \qquad 8.295 \text{km}. \ Ans.}$$

12. If a sprinter can run 0.00645 of a mile in 1.08 sec., how many meters can be run in a second? How many seconds will it take him to run 100^{m} ?

The sprinter in 1 sec. can run

$$\frac{0.00645}{1.08} \text{ mi.} = \frac{0.00645}{1.08} \times 1.6^{\text{km}} = \frac{0.00645}{1.08} \times 1.6 \times 1000^{\text{m}}$$

$$= \frac{0.645}{108} \times 1.6 \times 1000^{\text{m}} = \frac{\cancel{645}}{\cancel{108}} \times \cancel{\frac{8}{5}}^{\text{m}} = \frac{86^{\text{m}}}{9} = 95^{\text{m}}. \text{ Ans.}$$

$$\frac{27}{9}$$

$$100 + 95 = \frac{9}{56} \times \cancel{100} = \frac{450}{43} = 10.465. \qquad 10.465 \text{ sec. } Ans.$$

13. Two trains going in opposite directions pass each other in 3½ sec. If their lengths are 260 ft. and 200 ft., respectively, and the first train is going at the rate of 80km an hour, what is the rate of the second train?

$$80^{\text{km}} \text{ an hour} = \frac{80}{3600}^{\text{km}} \text{ a sec.} = \frac{80 \times \frac{5}{3}}{3600}^{\text{mi. a sec.}}$$

$$= \frac{80 \times \frac{5}{3} \times 5280}{3600} \text{ ft. a sec.} = 73\frac{1}{3} \text{ ft. a sec.}$$

$$\frac{80 \times \frac{5}{3} \times 5280}{3600} = \frac{10}{80} \times \frac{5}{8} \times \frac{5280}{3600} = \frac{220}{3} = 73\frac{1}{3}.$$

$$\frac{110}{3600} = \frac{100}{3} $

 $3\frac{110}{3} \times 73\frac{1}{3} = \frac{7}{2} \times \frac{220}{3} = \frac{770}{3} = 256\frac{2}{3}$; that is, the first train in $3\frac{1}{2}$ sec. goes $256\frac{2}{3}$ ft. of the 260 ft. +200 ft. =460 ft.

The second train, therefore, in $3\frac{1}{2}$ sec. goes 460 ft. $-256\frac{1}{3}$ ft. $=203\frac{1}{3}$ ft. The rate of the second train is $\frac{203\frac{1}{3}}{3\frac{1}{4}}$ ft. a second, $=3600 \times \frac{203\frac{1}{3}}{3\frac{1}{4}}$ ft. an hour $=\frac{3600}{5280} \times \frac{203\frac{1}{3}}{3\frac{1}{4}} \times 1\frac{3}{5}$ mi. an hour $=\frac{3600}{5280} \times \frac{203\frac{1}{3}}{3\frac{1}{4}} \times 1\frac{3}{5}$ mi. an hour.

$$\frac{3600}{5280} \times \frac{203\frac{1}{3}}{3\frac{1}{2}} \times 1\frac{3}{5} = \frac{\cancel{3699}}{\cancel{5289}} \times \frac{610}{\cancel{3}} \times \frac{\cancel{2}}{\cancel{7}} \times \frac{\cancel{8}}{\cancel{5}} = \frac{4880}{77} = 63.4.$$

$$\cancel{63.4}^{km} \text{ an hour. } Ans.$$

14. If a cubic inch of water converted into steam will produce mechanical force sufficient to raise a weight of 2200 lb. one foot high, how many meters high would the conversion into steam of a cubic centimeter of water raise a weight of one kilogram?

1 cu. in. = 16^{ccm} . 2200 lb. = $2200 \times \frac{5}{11}^{\text{kg}}$. 1 ft. = $\frac{1}{3}$ yd. = $\frac{1}{3}$ of 0.9^{m} . If 1^{ccm} of steam produces force sufficient to raise $2200 \times \frac{5}{11}^{\text{kg}} = \frac{\frac{1}{3}}{16} \cdot \frac{16}{16}$ high, it will produce a force sufficient to raise $1^{\text{kg}} = 2200 \times \frac{5}{11} \times \frac{\frac{1}{3}}{16} \cdot \frac{16}{16}$ high.

$$\begin{array}{c}
5 \\
29 \\
200 \\
2200 \times \frac{5}{11} \times \frac{1}{3} \times \frac{3}{10} \times \frac{1}{16} = \frac{75}{4} = 18.75.
\end{array}$$

$$18.75^{\text{m}}. Ans.$$

15. If a man takes 100 steps of 0.7^m each in a minute, how long will it take him to walk a distance of 28^{km}?

$$\frac{28 \times 1000}{100 \times 0.7} = \frac{\frac{4}{28} \times 1000 \times 10}{100 \times 7} = 400. \quad 400 \text{ min.} = 6 \text{ hr. 40 min.} \quad Ans.$$

16. A lot of land containing 63° 21° worth \$0.35 a square yard, is exchanged for a second lot containing 1h 5°. What is the cost per ar of the second lot?

 $\$0.35 \text{ a sq. yd.} = \frac{\$0.35}{\$} \text{ a centar} = \$0.42 \text{ a centar.} \quad 63^{\circ} 21^{\circ} = 6321^{\circ}.$

The first lot cost $6321 \times \$0.42$. $1^{ha} 5^{a} = 105^{a}$.

Therefore, the second lot cost per ar

$$\frac{301}{\cancel{5}\cancel{5}\cancel{5}\cancel{5}} = \$\frac{126.42}{5} = \$25.284. Ans.$$

17. Light travels in 8 min. 13 sec. from the sun to the earth, 153,624,000km. What is the velocity of light in miles per second?

8 min. 13 sec. = 493 sec.

The velocity of light per second is $\frac{153624000)^{km}}{493} = \frac{153624000 \times \frac{5}{4}}{493}$ mi.

$$\frac{153624000 \times \frac{5}{4}}{493} = \frac{\frac{153624999 \times 5}{493 \times 8}}{493 \times 8} = \frac{96015000}{493} = 194,756.6.$$
194,756.6 mi. Ans.

18. How many square feet of surface has a rectangular table that is 1.1^m long and 0.85^m wide?

The area of the table = $(1.1 \times 0.85)^{qm} = 1.1 \times 0.85 \times 1.1 \text{ sq. yd.}$

19. How many square meters of surface has a circular table that is 3½ ft. in diameter?

Radius = $\frac{1}{2}$ of $3\frac{1}{2}$ ft. = $1\frac{3}{4}$ ft.

The area of the table $=(\frac{3}{4} \times 1\frac{3}{4} \times 1\frac{3}{4})$ sq. ft.

$$= \frac{\frac{32 \times 1\frac{3}{4} \times 1\frac{3}{4}}{9}}{9} \text{ sq. yd.} = \frac{\frac{32 \times 1\frac{3}{4} \times 1\frac{3}{4}}{9} \times \frac{1\frac{3}{4}}{6}}{8}.$$

$$\frac{\frac{27}{7} \times \frac{13}{4} \times \frac{13}{4}}{9} \times \frac{5}{6} = \frac{\frac{22}{7}}{7} \times \frac{7}{4} \times \frac{7}{4} \times \frac{1}{9} \times \frac{5}{6} = \frac{385}{432} = 0.89. \quad 0.89^{qm}. \quad Ans.$$

20. If sound travels 340^m a second, how many feet distant is a cannon from a man who hears the report 13 sec. after he sees the flash?

 $13 \times 340^{m} = 13 \times 340 \times 1.1 \text{ yd.} = 13 \times 340 \times 1.1 \times 3 \text{ ft.} = 14,586 \text{ ft.}$ Ans.

340	4420
13	3.3
1020	13260
340	13260
4420	14586

21. How many square meters of zinc will be required to line a rectangular cistern open at the top, 12 ft. long, 10 ft. wide, and 8 ft. deep?

The perimeter of the bottom = $2 \times (12 + 10)$ ft. = 44 ft.

The area of the four sides $=(8 \times 44)$ sq. ft. =352 sq. ft.

The area of the bottom = (12×10) sq. ft. = 120 sq. ft.

352 sq. ft. + 120 sq. ft. = 472 sq. ft. = $\frac{472}{5}$ sq. yd. = $\frac{472}{5}$ × $\frac{5}{5}$ qm.

$$\frac{236}{472} \times \frac{5}{6} = \frac{1180}{27} = 43.7.$$
 43.7qm. Ans.

22. A rectangular tank is 3^m long, 2½^m wide, and 1½^m high, external measurement. If its sides are 0.1^m thick, how many gallons of water will the tank hold?

The internal measurements are: length $3^m - 2 \times 0.1^m = 2.8^m$; breadth $2.5^m - 2 \times 0.1^m = 2.3^m$; height $1.5^m - 0.1^m = 1.4^m$.

Volume = $(2.8 \times 2.3 \times 1.4)^{\text{cbm}} = 2.8 \times 2.3 \times 1.4 \times 1000^{1}$

$$=2.8 \times 2.3 \times 1.4 \times 1000 \times \frac{17}{16} \text{ qt.} = 2.8 \times 2.3 \times 1.4 \times 1000 \times \frac{17}{16} \times \frac{1}{4} \text{ gal.}$$

$$2.8 \times 2.3 \times 1.4 \times 1000 \times \frac{17}{16} \times \frac{1}{4} = \cancel{28} \times 23 \times \cancel{14} \times \frac{17}{\cancel{16}} \times \frac{1}{\cancel{4}} = \frac{19159}{8} = 23947.$$

23947 gal. Ans.

23. If a cube of pine wood 11.2cm on an edge weighs 2 lb., what is the specific gravity of the pine?

2 lb. =
$$2 \times \frac{5}{11}$$
 kg = $\frac{10}{11}$ kg.

Volume =
$$(1.12 \times 1.12 \times 1.12)^{\text{cdm}}$$
.

 $(1.12 \times 1.12 \times 1.12)^{cdm}$ of water weighs $(1.12 \times 1.12 \times 1.12)^{kg}$.

$$\frac{\frac{19}{1.12 \times 1.12 \times 1.12} = \frac{19}{11} \times \frac{\frac{25}{199}}{\frac{112}{28}} \times \frac{\frac{25}{199}}{\frac{112}{28}} \times \frac{\frac{25}{199}}{\frac{112}{28}} = \frac{78125}{120736} = 0.647. \text{ Ans.}$$

24. Find in kilograms the weight of water a cubical cistern will hold, 6 ft. on an edge.

The weight of the water is $6 \times 6 \times 6 \times 62\frac{1}{2}$ lb. $= 6 \times 6 \times 6 \times 62\frac{1}{2} \times \frac{5}{12} \times \frac{5}{$

$$6 \times 6 \times \cancel{6} \times \frac{125}{2} \times \frac{5}{11} = \frac{67500}{11} = 6136.4.$$
 6136.4kg. Ans.

25. Rain has fallen to the depth of half an inch. How many cubic meters of water has fallen on an acre of land?

$$1 \text{ A.} = 43,560 \text{ sq. ft.} ; \frac{1}{2} \text{ in.} = \frac{1}{24} \text{ ft.}$$

$$\text{Volume of water} = (43,560 \times \frac{1}{24}) \text{ cu. ft.} = \frac{43560 \times \frac{1}{24}}{27} \text{ cu. yd.}$$

$$= \frac{43560 \times \frac{1}{24}}{27} \times \frac{10^{\text{cbm}}}{13}.$$

$$\frac{605}{1815}$$

$$43569 \times \frac{1}{24} \times \frac{1}{27} \times \frac{10}{13} = \frac{6050}{117} = 51.7.$$

$$51.7^{\text{cbm}}. \text{ Ans.}$$

26. How many centimeters will the water sink in a cylindrical cistern 7 ft. in diameter, if 310 gallons of water is pumped out?

The radius $= \frac{1}{4}$ of 84 in. = 42 in.

Volume of the water = 310×231 cu. in.

Area of bottom of cistern = $(2/2 \times 42 \times 42)$ sq. in.

Therefore, the water will sink $\frac{310 \times 231}{\frac{24}{2} \times 42 \times 42}$ in. $=\frac{310 \times 231}{\frac{24}{2} \times 42 \times 42} \times 2\frac{11}{20}$ cm.

$$31 \times 21 \times 231 \times \frac{7}{22} \times \frac{1}{42} \times \frac{1}{42} \times \frac{1}{20} = \frac{527}{16} = 33. \qquad 33^{\text{cm}}. \quad Ans.$$

27. How many square yards of tin are required to cover the roof of a hemispherical dome 12^m in diameter?

Area =
$$\frac{1}{2}$$
 of $(\frac{2}{7} \times 12 \times 12)^{qm} = \frac{1}{2} \times \frac{2}{7} \times 12 \times 12 \times \frac{q}{5}$ sq. yd. $\frac{11}{2} \times \frac{22}{7} \times 12 \times 12 \times \frac{6}{5} = \frac{9504}{35} = 271.5$. 271.5 sq. yd. Ans.

28. If a cubic inch of iron weighs 4½ oz., what is the weight in kilograms of an iron ball 10cm in diameter?

1 cu. in. weighs $4\frac{1}{2}$ oz.; that is, 16^{ccm} weighs $\frac{4\frac{1}{16}}{16}$ lb., or $\frac{4\frac{1}{16}}{16} \times \frac{5}{11}^{\text{kg}}$.

Therefore, 1ccm weighs $\frac{1}{16} \times \frac{4\frac{1}{2}}{16} \times \frac{5}{11}$ kg.

Volume = $(\frac{1}{6} \times \frac{2}{7} \times 10 \times 10 \times 10)^{\text{ccm}}$.

Therefore, the iron ball weighs $\frac{1}{6} \times \frac{22}{7} \times 10 \times 10 \times 10 \times \frac{1}{16} \times \frac{41}{16} \times \frac{5}{11}$ kg.

$$\frac{1}{g} \times \frac{27}{7} \times \cancel{10} \times \cancel{10} \times \cancel{10} \times \cancel{10} \times \cancel{10} \times \frac{1}{\cancel{10}} \times \frac{3}{\cancel{2}} \times \frac{1}{\cancel{10}} \times \frac{5}{\cancel{11}} = \frac{1875}{448} = 4.2.$$

29. If a cubic inch of lead weighs 7 oz., what is the weight in kilograms of a lead pipe 3^m long, 6^{cm} in external diameter, if the pipe is 1^{cm} thick?

1 cu. in. weighs 7 oz.; that is, 16^{ccm} weighs $\frac{7}{16}$ lb., or $\frac{7}{16} \times \frac{5}{11}$ kg. Therefore, 1^{ccm} weighs $\frac{1}{16} \times \frac{7}{16} \times \frac{5}{11}$ kg.

External contents = $(300 \times \frac{22}{7} \times 3 \times 3)^{\text{ccm}}$.

Internal contents = $(300 \times 3/2 \times 2 \times 2)^{ccm}$.

$$300 \times \frac{22}{7} \times 3 \times 3 = \frac{59400}{7}; \quad 300 \times \frac{22}{7} \times 2 \times 2 = \frac{26400}{7}.$$

$$\frac{59400^{\text{ccm}}}{7} - \frac{26400^{\text{ccm}}}{7} = \frac{33000^{\text{ccm}}}{7}.$$

$$\frac{375}{3999}$$

$$\frac{39999}{7} \times \frac{1}{16} \times \frac{7}{16} \times \frac{5}{11} = \frac{1875}{32} = 58.6 \text{kg}. \quad Ans.$$

30. Find the cost at \$7.25 per meter of building a wall around a rectangular garden 90 ft. long and 55 ft. wide.

Length of wall = $2 \times (90 + 55)$ ft. = 290 ft. = $\frac{290}{3}$ yd. = $\frac{290}{3} \times \frac{9}{10}$ m.

$$\frac{290}{3} \times \frac{9}{10} \times \$7\frac{1}{4} = \frac{290}{3} \times \frac{3}{10} \times \$\frac{29}{4} = \$\frac{2523}{4} = \$630.75. \text{ Ans.}$$

31. The minute hand of a clock is 0.5^m long. How many feet does its point move in an hour?

The point moves
$$\frac{22}{7} \times 2 \times 0.5^{m} = \frac{22}{7} \times 2 \times \frac{1}{2} \times \frac{11}{10} \text{ yd.}$$

$$= \frac{22}{7} \times 2 \times \frac{1}{2} \times \frac{11}{10} \times 3 \text{ ft.} = \frac{363}{35} \text{ ft.} = 10.4 \text{ ft.} \text{ Ans.}$$

32. A spherical shot 3 in. in diameter is melted and then cast into a cylinder 9^{cm} in diameter. What is the height in centimeters of this cylinder?

Volume of shot = $(\frac{1}{6} \times \frac{2}{7} \times 3^8)$ cu. in. = $\frac{1}{6} \times \frac{2}{7} \times 27 \times 16^{\text{ccm}}$.

Area of base of cylinder = $(2/2 \times \frac{9}{2} \times \frac{9}{2})^{qcm}$.

Therefore, height of cylinder =
$$\left(\frac{\frac{1}{6} \times \frac{2}{7} \times 27 \times 16}{\frac{2}{7} \times \frac{9}{2} \times \frac{9}{2}}\right)^{cm}$$
.

$$\frac{1}{9} \times \frac{22}{7} \times \frac{27}{7} \times 16 \times \frac{7}{22} \times \frac{2}{9} \times \frac{2}{9} = \frac{32}{9} = 3\frac{5}{9}.$$
 35cm. Ans

33. What is the cost at \$18 per 1000 ft. board measure of 4 beams, each 4.5^m long, 7.5^{cm} wide, and 5^{cm} thick?

$$4.5^{m} = 4.5 \times 1.1 \text{ yd.} = 4.5 \times 1.1 \times 3 \text{ ft.}$$

$$7.5^{\text{cm}} = 0.075^{\text{m}} = 0.075 \times 1.1 \text{ yd.} = 0.075 \times 1.1 \times 3 \text{ ft.}$$

$$6^{\text{cm}} = 0.05^{\text{m}} = 0.05 \times 1.1 \text{ yd.} = 0.05 \times 1.1 \times 36 \text{ in.}$$

The number of feet board measure in the 4 beams

$$= 4 \times 4.5 \times 1.1 \times 3 \times 0.075 \times 1.1 \times 3 \times 0.05 \times 1.1 \times 36$$

$$= 4 \times \frac{9}{2} \times \frac{11}{10} \times 3 \times \frac{\cancel{13}}{\cancel{10000}} \times \frac{11}{10} \times 3 \times \frac{\cancel{3}}{\cancel{100}} \times \frac{11}{10} \times \cancel{30} = \frac{2910897}{100000} = 29.1.$$

$$29.1 \times \$ \frac{18}{1000} = \$ \frac{523.8}{1000} = \$ 0.52. \ Ans.$$

34. The radius of a cylindrical roller is 0.4^m and its length is 2.15^m. Find its volume in cubic feet.

Volume =
$$(2.15 \times \frac{27}{7} \times 0.4 \times 0.4)^{\text{cbm}}$$

= $(2.15 \times \frac{27}{7} \times \frac{2}{5} \times \frac{2}{5} \times \frac{13}{5})$ cu. yd.
= $(2.15 \times \frac{27}{7} \times \frac{2}{5} \times \frac{2}{5} \times \frac{13}{5} \times 27)$ cu. ft.
= 37.95 cu. ft. Ans.

$$\frac{43}{199} \times \frac{11}{7} \times \frac{22}{5} \times \frac{2}{5} \times \frac{13}{19} \times 27 = \frac{166023}{4375} = 37.95.$$

$$\frac{59}{25}$$

35. A cylindrical cistern, the circumference of whose base is 2.2^m, and whose depth is 2.1^m, is four fifths filled with water. Find in gallons the volume of the water, and in pounds the weight of the water.

Radius of base =
$$\frac{2.2^{\text{m}}}{2 \times \frac{3}{4}} = \frac{7 \times 2.2^{\text{m}}}{2 \times 22} = \frac{7^{\text{m}}}{20}$$
.

Volume of the water = $\left(\frac{4}{5} \times 2.1 \times \frac{22}{7} \times \frac{7}{20} \times \frac{7}{20}\right)^{\text{cbm}} = 0.6468^{\text{cbm}}$.

$$\frac{4}{5} \times \frac{21}{10} \times \frac{\cancel{22}}{\cancel{7}} \times \frac{\cancel{7}}{\cancel{20}} \times \frac{\cancel{7}}{\cancel{20}} = \frac{6468}{10000} = 0.6468.$$

 0.6468^{cbm} of water weighs $646.8^{\text{kg}} = 646.8 \times 2.2 \text{ lb.} = 1422.98 \text{ lb.}$ Ans.

$$\begin{array}{r}
 646.8 \\
 2.2 \\
\hline
 12936 \\
 12936 \\
\hline
 1422.96$$

$$6468^{\text{cbm}} = 646.8^{\text{l}} = 646.8 \times \frac{17}{16} \text{ qt.} = 646.8 \times \frac{17}{16} \times \frac{1}{4} \text{ gal.} = 171.8 \text{ gal.}$$
 Ans.

$$\frac{1617}{\cancel{6468}} \times \frac{17}{16} \times \frac{1}{\cancel{4}} = \frac{27489}{160} = 171.8.$$

Exercise 99. Page 218.

1. Which is the greater ratio, 5:8 or 6:9?

$$5:8 = \frac{5}{8} = \frac{15}{24}.$$

$$6:9 = \frac{5}{8} = \frac{15}{2} = \frac{15}{24}.$$

 \therefore 6:9 is the greater.

2. Which is the greater ratio, 7:10 or 9:12?

7:
$$10 = \frac{7}{10} = \frac{14}{20}$$
.
9: $12 = \frac{9}{12} = \frac{4}{4} = \frac{15}{20}$.
 \therefore 9: 12 is the greater.

3. Which is the greater ratio, 8:9 or 10:12?

8:9 =
$$\frac{1}{8}$$
 = $\frac{1}{8}$.
10:12 = $\frac{19}{12}$ = $\frac{1}{8}$ = $\frac{1}{8}$.
∴ 8:9 is the greater.

4. Which is the greater ratio, 6:12 or 8:14?

$$6: 12 = \frac{6}{12} = \frac{1}{2} = \frac{7}{14}.$$

$$8: 14 = \frac{8}{14}.$$

.. 8:14 is the greater.

5. Which is the greater ratio, 10 cwt.: 15 cwt. or \$7:\$9?

10 cwt. : 15 cwt. =
$$\frac{10 \text{ cwt.}}{15 \text{ cwt.}} = \frac{2}{3} = \frac{6}{3}$$
.

$$\$7:\$9=\frac{\$7}{\$9}=7.$$

 \therefore \$7:\$9 is the greater.

6. Which is the greater ratio, 5 dy.: 7 dy. or 8 ft.: 11 ft.?

5 dy.: 7 dy. =
$$\frac{5 \text{ dy.}}{7 \text{ dy.}}$$
 = $\frac{5}{7}$ = $\frac{5}{7}$.

8 ft.: 11 ft. =
$$\frac{8 \text{ ft.}}{11 \text{ ft.}} = \frac{8}{11} = \frac{5}{11}$$

.. 8 ft.: 11 ft. is the greater.

7. Which is the greater ratio, 9 yd.: 6 yd. or 5:3?

9 yd. : 6 yd. =
$$\frac{9 \text{ yd.}}{6 \text{ yd.}}$$
 = $\frac{2}{6}$.

$$5:3=\frac{5}{3}=\frac{10}{6}$$
.

 \therefore 5:3 is the greater.

8. Which is the greater ratio, $\frac{2}{3}$ lb. : $\frac{1}{2}$ lb. or $\frac{5}{3}$ yd. : $\frac{5}{3}$ yd. ?

$$\frac{2}{3}$$
 lb. $: \frac{1}{2}$ lb. $= \frac{2}{3} \frac{1}{1} \frac{1}$

.. § yd. : § yd. is the greater.

- 9. Find the ratio of 3 dry quarts to 2 pecks.
- .. 3 dry qt.: 2 pk. = 3 qt.: 16 qt. = 3:16. Ans.
- 10. Find the ratio of 2500 lb. to 1 ton.
- \therefore 2500 lb.: 1 t. = 2500 lb.: 2000 lb. = 5:4. Ans.
- 11. Find the ratio of a rectangular field 16 rd. long, 14 rd. wide to a rectangular field 14 rd. long, 12 rd. wide.

The ratio of the fields = $16 \times 14 : 14 \times 12$.

$$=\frac{\cancel{16}\times\cancel{14}}{\cancel{14}\times\cancel{12}}=\frac{4}{3}=4:3. Ans.$$

12. Find the ratio of a circle 1 in. in diameter to a circle 1 in. in radius.

The ratio of the circles =
$$\frac{1}{4} \times 3.1416 \times 1^2 : 3.1416 \times 1^2$$

= $\frac{\frac{1}{4} \times 3.1416 \times 1^2}{3.1416 \times 1^2} = \frac{1}{4} = 1 : 4$. Ans.

Exercise 100. Page 220.

1. Find the missing term of 24:18::16:?.

$$\frac{{\frac{3}{18 \times 16}}}{{\frac{24}{4}}} = 12. Ans.$$

2. Find the missing term of 35:?::15:21.

$$\frac{7}{\cancel{35} \times \cancel{21}} = 49. \ Ans.$$

3. Find the missing term of **45**: 40::?:32.

$$\frac{9}{\cancel{45} \times \cancel{32}} = 36. \text{ Ans.}$$

4. Find the missing term of 30:27::40:?.

$$\frac{9}{27 \times 49} = 36. \text{ Ans.}$$

5. Find the missing term of ?:36::4:3.

$$\frac{12}{36 \times 4} = 48$$
. Ans.

6. Find the missing term of 18:?::32:45.

$$\frac{\cancel{18} \times \cancel{45}}{\cancel{32}} = \frac{\cancel{405}}{\cancel{16}} = \cancel{25}_{\cancel{16}}^{5}. Ans.$$

7. Find the missing term of

$$\frac{\frac{2}{12 \times 5}}{\frac{18}{3}} = \frac{10}{3} = 3\frac{1}{3}. Ans.$$

8. Find the missing term of

$$\frac{8 \times 119}{17} = 56. \ Ans.$$

9. Find the missing term of

$$\frac{16 \times 12}{9} = \frac{64}{3} = 21\frac{1}{3}. Ans.$$

10. Find the missing term of

$$\frac{4}{3} = 68$$
. Ans.

Exercise 101. Page 221.

1. If 24 men can do a piece of work in 14 days, how long will it take 21 men to do it?

$$\frac{8}{\frac{24 \times 14 \, dy}{21}} = 16 \, dy. \, Ans.$$

2. A well is dug in 13 days of 9 hours each. How many days of 10 hours each would it have taken?

$$\frac{9 \times 13 \text{ dy.}}{10} = \frac{117}{10} \text{ dy.} = 11\frac{7}{10} \text{ dy.} \text{ Ans.}$$

3. A man who steps 2 ft. 5 in. takes 2480 steps in walking a certain distance. How many steps of 2 ft. 7 in. will be required for the same distance?

2 ft.
$$5 in. = 29 in.$$

2 ft. 7 in.
$$= 31$$
 in.

$$\frac{29 \times 2480}{31} = 2320. Ans.$$

4. If $\frac{5}{13}$ of a ton of hay costs \$6, what will $7\frac{5}{9}$ cwt. cost, at the same rate?

$$7\frac{5}{6} \text{ cwt.} = \frac{7\frac{5}{20}}{20} \text{ t.} = \frac{17}{45} \text{ t.}$$

$$\frac{5}{13} : \frac{17}{45} : : \$6 : \text{what?}$$

$$\frac{2}{45 \times \$6} = \frac{17 \times 13 \times \$6}{45 \times 5} = \$\frac{442}{75} = \$5.89. \text{ Ans.}$$

5. If 42 yd. of carpet 2 ft. 3 in. wide are required for a room, how many yards of carpet 2 ft. 4 in. wide will be required?

2 ft. 3 in. = 27 in. 2 ft. 4 in. = 28 in.

$$28 : 27 : : 42 \text{ yd.} : \text{ what ?}$$

$$\frac{3}{28 \times 42 \text{ yd.}} = \frac{81}{2} \text{ yd.} = 40\frac{1}{2} \text{ yd.} \text{ Ans.}$$

6. A court was paved with 950 stones, each containing 15 sq. ft., and is repaved with 836 stones of a uniform size. Find the surface of each.

$$\frac{950 \times 1\frac{5}{6} \text{ sq. ft.}}{836} = \frac{\frac{25}{950} \times 11}{\frac{836}{22}} \text{ sq. ft.} = \frac{21}{12} \text{ sq. ft.} Ans.$$

7. If a train, at the rate of $\frac{5}{15}$ of a mile per minute, requires $3\frac{1}{4}$ hours to make a certain distance, how long will it require at the rate of $\frac{7}{15}$ of a mile a minute?

$$\frac{\frac{7}{15} : \frac{5}{13} : : 3\frac{1}{4} \text{ hr. : what?}}{\frac{5}{13} \times \frac{3\frac{1}{4} \text{ hr.}}{7}} = \frac{15}{7} \times \frac{5}{13} \times \frac{13}{4} \text{ hr. } = \frac{75}{28} \text{ hr. } = 2\frac{19}{28} \text{ hr. } Ans.$$

8. When a post 4 ft. 8 in. high casts a shadow 7 ft. 3 in. long, how long a shadow will a post 11 ft. high cast?

4 ft. 8 in. =
$$4\frac{2}{3}$$
 ft. 7 ft. 3 in. = $7\frac{1}{4}$ ft.

$$4\frac{2}{3}: 11:: 7\frac{1}{4}$$
 ft. : what?
$$\frac{11 \times 7\frac{1}{4}$$
 ft. = $\frac{3 \times 11 \times 29}{14 \times 4}$ ft. = $17\frac{5}{56}$ ft. = 17 ft. $1\frac{1}{14}$ in. Ans.

9. When a post 5 ft. 7 in. high casts a shadow 8 ft. 5 in. long, how high is a steeple that casts a shadow of 202 ft.?

$$8_{1\frac{5}{8}}: 202::5_{1\frac{7}{8}}$$
 ft.: what? $\frac{202 \times 5_{1\frac{7}{8}}}{8_{1\frac{5}{8}}} = \frac{12 \times 202 \times 67}{101 \times 12}$ ft. = 134 ft. Ans.

10. If 4 men can mow a certain field in 10 hours, how many men will it take to mow it in 5 hours?

5:10::4 men: what?
$$\frac{2}{10 \times 4 \text{ men}} = 8 \text{ men. } Ans.$$

11. If a tap discharging 4 gal. a minute empties a cistern in 3 hours, how long will it take a tap discharging 7 gal. a minute to empty it?

7:4::3 hr.: what?
$$\frac{4 \times 3 \text{ hr.}}{7} = 15 \text{ hr. } Ans.$$

12. If a pipe discharging 3 gal. 1 pt. a minute fills a tub in 4 min. 20 sec., how long will it take a pipe discharging 83 qt. a minute to fill it?

166: 25:: 260 sec.: what?
$$\frac{25 \times 269 \text{ sec.}}{166} = 39\frac{13}{166} \text{ sec. } Ans.$$

13. If both pipes of Ex. 12 discharge at the same time into the tub, how long will it take to fill it?

25 pt. + 166 pt. = 191 pt. 191:25::260 sec. : what?
$$\frac{25 \times 260 \text{ sec.}}{191} = \frac{6500}{191} \text{ sec.} = 34_{191}^{6} \text{ sec.} \text{ Ans.}$$

14. How long will it take to fill a cistern of 165 gal. by a pipe that fills one of 120 gal. in 7 min. 16 sec.?

16 sec. =
$$\frac{4}{15}$$
 min. 120:165::7 $\frac{4}{15}$ min.: what?

$$\frac{165 \times 7\frac{4}{15} \text{ min.}}{120} = \frac{\cancel{165} \times 109}{120 \times \cancel{15}} \text{min.} = 9\frac{11}{120} \text{ min.} = 9 \text{ min.} 59\frac{1}{2} \text{ sec.} \quad Ans.$$

15. If a ship sails 1800 mi. in a fortnight, how long will it take to make a voyage of 5000 mi.?

1800:5000::2 wk.: what?

$$\frac{\frac{25}{5900} \times 2 \text{ wk.}}{1800} = \frac{50}{9} \text{ wk.} = 5\frac{5}{9} \text{ wk.}$$

$$\frac{5}{9} \text{ wk.} = 5 \text{ wk. 4 dy. nearly.} \quad Ans.$$

16. The wheels of a carriage are 6 ft. 9 in. and 9 ft. 6 in., respectively, in circumference. How many times will the larger turn while the smaller turns 3762 times?

$$\frac{6\frac{1}{4} \times 3762}{9\frac{1}{4}} = \frac{\cancel{2} \times 27 \times \cancel{3762}}{\cancel{19} \times \cancel{4}} = 2673. \text{ Ans.}$$

17. If $\frac{3}{25}$ of a ship is worth \$2167, what is $\frac{7}{17}$ of it worth?

$$\frac{8}{25}:\frac{7}{17}::82167:$$
 what?

$$\frac{\frac{7}{17} \times \$2167}{\frac{3}{15}} = \frac{25 \times 7 \times \$2167}{3 \times 17} = \$\frac{379225}{51} = \$7435.78. Ans.$$

18. What is the weight of 18 cu. ft. 432 cu. in. of stone, if 10 cu. ft. 864 cu. in. of the stone weighs 14 cwt. 7 lb.?

$$\frac{18\frac{1}{4} \times 1407 \text{ lb.}}{10\frac{1}{2}} = \frac{2 \times 73 \times 1407 \text{ lb.}}{21 \times 4} = \frac{4891}{2} \text{ lb.} = 2445\frac{1}{2} \text{ lb.}$$

$$2 = 1 \text{ t. 4 cwt. } 45\frac{1}{2} \text{ lb.} \quad Ans.$$

19. If 280 lb. of flour makes 360 lb. of bread, how many four-pound loaves can be made from 1 cwt. of flour?

$$\frac{100 \times 366 \text{ lb.}}{286} = \frac{900}{7} \text{ lb.} = 1284 \text{ lb.}$$

$$1284 \div 4 = 324. \text{ Ans.}$$

20. If a column of mercury 27.93 in. high weighs 0.76 of a pound, what is the weight of a column of mercury of the same diameter 29.4 in. high?

$$\frac{0.2 \quad 4}{29.4 \times 9.76 \text{ lb.}} = 0.8 \text{ lb.} \quad Ans.$$

$$\frac{27.93}{9.19}$$

21. How many francs will pay a bill of £100, when £42 10s. 8d. is equivalent to 1000.98 francs?

£42 10s. 8d. = £42
$$\frac{4}{15}$$
.

$$42\frac{8}{15}$$
: 100:: 1090.98 fr.: what?

$$\frac{100 \times 1090.98 \text{ fr.}}{42\frac{8}{15}} = \frac{15}{638} \times 109998 \text{ fr.} = 2565 \text{ fr. } Ans.$$

22. What is the weight of a cube of stone 2 ft. 2 in. on an edge, if a cube 1 ft. 4 in. on an edge weighs 537.6 lb.?

2 ft. 2 in. =
$$2\frac{1}{6}$$
 ft. 1 ft. 4 in. = $1\frac{1}{6}$ ft.

$$(1\frac{1}{8})^8: (2\frac{1}{8})^8: :537.6 \text{ lb.}: \text{ what }?$$

$$\frac{94}{216}$$
: : 537.6 lb.: what?

$$\frac{21}{672}$$

$$\frac{27}{64} \times \frac{2197}{216} \times \frac{5376}{10} \text{ lb.} = \frac{46137}{20} \text{ lb.} = 2306.85 \text{ lb.} Ans.$$

23. If a square field 50 yd. 10% in. on a side is worth \$2710\%, what is a square field 62 yd. 1 ft. on a side worth?

50 yd. 10% in. = 50% yd. 62 yd. 1 ft. = 62% yd.
$$(50\%)^2 : (62\%)^2 : \$2710\%$$
; what?
$$\frac{123904}{49} : \frac{34969}{9} : \$\frac{46080}{17} : \text{what?}$$

$$\frac{17}{123994} \times \frac{34969}{9} \times \$\frac{43089}{17} = \$4165. \text{ Ans.}$$

$$171$$

24. A gains 4 yd. on B in running 30 yd. How many yards will he gain while B is running 97½ yd.?

B runs 26 yd. while A is running 30 yd.

$$26:97\frac{1}{4}::4 \text{ yd.}:\text{what ?}$$

$$\frac{15}{\cancel{2}\cancel{5}\cancel{5} \times \cancel{4}\cancel{9}\cancel{d}} = 15 \text{ yd. } Ans.$$

25. If 10 cu. in. of gold weighs as much as 193 cu. in. of water, how many cubic inches are there in a nugget of gold that weighs as much as a cubic foot of water?

$$\frac{1728 \times 10 \text{ cu. in.}}{193} = \frac{17280}{193} \text{ cu. in.} = 89\frac{193}{193} \text{ cu. in.} Ans.$$

26. If a garrison of 1500 men has provisions for 13 months, how long will the provisions last if the garrison is reënforced by 700 men?

$$1500 + 700 = 2200.$$

$$\frac{15}{\cancel{2200}} \times \frac{13 \text{ mo.}}{\cancel{2200}} = \frac{195}{22} \text{ mo.} = 8\frac{19}{22} \text{ mo.} = 8 \text{ mo. } 26 \text{ dy. } Ans.$$

27. If a tree 38 ft. high is represented by a drawing 1½ in. high, what height on the same scale will represent a house 45 ft. high?

$$38:45::1\frac{1}{4}$$
 in.: what?

$$\frac{45 \times 3}{38 \times 2}$$
 in. $= \frac{135}{76}$ in. $= 1\frac{59}{76}$ in. Ans.

28. If a country 630 mi. long is represented on a raised map by a length of $5\frac{1}{2}$ ft., by what height ought a mountain of 15,750 ft. to be represented on the map?

630 mi. =
$$3,326,400$$
 ft. $5\frac{1}{2}$ ft. = 66 in.

$$\frac{\cancel{13759} \times \cancel{66} \text{ in.}}{\cancel{3326499}} = \frac{5}{16} \text{ in. } Ans.$$

$$\cancel{59499}$$

$$\cancel{16}$$

29. A train travels 1 of a mile in 18 sec. How many miles an hour does it travel?

1 hr. = 3600 sec.

18:3600:: 1 mi.: what?

$$\frac{200}{3699 \times \frac{1}{4} \text{ mi.}} = 50 \text{ mi. } Ans.$$

30. If $4\frac{1}{2}$ t. of coal fill a bin 9 ft. long, 5 ft. broad, 5 ft. high, how many cubic feet are required for the coal of a steamer that carries coal for 3 wk. at 20 t. a day?

$$9 \times 5 \times 5 = 225.$$

3 wk. = 21 dy.

 $21 \times 20 \text{ t.} = 420 \text{ t.}$

41:420::225 cu. ft.: what?

$$\frac{25}{9} = 21,000 \text{ cu. ft.} Ans.$$

31. If 2 lb. of rosin are melted with 5 oz. of mutton tallow, to make a grafting wax, how many ounces of tallow will 20 oz. of the wax contain?

$$2 lb. + 5 oz. = 2 lb. 5 oz. = 37 oz.$$

37:20::5 oz.: what?

$$\frac{20 \times 5 \text{ oz.}}{37} = \frac{100}{37} \text{ oz.} = 2\frac{25}{37} \text{ oz.}$$
 Ans.

Exercise 102. Page 225.

1. In how many days of 8 hr. will 60 men do the same work that 24 men can do in 15 dy. of 10 hr.?

$$\begin{array}{c|c} 8 & 10 \\ 60 & 24 \end{array}$$
 :: 15 dy.: what?

$$\frac{\frac{5}{10} \times \frac{3}{24} \times 13 \text{ dy.}}{8 \times 60} = \frac{15}{2} \text{ dy.} = 7\frac{1}{2} \text{ dy.} \text{ Ans.}$$

2. What is the expense of covering a room with drugget 4 ft. wide, at 91‡ cents a yard, if carpet 2 ft. 3 in. wide for the room costs \$ 70.50, at \$ 1.37‡ a yard?

\$0.91\frac{2}{3} = \$\frac{1}{1\frac{1}{2}}\$. \$1.37\frac{1}{2} = \$1\frac{1}{2}\$.

$$\frac{4}{1\frac{2}{3}} \left| \frac{2\frac{1}{4}}{1\frac{1}{2}} :: $70\frac{1}{2}$: what ?$$

$$\frac{2}{4} \times \frac{3}{4} \times \frac{71}{4} \times \frac{3}{4} \times \frac{71}{12} \times \frac{141}{2} = $\frac{423}{16} = 26.44. Ans.$$

3. If 4418 tons of iron ore produce \$36,190 worth of metal, when iron is at \$37.50 a ton, what will be the value of the iron at \$47 a ton from 2275 tons of ore?

$$\begin{array}{c|c}
37\frac{1}{4} & 47 \\
4418 & 2275
\end{array} : \$36,190 : \text{what?}$$

$$\frac{91}{75 \times \cancel{4418}} = \$\cancel{50070} = \$\cancel{23,356.67}. \quad Ans.$$

$$\frac{37\frac{1}{4} & 47}{3} = \$\cancel{23,356.67}. \quad Ans.$$

4. If a bar of iron 3\frac{1}{2} ft. long, 3 in. wide, and 2\frac{3}{2} in. thick weighs 93 lb., what will be the weight of a bar 3\frac{3}{2} ft. long, 4 in. wide, and 2\frac{1}{2} in. thick?

$$3\frac{1}{3}$$
 $3\frac{2}{3}$ 3 4 : : 93 lb. : what? $2\frac{3}{4}$ $2\frac{1}{4}$

$$\frac{11}{3} \times \frac{\cancel{3}}{\cancel{3}} \times \frac{\cancel{3}}{\cancel{2}} \times \frac{\cancel{3}}{\cancel{2}} \times \frac{\cancel{3}}{\cancel{11}} \times \frac{\cancel{3}1}{\cancel{9}3} \text{ lb.} = 124 \text{ lb. } Ans.$$

5. If 40 bu. of wheat can be grown on the same area as 48 bu. of barley, and 28 A. produce 840 bu. of wheat, how much barley will 38 A. produce?

$$\begin{array}{c|c}
40 & 48 \\
28 & 38 \\
\end{array} : 840 \text{ bu.} : \text{ what ?} \qquad \begin{array}{c|c}
6 & 39 \\
48 \times 38 \times 849 \text{ bu.} \\
\hline
49 \times 28 \\
\hline
5 & 38 \\
\end{array} = 1368 \text{ bu.}$$

6. If 18 men can dig a trench 150 ft. long, 6 ft. broad, and 4 ft. 6 in. deep in 12 days, in how many days will 16 men dig a trench 210 ft. long, 5 ft. broad, and 4 ft. deep?

7. A book of 810 pages, 40 lines to a page, and 60 letters to a line, is reprinted in pages of 50 lines, 72 letters to a line. How many pages will the new edition contain?

$$\begin{array}{c|c}
50 & 40 \\
72 & 60
\end{array} :: 810 : \text{what?} & \begin{array}{c}
10 & 6 & 45 \\
49 \times 69 \times 819 \\
\hline
59 \times 72 \\
5 & 4
\end{array} = 540. Ans.$$

8. If 3280 42-lb. shot cost \$3000, how many 32-lb. shot can be bought for \$4200?

$$\frac{3000}{32} \begin{vmatrix} 4200 \\ 42 \end{vmatrix} : :3280 : \text{ what ?} \qquad \frac{7}{\cancel{4200} \times \cancel{42} \times \cancel{3280}} = \cancel{6027}. \text{ Ans.}$$

9. What is the rate of wages, if 12 men earn in 10 dy. as much as 9 men earn in 14 dy. at \$1.50 a day?

$$\begin{array}{c|c}
12 & 9 \\
10 & 14
\end{array} :: \$ 1.50 : \text{ what ?} \\
\hline
0.05 \\
7 & 9.13 \\
9 \times 14 \times \$ 1.59 \\
\hline
12 \times 19 \\
4 & 2
\end{array} = \$ 3.15 \\
\hline
2 = \$ 1.575. Ans.$$

10. A rectangular reservoir 15 yd. long and 4 ft. deep holds 32,500 gal. What quantity of water will it hold if its length is increased by 18 ft. and its depth by 1 ft.?

$$\begin{array}{c|c} 15 & 21 \\ \hline 4 & 5 \end{array}$$
 :: 32,500 gal. : what?

$$\frac{7}{\cancel{21} \times \cancel{5} \times \cancel{32500}} \frac{8125}{\cancel{21} \times \cancel{5} \times \cancel{32500}} \frac{\text{gal.}}{\cancel{21}} = 56,875 \text{ gal. } Ans.$$

11. What must be the length of a bar of silver \(\frac{3}{4}\) in. square to weigh the same as a bar of gold \(\frac{1}{2}\) in. square and $6\(\frac{3}{4}\)$ in. long, if the weight of a cubic inch of silver to that of a cubic inch of gold is in the ratio 47:88?

$$\frac{\binom{3}{4}\binom{2}{2}^{2}}{47} \begin{vmatrix} \binom{1}{2}\binom{2}{2} & \cdots & \binom{3}{4} & \cdots & \binom{3}{4}\binom{1}{4} & \cdots & \binom{3}{4}\binom{1}{8} & \cdots & \binom{3}{4}\binom{1}{8} & \cdots & \binom{3}{4}\binom{1}{8}\binom{1}{8} & \cdots & \binom{3}{4}\binom{1}{8}$$

12. How far can A, who takes 3.1 ft. each step, walk, while B, who takes 2.3 ft. each step, walks 220 yd., if A takes 7 steps while B takes 11?

$$\begin{array}{c|c}
2.3 & 3.1 \\
11 & 7
\end{array} :: 220 \text{ yd.} : \text{what?} \\
\frac{20}{2.3 \times 11} & \frac{20}{2.3} \text{ yd.} = \frac{434}{2.3} \text{ yd.} = 188\frac{15}{23} \text{ yd.} \quad Ans.$$

13. If 6 hr. are needed to go a given distance at a given rate, how many hours are needed when the distance is diminished by one fourth and the rate increased by one half?

$$\frac{1}{1\frac{1}{2}} \begin{vmatrix} \frac{3}{4} & \vdots & 6 \text{ hr.} : \text{ what ?} \\ 1\frac{1}{2} & \frac{2}{3} \times \frac{3}{4} \times \frac{3}{6} \text{ hr.} = 3 \text{ hr. } Ans.$$

14. How many hours a day must 5 men work to mow a field in 8 dy. that 7 men can mow in 6 dy. of 10 hr.?

$$\begin{array}{c|c}
5 & 7 \\
8 & 6
\end{array} :: 10 \text{ hr.} : \text{ what ?} \qquad \frac{7 \times \cancel{6} \times \cancel{10} \text{ hr.}}{\cancel{5} \times \cancel{8}} = \frac{21}{2} \text{ hr.} = 10\frac{1}{2} \text{ hr.} \quad Ans.$$

15. If a bar of iron 10 ft. 6½ in. long, 3½ in. broad, and 3½ in. thick weighs 4 cwt. 20.21 lb., what is the length of a bar of iron that weighs a long ton if its breadth and thickness are 4½ in. and 4½ in., respectively?

16. If 27 men in 28 dy. of 10 hr. dig a trench 126 yd. long, 2½ yd. broad, 1½ yd. deep, how long a trench 2½ yd. broad and 1½ yd. deep will 56 men dig in 25 dy. of 8½ hr.?

17. If 34kg of wool makes 25m of cloth 0.6m wide, how long a piece of cloth 0.8m wide will 108.8kg of wool make?

$$\begin{array}{c|c}
34 & 108.8 \\
0.8 & 0.6
\end{array} : 25^{m} : \text{ what ?} \qquad \begin{array}{c}
4 \\
136 \\
\cancel{198.8} \times 0.6 \times 25^{m} \\
\cancel{34} \times \cancel{9.8}
\end{array} = 60^{m}. \text{ Ans.}$$

18. If an oak beam 5.40^m long, 0.63^m thick, and 0.57^m wide weighs 1469.25^{kg}, what is the weight of an oak beam 4.87^m long, 0.58^m thick, and 0.53^m wide?

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$$\frac{29}{487 \times 58 \times 53 \times 5877^{\text{kg}}} = \frac{488782907^{\text{kg}}}{430920} = 1134.2776^{\text{kg}}. \text{ Ans.}$$

19. A certain quantity of air has a volume of 195.5 cu. ft. at 27.8° C. What will be its volume at 100° C.?

$$100^{\circ} - 27.8^{\circ} = 72.2^{\circ}$$
. $72.2 \times 0.00367 = 0.264974$.

1:1.264974::195.5 cu. ft.: what?

 1.264974×195.5 cu. ft. = 247.3 cu. ft. Ans.

20. A quantity of air at a temperature of 15.6° C. has a volume of 4 cu. ft. under a pressure of 12 lb. per square inch. What will be its volume at 48.7° C. under a pressure of 14 lb. per square inch?

$$48.7^{\circ} - 15.6^{\circ} = 33.1.$$
 $33.1 \times 0.00367 = 0.121477.$ $14 \mid 12 \atop 1 \mid 1.121477 :: 4 \text{ cu. ft. : what ?}$

Exercise 103. Page 227.

1. If a man can mow $\frac{3}{11}$ of a field in a day, how long will it take another man to mow $\frac{5}{6}$ of a field $5\frac{1}{4}$ times as large, if the second man works $1\frac{3}{4}$ times as fast as the first, but only $\frac{7}{4}$ as many hours each day?

1st cause. 2d cause. 1st effect. 2d effect.

$$\left. \begin{array}{c} \frac{11}{3} \, \mathrm{dy.} \\ 1 \\ 1 \end{array} \right\} : \left. \begin{array}{c} ? \, \mathrm{dy.} \\ 1 \\ \frac{7}{3} \end{array} \right\} : : 1 : \frac{5}{3} \times 5\frac{1}{4}.$$

$$\frac{\frac{11}{1} \times \frac{5}{8} \times 5\frac{1}{2}}{1\frac{2}{8} \times \frac{7}{8}} = \frac{11}{3} \times \frac{5}{6} \times \frac{5}{21} \times \frac{3}{5} \times \frac{2}{7} = 11. \quad 11 \text{ dy. Ans.}$$

2. If 4 men or 7 boys can do a piece of work in 6 days, how long will it take 6 men and 9 boys to do the work?

4 men = 7 boys.

$$\therefore$$
 6 men = $10\frac{1}{2}$ boys.
 $10\frac{1}{2} + 9 = 19\frac{1}{2}$.

1st cause. 2d cause. 1st effect. 2d effect.

$${7 \text{ boys} \atop 6 \text{ dy.}}$$
 : ${19\frac{1}{2} \text{ boys} \atop ? \text{ dy.}}$:: 1 : 1.

$$\frac{7 \times 6}{19\frac{1}{2}} = \frac{7 \times \cancel{6} \times 2}{\cancel{3}\cancel{9}} = \frac{28}{13} = 2\frac{2}{13}.$$
 2\frac{2}{13} dy. Ans.

3. If 50 men working 9 hr. a day require 6 dy. to dig a trench 100 yd. long, 2 yd. wide, and 3 yd. deep, how many men working 10 hr. a day for 9 dy. will be required to dig a trench 50 yd. long, 6 yd. wide, and 5 yd. deep, in ground twice as hard to dig?

1st cause.
 2d cause.
 1st effect.
 2d effect

 50 men
 ? men
 10 hr.
 2 yd. :
$$\begin{cases} 50 \text{ yd.} \\ 6 \text{ yd.} \\ 5 \text{ yd.} \end{cases}$$

 6 dy.
 2 yd. : $\begin{cases} 50 \text{ yd.} \\ 6 \text{ yd.} \\ 5 \text{ yd.} \end{cases}$

$$\frac{\cancel{50} \times \cancel{9} \times \cancel{6} \times \cancel{2} \times 50 \times \cancel{6} \times \cancel{5}}{\cancel{10} \times \cancel{9} \times \cancel{100} \times \cancel{2} \times \cancel{3}} = 150. \quad 150 \text{ men. } Ans.$$

4. If 12 men in 9 dy. can harvest 40 A. of wheat, how many acres can 16 men harvest in 3 dy.?

1st cause. 2d cause. 1st effect. 2d effect.

$${12 \text{ men} \atop 9 \text{ dy.}}$$
 : ${16 \text{ men} \atop 3 \text{ dy.}}$:: 40 A. : ? A.

$$\frac{16 \times 3 \times 40}{12 \times 9} = \frac{160}{9} = 17\frac{7}{5}.$$
 17\frac{7}{4} A. Ans.

5. If 120 men can make an embankment $\frac{3}{4}$ of a mile long, 30 yd. wide, and 7 yd. high, in 42 dy., how many men will it take to make an embankment 1000 yd. long, 36 yd. wide, and 22 ft. high, in 30 dy.?

6. If 7 women in 8 dy. of 11 hr. each can make 22 dozen shirts, in how many days of 10 hr. each can 12 women make 360 dozen shirts?

1st cause. 2d cause. 1st effect. 2d effect.

7 women 8 dy. 12 women 2 : ? dy. 10 hr. 22 doz. : 360 doz.

11 hr.
$$\frac{4}{12 \times 19 \times 22} = 84$$
.

84 dy. Ans.

7. Twenty-five lamps used 5 hr. an evening for 40 dy. required a quantity of oil that cost \$4.25. How many lamps used 4 hr. an evening for 30 dy. can be furnished with oil at a cost of \$7.65?

8. If 8 horses can be kept 12 dy. for a certain sum when hay is worth \$15 a ton, how many days can 6 horses be kept for the same sum when hay is worth \$12 a ton?

9. Twenty horses working 14 wk., 6 dy. a week and 8 hr. a day, transport the output of a mine to the nearest wharf. In how many weeks will 24 horses do the same work, if they work 5 dy. a week and 7 hr. a day?

1st cause. 2d cause. 1st effect. 2d effect.

20 horses
14 wk.
6 dy.
8 hr.

24 horses
? wk.
5 dy.
7 hr.

1.

$$\frac{4}{20 \times 14 \times 5 \times 8} = 16$$
.

24 wk.
4 16 wk.
4 16 wk.
4 18.

10. If 6 men can reap a field of rye 200 yd. long and 150 yd. wide in 4 dy. of 12 hr. each, in how many days of 10 hr. each will 8 men reap a field 300 yd. long and 250 yd. wide?

11. If a boy can do only half as much work as a man, how many hours a day must 42 boys work to accomplish as much in 45 dy. as 27 men, working 10 hr. a day, would accomplish in 28 dy.?

$$42 \text{ boys} = 21 \text{ men.}$$

1st cause. 2d cause. 1st effect. 2d effect.
27 men 21 men 3 :: 1 :: 1.
28 dy.
$$\frac{3}{27} \times \frac{2}{10} \times \frac{4}{25} = 8$$
.

8 hr. Ans.

Exercise 104. Page 229.

1. Divide \$12,000 proportionally to the numbers 3, 4, 5.

$$3 + 4 + 5 = 12.$$

$$\frac{3}{12} \times \$ \cancel{12000} = \$ 3000.$$

$$\frac{4}{12} \times \$ \cancel{12000} = \$ 4000.$$

$$\frac{5}{12} \times \$ \cancel{12000} = \$ 5000.$$

2. Divide 815 tons proportionally to \(\frac{1}{4}\), \(\frac{2}{4}\), \(\frac{1}{4}\).

$$60 \times (\frac{1}{2}, \frac{2}{3}, \frac{3}{4}, \frac{4}{5}) = 30, 40, 45, 48.$$

 $30 + 40 + 45 + 48 = 163.$

$$\frac{30}{163} \times 815 \text{ t.} = 150 \text{ t.}$$

$$\frac{40}{163} \times 815 \text{ t.} = 200 \text{ t.}$$

$$\frac{45}{163} \times 815 \text{ t.} = 225 \text{ t.}$$

$$\frac{48}{163} \times 815 \text{ t.} = 240 \text{ t.}$$

3. Divide 6853 lb. of wool proportionally to 1½, 2½, 5½; also proportionally to the reciprocals of these numbers.

$$60 \times (\frac{7}{4}, \frac{14}{5}, \frac{35}{6}) = 105, 168, 350.$$

$$105 + 168 + 350 = 623.$$

$$\frac{105}{623} \times 6853 \text{ lb.} = 1155 \text{ lb.}$$

$$\frac{168}{623} \times 6853 \text{ lb.} = 1848 \text{ lb.}$$

$$\frac{350}{623} \times 6853 \text{ lb.} = 3850 \text{ lb.}$$

The reciprocals of

$$1\frac{3}{4}, 2\frac{4}{5}, 5\frac{5}{6} = \frac{4}{7}, \frac{5}{14}, \frac{5}{35}.$$

$$70 \times (\frac{4}{7}, \frac{5}{14}, \frac{5}{35}) = 40, 25, 12.$$

$$40 + 25 + 12 = 77.$$

$$\frac{40}{77} \times \cancel{6}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}$$

$$1b. = 3560 \text{ lb.}$$

$$\frac{25}{77} \times \cancel{6}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}$$

$$1b. = 2225 \text{ lb.}$$

$$\frac{12}{77} \times \cancel{6}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}\cancel{5}$$

$$1b. = 1068 \text{ lb.}$$

4. Two men purchase some property together, one paying \$1250 and the other \$1000. If the value of the property rises to \$3600, what will be the share of each?

\$1250 + \$1000 = \$2250.

$$\frac{250}{1250}$$
 \times \$8
 $\frac{250}{2250}$ \times \$8
 $\frac{200}{2250}$ \times \$8
 $\frac{200}{2250}$ \times \$8
\$8
\$8
\$900 = \$1600.

5. Gun metal is composed by weight of 3 parts of tin to 100 parts of copper. What weight of each of these metals is there in a cannon weighing 721 lb.?

$$3 + 100 = 103$$
.
 $\frac{3}{193} \times 721$ lb. = 21 lb., tin.
 $\frac{100}{193} \times 721$ lb. = 700 lb., copper.

6. Bell metal contains by weight 78 parts of copper and 22 parts of tin. What weight of each of these metals is there in a bell weighing 937 lb.?

$$78 + 22 = 100.$$

937 lb.

937 lb.

0.78

7496

1874

6559

1874

730.86 lb., copper.

206.14 lb., tin.

7. It takes 75kg of saltpetre, 12.5kg of charcoal, and 12.5kg of sulphur to make 100kg of powder. How many kilograms of each will be required to make 10,000,000 cartridges, each containing 55 of powder?

$$10,000,000 \times 5g = 50,000,000g = 50,000 kg.$$

$$75 kg + 12.5 kg + 12.5 kg = 100 kg.$$

$$\frac{75}{1999} \times 599999 kg = 37,500 kg, saltpetre.$$

$$\frac{125}{1999} \times 599999 kg = 6250 kg, charcoal.$$

$$\frac{125}{1999} \times 599999 kg = 6250 kg, sulphur.$$

8. Yellow copper contains by weight 2 parts of red copper and 1 part of zinc. How many ounces of red copper in an article of yellow copper that weighs 1 lb.?

$$2 + 1 = 3$$
. $\frac{2}{3} \times 16$ oz. $= \frac{32}{3}$ oz. $= 10\frac{2}{3}$ oz. Ans.

9. Type metal is an alloy containing by weight 39 parts of lead to 11 parts of antimony. How many pounds of each are required to make 957 lb. of type?

$$39 + 11 = 50.$$

$$\frac{89}{50} \times 957$$
 lb. $= \frac{87323}{50}$ lb. $= 746.46$ lb., lead. $\frac{11}{50} \times 957$ lb. $= \frac{10527}{50}$ lb. $= 210.54$ lb., antimony.

10. Plumbers' solder contains by weight 2 parts of lead and 1 part of tin. How many pounds of each are required to make 100 lb. of solder?

$$2 + 1 = 3$$
.
 $\frac{2}{3} \times 100 \text{ lb.} = \frac{200}{3} \text{ lb.} = 66\frac{2}{3} \text{ lb.}, \text{ lead.}$
 $\frac{1}{3} \times 100 \text{ lb.} = \frac{100}{3} \text{ lb.} = 33\frac{1}{3} \text{ lb.}, \text{ tin.}$

11. The air is composed of oxygen and nitrogen. In 100 volumes of air there are 21 volumes of oxygen and 79 of nitrogen. If the weight of a liter of oxygen is 1.4295s, and that of a liter of nitrogen is 1.2577s, how many grams of each gas does 100s of air contain?

1.4295g	1.25778
21	79
14295	113193
28590	88039
30.0195g	99.3583g

$$30.0195s + 99.3583s = 129.3778s$$
.
 $\frac{30.0195}{129.3778} \times 100s = 23.203s$, oxygen. Ans.
 $100s - 23.203s = 76.797s$, hydrogen. Ans.

12. At \$20.67 an ounce for pure gold, what is the value of the gold in a chain that weighs 3 oz. 4 dwt., if it is 18 carats fine (that is, 18 parts of pure gold out of 24)?

3 oz. 4 dwt. =
$$3\frac{1}{8}$$
 oz. = 3.2 oz. $\frac{13}{14} = \frac{3}{4} = 0.75$.

\$ 20.67

 $\frac{3.2}{4134}$
 $\frac{0.75}{330720}$
 $\frac{6201}{866.144}$
 $\frac{463008}{49.60800}$
\$ 49.61. Ans.

13. Two men agree to do a piece of work for \$63. They finish the work in 18 days, but one of them was absent 5 days of this time. How should the pay be divided?

$$18 \text{ dy.} + 18 \text{ dy.} = 31 \text{ dy.}$$

$$\frac{18}{17} \times 863 = 8 \cdot \frac{1134}{17} = 836.58. \qquad \frac{11}{17} \times 863 = 8 \cdot \frac{1134}{17} = 826.42.$$

14. Five men working together do a piece of work in 20 days, and receive as pay \$253. One of the men was absent 5 days, and another 2 days of this time. How should the pay be divided?

$$20 \text{ dy.} + 20 \text{ dy.} + 20 \text{ dy.} + 15 \text{ dy.} + 18 \text{ dy.} = 93 \text{ dy.}$$

$$\frac{20}{93} \times \$253 = \$\frac{5060}{93} = \$54.41. \qquad \frac{\cancel{15}}{\cancel{93}} \times \$253 = \$\frac{1265}{31} = \$40.80.$$

$$\frac{6}{\cancel{15}} \times \$253 = \$\frac{1518}{31} = \$48.97.$$

Hence, three should receive \$54.41 each, one \$40.80, and one \$48.97. Ans.

15. Standard silver consists of 37 parts of pure silver to 3 parts of copper. What weight of pure silver in the crown piece that weighs \frac{19}{17} oz. troy?

$$37 + 3 = 40.$$
 $\frac{37}{49} \times \frac{19}{11}$ oz. $= \frac{37}{44}$ oz. Ans.

Exercise 105. Page 232.

1. A, B, and C entered into partnership, A furnishing \$18,150; B, \$19,860; and C, \$10,890. If their profits were \$12,100, what was each man's share of the profits?

\$ 18,150 + \$ 19,360 + \$ 10,890 = \$ 48,400.

$$\frac{9075}{18130} \times $ 12109 = $ \frac{9075}{2} = $ 4537.50, A.$$

$$\frac{4}{2}$$

$$\frac{4840}{19369} \times $ 12109 = $ 4840, B.$$

$$\frac{5445}{48409} \times $ 12109 = $ \frac{5445}{2} = $ 2722.50, C.$$

2. Four men engaged in business together and made a profit of \$1200. How much of it should each man receive, if the first put in \$3000, the second \$5000, the third \$4200, and the fourth \$2400?

\$ 3000 + \$ 5000 + \$ 4200 + \$ 2400 = \$ 14,600.

$$\frac{3000}{14699} \times $ 1299 = $ \frac{18000}{73} = $ 246.57, 1st.$$

$$\frac{5000}{14699} \times $ 1299 = $ \frac{30000}{73} = $ 410.96, 2d.$$

$$\frac{4200}{73} \times $ 1299 = $ \frac{25200}{73} = $ 345.21, 3d.$$

$$\frac{2400}{73} \times $ 1299 = $ \frac{14400}{73} = $ 197.26, 4th.$$

3. A man dies owing three creditors \$8050, \$2970, and \$7170, respectively. If his assets, after deducting expenses, are \$13,646, how much will each creditor receive?

\$8050 + \$2970 + \$7170 = \$18,190.
$$\frac{805}{8959} \times $13646 = $6039.05.$$

$$\frac{297}{1819} \times $13646 = $2228.07.$$

$$\frac{717}{1819} \times $13646 = $5378.88.$$

$$\frac{717}{1819} \times $13646 = $5378.88.$$

4. Three heirs receive from an estate \$4700, \$3200, and \$12,500, respectively, on condition that they together pay a debt of \$2000. What amount will each have?

\$ 4700 + \$ 3200 + \$ 12,500 = \$ 20,400.

$$\frac{4700}{20400} \times $ 2000 = $ \frac{23500}{51} = $ 460.78.$$

$$\frac{3200}{20400} \times $ 2000 = $ \frac{16000}{51} = $ 313.73.$$

$$\frac{12500}{20400} \times $ 2000 = $ \frac{62500}{51} = $ 1225.49.$$
\$ 4700.

$$\frac{460.78}{$ 4239.22} = \frac{313.73}{$ 2886.27} = \frac{1225.49}{$ 11274.51} = \frac{1}{205} $

5. Arnold and Baker enter into partnership. Arnold puts in \$6000 for 8 mo., and Baker \$4000 for 6 mo. Their profits are \$2000. What is each man's share?

$$8 \times \$ 6000 = \$ 48000
6 \times 4000 = \frac{24000}{\$ 72000}
\frac{2}{\$ 72000}
\frac{2}{72999} \times \$ 2000 = \$ 1333.33, Arnold's.
\frac{24999}{72999} \times \$ 2000 = \$ 666.67, Baker's.
3$$

6. Dobson furnishes the firm of Dobson & Fogg with \$5000 for 13 mo.; Fogg furnishes \$7000 for 9 mo. Their profits are \$1700. What is the share of each?

$$\begin{array}{r}
13 \times \$5000 = \$65000 \\
9 \times 7000 = \frac{63000}{\$128000} \\
\frac{65}{\$5999} \times \$1799 = \$\frac{27625}{32} = \$863.28, \text{ Dobson's.} \\
128 \times \$1700 - \$863.28 = \$836.72, \text{ Fogg's.}
\end{array}$$

7. In a business partnership, A furnishes \$800, and after 3 mo. \$250 more; B furnishes \$950, and at the end of 2 mo. withdraws \$200; C furnishes \$650, and at the end of 6 mo. \$400 more. At the end of a year their profit is \$2516. How shall it be divided among them?

A. B. C.
$$12 \times \$800 = \$9600 \quad 12 \times \$950 = \$11400 \quad 12 \times \$650 = \$7800$$

$$9 \times 250 = 2250 \quad 10 \times 200 = 2000 \quad 6 \times 400 = 2400$$

$$\$11,850 + \$9400 + \$10,200 = \$31,450.$$

$$\frac{237}{31450} \times \$2516 = \$948, \text{ A's.} \quad \frac{188}{31450} \times \$2516 = \$752, \text{ B's.}$$

$$\frac{204}{31430} \times \$2516 = \$948, \text{ A's.} \quad \frac{9400}{31450} \times \$2516 = \$752, \text{ B's.}$$

8. Two partners, A and B, enter into partnership with capitals of \$3500 and \$8700, respectively, and A is to have 0.12 of the profits for managing the business. How shall a profit of \$1906.25 be divided between them?

$$$481.25 + $228.75 = $710$$
, A's. $$1906.25 - $710 = 1196.25 , B's.

9. A puts \$2100 into a business, and B \$1750. At the end of a year each puts in \$700 more, and C joins them with \$2500. How shall a profit of \$2166.50 be divided 18 months after C enters the firm?

A. B. C.
$$30 \times $2100 = $63000$$
 $30 \times $1750 = 52500 $18 \times $2500 = 45000 . $18 \times 700 = 12600$ 875600 865100

$$$75,600 + $65,100 + $45,000 = $185,700.$$

$$\frac{75699}{75699} \times \$ \frac{14}{199} = \$ 882, A's. \qquad \frac{217}{651} \times \$ \frac{7}{1999} = \$ 759.50, B's.$$

$$\frac{75699}{15475} \times \$ \frac{216659}{1999} \times \$ \frac{216659}{1999} \times \$ \frac{7}{199} = \$ 759.50, B's.$$

$$\frac{3}{450} = \frac{175}{185700} \times \$ \frac{216650}{199} = \$ 525, C's.$$

10. Three graziers hire a pasture, for which they pay \$132.50. One puts in 10 oxen for 3 months, another 12 oxen for 4 months, and the third 14 oxen for 2 months. How much of the rent ought each to pay?

$$3 \times 10 = 30
4 \times 12 = 48
2 \times 14 = 28
\hline
106$$

$$\frac{15}{106}$$

$$\frac{15}{106}$$

$$\frac{12}{48} \times \frac{125}{13250} = $60, 2d.$$

$$\frac{15}{106} \times \frac{125}{13250} = $37.50, 1st.$$

$$\frac{28}{106} \times \frac{13250}{100} = $35, 3d.$$

11. A begins business, with a capital of \$2400, on the 19th of March; and on the 17th of July admits B as a partner, with a capital of \$1800. December 31 the profits are \$943. What is the share of each?

From March 19 to Dec. 31 is 288 dy. From July 17 to Dec. 31 is 168 dy.

12. A and B join capitals in the ratio 7:11. At the end of 7 months A withdraws ½ of his, and B ½ of his; and, after 11 months more, they divide a profit of \$5148.50. What is the share of each?

$$\begin{array}{r}
 18 \times 7 &= 126 \\
 11 \times 3\frac{1}{2} &= \frac{38\frac{1}{2}}{87\frac{1}{2}} &= \frac{38\frac{1}{2}}{87\frac{1}{2}} &= \frac{525}{8}. \\
 525 + 946 &= 1471. \\
 \frac{21}{\cancel{525}} &= \cancel{514859} \\
 \frac{\cancel{514859}}{\cancel{199}} &= \$ 1837.50, A's.
 \end{array}$$

\$5148.50 - \$1837.50 = \$3311, B's.

13. Divide £65 9s. among three men, so that the first may have as many half-crowns as the second has shillings; and the second as many guineas as the third has pounds.

1st has 2½ times as much as 2d. 2d has ¾ as much as 3d.

3d has 1 part.

2d has
$$\frac{21}{100}$$
 part.

1st has $\frac{21}{8}$ part.

3d has 40 parts.

2d has 42 parts.

1st has 105 parts.

1st has 105 parts.

All have 187 parts.

£65 9s. = 1309s.

$$\frac{105}{187} \times 1309s. = 735s. = £36 15s.$$

$$\frac{42}{187} \times 1309s. = 294s. = £14 14s.$$

$$\frac{40}{187} \times 1309s. = 280s. = £14.$$

14. A and B begin business each with a capital of \$2000. A adds \$500 at the end of 2 months, and \$500 more at the end of 7 months; B adds \$800 at the end of 3 months. If the profits are \$3605.25 at the end of a year, what is the share of each?

$$12 \times \$2000 = \$24000$$

$$10 \times 500 = 5000$$

$$5 \times 500 = \frac{2500}{\$31500}$$

$$\$31,500 + \$31,200 = \$62,700.$$

$$21$$

$$315$$

$$345$$

$$31500 \times \$3505.25 - \$1811.25 = \$1794, B's.$$

15. Three partners in a restaurant furnish respectively \$500 for 7 months, \$600 for 8 months, and \$900 for 9 months. If they lose \$410, what is each one's share of the loss?

16. Two capitalists contribute, one \$10,000, the other \$12,000, to an enterprise which continues in operation for 10 years. Ten months after starting a third man becomes a partner and contributes \$15,000; and 2 years after this a fourth man contributes \$17,400. If the total profits are \$45,600, what amount does each partner receive?

$$120 \times \$10,000 = \$1200000$$

$$120 \times 12,000 = 1440000$$

$$110 \times 15,000 = 1650000$$

$$86 \times 17,400 = \frac{1496400}{\$5786400}$$

$$\frac{500}{\$786400} \times \$45600 = \$\frac{22800000}{2411} = \$9456.66.$$

$$\frac{1449000}{\$786400} \times \$45600 = \$\frac{27360000}{2411} = \$11,347.99.$$

$$\frac{1449000}{\$786400} \times \$45600 = \$\frac{27360000}{2411} = \$11,347.99.$$

$$\frac{16590000}{\$786400} + \$45600 = \$\frac{31350000}{2411} = \$13,002.90.$$

$$\frac{1496400}{\$786400} \times \$45600 = \$\frac{28431600}{2411} = \$11,792.45.$$

$$\frac{1496400}{\$786400} \times \$45600 = \$\frac{28431600}{2411} = \$11,792.45.$$

17. A began business with a capital of \$2500. After three years he invested \$1250 more, and took as a partner B, who invested \$5000. At the end of four years more the profits amounted to \$9562.50. What was the share of each?

A. B.
$$7 \times \$2500 = \$17500$$
 $4 \times \$5000 = \20000 . $4 \times 1250 = \frac{5000}{\$22500}$ $\$22,500 + \$20,000 = \$42,500$. $9 \quad 1125$ $\frac{22500}{42500} \times \$\frac{19125}{2} = \$\frac{10125}{2} = \5062.50 . $17 \quad 4 \quad 8 \quad 1125$ $\frac{20000}{42500} \times \$\frac{19125}{2} = \$4500$.

Exercise 106. Page 235.

1. There were 125 pupils at school on Monday, 130 on Tuesday, 128 on Wednesday, 132 on Thursday, and 125 on Friday. What was the average daily attendance?

2. A spring of water that yields 250 gal. an hour supplies a town containing 360 families. What is the average daily supply of water for each family?

$$\frac{24 \times 250}{360} \text{ gal.} = \frac{50}{3} \text{ gal.} = 16\frac{2}{3} \text{ gal.}$$
Ans.

3. A wine merchant put into an empty cask 15 qt. of brandy costing \$1.10 a quart, 66 qt. costing \$1.20 a quart, and 43 qt. costing \$1.40 a quart. At what price per quart must he sell the brandy to gain one fifth of the cost?

4. A grocer mixed 120 lb. of tea costing 50 cents a pound with 180 lb. costing 40 cents a pound. At what price per pound must be sell the mixture to make a profit of \$30 on the whole?

$$\begin{array}{r}
 120 \times \$0.50 = \$60.00 \\
 180 \times 0.40 = 72.00 \\
 \hline
 300 & \$132.00 \\
 \hline
 & 30. \\
 \hline
 & \$162. \\
 \hline
 300 & \$1.62
 \end{array}$$

5. A grocer buys two kinds of tea at 40 cents a pound and 56 cents a pound, respectively, and mixes them in the ratio of 5 to 3. What is his profit, if he sells 56 lb. of the mixture at 84 cents a pound?

$$5+3=8.$$
 $\frac{5}{8} \times \frac{5}{8}$ lb. = 35 lb.
 $\frac{3}{8} \times \frac{5}{8}$ lb. = 21 lb.
 $35 \times \$0.40 = \14.00
 $21 \times 0.56 = 11.76$
 $56 \times \$0.84 = \47.04 .
 $\$47.04 - \$25.76 = \$21.28$. Ans.

6. The average length of ten sticks is 2 ft. 10½ in.; one stick is 27½ in. long, another 37½ in. long, and the remaining eight are of the same length. What is the length of one of the remaining eight?

2 ft.
$$10\frac{1}{2}$$
 in. = $34\frac{1}{2}$ in.
 $10 \times 34\frac{1}{2}$ in. = 345 in.
 $27\frac{1}{2}$ in. + $37\frac{1}{2}$ in. = 65 in.
 $\frac{345 \text{ in.} - 65 \text{ in.}}{8} = \frac{280 \text{ in.}}{8} = 35 \text{ in.}$
Ans.

7. The average age of the boys in the four classes of a school is 18.4 yr., 17.9 yr., 16.8 yr., and 15.7 yr. The classes contain 29, 33, 34, and 33 boys, respectively. What is the average age of the boys in the school?

18. 4	17.9	16.8	15.7
29	33	34	33
1656	$\overline{537}$	$\overline{672}$	$\overline{471}$
368	537	504	471
533.6	590.7	$\overline{571.2}$	518.1

533.6	29	17.1
590.7	33	129)2213.6
571.2	34	129
518.1	33	923
2213.6	129	903
		206
		129
17.2 yr. A	ns.	77

8. Seven boys weigh respectively 119.7 lb., 105 lb., 178.3 lb., 165.3 lb., 142.8 lb., 109 lb., 154.2 lb. What is their average weight?

119.7 lb.
105.
178.3
165.3
142.8
109.
154.2
7)974.3 lb.
139.2 lb. Ans.

- 9. In what proportion should tea costing 60 cents a pound be mixed with tea costing 45 cents a pound that the cost of the mixture should be 54 cents a pound?
 - 1 lb. of the 60-cent tea loses in value \$0.06, and 1 lb. of the 45-cent tea gains in value \$0.09. Hence, to make a mixture worth \$0.54 a pound, the tea must be mixed in the ratio 9:6; that is, 3:2. Ans.
- 10. A merchant has teas that cost 80 cents, 60 cents, and 40 cents a pound, respectively. How many pounds of each kind shall he take to make a mixture of 1000 lb., so that in selling it at 70 cents a pound he may make a profit of 8 cents a pound?

- The cost of the mixture must be \$0.70 \$0.08 = \$0.62 a pound.
- The 80-cent tea loses in value \$0.18; the 60-cent gains in value \$0.02; and the 40-cent gains in value \$0.22. Hence, the merchant must mix the 80-cent and 60-cent in the ratio 2:18, that is, 1:9, and the 80-cent and the 40-cent in the ratio 22:18, that is, 11:9. Therefore, he takes the 80-cent, the 60-cent, and the 40-cent proportionally to 12:9:9; that is, 4:3:3.
- Hence, he takes $\frac{4}{10}$ of 1000 lb. = 400 lb. of the 80-cent; $\frac{8}{10}$ of 1000 lb. = 300 lb. of the 60-cent; and $\frac{8}{10}$ of 1000 lb. = 300 lb. of the 40-cent. Ans.
- 11. A grocer mixed black tea that cost him 28 cents a pound with green tea that cost him 42 cents, and by selling the mixture at 35 cents a pound he gained $\frac{1}{6}$ of its cost. What was the actual cost of the mixture a pound? In what ratio were the teas mixed?
 - If by selling the tea at 35 cents the merchant gained $\frac{1}{6}$ of its cost, the actual cost of the mixture was $\frac{4}{5}$ of 35 cents; that is, 30 cents. Ans.
 - The 42-cent tea loses in value 12 cents, and the 28-cent gains in value 2 cents. Hence, the merchant mixed the 42-cent and the 28-cent teas in the ratio 2:12; that is, 1:6. Ans.
- 12. A dealer has an order for 1000 bu. of wheat at 70 cents a bushel. In what proportion shall he mix three kinds of wheat at 66, 69, and 72 cents a bushel to fill the order?
 - The 66-cent wheat gains in value 4 cents a bushel and the 72-cent loses in value 2 cents.
 - Hence, the dealer must mix the 66-cent and 72-cent in the ratio 2:4; that is, 1:2.
 - The 69-cent wheat gains in value 1 cent and the 72-cent loses in value 2 cents.
 - Hence, the dealer must mix the 69-cent and the 72-cent in the ratio 2:1.
 - Therefore, the dealer must take the 66-cent, the 69-cent, and the 72-cent proportionally to 1:2:3. Ans.
- 13. A wine merchant mixes wines that cost \$0.95, \$1.05, \$1.10, and \$1.20 a gallon to make a mixture costing \$1.00 per gallon. How many gallons of each kind of wine does he take?

- The 95-cent wine gains in value 5 cents, and the 105-cent loses in value 5 cents.
- Hence, the merchant must take the 95-cent and the 105-cent in the ratio 1:1.
- The 95-cent wine gains in value 5 cents, and the 110-cent loses in value 10 cents.
- Hence, the merchant must take the 95-cent and the 110-cent in the ratio 2:1.
- The 95-cent wine gains in value 5 cents, and the 120-cent loses in value 20 cents.
- Hence, the merchant must take the 95-cent and the 120-cent in the ratio 4:1.
- Therefore, the merchant may take the 95-cent wine, the 105-cent, the 110-cent, and the 120-cent proportionally to 7:1:1:1. Ans.
- 14. A merchant wishes to fill a barrel that will hold 240 lb. of sugar with sugar costing $4\frac{1}{2}$, $4\frac{3}{4}$, and $5\frac{1}{8}$ cents a pound, respectively, so that the mixture may cost $4\frac{7}{8}$ cents a pound. How many pounds of each kind shall he take?
 - The 4½-cent sugar gains in value $\frac{2}{3}$ cent, and the 5½-cent loses in value $\frac{2}{3}$ cent.
 - Hence, the merchant must take the $4\frac{1}{2}$ -cent and the $5\frac{1}{4}$ -cent in the ratio $\frac{3}{4}$: $\frac{3}{4}$; that is, 2:3.
 - The 4\frac{1}{4}-cent sugar gains in value \frac{1}{8} cent, and the 5\frac{1}{8}-cent loses in value \frac{2}{4} cent.
 - Hence, the merchant must take the $4\frac{\pi}{4}$ -cent and the $5\frac{\pi}{4}$ -cent in the ratio $\frac{\pi}{4}:\frac{1}{4}$; that is, 2:1.
 - Therefore, the merchant may take the $4\frac{1}{2}$ -cent, the $4\frac{3}{4}$ -cent, and the $5\frac{1}{8}$ -cent proportionally to 2:2:4; that is, 1:1:2.
 - Hence, the merchant may take $\frac{1}{4}$ of 240 lb. = 60 lb. of the $\frac{41}{2}$ -cent, $\frac{1}{4}$ of 240 lb. = 60 lb. of the $\frac{43}{2}$ -cent, and $\frac{1}{2}$ of 240 lb. = 120 lb. of the $\frac{51}{2}$ -cent. Ans.
- 15. A grocer wishes to mix 12 lb. of coffee at 40 cents a pound and 20 lb. at 35 cents a pound with coffee at 28 cents a pound, so that the mixture may be worth 30 cents a pound. How many pounds at 28 cents must be use?

Hence, the average cost of the 32 lb. is $\$ \frac{11.80}{32} = \$ 0.36$.

The 28-cent gains in value 2 cents, and the 367-cent loses in value 67 cents.

Hence, the grocer must mix the 28-cent and the 367-cent in the ratio 67:2; that is, 55:16, or 110 to 32.

Hence, the grocer must use 110 lb. at 28 cents. Ans.

16. A grocer mixed 14 lb. of coffee costing 32 cents a pound, 18 lb. costing 35 cents a pound, 22 lb. costing 38 cents a pound, and 40 lb. costing 30 cents a pound. What is the cost of the mixture per pound, and at what price must be sell it to gain 0.25 of the cost?

$$14 \times \$ 0.32 = \$ 4.48$$
 $18 \times 0.35 = 6.30$
 $22 \times 0.38 = 8.36$
 $40 \times 0.30 = 12.00$
 8×31.14

Therefore, the cost of the mixture per pound is

$$\$\frac{31.14}{94} = \$0.331277$$
. Ans.

- 17. In what proportion may oils costing \$1.20, \$0.80, and \$0.60 a gallon be mixed that the mixture may cost \$0.70 a gallon?
 - The 120-cent oil loses in value 50 cents a gallon, and the 60-cent gains in value 10 cents.
 - Therefore, the 120-cent and the 60-cent must be mixed in the ratio 10:50; that is, 1:5.
 - The 80-cent oil loses in value 10 cents and the 60-cent gains in value 10 cents.
 - Therefore, the 80-cent and the 60-cent oils must be mixed in the ratio 10:10; that is, 1:1.
 - Hence, the 120-cent, the 80-cent, and the 60-cent oils may be mixed proportionally to 1:1:6. Ans.

Exercise 107. Page 237.

Reduce to a common fraction:

1.
$$20\% = \frac{20}{100} = \frac{1}{5}$$

2.
$$80\% = \frac{80}{100} = \frac{4}{5}$$

3.
$$25\% = \frac{25}{100} = \frac{1}{4}$$

4.
$$50\% = \frac{50}{100} = \frac{1}{2}$$

5.
$$75\% = \frac{75}{100} = \frac{3}{4}$$

6.
$$5\% = \frac{5}{100} = \frac{1}{20}$$

7.
$$10\% = \frac{10}{100} = \frac{1}{10}$$

8.
$$12\frac{1}{2}\% = \frac{12\frac{1}{3}}{100} = \frac{1}{8}$$

9.
$$16\frac{2}{3}\% = \frac{16\frac{2}{3}}{100} = \frac{1}{6}$$
.

10.
$$11\frac{1}{6}\% = \frac{11\frac{1}{6}}{100} = \frac{1}{9}$$

11.
$$62\frac{1}{2}\% = \frac{62\frac{1}{4}}{100} = \frac{5}{8}$$

12.
$$87\frac{1}{2}\% = \frac{87\frac{1}{2}}{100} = \frac{7}{8}$$

13.
$$66\frac{2}{3}\% = \frac{66\frac{2}{3}}{100} = \frac{2}{3}$$

14.
$$37\frac{1}{2}\% = \frac{37\frac{1}{4}}{100} = \frac{3}{8}$$

15.
$$83\frac{1}{8}\% = \frac{83\frac{1}{100}}{100} = \frac{5}{6}$$

16.
$$18\frac{3}{4}\% = \frac{18\frac{3}{4}}{100} = \frac{3}{16}$$

17.
$$95\% = \frac{95}{100} = \frac{19}{20}$$
.

18.
$$70\% = \frac{70}{100} = \frac{7}{10}$$

19.
$$144\frac{4}{9}\% = \frac{144\frac{4}{9}}{100} = \frac{13}{9}$$
.

20.
$$262\frac{1}{2}\% = \frac{262\frac{1}{2}}{100} = \frac{21}{8}$$
.

Exercise 108. Page 238.

Express as a rate per cent:

1.
$$\frac{1}{2} = \frac{1}{2}$$
 of $199\% = 50\%$.

2.
$$\frac{1}{4} = \frac{1}{4}$$
 of $\cancel{199}\% = 25\%$.

3.
$$\frac{3}{8} = \frac{3}{8}$$
 of $\cancel{199}\% = \frac{75}{2}\% = 37\frac{1}{2}\%$.

4.
$$\frac{1}{8} = \frac{1}{3}$$
 of $100\% = \frac{100}{3}\% = 33\frac{1}{3}\%$

5.
$$\frac{1}{6} = \frac{1}{6}$$
 of $199\% = \frac{50}{3}\% = 16\frac{1}{3}\%$.

6.
$$\frac{5}{6} = \frac{5}{6}$$
 of $199\% = \frac{250}{3}\% = 83\frac{1}{3}\%$.

7.
$$\frac{2}{3} = \frac{2}{3}$$
 of $100\% = \frac{200}{3}\% = 66\frac{2}{3}\%$

8.
$$\frac{4}{5} = \frac{4}{5}$$
 of 199% = 80%.

9.
$$\frac{8}{25} = \frac{8}{25}$$
 of $199\% = 32\%$

10.
$$\frac{7}{20} = \frac{7}{20}$$
 of $100 \% \% = 35 \%$.

11.
$$\frac{2}{9} = \frac{2}{9}$$
 of $100\% = \frac{200}{9}\% = 22\frac{2}{9}\%$.

12.
$$\frac{7}{16} = \frac{7}{16}$$
 of $199\% = \frac{175}{4}\% = 43\frac{3}{4}\%$.

13.
$$\frac{4}{11} = \frac{4}{11}$$
 of $100\% = \frac{400}{11}\% = 36\frac{4}{11}\%$.

14.
$$\frac{9}{32} = \frac{9}{32}$$
 of $199\% = \frac{225}{8}\% = 28\frac{1}{8}\%$.

15.
$$0.25 = 25 \%$$
.

16.
$$0.6 = 0.60 = 60 \%$$
.

18.
$$0.9 = 0.90 = 90 \%$$

19.
$$0.65 = 65\%$$
.

20.
$$0.45 = 45 \%$$

21.
$$0.2 = 0.20 = 20 \%$$

22.
$$0.33333 = 0.331 = 331\%$$

23.
$$0.16667 = 0.16\frac{2}{3} = 16\frac{2}{3}\%$$
.

24.
$$0.83333 = 0.831 = 831 \%$$

25.
$$0.875 = 0.87\frac{1}{2} = 87\frac{1}{2}\%$$

26.
$$1.375 = 1.37\frac{1}{2} = 137\frac{1}{2}\%$$

27.
$$2.66667 = 2.66\frac{2}{3} = 266\frac{2}{3}\%$$
.

28.
$$4.2525 = 4.25\frac{1}{4} = 425\frac{1}{4}\%$$

TEACHERS' EDITION.

Exercise 109. Page 240.

Find by using decimals:

1. 23% of 1728.

$$23\% = 0.23.$$

1728

0.23

5184

3456

397.44 Ans.

2. 44% of 1861.

$$44\% = 0.44.$$

1861

0.44

7444

7444

818.84 Ans.

3. 87% of 14.22.

$$87\% = 0.87.$$

14.22

0.87

9954

11376

12.3714 Ans.

4. 63% of 2.832.

$$63\% = 0.63.$$

2.832

0.63

8496

16992

1.78416 Ans.

5. 72 % of 841.

$$72\% = 0.72.$$

841

 $\frac{0.72}{1682}$

5887

605.52 Ans.

6. 2 % of 846.

$$2\% = 0.02.$$

846

0.02

6.92 Ans.

7. 9% of 24.87.

$$9\% = 0.09.$$

24.87

0.09

2.2383 Ans.

8. 122 % of 12.5.

$$122\% = 1.22.$$

12.5

1.22

250

250

 $\frac{125}{15.250}$ Ans.

9. 287 % of 48.2.

$$287\% = 2.87.$$

48.2

2.87

3374

3856

964

138.334 Ans.

 $\frac{0.01}{78.54}$ Ans.

11.
$$0.5\%$$
 of 144 .
 $0.5\% = 0.005$.
 $\frac{144}{0.005}$
 0.720 Ans.

12.
$$8752\%$$
 of 2645 .
$$8752\% = 87.52$$
.
$$2645$$

$$87.52$$

$$5290$$

$$13225$$

$$18515$$

$$21160$$

$$231490.40$$
 Ans.

13.
$$0.02 \%$$
 of 52.36 .
 $0.02 \% = 0.0002$.

$$\begin{array}{r} 52.36 \\ 0.0002 \\ \hline 0.010472 \end{array}$$
 Ans.

14. 2% of 3.

$$2\% = 0.02.$$

$$\frac{3}{0.02}$$

$$0.06$$
Ans.

15. 2.06 % of 312.

$$2.06\% = 0.0206$$
.
 312
 0.0206
 1872
 624
 6.4272 Ans.

Find by using common fractions:

16.
$$33\frac{1}{8}\%$$
 of 363. $33\frac{1}{8}\% = \frac{1}{8}$. $\frac{1}{8}$ of $\frac{121}{8}\% = 121$. Ans.

17. 20 % of 545.
20 % =
$$\frac{1}{5}$$
.
 $\frac{1}{5}$ of 545 = 109. Ans.

18. 25 % of 1728.

$$25\% = \frac{1}{4}$$
.
 $\frac{1}{4}$ of 1728 = 432. Ans.

19. 50% of 8642.

$$50\% = \frac{1}{2}.$$

$$\frac{4321}{2} \text{ of } 8642 = 4321. Ans.}$$

20. 75 % of 432.

$$75\% = \frac{3}{4}$$
.
 $\frac{108}{4}$ of $\frac{132}{4} = 324$. Ans.

21.
$$62\frac{1}{8}\%$$
 of 216. $62\frac{1}{8}\% = \frac{5}{8}$. $\frac{27}{8}$ of $2\cancel{1}\% = 135$. Ans.

22.
$$37\frac{1}{2}\%$$
 of 360 . $37\frac{1}{2}\% = \frac{3}{8}$. $\frac{45}{8}$ of $369 = 135$. Ans.

$$83\frac{1}{8}\% = \frac{8}{8}$$
.
$$\frac{5}{6} \text{ of } 486 = 405. Ans.$$

24.
$$66\frac{2}{3}\%$$
 of 456.

$$66\frac{2}{3}\% = \frac{2}{3}$$
.

$$\frac{2}{3}$$
 of $456 = 304$. Ans.

$$12\frac{1}{4}\% = \frac{1}{8}$$
.

 $\frac{1}{6}$ of 2.56 = 0.32. Ans.

$$144\% = \frac{1}{4}$$
.

 $\frac{1}{7}$ of 81.9 = 11.7. Ans.

27. 22% of 8.19.

$$22\frac{2}{3}\% = \frac{2}{3}$$
.

$$\frac{2}{9}$$
 of 8.19 = 1.82. Ans.

$$168\frac{1}{4}\% = 1\frac{1}{4}\frac{1}{6}$$
.

$$1_{\frac{11}{16}} \text{ of } 256 = \frac{27}{16} \times \frac{16}{256} = 432. \text{ Ans.}$$

29. 143¾ % of 288.

$$143\frac{3}{4}\% = 1\frac{7}{16}$$
.

$$1\frac{7}{16}$$
 of $288 = \frac{23}{16} \times \frac{18}{288} = 414$. Ans.

30. 70 % of 8432.

$$70\% = \frac{7}{10}$$

$$\frac{7}{19} \text{ of } 8432 = \frac{29512}{5} = 5902\frac{2}{5}. \text{ Ans.}$$

31. The population of a town in 1880 was 12,275, and it increased 8% in the next ten years. Find the population of the town in 1890.

12275	12275	
0.08	982	
982.00	13257	Ans.

32. How much metal will be obtained from 365 tons of ore, if the ore contains 7% of metal?

25.55 t. Ans.

33. If gunpowder contains 75% of saltpetre, 10% of sulphur, 15% of charcoal, how many pounds of each are there in a ton of powder?

1
$$t_{\rm h} = 2000 \, \text{lb}$$
.

Saltpetre, 1500 lb.; sulphur, 200 lb.; charcoal, 300 lb. Ans.

34. Air is composed by volume of 20.0265% of oxygen and 79.9735% of nitrogen. How many cubic feet of oxygen in 1750 cu. ft. of air?

0.200265

 $\frac{1750}{10013250}$

1401855

200265

350.463750

350.46375 cu. ft. Ans.

35. If 2% of a regiment of 750 men are killed in an engagement, 6% are wounded, and 4% are missing, what is the number still available for service?

$$2\% + 6\% + 4\% = 12\%$$
 $100\% - 12\% = 88\%$

$$\begin{array}{r} 750 \\ \underline{0.88} \\ 6000 \\ \underline{6000} \end{array}$$

$$\begin{array}{r} 6000 \\ \underline{Ans} \end{array}$$

36. A man sold a bicycle that cost him \$60, and lost 16\frac{2}{8}\% of the cost. For what price did he sell it?

$$16\frac{2}{3}\% = \frac{1}{6}$$
. $\frac{1}{6}$ of $$60 = 10 . $$60 - $10 = 50 . Ans.

37. A merchant sold hats that cost him \$1.50 each, and gained 33\frac{1}{3}\%. For what price did he sell them?

$$33\frac{1}{3}\% = \frac{1}{3}$$
. $\frac{1}{3}$ of \$1.50 = \$0.50.
\$1.50 + \$0.50 = \$2.00. Ans.

38. In a school of 80 children, 17½% are girls. Find the number of boys.

$$\begin{array}{ccc}
0.175 & 80 \\
\underline{80} & \underline{14} \\
14.000 & 66 & Ans.
\end{array}$$

39. The lead ore from a certain mine yields 60% of metal, and of the metal ‡ of 1% is silver. How much silver and how much lead will be obtained from 1200 t. of ore?

Silver, 5.4 t.; lead, 714.6 t. Ans.

40. If 13% of a population of 27,000,000 are foreign born, how many of the population are foreign born?

$$\begin{array}{r}
 27000000 \\
 0.13 \\
 \hline
 81000000 \\
 \hline
 27 \\
 \hline
 3510000. Ans.
 \end{array}$$

41. If iron expands $\frac{1}{6}$ of 1% when heated 185° F., what will be the expansion of iron when heated from -20° F. to $+120^{\circ}$ F.?

The difference in temperature between -20° F. and $+120^{\circ}$ F. is 140° F.

$$\begin{array}{c} 7 \\ 28 \\ 149 \\ 185 \\ 37 \end{array} \text{ of } 1\% = \frac{7}{74} \text{ of } 1\%. \text{ Ans.}$$

42. A tubular iron bridge 740 ft. long has one end fast to a pier. How much play must be allowed at the other end for the expansion of the iron, if the climate varies from -30° F. in winter to $+130^{\circ}$ F. in a July sun?

The difference in temperature between -30° F. and $+130^{\circ}$ F. is 160° F.

The expansion for 160° is

$$\frac{\frac{4}{189}}{\frac{189}{37}} \text{ of } \frac{1}{8} \text{ of } 1\% = \frac{4}{37} \text{ of } 1\%. \qquad \frac{4}{37} \text{ of } 1\% = \frac{4}{3700}.$$

$$\frac{4}{3799} \text{ of } 749 \text{ ft.} = \frac{4}{5} \text{ ft.} = 9\frac{1}{5} \text{ in. } Ans.$$

43. How much longer is 100 miles of iron rails at 118° F. than at 20° below zero?

$$100 \text{ mi.} = 528,000 \text{ ft.}$$

The difference in temperature between 118° F. and -20° F. is 138° F. The expansion for 138° is

$$\frac{69}{185} \text{ of } \frac{1}{8} \text{ of } 1\% = \frac{69}{740} \text{ of } 1\%. \qquad \frac{69}{740} \text{ of } 1\% = \frac{69}{74000}.$$

$$\frac{69}{74999} \text{ of } 528999 \text{ ft.} = \frac{18216}{37} \text{ ft.} = 492\frac{17}{37} \text{ ft. } Ans.$$

Exercise 110. Page 242.

1. What per cent of 64 is 16?

$$\frac{16}{64} = \frac{1}{4} = 25 \%$$
. Ans.

2. What per cent of 16 is 64?

$$\frac{64}{16} = 4 = 400 \%$$
. Ans.

3. What per cent of 450 lb. is 50 lb.?

$$\frac{50 \text{ lb.}}{450 \text{ lb.}} = \frac{1}{9} = 11\frac{1}{9}\%. \quad Ans.$$

4. What per cent of 50 lb. is 450 lb.?

$$\frac{450 \text{ lb.}}{50 \text{ lb.}} = 9 = 900 \%$$
. Ans.

5. What per cent of \$465 is \$130.20?

6. What per cent of \$832 is \$807.04?

7. What per cent of \$987 is \$2289.84?

8. A brick kiln contained 29,800 bricks, but after burning only 29,734 were found in good condition. What per cent had been spoiled in burning?

9. If a house worth \$4000 rents for \$360 a year, what per cent of its value is the rent?

$$\frac{$360}{$4000} = \frac{9}{100} = 9\%$$
 Ans.

10. If 75 bu. of corn are raised from 1 pk. of corn, what per cent is the increase?

75 bu. = 300 pk.
$$300 \div 1 = 300 = 30,000 \%. Ans.$$

11. Ten years ago the population of a city was 26,275; its present population is 31,530. What is the increase per cent?

12. If 3\{\frac{1}{4}\) tons of sulphur are required to make 31\{\frac{1}{4}\) tons of gun- powder, what per cent of gunpowder is sulphur?

$$\frac{3\frac{3}{4}}{31\frac{1}{4}} \text{ of } 100\% = \frac{\cancel{15}}{\cancel{4}} \times \frac{\cancel{4}}{\cancel{125}} \times \cancel{100}\% = 12\%. \text{ Ans.}$$

13. If a long ton of ore in a gold mine yields 5 oz. (troy) of gold, what is the yield per cent?

5 oz. troy =
$$\frac{5}{12}$$
 lb. troy = $\frac{3}{12}$ of $\frac{3769}{7999}$ lb. av. = $\frac{12}{35}$ lb. av. $\frac{12}{35}$ lb. av. $\frac{173}{35}$

 $1 \log ton = 2240 lb. av.$

$$\frac{\frac{13}{2240} \text{ of } 100\% = \frac{\cancel{3}}{\cancel{3}\cancel{5}} \times \frac{\cancel{1}}{\cancel{2240}} \times \cancel{100\%} = \frac{3}{196}\%. \text{ Ans.}$$

14. If 12½ tons of iron are obtained from 235 tons of ore, what per cent of the ore is iron?

$$\frac{12\frac{1}{2}}{235} \text{ of } 100\% = \frac{25}{2} \times \frac{1}{235} \times \frac{50}{47} \% = \frac{250}{47}\% = 5\frac{15}{17}\%. \text{ Ans.}$$

15. Find the gain per cent in population in New York from 1880 to 1890, if the population in 1880 was 1,206,594, and in 1890 was 1,513,501.

	0.2543
1513501 1206594	1206594)306907. 2413188
306907	6558820 6032970
	5258500 4826376
	4321240 3619782
25.44 %. Ans.	701458

16. Find the gain per cent in population in Chicago from 1880 to 1890, if the population in 1880 was 503,304, and in 1890 was 1,099,850.

	1.1852
1099850	503304)596546.
503304	503 304
596546	932420
	<u>503304</u>
	4291160
	4026432
	2647280
	2516520
	1307600
	1006608
118.53 %. Ans.	300992

17. Find the gain per cent in population in Philadelphia from 1880 to 1890, if the population in 1880 was 846,981, and in 1890 was 1,046,964.

	0.2361
1046964	846981)199983.
846981	1693962
199983	3058680
	2540943
	5177370
	5081886
	954840
	<u>846981</u>
23.61 %. Ans.	107859

18. Find the gain per cent in population in Brooklyn from 1880 to 1890, if the population in 1880 was 566,689, and in 1890 was 806,343.

806343	0.4229
566689	566689)239654.
239654	226 6756
	1297840
	1133378
	1644620
	1133378
	5112420
	5100201
42.29 %. Ans.	12219

19. Find the gain per cent in population in Boston from 1880 to 1890, if the population in 1880 was 362,535, and in 1890 was 448,477.

448477	0.2370
362535	362535)85942.
85942	725070
	1343500
	1087605
	2558950
	2537745
23.71 %. Ans.	212050

20. If 2 gal. of water are added to 25 gal. of alcohol, what per cent of the mixture is water? What per cent is alcohol?

$$2 \text{ gal.} + 25 \text{ gal.} = 27 \text{ gal.}$$

$$\frac{2}{27} \text{ of } 100 \% = \frac{200}{27} \% = 7\frac{1}{27} \%. \text{ Ans.}$$

$$\frac{25}{27} \text{ of } 100 \% = \frac{2500}{27} \% = 92\frac{15}{27} \%. \text{ Ans.}$$

21. If 5% of the present population of a town has been the increase in the preceding ten years, what per cent of the population ten years ago has been added?

The population ten years ago was 95% of the present population.

$$\frac{3}{93}$$
 of $100\% = \frac{100}{19}\% = 55\%$. Ans.

22. A man gained in weight in January 3%, and in February lost 3%. What per cent of his weight the first day of January is his weight the first day of March?

Feb. 1 the man weighed 103% of his weight Jan. 1.

Mar. 1 the man weighed 97% of his weight Feb. 1.

Therefore, Mar. 1 the man weighed 97% of 103% of his weight Jan. 1.

23. If 7 lb. of a certain article loses 3 oz. in weight by drying, what per cent of its original weight is water?

7 lb. = 112 oz.
$$\frac{3}{112}$$
 of $199\% = \frac{75}{28}\% = 2\frac{19}{28}\%$. Ans.

24. If 7 lb. of a dry article has lost 3 oz. by drying, what per cent of its original weight was water?

The original weight was 7 lb. + 3 oz. = 115 oz.

$$\frac{3}{115}$$
 of $199\% = \frac{60}{23}\% = 2\frac{11}{3}\%$. Ans.

25. If a dry article exposed to damp air absorbed 3 oz. of water, and then weighed 7 lb., what per cent of its present weight is water?

7 lb. = 112 oz.
$$\frac{3}{112}$$
 of $199\% = \frac{75}{28}\% = 2\frac{19}{28}\%$. Ans.

26. If rosin is melted with 20% of its weight of tallow, what per cent of tallow does the mixture contain?

$$100\% + 20\% = 120\%$$
. $\frac{20}{120} = \frac{1}{6} = 16\frac{2}{3}\%$. Ans.

27. If 20% of a mixture of tallow and rosin is tallow, what per cent of the weight of the rosin is the weight of the tallow?

20% of the mixture is tallow and 80% of the mixture is rosin.

$$\frac{20}{10} = \frac{1}{4} = 25 \%$$
. Ans.

28. Nitrogen gas, under standard pressure and temperature, is \(\frac{1}{3} \) of the weight of an equal volume of water. What is the specific gravity of nitrogen? How many gallons of nitrogen will it take to weigh as much as a pint of water?

$$\frac{1}{8}$$
 of $1\% = \frac{1}{800}$.

The specific gravity of nitrogen is $\frac{1}{800} = 0.00125$. Ans.

To weigh as much as 1 pt. of water will be required 800 pt. of nitrogen, or 100 gal. Ans.

29. Oxygen gas is $\frac{1}{7}$ of 1% of the weight of an equal volume of water. What is its specific gravity? How many gallons of oxygen will it take to weigh as much as a pint of water?

$$\frac{1}{7}$$
 of $1\% = \frac{1}{700}$.

The specific gravity of oxygen is $\frac{1}{700} = 0.00143$. Ans.

To weigh as much as 1 pt. of water will be required 700 pt. of oxygen, or 87½ gal. Ans.

30. If common air consists of 4 volumes of oxygen to 13 of nitrogen, what is its specific gravity?

Oxygen,
$$4 \times \frac{1}{700} = \frac{1}{175}$$
.
Nitrogen, $13 \times \frac{1}{800} = \frac{18}{800}$.
 $4 + 13 = 17$.

$$\frac{175 + \frac{18}{800}}{17} = \frac{1}{17} \text{ of } \frac{123}{5600} = \frac{123}{95200}.$$

$$0.001292 \text{ Ans.}$$

$$95299)1.23$$

$$\frac{952}{2780}$$

$$\frac{1904}{8760}$$

16

31. How many gallons of air will it take to weigh as much as a pint of water?

To weigh as much as 1 pt. of water will be required

$$\frac{95200}{123}$$
 pt. of air. $\frac{95200}{123}$ pt. = $773\frac{121}{123}$ pt. = $96\frac{92}{123}$ gal. Ans.

Exercise 111. Page 244.

1. 15 is \ of what number? 15 is 75 per cent of what number?

$$15 \div \frac{3}{4} = \frac{4}{3}$$
 of $15 = 20$. Ans. $15 \div \frac{75}{100} = 20$. Ans.

2. \$500 is 4% of what sum of money?

$$\$500 \div \frac{4}{100} = 25 \times \$500 = \$12,500$$
. Ans.

3. Find the number of which 324 is 27 %.

$$324 \div \frac{27}{100} = \frac{100}{27} \times 324 = 1200$$
. Ans.

4. 288 is 20% more than what number?

$$288 \div \frac{120}{100} = \frac{100}{120} \text{ of } 288 = 240. Ans.}$$

5. 145 is 25 % more than what number?

$$145 \div \frac{125}{100} = \frac{\overset{4}{100}}{\overset{123}{3}} \times \overset{29}{143} = 116. \text{ Ans.}$$

6. 1240 is 55% less than what number?

$$1240 \div \frac{45}{100} = \frac{\cancel{100}}{\cancel{45}} \times 1240 = \frac{24800}{9} = 2755\frac{3}{5}. \text{ Ans.}$$

7. 260 is 331 % less than what number?

$$260 \div \frac{66\frac{2}{3}}{100} = \frac{3}{2} \times \frac{130}{260} = 390. \quad Ans.$$

8. 91 is 40 % more than what number?

$$91 \div \frac{140}{100} = \frac{100}{140} \times \frac{13}{91} = 65$$
. Ans.

9. 901 is 6½ % more than what number?

$$901 \div \frac{1061}{100} = \frac{\cancel{400}}{\cancel{423}} \times \cancel{901} = 848. \quad Ans.$$

10. If $8\frac{\pi}{4}$ % of a number is 4140.15, what is the number?

$$4140.15 \div \frac{8\frac{3}{4}}{100} = \frac{400}{35} \times 4149.15 = 47,316$$
. Ans.

11. If 3% of a number is $2\frac{5}{8}$, what is the number?

$$2\frac{5}{8} + \frac{3}{100} = \frac{\cancel{199}}{\cancel{3}} \times \frac{\cancel{21}}{\cancel{3}} = \frac{175}{2} = 87\frac{1}{2}$$
. Ans.

12. If 140% of a number is 630, what is the number?

$$630 \div \frac{140}{100} = \frac{\cancel{100}}{\cancel{140}} \times \cancel{030} = 450. \quad Ans.$$

13. If 61% of a number is 33.25, what is the number?

$$33.25 \div \frac{6\frac{1}{4}}{100} = \frac{400}{25} \times 33.25 = 532$$
. Ans.

14. A town, after decreasing 11%, has 4539 inhabitants. Find its number at first.

$$4539 \div \frac{89}{100} = \frac{100}{89}$$
 of $4539 = 5100$. Ans.

15. In a certain school there are 200 girls, and the number of girls is 40% of the whole number of pupils. How many pupils in the school?

$$200 \div \frac{40}{100} = \frac{100}{40} \times 200 = 500$$
. Ans.

16. A manufactory uses 24 tons of coal a day, 20% of which is lost in smoke. How much coal would be needed if this waste could be prevented?

$$100\% - 20\% = 80\% = \frac{4}{5}$$
.
 $\frac{4}{5}$ of 24 t. = $\frac{9.6}{5}$ t. = $19\frac{1}{5}$ t. Ans.

17. A town, after decreasing 25%, has 4539 inhabitants. Find its number at first.

$$4539 \div \frac{75}{100} = \frac{\overset{4}{\cancel{100}}}{\overset{\cancel{100}}{\cancel{100}}} \times \overset{1513}{\cancel{1500}} = 6052. \quad Ans.$$

18. If the ore from a mine yields $\frac{3}{80}$ of 1% of pure gold, how many long tons of ore must be taken to obtain 7 lb. (troy) of gold?

19. Goods were sold, at a loss of 3%, for \$2667.50. What was the cost?

\$2667.50 +
$$\frac{97}{100} = \frac{100}{97} \times $2667.59 = $2750$$
. Ans.

20. A tradesman, in selling goods, deducts from the marked price 5% for cash. What was the marked price of goods for which he received \$14.25?

$$\$ 14.25 + \frac{95}{100} = \frac{100}{93} \times \$ \cancel{14.23} = \$ 15.$$
 Ans.

21. If an ore loses 41½% of its weight in roasting, and 43½% of the remainder in smelting, how much ore will be required to yield 1000 tons of metal?

The part remaining after roasting is $100\% - 41\frac{1}{2}\% = 58\frac{1}{2}\%$. The part remaining after smelting is

$$58\frac{1}{2}\% - 43\frac{1}{2}\% \text{ of } 58\frac{1}{2}\% = 58\frac{1}{2}\% - 25\frac{1}{2}\frac{1}{2}\% = 32\frac{1}{2}\frac{1}{2}\%.$$

$$1000 \div \frac{32\frac{1}{2}\frac{1}{2}}{100} = 1000 \times \frac{32}{1053} \times 100 = \frac{3200000}{1053} = 3038\frac{986}{1053} = 3038.936.$$

$$3038.936 \text{ t. } Ans.$$

22. How many pounds of tallow must be mixed with 8½ pounds of rosin that the mixture may contain 15% of tallow?

The mixture contains 15% of tallow and 85% of rosin.

$$8\frac{1}{4} \div \frac{85}{15} = \frac{\frac{3}{15}}{\frac{55}{5}} \times \frac{17}{2} = \frac{3}{2} = 1\frac{1}{4}$$
. Ans.

Exercise 112. Page 246.

1. Find the net amount of a bill of \$1550, if a discount of 5% is made for cash.

2. Find the net amount of a bill of \$88, if the discounts are 20 and 10.

3. Find the net cash amount of a bill of \$800, if the discounts are 75, 5, and $2\frac{1}{2}$.

4. Find the net cash amount of a bill of \$272, if the discounts are \(\frac{1}{4}\), 10, and 5.

5. Find the net cash amount of a bill of \$1440, if the discounts are 55, 10, and 5.

6. Find the net cash amount of a bill of \$1125, if the discounts are \(\frac{1}{4}\), 10, 10, 10, and 5.

7. Find the net amount of a bill of \$872.29, if the discounts are \(\frac{1}{2}\), 20, and 25.

8. Find the difference between a single discount of 50% and two successive discounts of 25% and 25% off a bill of \$1272.36.

9. An agent bought 25 sewing machines with 15, 10, and 5 off the list price of \$40 each, and sold them at a discount of 10% off the list price. What was the net amount he received for the sewing machines and his profit?

10. An agent bought a bicycle with 25 and 5 off the list price of \$100. If he received an additional discount of 2½% for cash, and sold the bicycle at a discount of 12½% off the list price, what was the selling price and his profit?

11. A collector collects 65% of a debt of \$727, and charges 5% of the amount he collected. What was the net amount for the creditor?

Exercise 113. Page 248.

1. If goods are bought for \$415, and sold for \$500, what is the gain per cent?

Gain = \$500 - \$415 = \$85.

$$\frac{85}{415}$$
 of $100\% = \frac{1700}{83}\% = 20\frac{19}{15}\%$. Ans.

2. If goods are bought for \$415, and sold for \$400, what is the loss per cent?

Loss = \$415 - \$400 = \$15.

$$\frac{3}{415}$$
 of 100% = $\frac{300}{83}$ % = $3\frac{51}{83}$ %. Ans.

3. A farmer buys 24 head of cattle at \$80 a head. After losing 6 head, he sells the remainder at \$105 a head. What does he gain or lose per cent?

$$24 \times $80 = $1920.$$

$$18 \times \$105 = \$1890.$$

$$Loss = $1920 - $1890 = $30.$$

$$\frac{39}{1929} \text{ of } 199\% = \frac{25}{16}\% = 1\frac{9}{16}\%.$$

Therefore, he loses $1\frac{9}{16}$ %. Ans.

4. Teas at 68 cents, 86 cents, and 96 cents a pound are mixed in equal quantities, and sold at 90 cents a pound. Find the gain per cent.

Cost per pound =
$$\frac{1}{8}(68 + 86 + 96)$$
 cents = $83\frac{1}{8}$ cents.

$$Gain = 90 cents - 83\frac{1}{3} cents = 6\frac{2}{3} cents$$
.

$$\frac{61}{831} \text{ of } 100\% = \frac{\cancel{20}}{\cancel{3}} \times \frac{\cancel{3}}{\cancel{250}} \times \cancel{100}\% = 8\%. \text{ Ans.}$$

5. By selling goods for \$1173.92 a merchant gains \$153.12. Find the gain per cent.

$$Cost = $1173.92 - $153.12 = $1020.80.$$

$$\begin{array}{r}
 0.15 \\
 102080)15312. \\
 \underline{102080} \\
 \hline
 510400 \\
 510400
\end{array}$$

15%. Ans.

6. What was the cost, when 17½% was gained by selling goods for \$253.80?

\$253.80 ÷
$$\frac{117\frac{1}{2}}{100}$$
 = 100 × $\frac{2}{235}$ × \$253.80 = \$216. Ans.

7. A wine merchant mixes 24 gal. of wine, at \$7 a gallon, with 18 gal. at \$5 a gallon, and sells the whole at \$7 a gallon. What does he gain per cent?

Cost =
$$24 \times \$7 + 18 \times \$5 = \$168 + \$90 = \$258$$
.
Selling price = $(24 + 18) \times \$7 = 42 \times \$7 = \$294$.
Gain = $\$294 - \$258 = \$36$.
 $\frac{36}{258}$ of $100\% = \frac{600}{43}\% = 13\frac{11}{43}\%$. Ans.

8. By selling a horse for \$200, a dealer loses 12½%. What would he have gained or lost per cent if he had sold the horse for \$250?

Cost = \$200 ÷
$$\frac{87\frac{1}{2}}{100}$$
 = $\frac{8}{7}$ of \$200 = \$ $\frac{1600}{7}$ = \$228\frac{1}{2}.

If he had sold the horse for \$250, the gain would have been

\$250 - \$228\frac{1}{2} = \$21\frac{1}{3}.\$
$$\frac{21\frac{1}{7}}{228\frac{1}{7}} \text{ of } 100\% = \frac{150}{1600} \text{ of } 100\% = \frac{75}{8}\% = 9\frac{1}{8}\%.$$
Gain, $9\frac{1}{8}\%$. Ans.

9. A spirit merchant buys 75 gal. of spirits at \$3.25 a gallon, and, after drawing off 10 gal., sells the remainder so as to gain 5% on the cost of the whole. What is the selling price per gallon?

A 0 0 F	\$3.9375 Ans.		
\$ 3.25 75	65)\$ 255.9375		
	195		
1625 2275 \$ 243.75, cost. 1.05 121875 24375 \$ 255.9375 75 gal 10 gal. = 65 gal.	609		
	58 5		
	243		
	195		
	487		
	455		
	325		
	325		

10. A man owns two city lots worth respectively \$9845 and \$12,155. If the first gains in value 32%, and the second loses 13%, what is the gain or loss per cent in the value of the two lots?

TEACHERS' EDITION.

\$ 9845

$$\frac{1.32}{19690}$$
 $\frac{0.87}{85085}$
 $\frac{29535}{9845}$
 $\frac{9845}{12995.40}$
 $\frac{1}{8}$
 $\frac{12995.40}{10574.85}$
 $\frac{12155}{12155}$
 $\frac{12155}{122000}$
\$ 23570.25
$$\frac{12155}{123570.25}$$
 $\frac{12155}{123570.25}$

$$\begin{array}{r}
0.0713 \\
22999)1.57025 \\
\underline{154} \\
30 \\
\underline{22}
\end{array}$$

82 66

16

7.14 % gain. Ans.

11. A tradesman marks a hat \$5, but takes off 5%. If his profit is 14%, what was the cost of the hat?

Selling price = \$5 - 5% of \$5 = \$5 - \$0.25 = \$4.75.

$$\$4.75 \div \frac{114}{100} = \frac{\cancel{100}}{\cancel{114}} \times \$\frac{\cancel{19}}{\cancel{4}} = \$\frac{25}{6} = \$4.16\frac{2}{3}.$$
 Ans.

12. What would a dishonest dealer gain per cent by using a false weight of 15 oz. instead of a pound?

Gain = 16 oz. - 15 oz. = 1 oz.
$$\frac{1}{15}$$
 of $199\% = \frac{20}{3}\% = 6\frac{2}{3}\%$. Ans.

13. A dishonest dealer gains 12% by using false weights. What is the real weight of his pound?

His pound weighs 16 oz.
$$\div \frac{112}{100} = \frac{100}{112}$$
 of 16 oz. $= \frac{100}{7}$ oz. $= 143$ oz. Ans.

14. What per cent above cost must a merchant mark his goods that he may take off 20 % from the marked price, and still make 20 % on the cost?

Since the merchant is to make 20% on the cost of the goods, the selling price is 120% of the cost price.

Since the selling price is to be 20% below the marked price, the selling price is 80% of the marked price.

Therefore, the marked price will be 100 of 120% of the cost price, or 150% of the cost price; that is, the goods must be marked 50% above cost.

15. What per cent above cost must a merchant mark his goods to take off 10%, and still gain 17%?

Selling price = 117% of cost price.

Selling price = 90 % of marked price.

Therefore, marked price =
$$\frac{10}{99}$$
 of 117% = 130% of cost price.

30% above cost. Ans.

16. What per cent above cost must a merchant mark his goods to take off $12\frac{1}{2}$ %, and still gain $12\frac{1}{4}$ %?

Selling price = $112\frac{1}{2}\%$ of cost price.

Selling price = $87\frac{1}{2}$ % of marked price.

Therefore, marked price =
$$\frac{100}{874}$$
 of $1124\% = \frac{900}{7} = 1284\%$ of cost price.

284% above cost. Ans.

17. What per cent above cost must a merchant mark his goods to take off 15%, and still gain 15%?

Selling price = 115% of cost price.

Selling price = 85 % of marked price.

Therefore, marked price

$$= \frac{100}{85} \text{ of } 115\% = \frac{2300}{17}\% = 135\frac{5}{17} \text{ of cost price.}$$

$$35\frac{5}{17}\% \text{ above cost. } Ans.$$

18. What per cent above cost must a merchant mark his goods to e off 33½%, and still gain 33½%?

Selling price = $133\frac{1}{4}\%$ of cost price.

Selling price = $66\frac{2}{3}$ % of marked price.

Therefore, marked price

$$=\frac{100}{667}$$
 of 1337% = 200% of cost price. 100% above cost. Ans.

19. A man bought a horse for \$70, and sold him for \$80. What per cent did he gain? What per cent of the selling price of the horse did he gain?

Gain = \$80 - \$70 = \$10.

$$\frac{19}{79}$$
 of $100\% = \frac{100}{7}\% = 147\%$. Ans.
 $\frac{19}{7}$ of $199\% = \frac{25}{2}\% = 121\%$. Ans.

20. If a merchant clears \$800 by selling goods for 12½% profit, what was the cost of the goods, and for how much were they sold?

\$
$$800 \div \frac{12\frac{1}{100}}{100} = 8 \times $800 = $6400$$
, cost. Ans.
\$ $6400 + $800 = 7200 , selling price. Ans.

21. A man selling eggs at \$0.40 a dozen gains 33\frac{1}{3}\%; what was the cost? Another, selling at the same price, gains 33\frac{1}{3}\% of his receipts; what did his eggs cost?

$$\$0.40 + \frac{133\frac{1}{3}}{100} = \frac{3}{4} \text{ of } \$0.40 = \$0.30. Ans.$$

$$33\frac{1}{2}\%$$
 of $$0.40 = $0.13\frac{1}{2}$, gain.

$$\$0.40 - \$0.13\frac{1}{3} = \$0.26\frac{2}{3}$$
. Ans.

22. A man lost 10% by selling a carriage for \$117. At what price should he have sold it to make 10%?

Cost = \$117 ÷
$$\frac{90}{100} = \frac{\cancel{100}}{\cancel{90}} \times \cancel{$117} = \cancel{$130}.$$

\$130 + 10% of \$130 = \$130 + \$13 = \$143. Ans.

23. If a real estate dealer gained \$600 by selling a farm for 20% profit, what was the cost of the farm, and for how much did he sell it? $$600 \div {}_{100}^{20} = 5 \times $600 = 3000 . Ans. \$3000 + \$600 = \$3600. Ans.

Exercise 114. Page 250.

1. Find the commission on \$2595, at 21%.

\$64.88. Ans.

2. An agent sells 200 bbl. of flour at \$6.25, and 600 gal. of molasses at 65 cents, and charges a commission of 1½%. What are the net proceeds?

3. A commission merchant received \$1640 to buy corn, and charged a commission of 2½%. What is his commission, and how many bushels of corn at 62½ cents a bushel can he buy?

\$
$$1640 \div \frac{102\frac{1}{4}}{100} = \frac{200}{293} \text{ of } $ 1949$$

= \$ 1600.

Commission

$$=$$
 \$ 1640 $-$ \$ 1600 $=$ \$ 40. Ans.

\$
$$1600 \div $ 0.62 \frac{1}{2} = \frac{8}{5} \text{ of } 1500$$

bu. Ans. = 2560.

4. An agent sells a consignment of cotton for \$5216. He pays \$51 for storage, and charges a commission of 21%. What are the net proceeds?

5. An agent sold butter for \$1570, and remitted \$1546.45.

What was the rate per cent of

\$ 5047.64 Ans.

Commission

commission?

$$= $1570 - $1546.45 = $23.55.$$

6. What are the net proceeds from the sale of 2250 bbl. of flour at \$6.25 a barrel, if the charge for freight is 50 cents a barrel, the commission for selling 2%, and the commission for guaranteeing payment 1½%?

7. An agent sells 350 crates of peaches at \$2.60. If the commission is 4½%, find the net proceeds.

8. An agent sells 420 acres of land at \$40 an acre, and charges 1½% commission. What is his commission?

9. An agent, charging 4½% commission, receives for his services \$313. Find the amount of his sales.

 $$313 \div 0.045 = 6955.56 . Ans.

$$\begin{array}{r}
 6955.55 \\
 45)313000. \\
 \underline{270} \\
 430 \\
 \underline{405} \\
 \underline{250} \\
 \underline{225} \\
 \underline{250} \\
 \underline{255} \\
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 \underline{255} \\
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 \underline{250$$

10. A merchant buys 730 yd. of carpeting at \$1.25 a yard, and pays his agent \(\frac{2}{4}\) of 1% commission. If the freight amounts to \(\frac{2}{2}3.58\), at what price per yard must he sell the carpeting to gain 20%?

365

11. An agent sells a consignment of goods for \$2100. He pays \$33.50 for freight, and remits \$2024.50. Find his rate of commission.

12. An agent sells 5000 lb. of cotton at 14 cents a pound, charging 2% commission. With the net proceeds he buys cotton cloth at 10 cents a yard, charging 1½% commission. How many yards of cloth does he buy?

$$\begin{array}{ccc} \$ \ 0.14 & \$ \ 700 \\ \hline \$ \ 700. & 14 \\ \hline \$ \ 700. & \$ \ 686, \ \text{net proceeds.} \\ \hline 0.02 \\ \hline \$ \ 14. & \end{array}$$

Amount paid for cloth

$$= \$686 \div \frac{101\frac{1}{2}}{100} = \frac{200}{293} \times \$686$$

$$= \$\frac{19600}{29}$$

$$= \$675.86.$$

$$\$675.86 \div \$0.10 = 6758.6.$$
 Ans.

13. An agent sold 500 bbl. of flour at \$5.50 a barrel, and charged 2½% commission; the expenses for freight, etc., were \$250. With the net proceeds he bought sugar at 4½ cents a pound, charging 2½% commission. How much sugar did he buy, and what was his total commission?

Amount paid for sugar = \$2431.25 + 1.025 = \$2371.95.

$$\begin{array}{r} 2371.95 \\ 1025)2431250. \\ \underline{2050} \\ 3812 \\ \underline{3075} \\ 7375 \\ \underline{7175} \\ \underline{2000} \\ \underline{1025} \\ \underline{9750} \\ \underline{9225} \\ \underline{5250} \\ \underline{5125} \\ \underline{125} \\ \end{array}$$

Commission for buying =\$2431.25-\$2371.95=\$59.30Commission for selling = \$68.75Total commission = \$128.05Ans.

14. A collector's commission for collecting taxes, at 1½%, is \$206.55. What sum did he collect?

$$\$206.55 \div \frac{1\frac{1}{2}}{100} = \frac{200}{3} \times \$296.55$$

$$= \$13,770. Ans.$$

15. An agent received \$2961 to purchase goods, and charged 5% commission. What was his commission?

$$\begin{array}{l} \$2961 \div \frac{105}{100} = \frac{\cancel{100}}{\cancel{100}} \times \$\cancel{2901} \\ = \$2820. \end{array}$$

\$2961 - \$2820 = \$141, commission. Ans.

16. An agent buys 3100 bbl. of flour at \$4.50 a barrel, and charges 1½% commission. What is his commission?

17. A broker receives \$6150 to invest in cotton, at 7\frac{1}{3} cents a pound. If his commission is 2\frac{1}{2}\%, how many pounds of cotton can he buy?

Amount expended for cotton
$$= \$6150 \div 1.025 = \$6000.$$

$$\$6000 \div \$0.07 = 6000 \times \frac{800}{59}$$

$$= \frac{4800000}{59} = 81355.9.$$

$$81,355.9 \text{ lb. } Ans.$$

18. An agent sells 1100 bbl. of flour at \$4.50 a barrel, and charges 2½% commission. He invests the proceeds in steel at 1½ cents a pound, charging 1½% commission. What is his entire commission, and how many long tons of steel does he buy?

Amount expended for steel = $$4826.25 \div 1.015 = 4754.93 .

1 long ton costs $2240 \times \$0.01\frac{1}{4} = \33.60 .

141.5 Commission for selling = \$4826.25 - \$4754.93 = \$71.32. $\frac{336}{1394}$ $\frac{1344}{509}$ $\frac{71.32}{105.07}$

141.5 t. Ans. $\frac{1680}{53}$

Exercise 115. Page 252.

1. Find the premium of the fire insurance on a house for \$2650 at \(\frac{1}{4}\) of 1%.

336

1733

2. Find the premium for insuring a man's life for \$2500, at an age for which the rate is 21%.

3. At 6\\ %, what premium will be paid on a vessel worth \ 36,400, insured for \ its value?

4. A vessel worth \$16,000 is insured for \(\frac{1}{4}\) its value at 7\(\frac{1}{4}\). What is the premium?

\$195.07, commission.

Ans.

5. The premium of insurance at 1½% is \$150. What is the amount insured?

$$\$150 \div \frac{1\frac{1}{4}}{100} = \frac{400}{5} \times \$159 = \$12,000.$$
Ans.

6. A vessel valued at \$128,000 is insured for \$\frac{1}{2}\$ its value at \$3\frac{7}{2}%\$. What is the net loss to the owners, if the vessel is destroyed during the third year after it is insured?

Gross loss = \$128,000 +
$$3 \times $3720$$

= \$ 128,000 + \$ 11,160
= \$ 139,160.
Net loss = \$139,160 - \$96,000
= \$43,160. Ans.

7. A building worth \$7500 is insured for \(\frac{2}{3} \) its value, at \(\frac{1}{3} \) of 1% per annum. What is the annual premium?

8. Four companies insure a store and contents for \$60,000. One company takes \$20,000, at \{ \} of 1\%; a second takes \$10,000, at \{ \} of 1\%; a third, \$15,000, at \{ \} of 1\%; a fourth, the remainder, at \{ \} of 1\%. What is the premium?

The remainder = \$60,000 - (\$20,000 + \$10,000 + \$15,000) = \$15,000.

9. If the store of Ex. 8 is damaged to the extent of \$4500, what amount does each company pay?

$$\frac{29999}{89999} \text{ of } \$4599 = \$1500, 1st Co.}$$

$$\frac{19999}{899999} \text{ of } \$4599 = \$750, 2d Co.}$$

$$\frac{15999}{899999} \text{ of } \$4599 = \$1125, 3d Co. and 4th Co.}$$

10. A man insures his life for \$10,000, paying \$350 a year in advance, and dies the day before the fifth premium is due. The company pays his widow \$10,000. How much has the company lost by him, if the interest gained on the premiums paid amounts to \$175?

\$ 350	\$ 10000.
4	1575.
\$ 1400	\$ 8425. Ans.
175	•
\$ 1575	

11. A merchant shipped a cargo to London, and took a policy of \$100,800 at 3½%, to cover both the cargo and the premium. Find the value of the cargo.

12. Three companies insure, at \(\frac{1}{4}\) its value, a building worth \(\frac{1}{6}16,000\). The first company takes \(\frac{1}{4}\) the risk at \(\frac{1}{4}\) of 1%; the second, \(\frac{1}{4}\) at \(\frac{1}{4}\) of 1%; and the third, the remainder at \(\frac{1}{4}\) of 1%. Find the total premium.

```
      \frac{3}{4} of $ 16,000 = $ 12,000.
      \frac{7}{4} of $ 4800 = $ 42.

      \frac{1}{3} of $ 12,000 = $ 4000.
      $ 12,000 - ($ 4000 + $ 4800) = $ 3200.

      \frac{3}{4} of $ 4000 = $ 30.
      \frac{3}{4} of $ 3200 = $ 24.

      \frac{3}{4} of $ 12,000 = $ 4800.
      $ 30 + $ 42 + $ 24 = $ 96. Ans.
```

13. S. Williams pays \$18.40 premium for insuring his house for \ its value at 1\ \frac{1}{2}\%. What is the value of his house?

Policy = \$ 18.40 ÷
$$\frac{1\frac{1}{3}}{100}$$
 = $\frac{200}{3}$ × \$ 18.40 = \$ 1226\frac{3}{3}\$.

Value of house = \$ 1226\frac{3}{3} ÷ $\frac{2}{3}$ = $\frac{3}{2}$ × \$ $\frac{3689}{3}$ = \$ 1840. Ans.

14. Find the annual premium for an ordinary life policy of \$5000 issued to a man 30 years old, if the rate of insurance is 1.93%.

15. What is the annual premium for an ordinary life policy of \$12,000 issued to a man 40 years old, if the rate of insurance is 2.661%?

\$319.32. Ans.

Exercise 116. Page 255.

Make a table for a tax rate of 16 mills.

PROP.	TAX.	PROP.	TAX.	Prop.	TAX.	Prop.	TAX.
\$ 1	\$ 0.016	\$ 10	\$ 0.16	\$100	\$ 1.60	\$ 1000	\$ 16.00
2	0.032	20	0.32	200	3.20	2000	32.00
3	0.048	30	0.48	300	4.80	3000	48.00
4	0.064	40	0.64	400	6.40	4000	64.00
5	0.080	50	0.80	500	8.00	5000	80.00
6	0.096	60	0.96	600	9.60	6000	96.00
7	0.112	70	1.12	700	11.20	7000	112.00
8	0.128	80	1.28	800	12.80	8000	128.00
9	0.144	90	1.44	900	14.40	9000	144.00

1. Find the tax on property assessed at \$7500.

Tax on
$$$7000 = $112.00$$

Tax on $500 = 8.00$
Total tax = $$120.00$ Ans.

2. Find the tax on property assessed at \$4825.

Tax on
$$$4000 = $64.00$$

Tax on $800 = 12.80$
Tax on $20 = 0.32$
Tax on $5 = 0.08$
Total tax = $$77.20$ Ans.

3. Find the tax on property assessed at \$9685.

Tax on
$$\$9000 = \$144.00$$

Tax on $600 = 9.60$
Tax on $80 = 1.28$
Tax on $5 = 0.08$
Total tax = $\$154.96$ Ans.

4. Find the tax on property assessed at \$10,727.

Tax on \$10000 = \$160.00
Tax on
$$700 = 11.20$$

Tax on $20 = 0.32$
Tax on $7 = 0.11$
Total tax = \$171.88 Ans.

5. Find the tax on property assessed at \$12,863.

Tax on
$$$10000 = $160.00$$

Tax on $2000 = 32.00$
Tax on $800 = 12.80$
Tax on $60 = 0.96$
Tax on $3 = 0.05$
Total tax = $$205.81$ Ans.

6. Find the tax on property assessed at \$16,458.

Tax on
$$\$10000 = \$160.00$$

Tax on $6000 = 96.00$
Tax on $400 = 6.40$
Tax on $50 = 0.80$
Tax on $8 = 0.13$
Total tax = $\$263.33$ Ans.

7. Find the tax on property assessed at \$38,249.

Tax on
$$\$30000 = \$480.00$$

Tax on $8000 = 128.00$
Tax on $200 = 3.20$
Tax on $40 = 0.64$
Tax on $9 = 0.14$
 $\$611.98$ Ans.

\$2500 on his real estate and \$5200 on his personal property, and pays for two polls at \$1.50 each. If the rate is \$12.18 on \$1000, what is his total tax?

9. If the tax rate of a town is \$12.25 on \$1000, and the amount of the levy \$11,788.50, what is the assessed valuation of the town?

\$962326.53 Ans.

10. If the assessed valuation of a town is \$1,777,000, and the levy is \$29,231.65, what is the rate on \$1000?

\$0.01645 on \$1

= \$ 16.45 on \$ 1000. Ans.

TEACHERS' EDITION.

11. What sum must be assessed that \$15,000 may remain after paying 2% commission for collecting the taxes?

\$15,000 is 98% of amount assessed.

12. For building a schoolhouse a tax of \$1857.60 was levied upon a school district, assessed valuation \$1,935,000. What was the tax on property assessed at \$6250?

13. In a certain town there are 1350 polls. The assessed valuation of the real estate is \$713,250, and of the personal property is \$738,954. The poll tax is \$2 per poll, and the tax on property is 1½%. Only 96% of the property tax can be collected, and the collector is paid 2½% of the amount collected. How much does the town receive from the taxes? How much does the collector receive for his services?

Poll tax = $1350 \times \$2 = \2700 . Assessed valuation of town = \$713,250 + \$738,954 = \$1,452,204.

> \$ 1452204 0.01\frac{1}{3} 181525\frac{1}{4} 1452204 \$ 16337.29\frac{1}{4}

4 otal tax = \$2700 + \$16,337.30 = \$19,037.30.

 $A_{\text{mount collected}} = 0.96 \text{ of } 0.007.80 = 0.18,275.8$

Collector receives 0.025 of \$18, \$75.81 = \$450.00. Ans.

Town receives \$18, 275.81 - \$456.99 = \$17,818.91 Ans. (17,

\$19081.30 0.96 11422380 17163676 \$18275.8080 5 0 2 5

91976.61 0.025 9197905 3655162 8 456.89525

4703 - 73

Exercise 117. Page 257.

1. What is the duty at 2½ cents a pound on 320 boxes of raisins each containing 40 pounds?

\$320. Ans.

2. What is the duty at 6 cents a gallon on 420 hhd. of best molasses of 63 gal. each?

26460 gal.	·
252	\$ 1587.60. Ans.
1260	1587.60
420	0.06
63 gal.	26460

3. What is the duty at \$4 a dozen bottles on 50 cases of champagne, each containing 24 pint bottles, if breakage of 5% is allowed?

Each case contains 2 doz. bottles.

$$50 \times 2 \text{ doz.} = 100 \text{ doz.}$$
 $100 \text{ doz.} - 5 \text{ doz.} = 95 \text{ doz.}$ Breakage = 5 % of 100 doz. = 5 doz. $95 \times $4 = 380 . Ans.

4. Find the duty on 150 gross of spectacles, cost price \$1.20 a dozen; specific duty 45 cents a dozen, breakage allowed 2½%; and 20% ad valorem.

150 gross=1800 doz. Breakage=
$$2\frac{1}{2}$$
% of 1800 doz.=45 doz.
1800 doz.=45 doz.=1755 doz.

3789.75 + 3421.20 = 31210.95. Ans.

421.20, ad valorem.
0.20
2106.
1755
35100
1.20
1755

5. Find the duty on 100 shotguns, cost price \$8.50 each; specific duty of \$4 each, and 15% ad valorem.

\$4	\$8.50	
100	100	
\$400, specific.	\$ 850	
<u>-</u>	0.15	
\$ 400.	4250	
127.50	850	
\$ 527.50 Ans.	\$127.50, ad valorem.	

6. Find the duty at \$1 per M on 12,500 ft. of whitewood boards, planed on one side, if an additional duty of 50 cents per M is collected for each side planed.

12,500 = 12.5 M. Duty per M = \$1 + \$0.50 = \$1.50.

12.5

$$\frac{1.50}{6250}$$

12.5

18.750 \$18.75. Ans.

7. Find the duty on 500 boxes of cigars, gross weight 475 lb., tare 40%, costing 82½ cents per box in Havana. Specific duty \$4.50 per pound; and 25% ad valorem.

475 lb.

\$ 1385.63 Ans.

8. Find the duty on 400 pairs of woolen blankets, cost price \$1.75 per pair; weighing 7½ lb. per pair, tare 5%. Specific duty 33 cents per pound, ad valorem 40%.

$$400 \times 7\frac{1}{4}$$
 lb. = 2900 lb.

Tare = 5 % of 2900 lb. = 145 lb.

Net weight = 2900 lb. - 145 lb. = 2755 lb.

 2755
 0.33
 81.75
 0.33
 8265
 8700 .
 0.40
 0.40
 0.40
 0.40
 0.40
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9. Find the duty on 12 boxes of skein silk, each box weighing 40 lb.; cost price \$2.125 per pound, tare 10%. Specific duty 50 cents per pound, ad valorem 15%.

\$ 1189.15 Ans.

 $12 \times 40 \text{ lb.} = 480 \text{ lb.}$ Tare = 10 % of 480 lb. = 48 lb. Net weight = 432 lb. $\frac{432}{0.50}$ $\frac{432}{216.00}$, specific. $\frac{432}{4250}$ $\frac{6375}{8500}$ $\frac{8500}{918}$ $\frac{0.15}{4590}$

137.70

\$ 353.70 Ans.

10. Find the duty on 150 gross of clay tobacco pipes, cost price 55 cents a gross. Specific duty 15 cents a gross, and 25 % ad valorem.

918

\$ 137.70, ad valorem.

8 0.15	8 0.55
150	150
750	2750
15	55
\$ 22.50, specific.	8 82.50
	0.25
\$ 22.50	41250
20.63	16500
\$43.18 Ans.	\$ 20.625, ad valorem.

11. A New York merchant bought in London 400 gal. of cologne at \$1.25 a gallon, and commission and other expenses amounted to \$56.25. At what price per pint must be sell the cologne to gain 40% on the cost, if he paid a specific duty of 60 cents a gallon, and an ad valorem duty of 45%?

 $400 \times \$1.25 = \$500.$ Total cost = \$500 + \$56.25 = \$556.25.Specific duty = $400 \times \$0.60 = \$240.$

Ad valorem duty = 45% of \$556.25 = \$250.31.

Total cost in New York

= \$556.25 + \$240 + \$250.31 = \$1046.56. $400 \text{ gal.} = 400 \times 8 \text{ pt.} = 3200 \text{ pt.}$

Total selling price must be

\$1046.56 + 40 % of \$1046.56 = \$1046.56 + \$418.62 = \$1465.18.

Selling price per pint must be

$$\$1465.18 \div 3200 = \$0.458$$
. Ans.

12. Find the duty on 750 lb. of glue, cost price 40 cents; specific duty of 15 cents a pound, tare 2%; and ad valorem duty of 25%.

$$750 \times \$ 0.40 = \$ 300.$$

Tare = 2% of 750 lb. = 15 lb.

Net weight = 750 lb. - 15 lb. = 735 lb.

110.25, specific.

Total duty \$110.25 + \$75 = \$185.25. Ans.

13. A Boston merchant bought in Sheffield 50 gross of razors at a net price of \$4.25 a dozen. At what price per dozen must be sell the razors to gain 33\frac{1}{3}\% on the net cost, if he paid a specific duty of \$1.75 a dozen, and an ad valorem duty of 20\%?

$$50 \text{ gross} = 600 \text{ doz}.$$

Net cost = $600 \times \$4.25 = \2550 .

Specific duty = $600 \times \$1.75 = \1050 .

Ad valorem duty = 20 % of 2550 = 510. Total cost = 2550 + 1050 + 510 = 4110.

Total selling price must be

 $$4110 + 33\frac{1}{8}\% \text{ of } $4110 = $4110 + $1370 = $5180.$

Selling price per dozen must be

$$$5480 + 600 = $9.13$$
. Ans.

Exercise 118. Page 259.

1. Find the interest on \$125.65 for 1 mo. at 6%.

1 mo. =
$$\frac{1}{12}$$
 yr.
\$ 125.65
0.06
12 \$ 7.5390
\$ 0.62825

\$0.63. Ans.

2. Find the interest on \$1165 for 3 yr. at 5%.

3. Find the interest on \$1296.50 for 2 mo. at $5\frac{1}{2}$ %.

2 mo. =
$$\frac{1}{6}$$
 yr.
\$ 1296.50
0.055
648250
648250
6 \$ 71.30750
\$ 11.88458
\$ 11.88. Ans.

4. Find the interest on \$630.50 for 3 yr. at 4%.

5. Find the interest on \$231.50 for 3 yr. 8 mo. at 4½%.

\$38.20. Ans.

6. Find the interest on \$580.40 for 2 yr. 4 mo. at 6 %.

7. Find the interest on \$285.85 for 1 yr. 7 mo. at 4 %.

1 yr. 7 mo. =
$$1\frac{7}{12}$$
 yr.
\$285.85

$$\frac{0.04}{\$11.4340}$$

$$\frac{1\frac{7}{12}}{6669\frac{8}{8}}$$

$$\frac{11434}{\$18.103\frac{8}{8}}$$
\$18.10. Ans.

TEACHERS' EDITION.

8. Find the interest on \$1275.35 for 3 yr. 2 mo. at $3\frac{1}{2}$ %.

\$ 141.35. Ans.

Exercise 119. Page 260.

1. Find the interest at 6% on \$744.20 for 3 yr. 6 mo. 18 dy.

3 yr.	6 mo.	18 dy.	\$ 744.20
\$ 0.18	0.03	0.003	0.213
0.03			223260
0.003			74420
8 0.213			. 148840
	\$ 158	3.51. Ans.	\$ 158.51460

2. Find the interest at 6% on \$625.44 for 6 yr. 7 mo. 12 dy.

6 yr.	7 mo.	12 dy.	\$ 625.44
\$ 0.36	0.035	0.002	0.397
0.035			437808
0.002			562896
\$ 0.397			187632
	\$ 248.	30. Ans.	\$ 248.29968

3. Find the interest at 6% on \$124.87 for 2 yr. 10 mo. 16 dy.

2 yr.	10 mo.	16 dy.	\$ 124.87
\$ 0.12	0.05	0.0023	0.1723
0.05		•	83242
$0.002\frac{2}{3}$			24974
\$0.172			87409
•		12487	
\$ 21.56. Ans.		\$ 21.580883	

4. Find the interest at 6% on \$847.64 from Jan. 12, 1896 to Aug. 7, 1899.

yr.	mo,	dy.	\$ 847.64
1899	8	7	_ 0.214 1
1896	1	12	141271
3	6	25	339056
			84764
3 yr.	6 mo.	25 dy.	169528
\$ 0.18	0.03	0.0041	\$ 181.53623 1
0.03		-	-
0.0041			
\$ 0.214 }			\$ 181.54. Ans.

5. Find the interest at 6% on \$84.84 from Mar. 22, 1895 to Jan. 1, 1898.

yr.	mo.	dy.	\$84.84
1898	1	1	0.1665
1895	3	22	42420
2	8	9	50904
			50904
2 yr.	9 mo.	9 dy.	8484
\$ 0.12	0.045	0.0015	\$ 14.125860
0.045			
0.0015			
\$ 0.1665			\$ 14.13. A

6. Find the interest at 6% on \$1248.27 from Apr. 7, 1894 to May 17, 1897.

yr.	mo.	dy.	\$ 1248.27
1897	5	17	0.1863
1894	4	7	83218
3	1	10	748962
			998616
3 yr.	1 mo.	10 dy.	124827
\$ 0.18	0.005	0.001	\$ 233.01040
0.005		•	
0.0013			
\$ 0.186			\$ 233.01. Ans.

\$0.13. Ans.

Exercise 120. Page 261.

1. Find the interest at 6% on \$1278.75 for 1 mo.; 2 mo.; 3 mo.; 4 mo.

Interest on \$ 1278.75 for 2 mo. = \$ 12.7875 = \$ 12.79. Ans. Interest on \$ 1278.75 for 1 mo. = $\frac{1}{2}$ of \$ 12.7875 = \$ 6.39. Ans. Interest on \$ 1278.75 for 3 mo. = $\frac{3}{2}$ of \$ 12.7875 = \$ 19.18. Ans. Interest on \$ 1278.75 for 4 mo. = $\frac{3}{2}$ × \$ 12.7875 = \$ 25.58. Ans.

2. Find the interest at 6% on \$2265.50 for 1 mo.; 2 mo.; 3 mo.; 4 mo.

Interest on \$2265.50 for 2 mo. = \$22.655 = \$22.66. Ans. Interest on \$2265.50 for 1 mo. = $\frac{1}{2}$ of \$22.655 = \$11.33. Ans. Interest on \$2265.50 for 3 mo. = $\frac{3}{2}$ of \$22.655 = \$33.98. Ans. Interest on \$2265.50 for 4 mo. = $2 \times $22.655 = 45.31 . Ans.

- 3. Find the interest at 6% on \$1840.25 for 30 dy.; 60 dy.; 90 dy. Interest on \$1840.25 for 30 dy. = $5 \times $1.84025 = 9.20 . Ans. Interest on \$1840.25 for 60 dy. = $10 \times $1.84025 = 18.40 . Ans. Interest on \$1840.25 for 90 dy. = $15 \times $1.84025 = 27.60 . Ans.
- **4.** Find the interest at 6% on \$1946.75 for 30 dy.; 60 dy.; 90 dy. Interest on \$1946.75 for 30 dy. = $5 \times $1.94675 = 9.73 . Ans. Interest on \$1946.75 for 60 dy. = $10 \times $1.94675 = 19.47 . Ans. Interest on \$1946.75 for 90 dy. = $15 \times $1.94675 = 29.20 . Ans.

Exercise 121. Page 262.

1. Find the interest on \$680.40 for 2 yr. 4 mo. 6 dy. at 6%.

2 yr.	4 mo.	6 dy.		\$ 680.40		
80.12	0.02	0.001	0.141			
0.02				68040		
0.001				272160		
\$0.141				68040		
• • • • • • • • • • • • • • • • • • • •			•	8 95.93640	\$ 95.94.	Ans.

2. Find the interest on \$25.62 for 30 dy. at 6%.

30 dy.	\$ 25.62
8 0.005	0.005
₩ 33333	\$ 0.12810

3. Find the interest on \$85.85 for 1 yr. 7 mo. 21 dy., at 6 %

1 yr.	7 mo.	21 dy.	\$85. 85
\$0.06	0.035	0.0035	0.0985
0.035			42925
0.0035			68680
\$0.0985			77265
\$8.46. Ans.			8 8.456225

4. Find the interest on \$1100 for 3 yr. 4 mo., at 5%.

3 yr.	4 mo.	\$1100
8 0.18	0.02	0.20
0.02	0.02	6 \$ 220.00
		36.67
\$ 0.20	•	\$ 183.33 Ans.

5. Find the interest on \$1275 for 3 yr. 2 mo. 15 dy., at 8 %

3 yr.	2 mo.	15 dy.	\$ 1275
\$ 0.18	0.01	0.01 0.0025	0.1925
0.01			6375
0.0025			2550
80.1925			11475
Q 0.1020			1275
			8 245.4375
			81.8125
			8 327.25 Ans.

6. Find the interest on \$475.16 for 27 dy., at $4\frac{1}{2}$ %.

	27 dy.	\$475.16
	8 0.0045	0.0045
* • • • • • • • • • • • • • • • • • • •	*	237580
		190064
		4 \$2.138220
		0.534555
1.60.	Ans.	\$ 1.603665

7. Find the interest on \$1290.50 for 60 dy., at 6 %.

	60 dy.	\$ 1290.50
	80.01	0.01
\$ 12.91.	W	\$ 12.9050

8. Find the interest on \$125 for 1 yr. 2 mo. 2 dy., at 9%.

1 yr.	2 mo.	2 dy.		\$ 125
\$0.06	0.01	0.0001		0.0701
0.01		•		412
$0.000\frac{1}{3}$				8750
\$0.070			2	\$8.7914
_				4.395
Ans.			`	\$13.186

9. Find the interest on \$250.80 for 10 mo. 10 dy., at $3\frac{1}{2}$ %.

\$13.19.

10. Find the interest on \$258.85 from Mar. 6 to June 24, at 5%

11. Find the interest on \$380 for 2 yr. 11 mo. 27 dy., at 4½%.

2 yr.	11 mo.	27 dy.	\$ 0.1795
\$ 0.12	0.055	0.0045	380
0.058	5		143600
0.004	15		5385
\$ 0.179)5		4 8 68.2100
			17.0525
			\$51.1575
			\$51.18. Ans.

. 100 · 12. -Tins - - 11 m-___ ナナムデニ - Livering 本层 IP TIM 13 Fut the treese of Table or Land 4 to Land 4 \$ "LE. 40 7 n - 2- 1 11.3 和 万万 1.44 小二二十八 1 44 14. THE 4 4 to moil 唐川 写法 3. July

14. Fint the anemer in Post in trading the fire with

2 17 8 17 8 2 1 10.1 6 11 50 21 50 21 51 21 51 3234 568.6171

\$68.62 Ans.

\$17 45. Ans.

マンド まん

15. Find the interest on \$80,50 for 90 dy., at 6%.

\$630.50 \$0.015 \$0.015 315250 63050 \$9.45750

\$9.46. Ans.

16. Find the interest on \$547.60 from Feb. 20 to Dec. 5, at 6½ %.

17. Find the interest on \$875 from May 5, 1897 to June 21, 1898, at $5\frac{1}{2}$ %.

18. Find the interest on \$758.50 from Jan. 5 to July 1, at 4½%.

mo. dy.	\$758.50
7 1	$0.029\frac{1}{8}$
1 5	25283 1
5 26	682650
F	151700
5 mo. 26 dy.	4 \$22.249331
\$0.025 0.0041	5.56233
0.004	\$ 16.68700
\$0.029 }	\$16.69. Ans

19. Find the interest on \$342.42 from Feb. 5, 1897 to Mar. 15, 1899, at 7%.

yr.	mo.	d y .	\$ 342.42
1899	3	15	0.1263
1897	2	5	22828
2	1	10	205452
_	_		68184
2 yr.	1 mo.	10 dy.	34242
80.12	0.005	0.0013	6 \$43.37320
0.005		•	7.2288
0.001	3		\$50.6020
\$0.126	33		\$50.60. Ans.

20. Find the interest on \$540 from Mar. 5 to Sept. 21, at 31%.

mo.dy.\$540921
$$0.032\frac{3}{2}$$
 $\frac{3}{5}$ $\frac{5}{360}$ 6 16 1080 $\frac{6}{80.03}$ $0.002\frac{3}{2}$ $\frac{12}{317.640}$ $\frac{0.002\frac{3}{2}}{30.032\frac{3}{2}}$ $\frac{7}{310.29}$

21. Find the amount of \$431.50 for 2 yr. 8 mo., at 41%.

2 yr.	8 mo.	\$431.50
8 0.12 0.04	0.16	
0.04	0.02	258900
\$ 0.16		43150
Φ υ. 10		4 \$69.0400
	17.26	
	\$51.78	
	431.50	
	\$483.28 Ans	

22. Find the amount of \$476.50 from July 5, 1897 to Feb. 9, 1898, at 4%.

23. Find the amount of \$319.20 from Apr. 7 to Aug. 31, at 3½%.

24. Find the amount of \$6460 from June 15, 1897 to May 7, 1899, at $4\frac{1}{4}$ %

yr. mo.	dy.	\$ 6460
1899 5	7	0.1134
1897 6	<u> 15</u>	43064
1 10	22	19380
1 yr. 10 mo	. 22 dy.	6460
\$ 0.06 0.05	0.0034	6460
0.05	01110 3	24 \$ 734.286 ₄
0.0031		\$ 30.5953
\$ 0.113 3		17
\$ 520.12		2141671
6460.		305953
\$ 6980.12 An	3.	\$ 520,1201

25. Find the amount of \$150 from Aug. 5, 1897 to Mar. 17, 1899, at 7%.

yr.	mo.	dy	•	\$ 150
1899	3	17		0.097
1897	8	5	1	1050
1	7	12	-	1350
1	•	12		6 \$ 14.550
1 yr.	7 m	0.	12 dy.	2.425
\$ 0.06	0.03	35	0.002	\$ 16.975
0.035				\$ 16.98
0.002				150.
\$ 0.097	•			\$ 166.98 Ans.

26. Find the amount of \$527.20 from Jan. 1 to Nov. 20, at 41 %.

mo.
 dy.
 \$ 527.20

 11
 20

$$0.053\frac{1}{2}$$

 1
 1
 $8786\frac{2}{3}$

 10
 19
 263600

 10 mo.
 19 dy.
 263600

 \$0.05
 $0.003\frac{1}{3}$
 7.00736

 \$0.053\frac{1}{3}\$
 \$ 21.02210

 \$548.22
 Ans.

27. Find the amount of \$1250 from Nov. 15, 1897 to Mar. 1, 1898, at 5%.

28. Find the amount of \$624.36 from Mar. 5 to Dec. 20, at $7\frac{3}{10}$ %.

mo.	dy.	\$ 624.36
12	20	· 0.0 4 75
3	5	312180
9	15	437052
9 mo.	15 dy.	249744
\$0.045	0.0025	6 \$ 29.657100
0.0028	5	\$ 4.94285
\$0.047	5	7.3
•	36.08	1482855
-	24.36	3459995
	30.44 Ans.	\$ 36.082805

29. Find the amount of \$12,260 from May 6 to Oct. 24, at 33 %-

mo.	dy.	\$ 12260
10	24	0.028
5		98080
5	18	24520
		8 \$ 343.280
5 mo.	18 dy.	\$42.91
\$ 0.025	0.003	5
0.003		\$214.55
\$ 0.028	12260.	
		\$ 12474.55 Ans.

30. Find the amount of \$11,216 from Oct. 20 to Dec. 31, at 1% a month.

% a month is 12% a year.		\$ 11216
mo.	dy.	0.0115
12	31	93464
10	20	11216
2	11	11216
2 mo.	11 d y .	\$ 132.722 3
\$ 0.01	0.0015	8 265.445
0.001		11216.
\$ 0.011 §		\$11481.45 A

Exercise 122. Page 264.

1. Find the rate per cent when the interest on \$326 for 15 yr. is \$220.05.

$$r = \frac{i}{pt}$$
.

Here

i = \$220.05; p = \$326; t = 15 yr.

Hence,

$$r = \frac{220.05}{326 \times 15} = 0.045.$$

Therefore, the rate required is 41 %.

2. Find the rate per cent when the interest on \$745 for 18 yr. is \$603.45.

$$r = \frac{i}{pt}$$

Here

i = \$603.45; p = \$745; t = 18 yr.

Hence,

$$r = \frac{603.45}{745 \times 18} = 0.045.$$

Therefore, the rate required is 4½ %.

3. Find the rate per cent when \$980 amounts to \$1016.75 in 9 mo.

$$r = \frac{i}{pt}$$

Here i=\$1016.75-\$980=\$36.75; p=\$980; t=9 mo.=0.75 yr.

Hence,

$$r = \frac{36.75}{980 \times 0.75} = 0.05.$$

Therefore, the rate required is 5%.

4. Find the rate per cent when the interest on \$470.50 is \$141.15 for 5 yr.

$$r=\frac{i}{pt}$$

Here

$$i = $141.15$$
; $p = 470.50 ; $t = 5$ yr.

Hence,

$$r = \frac{141.15}{470.50 \times 5} = 0.06.$$

Therefore, the rate required is 6%.

5. Find the rate per cent when \$3631.25 amounts to \$3715.98 for 7 mo.

$$r = \frac{i}{pt}$$

Here

i = \$3715.98 - \$3631.25 = \$84.73;

p = 3631.25; t = 7 mo. $= \frac{7}{12}$ yr.

Hence,

$$r = \frac{84.73}{3631.25 \times \frac{7}{12}} = 0.04.$$

Therefore, the rate required is 4 %.

6. Find the rate per cent when the interest on \$997.75 is \$199.55 for 5 yr. 4 mo.

$$r=\frac{i}{pt}$$

Here i = \$199.55; p = \$997.75; t = 5 yr. 4 mo. $= 5\frac{1}{3}$ yr.

Hence,

$$r = \frac{199.55}{997.75 \times 5\frac{1}{4}} = 0.0375.$$

Therefore, the rate required is 33 %.

7. Find the rate per cent when \$350 amounts to \$406.70 in 3 yr 7 mo. 6 dy.

$$r = \frac{i}{pt}$$

Here

$$i = $406.70 - $350 = $56.70$$
;

p = \$350; t = 3 yr. 7 mo. 6 dy. = 3.6 yr.

Hence,

$$r = \frac{56.70}{350 \times 3.6} = 0.045.$$

Therefore, the rate required is 41%.

8. Find the rate per cent when the interest on \$6875 is \$68.75 for 90 dy.

$$r = \frac{i}{pt}$$

Here

i = 868.75; p = 86875; t = 90 dy. = 0.25 yr.

Hence, $r = \frac{68.75}{6875 \times 0.25} = 0.04$.

Therefore, the rate required is 4%.

9. Find the rate per cent when the interest on \$642 is \$10.70 for 5 mo.

$$r = \frac{i}{nt}$$
.

Here

i = \$10.70; p = \$642; t = 5 mo. $= \frac{5}{12}$ yr.

Hence,

$$r = \frac{10.70}{642 \times \frac{5}{12}} = 0.04.$$

Therefore, the rate required is 4 %.

10. Find the rate per cent when the interest on \$8432 for 2 yr. 7 mo. 23 dy. is \$1339.28.

$$r = \frac{i}{pt}$$

Here i = \$1339.28; p = \$8432; t = 2 yr. 7 mo. 23 dy. $= 2\frac{288}{380}$ yr.

Hence,
$$r = \frac{1339.28}{8432 \times 2\frac{233}{300}} = 0.06.$$

Therefore, the rate required is 6%.

11. Find the rate per cent when a sum of money is doubled in 14 yr.

$$r=\frac{i}{pt}$$

Here

$$i = $1; p = $1; t = 14 yr.$$

Hence,

$$r = \frac{1}{1 \times 14} = 0.07 \frac{1}{7}.$$

Therefore, the rate required is 71%.

12. Find the rate per cent when an investment for 4 yr. 2 mo. produces a sum equal to $\frac{5}{14}$ of the capital.

$$r = \frac{i}{pt}$$
.

Here

$$i = \$ \frac{5}{24}$$
; $p = \$ 1$; $t = 4$ yr. 2 mo. $= 4\frac{1}{8}$ yr.

Hence,

$$r = \frac{\frac{5}{24}}{1 \times 4\frac{1}{4}} = 0.05.$$

Therefore, the rate required is 5%.

13. Find the rate per cent when an investment for 3 yr. 1 mo. 15 dy. produces a sum equal to 1 of the capital.

$$r=rac{i}{pt}$$

Here $i = \frac{1}{4}$; $p = \frac{1}{4}$; t = 3 yr. 1 mo. 15 dy. = $\frac{3}{4}$ yr.

Hence, $r = \frac{\frac{1}{1}}{1 \times 3\frac{1}{1}} = 0.04.$

Therefore, the rate required is 4 %.

14. Find the time in which the interest on \$450 will amount to \$72, at 4%.

$$t = \frac{i}{pr}$$

Here

$$i = \$72$$
; $p = \$450$; $r = 4\% = 0.04$.

Hence,

$$t = \frac{72}{450 \times 0.04} = 4.$$

Therefore, the time required is 4 yr.

15. Find the time in which the interest on \$487.50 will amount to \$39, at 4%.

$$t = \frac{i}{pr}$$

Here

$$i = $39; p = $487.50; r = 4\% = 0.04.$$

Hence,

$$t = \frac{39}{487.50 \times 0.04} = 2.$$

Therefore, the time required is 2 yr.

16. Find the time in which the interest on \$238.75 will amount to \$64.46, at 41%.

$$t=\frac{i}{pr}$$

Here

$$i = $64.46$$
; $p = 238.75 ; $r = 4\frac{1}{2}\% = 0.045$.

Hence,

$$t = \frac{64.46}{238.75 \times 0.045} = 6.$$

Therefore, the time required is 6 yr.

17. Find the time in which the sum of \$1587.75 will amount to \$1611.68, at $5\frac{1}{4}$ %.

$$t = \frac{i}{pr}$$

Here

i = \$ 1611.68 - \$ 1587.75 = \$ 23.93; p = \$ 1587.75; $r = 5\frac{1}{2}\% = 0.055$.

Hence,
$$t = \frac{23.93}{1587.75 \times 0.055} = 0.274.$$

Therefore, the time required is 0.274 yr. = 3 mo. 9 dy.

18. Find the time in which the sum of \$1 will double itself, at 4%.

$$t = \frac{i}{pr}$$

Here

$$i = \$1; p = \$1; r = 4\% = 0.04.$$

Hence,

$$t = \frac{1}{1 \times 0.04} = 25.$$

Therefore, the time required is 25 yr.

19. Find the time in which the sum of \$10 will amount to \$17, at 6%.

$$t=\frac{i}{pr}$$

Here i = \$17 - \$10 = \$7; p = \$10; r = 6% = 0.06.

Hence,
$$t = \frac{7}{10 \times 0.06} = 11\frac{2}{8}$$
.

Therefore, the time required is $11\frac{2}{3}$ yr. = 11 yr. 8 mo.

20. Find the time in which the sum of \$502.67 will amount to \$578.07, at $4\frac{1}{2}$ %.

$$t = \frac{i}{pr}$$

Here i=\$578.07-\$502.67=\$75.40; p=\$502.67; $r=4\frac{1}{2}\%=0.045$.

Hence,
$$t = \frac{75.40}{502.67 \times 0.045} = 3.333.$$

Therefore, the time required is 3.333 yr. = 3 yr. 4 mo.

21. Find the time in which the interest on \$537.50 will amount to \$80.62, at 4%.

$$t=\frac{i}{pr}$$

Here

i = \$80.62; p = \$537.50; r = 4% = 0.04.

Hence,

$$t = \frac{80.62}{537.50 \times 0.04} = 3.750.$$

Therefore, the time required is 3.750 yr. = 3 yr. 9 mo.

22. Find the time in which the interest on \$6875 will amount to \$75.05, at 4½%.

$$t = \frac{i}{pr}$$

Here

i = \$75.05; p = \$6875; $r = 4\frac{1}{4}\% = 0.0425$.

Hence,

$$t = \frac{75.05}{6875 \times 0.0425} = 0.2569.$$

Therefore, the time required is 0.2569 yr. = 3 mo. 2 dy.

23. Find the time in which the interest on \$8520 will amount to \$1746.60, at 6%.

$$t=\frac{i}{pr}$$

Here

i = \$1746.60; p = \$8520; r = 6% = 0.06.

Hence,

$$t = \frac{1746.60}{8520 \times 0.06} = 3\frac{5}{12}.$$

Therefore, the time required is $3\frac{5}{12}$ yr. = 3 yr. 5 mo.

24. Find the principal that will produce \$90 interest in 3 yr., at 4 %

$$p = \frac{i}{rt}$$

Here

$$i = $90$$
; $r = 4\% = 0.04$; $t = 3$ yr.

Hence,

$$p = \$ \frac{90}{0.04 \times 3} = \$ 750.$$

Therefore, the principal required is \$750.

25. Find the principal that will produce \$63 interest in 3 yr., at 61%.

$$p=\frac{i}{rt}$$

Here

$$i = $63$$
; $r = 6\frac{1}{4}\% = 0.0625$; $t = 3$ yr.

Hence,

$$p = \$ \frac{63}{0.0625 \times 3} = \$ 336.$$

Therefore, the principal required is \$336.

26. Find the principal that will produce \$100 interest in 8 yr. 6 mo., at 5%.

$$p = \frac{i}{rt}$$

Here i = \$100; r = 5% = 0.05; t = 8 yr. 6 mo. = 8.5 yr.

Hence,

$$p = \$ \frac{100}{0.05 \times 8.5} = \$ 235.29.$$

Therefore, the principal required is \$235.29.

27. Find the principal that will produce \$1746.60 interest in 3 yr. 5 mo., at 6%.

$$p=\frac{i}{rt}$$
.

Here i = \$1746.60; r = 6% = 0.06; $t = 3 \text{ yr. } 5 \text{ mo.} = 3\frac{5}{12} \text{ yr.}$

Hence,

$$p = \$ \frac{1746.60}{0.06 \times 3\frac{5}{10}} = \$ 8520.$$

Therefore, the principal required is \$8520.

28. Find the principal that will produce \$12 interest in 7 mo., at 5%.

$$p=\frac{i}{rt}$$

Here i = \$12; r = 5% = 0.05; t = 7 mo. $= \frac{7}{12}$ yr.

Hence,
$$p = \$ \frac{12}{0.05 \times \frac{7}{4}} = \$ 411.43.$$

Therefore, the principal required is \$411.43.

29. Find the principal that will produce \$50 interest in 228 dy., at 41%.

$$p = \frac{i}{rt}$$

Here i = \$50; $r = 4\frac{1}{2}\% = 0.045$; t = 228 dy. $= \frac{19}{30}$ yr.

Hence, $p = \$ \frac{50}{0.045 \times \frac{19}{10}} = \$ 1754.39.$

Therefore, the principal required is \$1754.39.

30. Find the principal that will produce \$1339.28 interest in 2 yr. 7 mo. 24 dy., at 6%.

$$p = \frac{i}{rt}$$

Here i = \$1339.28; r = 6% = 0.06; t = 2 yr. 7 mo. 24 dy. = 2.65 yr.

Hence, $p = \$ \frac{1339.28}{0.06 \times 2.65} = \$ 8423.14.$

Therefore, the principal required is \$8423.14.

31. Find the principal that will produce \$1312.65 interest in 2 yr. 3 mo., at 6%.

$$p=\frac{i}{rt}$$

Here i = \$1312.65; r = 6% = 0.06; t = 2 yr. 3 mo. = 2.25 yr.

Hence, $p = \$ \frac{1312.65}{0.06 \times 2.25} = \$ 9723.33.$

Therefore, the principal required is \$9723.33.

32. Find the principal that will produce \$750 interest in 3 yr. 8 mo., at 5%.

$$p = \frac{i}{rt}$$

Here i = \$750; r = 5% = 0.05; t = 3 yr. 8 mo. $= 3\frac{2}{3}$ yr.

Hence,
$$p = \$ \frac{750}{0.05 \times 3\frac{3}{4}} = \$ 4090.91.$$

Therefore, the principal required is \$4090.91.

33 Ind the principal and The united to I all it I was seen in I will be a first the first than the seen in I will be a first the first than the seen in I will be a first than the seen in I wi

$$p = \frac{t}{1 - \tau}$$

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810000

$$p = \frac{4}{3} \frac{40}{114} = \frac{4}{3} \frac{40}{112} = \frac{4}{3} \frac{40}{112}$$

Therefore the printing a regularity of \$100

34 First the principal that will amount to \$ Million 2 yr. 8 mo at \$1 %

$$p = \frac{1}{1 + rt}$$

Here a + \$30 110 %; r = 4; % = 9 % 125; t = 2 yr. 6 mo. = 2.5 yr.

Here
$$p = 3$$
 $\frac{26(13.4)}{1 + 9(24.25) \times 2.5} = 3\frac{26(113.54)}{1.195(25)} = 3.21.029.00.$

Therefore the principal tendined is \$21.689.60.

35. Find the principal that will amount to \$6000 in 21 dy., at 5%.

$$p = \frac{a}{1 + rt}$$

Here a = 8%%; r = 5% = 0.05; $t = 21 \text{ dy.} = \frac{7}{120} \text{ yr.}$

Hence,
$$p = 3 + \frac{6000}{1 + 0.05 \times 125} = 3 + \frac{6000}{12455} = 35992.55.$$

Therefore, the principal required is \$5982.55.

36. Find the principal that will amount to \$297.60 in 8 mo., at 6%.

$$p = \frac{a}{1 + rt}$$

Here a = \$207.60; r = 6% = 0.06; t = 8 mo. $= \frac{1}{4}$ yr.

Hence,
$$p = \$ \frac{297.60}{1 + 0.06 \times \frac{2}{3}} = \$ \frac{297.60}{1.04} = \$ 286.15.$$

Therefore, the principal required is \$286.15.

37. Find the principal that will amount to \$6378.75 in 1 yr. 1 mo., at 5%.

$$p=\frac{a}{1+rt}$$

Here a = \$6378.75; r = 5% = 0.05; t = 1 yr. 1 mo. $= 1\frac{1}{12}$ yr.

Hence,
$$p = \$ \frac{6378.75}{1 + 0.05 \times 1\frac{1}{12}} = \$ \frac{6378.75}{1\frac{13}{240}} = \$ 6050.99.$$

Therefore, the principal required is \$6050.99.

38. Find the principal that will amount to \$21,047.95 in 1 yr. 7 mo. 21 dy., at $4\frac{1}{2}$ %.

$$p=\frac{a}{1+rt}$$

Here

$$a = $21,047.95$$
; $r = 4\frac{1}{2}\% = 0.045$;

$$t = 1$$
 yr. 7 mo. 21 dy. = $1\frac{77}{120}$ yr.

Hence,
$$p = \$ \frac{21047.95}{1 + 0.045 \times 1_{1/20}^{7/2}} = \$ \frac{21047.95}{1.073875} = \$ 19,600.$$

Therefore, the principal required is \$19,600.

39. Find the principal that will amount to \$185.09 in 2 yr. 3 mo. 18 dy., at 5%.

$$p=\frac{a}{1+rt}.$$

Here a = \$185.09; r = 5% = 0.05; t = 2 yr. 3 mo. 18 dy. = 2.3 yr.

Hence,
$$p = \$ \frac{185.09}{1 + 0.05 \times 2.3} = \$ \frac{185.09}{1.115} = \$ 166.$$

Therefore, the principal required is \$ 166.

40. Find the principal that will amount to \$659.40 in 2 yr. 11 mo. 15 dy., at 6%.

$$p = \frac{a}{1 + rt}$$

Here a = \$659.40; r = 6% = 0.06; $t = 2 \text{ yr. } 11 \text{ mo. } 15 \text{ dy.} = 2\frac{3}{2}$ yr.

Hence,
$$p = \$ \frac{659.40}{1 + 0.06 \times 2\frac{23}{24}} = \$ \frac{659.40}{1\frac{71}{400}} = \$ 560.$$

Therefore, the principal required is \$ 560.

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M As what have per some will \$ hours. If you make \$ 25.72 inceress in \$ not \$ 15.7

 $r = \frac{1}{2r}$

Here t = 4 A, $\lambda = \rho = 4$ (e2) A) t = 4 ma, $\theta = \frac{1}{12}$ yr.

 $\frac{27.72}{1027.21 \times 1.15} = 0.07.$

Investige the sun expensed in The

45. The principal is \$653; the interest, \$5.52; the rate, 8%. Find the time.

$$t=\frac{i}{pr}.$$

Here

$$i = $5.52$$
; $p = 653 ; $r = 8\% = 0.08$.

Hence,

$$t = \frac{5.52}{653 \times 0.08} = 0.1057.$$

Therefore, the time required is 0.1057 yr. = 1 mo. 8 dy.

46. Find the amount of \$520 for 2 mo. 3 dy., at $4\frac{1}{2}$ %.

47. What sum bearing interest at 4½% will yield an annual income of \$1000?

$$p = \frac{i}{rt}$$

Here

$$i = $1000$$
; $r = 4\frac{1}{2}\% = 0.045$; $t = 1$ yr.

Hence,

$$p = \$ \frac{1000}{0.045 \times 1} = \$ 22,222.22.$$

Therefore, the principal required is \$22,222.22.

48. In what time will \$4000 amount to \$4625, at $5\frac{1}{2}\%$?

$$t = \frac{i}{pr}$$

Here i = \$4625 - \$4000 = \$625; p = \$4000; $r = 5\frac{1}{2}\% = 0.055$.

Hence,
$$t = \frac{625}{4000 \times 0.055} = 2.841.$$

Therefore, the time required is 2.841 yr. = 2 yr. 10 mo. 3 dy.

49. At what rate per cent will \$3000 produce \$250 interest in 1 yr. 10 mo. 7 dy.?

$$r = \frac{i}{pt}$$
.

Here i = \$250; p = \$3000; t = 1 yr. 10 mo. 7 dy. $= 1\frac{327}{120}$ yr.

Hence,
$$r = \frac{250}{3000 \times 1\frac{3}{3}\frac{3}{5}} = 0.045$$
.

Therefore, the rate required is 41 %-

50. Find the interest on \$1721.84 from April 1 to Nov. 12, at 41%.

51. How long must \$3904.92 be on interest to amount to \$4568.76, at 5%?

$$t = \frac{i}{pr}$$

Here i = \$4568.76 - \$3904.92 = \$663.84; p = \$3904.92;

$$r = 5 \% = 0.05.$$

Hence,

$$t = \frac{663.84}{3904.92 \times 0.05} = 3.400.$$

Therefore, the time required = 3.400 yr. = 3 yr. 4 mo. 24 dy.

52. Find the interest on \$137.60 from July 3 to Dec. 12, at $7\frac{2}{10}$ %.

mo.	dy.	\$ 137. 6 0
12	12	0.0265
7 5	3 9	68800 82560 27520
5 mo.	9 dy.	6 \$ 3.646400
\$ 0.025	0.0015	\$ 0.607733 7.3
0.0015		1823199
\$ 0.0265		4254131
₩ 0.0200		\$ 4.4364509

\$4.44. Ans.

53. Find the interest on \$680.20, at $7\frac{1}{2}$ %, for 73 dy., reckoning 365 dy. for a year.

The interest on \$1 for 1 yr. at $7\frac{1}{4}$ % is \$0.075.

The interest on \$1 for 73 dy., that is $\frac{78}{865}$ yr., or $\frac{1}{6}$ yr., $=\frac{1}{6}$ of \$0.075 = \$0.015.

\$ 680.20 0.015 340100 68020 \$ 10.20300

\$ 10.20. Ans.

Exercise 123. Page 268.

1. Find the day of maturity, and amount due, having given face of note, \$530.25; date of note, Jan. 12, 1897; time, 60 dy.; and rate of interest, 6%.

Time to run is 19 dy. in Jan., 28 dy. in Feb., 13 dy. in Mar.

Hence, day of maturity is Mar. 13, 1897. Ans.

Interest on \$530.25 at 6% for 60 dy. is $10 \times $0.53025 = 5.30 .

\$530.25 + \$5.30 = \$535.55. Ans.

2. Find the day of maturity, and amount due, having given face of note, \$687.45; date of note, Mar. 22, 1897; time, 90 dy.; and rate of interest, 5%.

Time to run is 9 dy. in Mar., 30 dy. in Apr., 31 dy. in May, 20 dy. in June.

Hence, day of maturity is June 20, 1897. Ans.

90 dy.	\$ 687.45
8 0.015	0.015
\$ 8.59 6 87. 4 5	343725 68745
\$696.04 Ans.	6 \$ 10.31175 1.7186
	88.5931

3. Find the day of maturity, and amount due, having given face of note, \$286.75; date of note, Aug. 5, 1897; time, 4 mo.; and rate of interest, 4%.

Day of maturity is 4 mo. after Aug. 5, 1897; that is, Dec. 5, 1897.

Ans.

4. Find the day of maturity, and amount due, having given face of note, \$944.40; date of note, Oct. 20, 1897; time, 3 mo.; and rate of interest, $4\frac{1}{2}$ %.

Day of maturity is 3 mo. after Oct. 20, 1897; that is, Jan. 20, 1898.

Ans.

5. Find the day of maturity, and amount due, having given face of note, \$1262.72; date of note, Oct. 5, 1897; time, 30 dy.; and rate of interest, $5\frac{1}{2}$ %.

Time to run is 26 dy. in Oct., 4 dy. in Nov. Hence, day of maturity is Nov. 4, 1897. Ans.

6. Find the day of maturity, and amount due, having given face of note, \$1875.44; date of note, Dec. 16, 1897; time, 6 mo.; and rate of interest, 4%.

Day of maturity is 6 mo. after Dec. 16, 1897; that is, June 16, 1898. Ans.

6 mo.	\$ 1875.44
\$ 0.03	0.03
\$ 37.51	3 \$ 56.2632 18.7544
1875.44	
8 1912.95 Ans.	\$ 37.5088

7. Find the day of maturity, and amount due, having given face of note, \$1521.87; date of note, Apr. 30, 1897; time, 1 mo.; and rate of interest, 6%.

Day of maturity is 1 mo. after Apr. 30, 1897; that is, May 30, 1897. Ans.

8. Find the day of maturity, and amount due, having given face of note, \$2849.65; date of note, May 22, 1897; time, 2 yr.; and rate of interest, $3\frac{1}{4}$ %.

Day of maturity is 2 yr. after May 22, 1897; that is, May 22, 1899. Ans.

Interest on \$ 1 for 2 yr. at $3\frac{1}{2}\%$ is \$ 0.07.

\$ 2849.65	\$ 199.48
0.07	2849.65
8 199.4755	\$ 3049.13 Ans.

9. Find the day of maturity, and amount due, having given face of note, \$1968.10; date of note, July 10, 1897; time, 2 mo.; and rate of interest, $4\frac{1}{2}\%$.

Day of maturity is 2 mo. after July 10, 1897; that is, Sept. 10, 1897. Ans.

2 mo.		\$ 1968.10		
8 0.01			0.01	
\$ 14.76 1968.10		4	\$ 19.6810 4.92025	
\$ 1982.86	Ans.		\$ 14.76075	

Find the amount due Dec. 3, 1898, on the following demand notes:

10. \$875.18.

CONCORD, N. H., May 10, 1897.

On demand, I promise to pay George H. Chick, or order, Eight Hundred Seventy-five and 10 Dollars, with interest at 5%. Value received.

Frederick D. Sibley.

yr. 1898	mo. 12	dy. 3		\$ 875.18 0.093\$
1897	5	10		729314
1	6	23		262554
				787662
1 yr.	6 mo	. 2	3 dy.	6 82.121054
\$ 0.06	0.03		.0031	13.68684
0.03	0.00	U.	oog	\$ 68.43421
0.003				\$ 68.43
\$ 0.093				875.18
				\$943.61 Ans.

11. **\$**642.75.

LAKEWOOD, N. J., Oct. 25, 1897.

On demand, I promise to pay Harry Jones, or order, Six Hundred Forty-two and $\frac{75}{100}$ Dollars, with interest at $4\frac{1}{2}$ %. Value received.

GEORGE B. ATKINS.

yr.	mo.	dy.		\$642.75	
1898	12	3		0.066	
1897	10	25		21425	_
1	1	8		385650	
				385650	
1 yr.	1 m	0.	8 dy.	4 \$ 42.63575	
\$ 0.06	0.00)5	0.0011	10.65894	
0.005	0.00	,0	0.0013	\$ 31.97681	
0.001	ł			\$ 31.98	
\$ 0.066	- }			642.75	
				\$ 674.73	Ans.

12. \$ 1286.50.

ATLANTA, GA., Apr. 22, 1897.

On demand, I promise to pay Clarence E. Garland, or order, Twelve Hundred Eighty-six and $\frac{50}{100}$ Dollars, with interest at $5\frac{1}{4}$ %. Value received.

ROBERT PAGE.

yr.	mo.	dy.			\$ 1286.50	
1898 1897	12 4	3 22			0.096	•
1001	<u> </u>				107208]	•
1	7	11			771900	
					1157850	
1 yr.	7 m	Ю.	11 d y .	12	\$ 124.57608 1	
\$ 0.06	0.08	25	0.001‡		10.38134	
0.035	0.00	,0	0.0018		\$ 114.19474	•
0.001	<u> </u>				\$114.19	
\$ 0.096	- }				1286.50	
					\$ 1400.69	Ans

13. \$2548.25.

St. Paul, Minn., June 17, 1897.

On demand, I promise to pay Fred Lacey, or order, Twenty-five Hundred Forty-eight and $\frac{25}{100}$ Dollars, with interest at 7%. Value received.

WILLIAM P. WISSMAN.

yr. 1898	mo. 12	dy 3		\$ 2548.25 0.087 {
1897	6	17		1698831
1	5	16		1783775 2038600
1 yr.	5 m	o.	16 dy.	6 \$ 223.396581
\$ 0.06 0.025	0.02	25	0.0023	\$ 260.62934
0.002	2			\$ 260 .63
\$ 0.087	- }			2548.25
				\$ 2808.88 Ans

14. \$418.33.

OAKLAND, CAL., Dec. 23, 1897.

On demand, I promise to pay Albert J. Farnham, or order, Four Hundred Eighteen and \$\frac{83}{100}\$ Dollars, with interest at \$4\frac{1}{2}\%. Value received.

Austin C. Wiggin.

yr.	mo.	dy.	\$ 418.33
1898	12	3	0. 05 3
1897	12	23	27888
	11	10	209165
	40	•	4 \$ 23.7053 3
11 mo.	10	dy.	5.9263
\$0.05 5	0.0	013	\$17.7790
0.001	2 3		\$ 17.78
\$ 0.056	}		418.33
			\$436.11 Ans.

15. \$7486.45.

WATERTOWN, IA., Apr. 16, 1898.

On demand, I promise to pay Harry D. Smith, or order, Seven Thousand Four Hundred Eighty-six and $\frac{45}{100}$ Dollars, with interest at 5%.

Frank J. Leavitt.

yr.	mo.	dy.	\$7486.45
1898	12	3	0.037
1898	4	16	623870\$
	7	17	5240515
7	177	3	2245935
7 mo.	17	<u>dy.</u>	6 \$ 283.23735}
\$0.035	0.0	025	47.2062
0.002	<u>5</u>		\$ 236.0311
\$ 0.037			\$ 236.03
			7486.45
			\$ 7722.48 A

Exercise 124. Page 274.

Find the day of maturity, the time to run, the discount, and the proceeds of the following notes, without grace:

1. **8** 750.

New York, Jan. 1, 1897.

Four months from date, I promise to pay to the order of James Fay Seven Hundred Fifty Dollars, value received.

Payable at the National Bank of the Republic.

Discounted at 5%, Jan. 12.

JOHN PRAY.

11.35

Day of maturity is 4 mo. after Jan. 1, 1897; that is, May 1, 1897. Time to run is 19 dy. in Jan., 28 dy. in Feb., 31 dy. in Mar., 30 dy. in Apr., 1 dy. in May = 109 dy.

Discount on \$750 for 109 dy. at $6\% = 18\frac{1}{6} \times \0.75 .

$$\$0.75$$
 $\frac{18\frac{1}{8}}{12\frac{1}{2}}$
 $8750.$
 $\frac{11.35}{12\frac{1}{2}}$
 8738.65
 $Ans.$
 $8750.$
 $\frac{11.35}{12.35}$
 $\frac{11.35}{12.35}$
 $\frac{11.35}{12.35}$
 $Ans.$

2. **\$** 4325.50.

Boston, Mar. 4, 1897.

Sixty days from date, I promise to pay to James Finn, or order, Four Thousand Three Hundred Twenty-five and $\frac{50}{100}$ Dollars, value received.

Payable at the Merchants National Bank.

Discounted at 5½%, Mar. 8.

GEORGE BELLOWS.

Day of maturity is 60 dy. after Mar. 4, 1897; that is, May 3, 1897. Time to run is 23 dy. in Mar., 30 dy. in Apr., 3 dy. in May = 56 dy. Discount on \$4325.50 for 56 dy. at $6\% = 9\frac{1}{3} \times 4.3255 .

3. \$1300.

RICHMOND, VA., July 14, 1897.

Ninety days from date, I promise to pay to the order of Peter Bright Thirteen Hundred Dollars, value received.

Payable at the First National Bank.

Discounted at 4 %. Aug. 3.

GEORGE WRIGHT.

Day of maturity is 90 dy. after July 14, 1897; that is, Oct. 12, 1897. Time to run is 28 dy. in Aug., 30 dy. in Sept., 12 dy. in Oct. = 70 dy. Discount on \$ 1300 for 70 dy. at $6\% = 11\frac{7}{4} \times $ 1.30$.

4. \$1456.30.

CHARLESTON, S. C., Aug. 27, 1897.

Three months after date, I promise to pay to the order of John George Fourteen Hundred Fifty-six and $\frac{80}{100}$ Dollars, value received.

Payable at the Second National Bank.

Discounted at 5 %, Sept. 10.

JOHN WALDORF.

Day of maturity is 3 mo. after Aug. 27, 1897; that is, Nov. 27, 1897. Time to run is 20 dy. in Sept., 31 dy. in Oct., 27 dy. in Nov. = 78 dy. Discount on \$1456.30 for 78 dy. at $6\% = 13 \times 1.4563 .

5. \$4550.36.

BALTIMORE, MD., NOV. 10, 1897.

Four months after date, I promise to pay to the order of John Callender Four Thousand Five Hundred Fifty and $\frac{36}{100}$ Dollars, value received.

Payable at the National Mechanics Bank.

Discounted at 5½%, Nov. 24.

JAMES BARTON.

Day of maturity is 4 mo. after Nov. 10, 1897; that is, Mar. 10, 1898. Time to run is 6 dy. in Nov., 31 dy. in Dec., 31 dy. in Jan., 28 dy. in Feb., 10 in Mar. = 106 dy.

Discount on \$4550.36 for 106 dy. at $6\% = 17\frac{2}{3} \times 4.55036 .

6. \$5000.

CHICAGO, ILL., Dec. 23, 1897.

Six months after date, we jointly and severally promise to pay to John Adams, or order, Five Thousand Dollars, value received, with interest at 5 per cent.

Payable at the Metropolitan National Bank.

Discounted at 4 %, Jan. 21, 1898.

WILLIAM DUNN,

F. R. CROCKETT.

Day of maturity is 6 mo. after Dec. 23, 1897; that is, June 23, 1898.

Time to run is 10 dy. in Jan., 28 dy. in Feb., 31 dy. in Mar., 30 dy. in Apr., 31 dy. in May, 23 dy. in June = 153 dy.

Discount on \$5125 for 153 dy. at $6\% = 25.5 \times 5.125 ; at $4\% = 17 \times 5.125 .

Find the day of maturity, the time to run, the discount, and the proceeds of the following notes, with grace:

7. \$4760.

MILWAUKEE, WIS., Jan. 1, 1897.

Ninety days after date, I promise to pay to the order of James Pike Four Thousand Seven Hundred Sixty Dollars, value received.

Payable at the Wisconsin National Bank.

Discounted at 4½%, Feb. 15.

WILLIAM CLEMENT.

Day of maturity is 93 dy. after Jan. 1, 1897; that is, Apr. 4, 1897. Time to run is 13 dy. in Feb., 31 dy. in Mar., 4 dy. in Apr. = 48 dy. Discount on \$4760 for 48 dy. at $6\% = 8 \times 4.76 ; at $4\frac{1}{2}\% = 6 \times 4.76 .

8. **\$**2017.85.

St. Paul, Minn., Jan. 14, 1897.

Three months after date, I promise to pay to the order of John Brown Two Thousand Seventeen and $\frac{85}{100}$ Dollars, value received.

Payable at the German-American National Bank.

Discounted at 7%, Mar. 1.

TIMOTHY BRUCE.

Day of maturity is 3 mo. 3 dy. after Jan. 14, 1897; that is, Apr. 17, 1897.

Time to run is 30 dy. in Mar., 17 dy. in Apr. = 47 dy.

Discount on \$2017.85 for 47 dy. at 6% = 7 \\$ \times \$2.01785.

8 18.44. Ans.

9. \$9040.

GALVESTON, TEX., Jan. 19, 1897.

Sixty days from date, I promise to pay to the order of Charles Carroll Nine Thousand Forty Dollars, value received.

Payable at the First National Bank.

Discounted at 5½ %, Feb. 16.

JAMES MONROE.

Day of maturity is 63 dy. after Jan. 19, 1897; that is, Mar. 23, 1897. Time to run is 12 dy. in Feb., 23 dy. in Mar. = 35 dy.

Discount on \$9040 for 35 dy. at $6\% = 5\frac{5}{6} \times 9.04 .

10. **8** 215.

Augusta, ME., Jan. 28, 1897.

Thirty days after date, I promise to pay to the order of James Fogg Two Hundred Fifteen Dollars, value received.

Payable at the Maine National Bank.

Discounted at 6%, Feb. 3.

John Moses.

Day of maturity is 33 dy. after Jan. 28, 1897; that is, Mar. 2, 1897. Time to run is 25 dy. in Feb., 2 dy. in Mar. = 27 dy.

Discount on \$215 for 27 dy. at $6\% = 4.5 \times 0.215 .

80.97. Ans.

11. \$2216.85.

Омана, Neb., Dec. 15, 1897.

Ninety days after date, I promise to pay to the order of F. C. Green Two Thousand Two Hundred Sixteen and $\frac{85}{100}$ Dollars, value received. Payable at the Omaha National Bank.

Discounted at 7%, Jan. 8, 1898.

W. C. COLBURN.

Day of maturity is 93 dy. after Dec. 15, 1897; that is, Mar. 18, 1898.

Time to run is 23 dy. in Jan., 28 dy. in Feb., 18 dy. in Mar. = 69 dy. Discount on \$2216.85 for 69 dy. at $6\% = 11.5 \times 2.21685 .

Find the proceeds of the following drafts, with grace:

12. Draft for \$620 at 60 days; rate of discount 6%; exchange $\frac{1}{4}$ %. Discount on \$620 for 63 dy. at $6\% = 10\frac{1}{2} \times $0.62 = 6.51 .

Exchange $= \frac{1}{3}\%$ of \$700 = \$0.88.

Total discount = \$6.51 + \$0.88 = \$7.39.

Proceeds = \$620 - \$7.39 = \$612.61. Ans.

13. Draft for \$890 at 90 days; rate of discount $4\frac{1}{4}\%$; exchange $\frac{1}{4}\%$. Discount on \$890 for 93 dy. at $6\% = 15.5 \times 0.89 .

Exchange = $\frac{1}{4}$ % of \$900 = \$2.25.

Total discount = \$10.35 + \$2.25 = \$12.60.

Proceeds = \$890 - \$12.60 = \$877.40. Ans.

14. Draft for \$12,500 at 60 days; rate of discount 5%; exchange 15 cents on \$1000.

Discount on \$12,500 for 63 dy. at $6\% = 10.5 \times 12.50 .

Exchange = $12\frac{1}{4} \times \$0.15 = \1.88 .

Total discount = \$109.38 + \$1.88 = \$111.26.

Proceeds = \$12,500 - \$111.26 = \$12,388.74. Ans.

15. Draft for \$1260 at 30 days; rate of discount 51%; exchange 1%.

Discount on \$1260 for 33 dy. at $6\% = 5.5 \times 1.26 .

Exchange $= \frac{1}{3}\%$ of \$1300 = \$1.63.

Total discount = \$6.35 + \$1.63 = \$7.98.

Proceeds = \$1260 - \$7.98 = \$1252.02. Ans.

16. Draft for \$1430 at 3 months; rate of discount 6%; exchange \(\frac{1}{4} \)%.

Exchange = $\frac{1}{4}$ % of \$1500 = \$3.75.

Total discount = \$22.17 + \$3.75 = \$25.92.

Proceeds = \$1430 - \$25.92 = \$1404.08. Ans.

17. Draft for \$1875 at 4 months; rate of discount 5%; exchange \frac{1}{3}%.

\$ 1875 0.0205 9375 3750 6 \$ 38.4375 6.40625 \$ 32.03125

Exchange = $\frac{1}{8}$ % of \$1900 = \$2.38.

Total discount = \$32.03 + \$2.38 = \$34.41.

Proceeds = \$1875 - \$34.41 = \$1840.59. Ans.

18. Draft for \$22,843 at 60 days; rate of discount 4½%; exchange 25 cents on \$1000.

Discount on \$22,843 for 63 dy. at $6\% = 10.5 \times 22.843 .

Exchange = $22.9 \times \$0.25 = \5.73 .

Total discount = \$179.89 + \$5.73 = \$185.62.

Proceeds = \$22,843 - \$185.62 = \$22,657.38. Ans.

19. Draft for \$18,000 at 2 months; rate of discount 5%; exchange \frac{1}{3}%.

Exchange = $\frac{1}{8}$ % of \$18,000 = \$22.50.

Total discount = \$157.50 + \$22.50 = \$180.

Proceeds = \$18,000 - \$180 = \$17,820. Ans.

20. Draft for \$3437.50 at 90 days; rate of discount 5%; exchange \frac{1}{2}%.

Discount on \$3437.50 for 93 dy. at $6\% = 15.5 \times 3.4375 .

Exchange = $\frac{1}{4}$ % of $\frac{3500}{4}$ = $\frac{4}{3}$ 8.75.

Total discount = \$44.40 + \$8.75 = \$53.15.

Proceeds = \$3437.50 - \$53.15 = \$3384.35. Ans.

21. Draft for \$1287.50 at 60 days; rate of discount 4½%; exchange ½%.

Discount on \$1287.50 for 63 dy. at $6\% = 10.5 \times 1.2875 .

Exchange = $\frac{3}{8}$ % of 31300 = 4.88.

Total discount = \$10.14 + \$4.88 = \$15.02.

Proceeds = \$1287.50 - \$15.02 = \$1272.48. Ans.

22. Draft for \$866.65 at 3 months; rate of discount 5%; exchange $\frac{1}{3}\%$.

Exchange $= \frac{1}{8}\%$ of \$900 = \$1.13.

Total discount = \$11.19 + \$1.13 = \$12.32.

Proceeds = \$866.65 - \$12.32 = \$854.33. Ans.

Exercise 125. Page 277.

1. Find the present worth of \$500 due in 11 mo., if money is worth 5%.

$$\$\frac{500}{1.045\frac{5}{8}} = \$\frac{3000}{6.275} = \$478.09$$
. Ans.

$$\begin{array}{r} 478.08 \\ 6275)3000000. \\ \underline{25100} \\ 49000 \\ \underline{43925} \\ \overline{50750} \\ \underline{50200} \\ \underline{55000} \\ \underline{4800} \end{array}$$

2. Find the present worth and discount of \$3334.62 due in 2 yr., if money is worth 4½%.

Amount of \$1 for 2 yr. at $4\frac{1}{4}$ % is \$1.09.

$$\$\frac{3334.62}{1.09} = \$3059.28$$
. Ans.

3. Find the present worth and discount of \$4261.33 due in 1 yr. 6 mo., if money is worth 6%.

Amount of \$1 for 1 yr. 6 mo. at 6% is \$1.09.

$$\$\frac{4261.33}{1.09} = \$3909.48$$
. Ans.

4. Find the present worth and discount of \$2416.50 due in 7 mo., if money is worth 5%.

$$\begin{array}{r}
 7 \text{ mo.} \\
 \hline
 8 0.035 \\
 \hline
 0.005\frac{5}{8} \\
 \hline
 $0.029\frac{1}{8}
\end{array}$$

$$\$ \frac{2416.50}{1.029\frac{1}{8}} = \$ \frac{14499}{6.175} = \$ 2348.02.$$

$$2348.01$$

$$6175)14499000.$$

5. Find the present worth of \$678.40 due in 16 mo., if money is worth $4\frac{1}{4}$ %.

$$\begin{array}{c}
16 \text{ mo.} \\
4 \boxed{\$0.08} \\
0.02 \\
\$0.06
\end{array}$$

$$\begin{array}{c}
678.40 \\
1.06
\end{array} = \$640. \text{ Ans.} \\
640 \\
106) 67840 \\
636 \\
\hline
424 \\
424 \\
\hline
0
\end{array}$$

6. Find the present worth and discount of \$574.17 due in 2 yr. 3 mo., if money is worth 5½%.

$$\frac{2 \text{ yr.}}{\$0.12} \frac{3 \text{ mo.}}{0.015}$$

$$\frac{0.015}{\$0.135}$$

$$\frac{0.015}{\$0.12}$$

$$\$\frac{574.17}{1.12} = \$512.65. \text{ Ans.}$$

$$\frac{512.65}{112)57417.}$$

$$\frac{560}{141}$$

$$\frac{112}{297}$$

224

730

672

580

560

20

8 574.17

512.65

801.52 Ans.

7. Find the present worth and discount of \$625.13 due in 8 mo., if money is worth 4%.

8. Find the present worth and discount of \$715.20 due in 1 yr. 4 mo., if money is worth 3½%.

Exercise 126. Page 278.

1. Find the exact interest at 1 67, on \$652.74 for 250 days.

6 230	\$ 0.69274	8 25.56416
413	413	\$ 0.2%64
	461824	0.09621
	69:7274	0.00!#52
	277098	0.00096
	\$ 28.894163	8 0.39543
		\$ 28.4 6873
		28.47. Ans.

2. Find the exact interest at 6 % on \$ 1472.38 from Jan. 7, 1897 to Oct. 4, 1897.

24	\$ 1.47238	\$ 66.2571
28	45	8 0.6625
31	736190	0.2208
30	588952	0.0220
31	8 66.25710	0.0022
30	400.20110	\$ 0.9075
31 31		
30		\$ 65.3496
4		\$65.35. Ans.
6 270		
45		

3. Find the exact interest at 6% on \$1247.75 from Mar. 4, 1897 to Dec. 22, 1897.

27	\$ 1.24775	\$ 60.93179
30	48}	\$ 0.60931
31	1039791	0.20310
30	998200	0.02031
31	499100	0.00203
31	\$ 60.931794	\$ 0.83475
30	V 00.00110 g	
31 30		\$60.09704
22		60.10. Ans
6 293		50.10. AAS
483		

4. Find the exact interest at 6% on \$1898.48 from Feb. 26, 1897 to Aug. 12, 1899.

2	\$ 1.89848	\$ 52.84102
31	275	\$ 0.52841
30	158206	0.17613
31	1328936	0.01761
30	379696	0.00176
31 12	\$ 52.84102}	8 0.72391
6 167 27 §		\$ 52.11711
2 y	r.	1898.48
8 0. :	_ 12	0.12
~ • • • • • • • • • • • • • • • • • • •		379696
		189848
	8	227.8176
	8	227.82

52.12

\$279.94 Ans.

Exercise 127. Page 279.

1. Find the amount at annual interest of \$1247.75 for 3 yr. 5 mo. 10 dy., at 6%.

3 yr		5 mo.	10 dy.	\$ 1247.75 0.20 ‡
\$ 0.1 0.0		0.025	0.0013	83183 1 2495500
0.0	013			\$ 257.8683 }
\$ 0.2	063			\$ 1247.75 0.06
yr.	mo.	dy.		\$74.8650
2	5	10		\$ 7 4 .87
1,	5	10		0.26
	5	10		44922
4	4	- 		14974
-	*		•	\$ 19.4662
4 yr		4 mo.		• 8 257.87
80.2	A	0.02		19.47
0.0		0.02		\$ 277.34
	4			1247.75
\$ 0.2	6			\$ 1525.09 Ans.

2. Find the interest due on \$987.25 in 4 yr. 9 mo. 6 dy., interest at 4%, payable annually.

4 yr	. 9 mo.	в dy.	\$ 987.25 0.286
8 0.24		0.001	592350
0.0	01		789800 197450
\$ 0.28 yr.	mo. dy	·•	3 \$ 282.35350 94.1178
3 2	9 6		\$ 188.2357
1	9 6 9 6		\$ 987.25 0.04
9	0 24	•	\$ 39.4900
9 yr			\$ 39.49 0.544
8 0.5 0.0			15796 15796
\$ 0.5	44 8 188	2 94	19745
	-	1.32	3 \$ 21.48256 7.16085
	\$ 202	2.56 Ans.	§ 14.32171

3. Find the interest due on \$742.60 in 5 yr. 11 mo. 27 dy., interest at 4½%, payable annually.

£	11	07 4	A 740 00
5 yr.	11 mo.	27 dy.	\$ 742.60 0.3505
\$ 0.30	0.055	0.0045	0.3595
0.055			371300
0.0048	5		668340
	-		371300
\$ 0.3595	•		222780
		d-	4 8 266.964700
yr.	mo.	dy.	66.7412
4	11	27	\$ 200.2235
3	11	27	•
2	11	27	\$ 742.60
1	11	27	0.045
•	- -		371300
	11	27	297040
14	11	15	\$ 33.41700
14 yr.	11 mo.	15 dy.	8 33. 42
8 0.84	0.055	0.0025	0.8975
•	0.000	0.0020	16710
0.055	_		23394
0.002	5		30078
\$ 0.8978	5		26736
	\$ 20	00.22	4 29.994450
	ź	22.50	7.49861
		22.72 Ans.	<u> </u>

4. Find the interest due May 19, 1898, on a note dated Dec. 26, 1894, for \$1224.60, with interest payable annually, at 5%, if no interest has been paid.

yr.	mo.	dy.	\$ 1224.60
1898	5	19	0.203
1894	12	<u> 26</u>	100050
3	4	23	102050
_	_		367380
3 yr.	4 mo.	23 dy.	244920
\$ 0.18	0.02	0.003 §	6 \$249.61430
0.02 0.003	2.5		41.6024
\$0.208	_X_		\$ 208.0119
yr.	mo.	dy.	
2	4	23	\$ 1224.60
1	4	23	0.05
	4	23	0.03
4	2	9	\$ 61.2300

4 yr.	2 mo.	9 dy.	\$61.23
80.24	0.01	0.0015	0.2515
0.01			30615
0.0015			6123
8 0.2515	•		30615
6 0.7010	A 00	0 01	12246
	-	8.01	6 \$ 15.399345
		2.83 ——	2.56656
	\$ 22	0.84 Ans.	\$ 12.83278

5. Find the amount due May 27, 1898, on a note dated Jan. 4, 1896, for \$215.50, with interest payable annually at 5½%, if no interest has been paid.

6. Find the amount due Jan. 16, 1897, on a note dated Jan. 8, 1895, for \$3115.20, with interest payable annually at 5%, if no interest has been paid.

yr. mo. dy.	\$ 3115.20
1897 1 16	0.121
1895 1 8	103840
2 0 8	311520
	623040
2 yr. 8 dy.	
\$ 0.12 0.001 1	311520
0.001	6 \$377.97760
\$0.121 1	62.9963
•	\$ 31 4 .9813
yr. mo. dy.	\$ 3115. 20
1 0 8 8	0.05
1 0 16	\$ 155.7600
1 yr. 16 dy.	\$ 155.76
\$0.06 0.0023	$0.062\frac{3}{3}$
0.0023	10384
\$0.062 ₃	31152
	93456
	6 \$9.76096
	1.62682
	\$8.13414
	0 014 0 0
	\$ 31 4. 98
	8.13
	\$ 323.11
	3115.20
	\$3438.31 Ans.



TEACHERS' EDITION.

Exercise 128. Page 280.

1. Find the amount of \$356 25 for 4 yr., at 5 % compound interest.

8 356.25 0.05**\$17.6125** 356,25 8 374.06 0.05**8** 18,7030 374.06 \$ 392.76 0.05**8** 19.6380 892.76 \$412.40 0.05**8** 20.6200 412.40 \$433.02 Ans.

2. Find the amount of \$637.50 for 2 yr. 6 mo., at 4% compound interest.

6 mo. at 4 % \$ 0.02 \$ 13.7904 689.52 \$ 703.31 Ans. 3. Find the compound interest on \$800 for 3 yr. 9 mo., at 6%.

8 800. 0.08**\$48.** JUHE **\$848.** 0.06\$ 50.88 **648.** \$898,88 0.068 53.9328 898.68 \$ 952.81 9 mo. 0.045\$0.045 476405 381124 \$42.87645 952.81 995.69 800. \$ 195.69 Ans.

4. Find the compound interest on \$89.35 for 4 yr. 9 mo., at 5%.

_	
\$39.3 5	
0.05	
\$ 1.9675	
39.35	
\$ 41.32 0.05	9 mo. at 5 %.
\$ 2,0660	\$ 0.0376
_41.32	\$47.84
43.39	0.0375
0.06	23920
\$2.1695	33488
43.39	14852
\$45.58	\$1.794000
0.05	47.84
\$ 2.2780	49.63
45.56	89.35
47.84	\$ 10.28 Ans

5. Find the compound interest on \$300 for 2 yr., at 4%, interest being compounded semi-annually.

The interest is 2% semi-annually.

\$ 300 0.02
\$ 6.
300.
\$ 306.
0.02
\$ 6.12
306.
\$ 312.12
0.02
6.2424
312.12
\$ 318.36
0.02
\$ 6.3672
318.36
324.73
300.
\$ 24.73 Ans.

6. Find the compound interest on \$525 for 1 yr. 6 mo., at 5%, interest being compounded quarterly.

The interest is 11% quarterly.

```
$ 525.
                        0.0125
                           2625
                          1050
                         525
                       86.5625
                      525.
                     $ 531.56
                      0.0125
                      265780
                     106312
                     53156
                  86.644500
                  531.56
                 $ 538.20
                  0.0125
                  269100
                 107640
                 53820
              8 6.727500
              538.20
            $ 544.93
              0.0125
              272465
             108986
             54493
          8 6.811625
          544.93
        $ 551.74
          0.0125
         275870
        110348
        55174
      8 6.896750
     551.74
    $ 558.64
     0.0125
     279320
    111728
    55884
  $ 6.983000
 558.64
8 565.62
 525.
 $40.62 Ans.
```

7. Find the compound interest on \$10,000 for 6 mo., at 6 %, interest being compounded monthly.

The interest is ½ % monthly.

```
$ 10000.
                        0.005
                     $ 50.000
                    10000.
                  $ 10050.
                    0.005
                 $ 50.250
               10050.
              $ 10100.25
                   0.005
              $ 50.50125
            10100.25
          $ 10150.75
               0.005
          $ 50.75375
        10150.75
       $ 10201.50
            0.005
       $ 51.00750
     10201.50
   $ 10252.51
        0.005
   $ 51.26255
 10252.51
$ 10303.77
 10000.
  $ 303.77 Ans.
```

Exercise 129. Page 282.

1. A note of \$618.75, dated Apr. 17, 1897, payable on demand, bears the following endorsements: June 5, \$126.50; Aug. 20, \$137.25; Nov. 17, \$210. What is due Jan. 1, 1898, reckoning interest at 6%?

yr.	mo.	dy.	yr.	mo.	dy.	yr.	mo.	dy.	yr.	mo.	dy.
1898	1	1	1898	1	1	1898	1	1	1898	1	1
1897	4	17	1897	6	5	1897	8	20	1897	11	17
	8	14		6	26		4	11		1	14
8 mo.	14	dy.	6 mo.	26	dy.	4 mo.	_11	dy.	1 mo	. 14	dy.
\$0.04	0.0	0021	\$0.03	0.0	011	\$ 0.02	0.0	0015	\$ 0.00	5 0.	0021
0.00	21	•	0.004	41	•	0.00	18	•	0.00	$2\frac{1}{4}$	
\$ 0.04	121		\$ 0.03-	4 }		\$ 0.02	14		\$0.00	\$ 17	

\$ 618.75	\$ 126.50	\$ 137.25	\$ 2 10.
$0.042\frac{1}{8}$	0.034	0.0214	0.0071
20625	42163	114371	70
123750	50600	13725	1470
247500	37950	27450	\$ 1.540
\$ 26.19375	\$ 4.34316 }	\$ 2.99662 }	210.
618.75	126.50	137.25	\$ 211.54
\$ 644.94	\$ 130.84	\$ 140.25	
	\$ 130.84	\$ 644.94	
	140.25	482.63	
	211.54	\$ 162.31 Ans.	
	\$482.63		

2. A note of \$1000, dated Apr. 1, 1897, payable on demand, with interest at 5%, bears the following endorsements: May 6, \$200; July 5, \$225.37; Oct. 18, \$322. What is due Jan. 1, 1898?

yr. mo. dy	y. yr. mo. dy.	yr. mo. dy.	yr. mo. dy.
1898 1 1	1898 1 1	1898 1 1	1898 1 1
1897 4 1	1897 5 6	1897 7 5	1897 10 18
9 (5 26	2 13
9 mo.	7 mo. 25 dy.	5 mo. 26 dy.	2 mo. 13 dy.
\$ 0.045	\$ 0.035 0.0041	\$0.025 0.004\frac{1}{3}	\$0.01 0.002 1
	$0.004\frac{1}{6}$	0.004	$0.002\frac{1}{6}$
	\$ 0.039}	\$ 0.029 1	\$ 0.012 1
\$0.045	\$ 0.0391	\$ 22 5.37	\$ 32 2.
1000	200	$0.029\frac{1}{3}$	$0.012\frac{1}{6}$
6 \$ 45.000	331	75121	533
7.50	7800	202833	644
\$37.50	6 8 7.8331	45074	322
1000.	1.305	6 \$6.61085}	6 8 3.917
\$ 1037.50	\$ 6.528	1.1018	0.653
	200.	\$ 5.5090	\$ 3.264
	\$ 206.53	225.37	322.
		\$ 230.88	\$ 325.26
	\$ 206.53	\$ 103 7.5 0	
	230.88	762.67	
	325.26	\$ 274.83 Ans	3.
	8 762.67		

3. A note of \$835.25, dated July 1, 1897, payable on demand, with interest at $4\frac{1}{2}$ %, bears the following endorsements: Aug. 20, \$157.50; Sept. 21, \$180.25; Oct. 5, \$200; Dec. 1, \$80. What is due Jan. 1, 1898?

4. A note of \$1247.50, dated Mar. 10, 1897, payable on demand, with interest at 5%, has the following endorsements: \$350.40, Apr. 14, 1897; \$212.85, June 16, 1897; \$316.45, Aug. 25, 1898. What is due Oct. 18, 1897?

\$ 1247.50	\$ 350.40	\$212.85	\$ 316.45
$0.036\frac{1}{4}$	0.0304	$0.020\frac{1}{4}$	0.0085
415831	23360	7095	26370
748500	1051200	425700	25 3160
374250	6 3 10.74560	6 \$ 4.32795	6 \$2.79530}
6 \$45.325831	1.7909	0.72132	0.4659
7.5543	\$8.9547	\$ 3.60663	\$2.3294
\$37.7715	350.40	212.85	316.45
1247.50	\$ 359.35	\$ 216.46	\$318.78
\$ 1285.27	-		
	\$ 359.35	\$ 1285.27	
	216.46	<u>894.59</u>	
	3 18.78	\$390.68 Ans.	
	8 894.59		

5. A note of \$1648.25, dated Jan. 22, 1897, payable on demand, with interest at 5%, has the following endorsements: \$212.60, Mar. 1, 1897; \$168.40, May 26, 1897; \$244.40, Aug. 4, 1897; \$744.80, Oct. 1, 1897. What is due Jan. 22, 1898?

yr. mo. dy.	yr. mo. dy	yr. mo. dy.	yr. mo. dy.	yr. mo. dy.
1898 1 22	1898 1 22	1898 1 22	1898 1 22	1898 1 22
1897 1 22	1897 3 1	1897 5 26	1897 8 4	1897 10 1
1 0 0	10 21	7 26	5 18	3 21
1 yr. 1	l 0 mo. 21 dv.	7 mo. 26 dy.	5 mo. 18 dy.	3 mo. 21 dy.
	\$ 0.05 0.0035	\$0.035 0.004	\$0.025 0.003	\$0.015 0.0035
_	0.0035	0.004	0.003	0.0035
•	0.0535	\$0.039 }	\$0.028	\$ 0.0185
\$ 1648.25	\$212.6 0	\$ 168.40	\$244.40	\$ 744.80
0.06	0.0535	0.0391	0.028	0.0185
6 \$98.8950	106300	5613 1	195520	372400
16.4825	63780	151560	48880	595840
\$82.4125	106300	50520	6 \$6.84320	7 448 0
1648.25	6 \$11.374100	6 \$6.62373}	1.1405	6 \$ 13.778800
\$ 1730.66	1.8957	1.10395	\$5.7027	2.2965
	\$9.4784	\$5.51978	244.40	\$11.4823
	212.60	168.40	\$250.10	744.80
	\$ 222.08	\$ 173.92		\$756.28
	\$ 222.		\$ 1730.66	
	173.9		1402.38	
	250.]	_	\$328.28 Ans.	1
	<u>758.9</u>	<u> </u>		

\$ 1402.38

Exercise 130. Page 284.

1. A note of \$2000, dated Jan. 22, 1896, and drawing interest at 6%, had the following endorsements: May 20, 1896, \$100; July 20, 1896, \$325; Nov. 2, 1896, \$20; Dec. 23, 1896, \$125. Find the balance due Mar. 1, 1897.

yr.	mo.	d y .	\$ 0.019 }
1896	5	20	2000
1896	1	22	13331
	3	28	38000
		$0.019\frac{2}{8}$	\$ 39.333\\\2000.
yr.	mo.	dy.	\$ 2039.33
1896	7	20	100.
1896	5	<u>20</u>	\$ 1939.33
	2	0	0.01
		0.01	\$ 19.3933 1939.33
yr.	mo.	dy.	\$ 1958.72
1896	11	2	325.
1896	7	20	\$ 1633.72
	3	12	0.017
		0.017	1143604
		0.041	163372
			\$ 27.77324

Payment less than interest.

2. A note of \$1662.50, dated Jan. 15, 1896, and drawing interest at 5½%, had the following endorsements: Apr. 30, 1896, \$25; June 24, 1896, \$25; Sept. 2, 1896, \$625; Jan. 30, 1897, \$700. Find the balance due May 12, 1897.

yr. 1896	mo. 4	d y. 30	\$ 1662.50 0.0175
1896	1	15	831250
	3	15	1163750
	0.0175		166250
	· ·	.0110	12 \$ 29.093750 2.42448
			\$26.66927

Payment less than interest.

3. A note of \$4560, dated Jan. 22, 1896, and drawing interest at 5%, had the following endorsements: Jan. 11, 1897, \$2000; Aug. 31, 1897, \$500; Jan. 15, 1898, \$1200; Mar. 4, 1898, \$860. Find the balance due June 15, 1898.

yr.	mo.	dy.	\$ 4560.	
1897	1	11	0.058	
<u> 1896 </u>	1	22	760	
	11	19	36480	
		$0.058\frac{1}{6}$	22800	
		313336	. 6 \$ 265.240	
			44.207	
			\$ 221.033	
		_	4560.	
yr.	mo.	dy.	\$ 4781.03	
1897	8	31	2000.	
1897	<u>_</u>	11	\$ 2781.03	
	7	20	$0.038\frac{1}{4}$	
		0.0381	92701	
		•	2224824	
			834309_	-
			6 \$ 106.60615	
		_	17.7677	
yr.	mo.	dy.	\$ 88.8384	
1898	1	15	2781.03	
1897	8	31	\$ 2869.87	
	4	14	500.	
		$0.022\frac{1}{4}$	\$ 2369.87	
		•	0.022	
			789953	
			473974	
		_	473974	
yr.	mo.	dy.	6 \$ 52.92709 {	\$ 8.26
1898	3	4	8.82118	1213.98
1898	1	15	\$ 44.10591	\$ 1222.24
	1	19	2369.87	860.
		0.0081	\$ 2413.98	\$ 362.24
		•	1200	0.0165
			\$ 1213.98	30186 2
			0.008	217344
		_	20233	36224
yr.	mo.	dy.	<u>.971184</u>	6 8 6.097703
1898	6	15	6 \$ 9.91417	1.0163
1898	3	4	1.65236	\$ 5.0814
	3	11	8 8.26181	<u>362.24</u>
		0.016	•	snA 28.706 \$

4. A note of \$785.50, dated Jan. 30, 1896, and drawing interest at 5%, had the following endorsements: July 17, 1896, \$100; Jan. 29, 1897, \$100; Dec. 31, 1897, \$20; Mar. 16, 1898, \$300; June 18, 1898, \$50. Find the balance due July 23, 1898.

yr.	mo.	dy.	\$ 785.50	
1896	7	17	0.0275	
1896	1	30	654581	
	5	17	549850 ·	
	-	.027	157100	
		.0216	6 \$ 21.863081	
		•	3.64385	\$ 18.77
yr.	mo.	dy.	8 18.21923	703.72
1897	1	29	785.50	
1896	7	17		\$ 722.49
	6		\$ 803.72	100.
	U	12	100.	\$622.49
		0.032	\$ 703.72	0.0551
			0.032	207494
yr.	mo.	\mathbf{dy} .	140744	311245
1897	12	3 1	211116	311245
1897	1	29	6 \$ 22.51904	6 8 34.44444
	11	2	[7	
	**	~	3.753	5.74074
	0	.055}	\$ 18.766	\$28.7037

Payment less than interest.

yr.	mo.	dу.	8 622.49	
1898	3	16	0.0125	
1897	12	31		
1001			311245	
	2	15	124498	
	0	.0125	62249	
	U	.0120	6 8 7.781125	
			1.296854	
		3	\$ 6.484271	\$ 4.31
yr.	mo.	dy.		337.68
1898	6	18	28.7037	
1898	3	16	622.49	\$341.99
	3	2	8 657.68	50
	_		\$20 + \$300 = 320.	\$ 2 91.99
	0	.015}	8 337.68	0.005
			0.0151	243321
			11256	145995
yr.	mo.	dy.	168840	6 \$ 1.703271
1898	7	23	33768	0.28388
1898	6	18		
1000			6 \$ 5.17776	\$ 1.41939
	1	5	0.86296	291.99
•	0	.005	\$4.3148	\$293.41 Ans.

5. A note of \$300.25, dated Aug. 4, 1896, and drawing interest at 4½%, had the following endorsements: Oct. 14, 1896, \$100; July 21, 1897, \$100; Oct. 11, 1897, \$50; Jan. 19, 1898, \$50. Find the amount due July 22, 1898.

yr. 1896 1896	mo. 10 8	dy. 14 4	$ \begin{array}{r} 300.25 \\ \hline 0.0113 \\ \hline 200163 \end{array} $	
	2	10 0.011 3	30025 30025 4 \$ 3.50291	
			0.87573 \$ 2.62718 300.25	
yr. 1897 1896	mo. 7 10	dy. 21 14	\$ 302.88 100. \$ 202.88	
	9	7 0.046 1	$ \begin{array}{r} 0.046 \frac{1}{8} \\ \hline 3381 \frac{1}{8} \\ 121728 \end{array} $	
			81152 4 8 9.36629 1 2.34157	
yr. 1897 1897	mo. 10 7	dy. 11 21	\$ 7.02472 202.88	
	2	20 0.013 1	\$ 209.90 100. \$ 109.90	
		3	0.013½ 3663½ 32970 10990	
yr. 1898 1897	mo. 1 10	dy. 19 11	4 8 1.465331 0.36633 8 1.09900	\$ 0.75 6 1.
	3	8 0.016]	109.90 \$ 111. 50.	\$61.75 50. \$11.75
		_	$ \begin{array}{r} \hline 861. \\ 0.016 \\ \hline 20 \\ \end{array} $	0.0305 5875 3525
yr. 1898 1898	mo. 7 1 6	dy. 22 19 3	366 61 4 \$ 0.9961	4 0.358375 0.089594 8 0.268781
		.0305	0.249 ♣ 0.747	11.75 \$12.02 Ans.

1000	4	12	9836
	5	10	29 508
		0.0264	6 \$ 39.344
		310208	6.557
			\$ 32.787
yr.	mo.	dy.	1475.40
1896	12	26	\$ 1508.19
1896	7	22	370.
	5	4	\$ 1138.19
•	(0.0253	0.0252
	`	0.0208	758791
			569095
yr.	mo.	dy.	227638
1897	8	24	6 8 29.213541
1896	12	26	4.86892
	7	28	\$ 24.34462
	0	.0394	1138.19
	J		\$ 1162.53
			426.50
yr.	mo.	dy.	\$ 736.03
1897 1897	10	6	0.0394
1001	8	<u>24</u>	490683
	1	12	662427°
	0	0.007	220809 6 8 29 195852
			A =0.100004
			4.86597
yr.	nio.	dy.	\$ 24.32988
1898	4	1.4	736.03

i

7. A note of \$5762.45, dated Jan. 2, 1896, and drawing interest at 5%, had the following endorsements: May 17, 1896, \$500; Oct. 12, 1896, \$750; Feb. 4, 1897, \$1000; Aug. 25, 1897, \$1250; Mar. 1, 1898, \$1500; June 15, 1898, \$1050. Find the balance due Oct. 2, 1898.

yr.	mo.	dy.	8 5762.45	
1896	5	17	0.0225	
1896	1	2	2881225	
	4	15	1152490	
		225	1152490	
	U. U		6 8 129.655125	
yr.	mo.	dy.	21.6092	\$ 106.15
1896	10	12	\$ 108.0459	3802.22
1896	5	17	5762.45	\$ 3908.37
	4	25	8 5870.50	1250.
		241	500.	\$ 2658.37
	0.0	218	8 5370.50	0.031
yr.	mo.	dy.	0.0241	265837
1897	2	4	895081	797511
1896	10	12	2148200	6 82.40947
	3	22	1074100	13.73491
	0.0	184	6 8 129.787081	\$ 68.67456
	0.0	3	21.63118	2658.37
yr.	mo.	dy.	\$ 108.15590	8 2727.04
1897	8	25	5370. 50	1500.
1897	2_	4	\$ 5478.66	\$ 1227.04
	8	21	750.	0.0171
	0.0	335	\$ 4728.66	40901
			0.0182	858928 3
yr.	mo.	dy.	315244	122704
1898	3	1	3782928	6 21.208691
1897	8	25	4 72866	3.54478
	6	6	6 88.26832	\$ 17.72391
	0.	.031	14.71139	1227.04
			8 73.55693	8 1244.76
yr.	mo.	dy.	4728.66	1050.
1898	6	15	8 4802.22	8 194.76
1898	3	1	1000.	0.017
	3	14	\$ 3802.22	16230
	0.0	171	0.0335	136332
		•	1901110	19476
yr.	mo.	dy.	1140666	6 \$ 3.47322
1898	10	2	1140666	0.57887
1898	6	<u>15</u>	6 \$ 127.374370	\$ 2.89435
	3	17	21.22906	194.76
	0.0	175	\$ 106.14531	§ 197.85 Ans.

Exercise 131. Page 287.

1. Find, by the New Hampshire Rule, and also by the Vermont Rule, the amount due Sept. 22, 1896, on a note for \$1750, dated June 6, 1892, with interest annually at 6%, which has the following endorsements: Aug. 12, 1893, \$300; Dec. 23, 1893, \$200; Jan. 15, 1895, \$50; Apr. 23, 1896, \$800.

(By the New Hampshire Rule.)

Principal,		\$ 1750.00		
1st annual interest,		\$ 105.00		
Int. on 1st annual interest for 1	yr.,			\$6.30
2d annual interest,			105.00	
		\$1750.00	\$210.00	\$ 6.30
Payment Aug. 12, 1893,	\$ 300.00			•
Int. on payment June 6, 1894,	14.70			
Payment Dec. 23, 1893,	200.00			
Int. on payment June 6, 1894,	5.43			
Amt. of payments June 6, 1894,	\$ 520.13 =	= \$ 303.83	+\$210.00-	+\$6.30
Principal June 6, 1894,		\$1446.17		
3d annual interest,			\$86.77	
		\$ 1532.94		
As payment Jan. 15, 1895, does	not excee	ed		
the annual interest, deduct pa	yment witl	h-		
out interest,	-	50.00		
Principal June 6, 1895,		\$ 1482.94		
4th annual interest,		•	\$88.98	
Payment Apr. 23, 1896,	\$800.00		•	
Int. on payment June 6, 1896,	5.73			
Amt. of payment June 6, 1896,		\$716.7 5-	+ \$88.98	
Principal June 6, 1896,	• • • • • • • • • • • • • • • • • • • •	\$ 766.19	, , , , , , , , , , , , , , , , , , , ,	
5th annual interest,		13.54		
Amt. due Sept. 22, 1896,		\$ 779.73	Ans.	
	¥			

Ans.

(By the Vermont Rule.)

Principal June 6, 1894,	\$ 1446.17		
3d annual interest,	\$ 86.77		
Payment Jan. 15, 1895,	\$ 50.00		
Int. on payment June 6, 1895,	1.18		
Amt. of payment June 6, 1895,	\$51.18= \$51.18		
	\$1446.17 + \$35.59		
Principal June 6, 1895,	\$ 1481.76		
4th annual interest,	\$88.91		
Payment Apr. 23, 1896,	\$ 800.00		
Int. on payment June 6, 1896,	5.73		
Amt. of payment June 6, 1896,	\$805.73 = \$716.82 + \$88.91		
Principal June 6, 1896,	\$ 764.94		
5th annual interest,	13.51		
Amt. due Sept. 22, 1896,	\$ 778.45 Ans.		

2. Find by the Connecticut Rule the amount due Sept. 22, 1896, on a note for \$1500, dated Aug. 9, 1892, with interest annually at 6%, which has the following endorsements: Mar. 17, 1893, \$250; Apr. 19, 1894, \$50; Sept. 21, 1895, \$500; June 26, 1896, \$600.

Principal,	\$ 1500.00
Int. on principal to Aug. 9, 1893,	90.00
Amt. of principal Aug. 9, 1893,	\$ 1590.00
Payment Mar. 17, 1893, \$250.00	••
Int. on payment to Aug. 9, 1893, 5.95	2
Amt. of payment Aug. 9, 1893,	\$ 255.92
New principal Aug. 9, 1893,	\$ 1334.08
Int. on principal to Aug. 9, 1894,	80.04
Amt. of principal Aug. 9, 1894,	\$ 1414.12
Payment Apr. 19, 1894 (less than interest),	50.00
New principal Aug. 9, 1894,	\$ 1364.12
Int. on principal Sept. 21, 1895,	91.40
Amt. of principal Sept. 21, 1895,	\$ 1455.52
Payment Sept. 21, 1895,	500.00
New principal Sept. 21, 1895,	\$ 955.52
Int. on principal to June 26, 1896,	43.79
Amt. of principal June 26, 1896,	\$ 999.31
Payment June 26, 1896,	600.00
New principal June 26, 1896,	\$ 399.31
Int. on principal to Sept. 22, 1896,	5.72
Amt. due Sept. 22, 1896,	8 405.03

Exercise 132. Page 290.

1. What is the cost of 25 shares of Boston and Maine R.R. stock at 167, brokerage \(\frac{1}{4}\)?

$$$167 + $0.25 = $167.25.$$

$$$167.25$$

$$25$$

$$83625$$

$$33450$$

$$$4181.25 Ans.$$

2. How many shares of Illinois Central R.R. stock at 101% can be bought for \$20,400, brokerage %?

$$\$ 101\frac{7}{8} + \$\frac{1}{8} = \$ 102.$$

$$200 Ans.$$

$$102)20400$$

$$\frac{204}{00}$$

3. What is the annual income from 150 shares of Lake Shore and Michigan Southern Ry. stock that pays an annual dividend of 6%?

Each share pays \$6 dividend. $150 \times $6 = 900 . Ans.

- 4. How much must be invested in 6% stock at 107 to yield an annual income of \$240, brokerage ½?
 - \$6 is the dividend from 1 share.
- \$240 dividend requires $^{2}2^{0}=40$ shares.

$$$107 + $0.25 = $107.25.$$

$$$107.25$$

$$\frac{40}{$4290.00} Ans.$$

5. What per cent does the investment yield, if Lake Shore and Michigan Southern Ry. stock is bought at 170? The stock pays 6% dividend; no brokerage reckoned.

Each \$170 invested pays \$6 dividend.

6. Find the cost of 350 shares of Chicago, Milwaukee and St. Paul Ry. stock at 934, brokerage 4.

$$\$93\frac{1}{8} + \$\frac{1}{8} = \$93\frac{1}{8} = \$93.50$$

$$\frac{350}{467500}$$

$$\frac{2805}{\$32725.00} Ans.$$

7. Find the cost of 165 shares of Michigan Central R.R. stock at 105³, brokerage ¹/₃.

\$
$$105\frac{3}{4} + \frac{3}{8} = \frac{3}{4} \cdot 105.875$$

\$ 105.875

\[\frac{165}{529375}
\]

\$ 635250

\[\frac{105875}{\$17469.375}
\]

\$ $17,469.38$. Ans.

8. Find the cost of 35 shares of Reading R.R. stock at 23\frac{1}{6}, brokerage \frac{1}{6}.

\$ 826.88. Ans.

9. What is the cost of 25 U. S. 4% registered 1925 bonds of \$1000 each, at $127\frac{1}{5}$, brokerage $\frac{1}{5}$? $$127\frac{1}{5} + $\frac{1}{5} = $127\frac{1}{5} = 127.25 . $10 \times $127.25 = 1272.50 . $25 \times $1272.50 = $31,812.50$. Ans.

10. What is the cost of 40 Northern Pacific R.R. 1st mortgage 6% registered bonds of \$1000 each, at 1197, brokerage 1?

$$\$119\frac{7}{8} + \$\frac{1}{8} = \$120.$$
 $10 \times \$120 = \$1200.$
 $40 \times \$1200 = \$48,000.$ Ans.

11. What per cent income does the investment of Example 10 yield?

Each \$120 invested yields an income of \$6.

12. What is the annual income received from the investment of Example 10?

Each bond yields 6% of \$1000 = \$60. $40 \times \$60 = \$2400.$ Ans.

13. What is the annual income from 200 shares of Chicago and Northwestern Ry. stock that pays an annual dividend of 5%?

Each share pays \$5 dividend.

$$200 \times $5 = $1000$$
. Ans.

14. What is the cost of the investment of Example 13 at 1227, brokerage 1?

$$\$122\frac{7}{8} + \$\frac{1}{8} = \$123.$$

 $200 \times \$123 = \$24,600.$ Ans.

15. What per cent income does the investment of Example 13 yield?

Each \$123 invested yields \$5 income.

16. How many shares of New York Central stock can be bought for \$4757.50 at $107\frac{7}{4}$, brokerage $\frac{1}{4}$? $$107\frac{7}{4} + $\frac{1}{4} = $108\frac{1}{4} = 108.125 .

18. What is the annual income from the investme Each bond yields 7% of \$500 = \$35.

$$12 \times $35 = $420$$
. Ans.

19. What sum of money must be invested in Nor 1st mortgage 6's at 119½ to produce an annual income age ½?

Each bond of \$1000 yields \$60 income.

\$2400 income requires $\frac{2400}{60} = 40$ bonds.

$$\$119\frac{1}{2} + \$\frac{1}{8} = \$119\frac{5}{8} = \$119.625.$$

Each bond costs $10 \times $119.625 = 1196.25 .

\$1196.25

40

\$47850.00 Ans.

20. What sum of money must be invested in Wal 5% bonds at 1074 to produce an annual.

21. What sum of money must be invested in Louisville and Nashville R.R. unified gold 4% bonds at 841 to produce an annual income of \$320, brokerage 1?

Each bond of \$1000 yields \$40 income.

\$320 income requires $\frac{$20}{40}$ = 8 bonds.

$$\$841 + \$1 = \$841 = \$84.50.$$

Each bond costs $10 \times $84.50 = 845 .

22. What sum of money must be invested in St. Louis and San Francisco Ry. general mortgage 5% bonds at 100½ to produce an annual income of \$600, brokerage ½?

Each bond of \$1000 yields \$50 income.

\$ 600 income requires $\frac{600}{50} = 12$ bonds.

$$\$ 100\frac{1}{4} + \$ \frac{1}{8} = \$ 100\frac{5}{8} = \$ 100.625.$$

Each bond costs $10 \times \$ 100.625 = \$ 1006.25$.

23. How many shares of Chicago and Northwestern Ry. stock can be bought for \$14,670 at 122\frac{1}{2}, brokerage \frac{1}{2}? What is the brokerage? If 5% dividends are paid, what per cent on his investment does the purchaser receive?

$$\$122\frac{1}{8} + \$\frac{1}{8} = \$122\frac{1}{4} = \$122.25.$$

120 shares. Ans.

Brokerage = $\frac{1}{4}$ % of $\frac{12,000}{4}$ = $\frac{15}{4}$. Ans.

Each \$122.25 invested yields \$5 dividend.

$$\begin{array}{r}
0.0408 \\
12225)500.00 \\
\underline{48900} \\
110000 \\
\underline{97800} \\
12200
\end{array}$$

24. How many shares of Michigan Central R.R. stock can be bought for \$16,940 at 105‡, brokerage ‡? What is the brokerage? If 4% dividends are paid, what per cent on his investment does the purchaser receive?

$$$105\frac{1}{4} + $\frac{1}{4} = $105\frac{7}{4} = $105.875.$$

160 shares. Ans.

Brokerage = $\frac{1}{2}$ % of \$16,000 = \$20. Ans.

Each \$ 105.875 invested yields \$4 dividend.

$$\begin{array}{r}
0.0377\\
105875)4000.00\\
\underline{317625}\\
823750\\
\underline{741125}\\
826250\\
\underline{741125}\\
85125
\end{array}$$

3.78 %. Ans.

25. What is the cost of 40 shares of Central R.R. of New Jersey stock at 927, brokerage 1? What is the brokerage? If 6% dividends are paid, what per cent on his investment does the purchaser receive?

$$\$92\frac{7}{8} + \$\frac{1}{4} = \$93\frac{1}{8} = \$93.125.$$

$$\frac{\$93.125}{40}$$

$$\frac{40}{\$3725.000}$$
Ans.

Brokerage = $\frac{1}{4}$ % of \$4000 = \$10. Ans.

Each \$93.125 invested yields \$6 dividend.

$$\begin{array}{r} 0.0644 \\ 93125 \overline{\smash{\big)}\,6000.00} \\ \underline{558750} \\ 412500 \\ \underline{372500} \\ 400000 \\ \underline{372500} \\ 27500 \end{array}$$

6.44 %. Ans.

TEACHERS' EDITION.

26. What is the cost of 250 shares of Pullman Palace Car Co. stock at 1711, brokerage 1? What is the brokerage? If 8% dividends are paid, what per cent on his investment does the purchaser receive?

$$$171\frac{1}{4} + $\frac{1}{8} = $171\frac{3}{8} = $171.375.$$

\$ 171.375 250 8568750 342750 \$ 42843.75 Ans.

Brokerage = $\frac{1}{6}$ % of \$25,000 = \$31.25. Ans.

Each \$171.375 invested yields \$8 dividend.

 $\begin{array}{r}
0.0468 \\
171375)8000.00 \\
\underline{685500} \\
1145000 \\
\underline{1028250} \\
1028250 \\
\underline{139250}$

4.67 %. Ans.

27. What per cent on his investment does a purchaser receive who buys New York, New Haven and Hartford R.R. stock at 1801, if annual dividends of 8% are declared?

Each \$ 180.50 invested yields \$ 8 dividend.

4.43% Ans.

Each \$107.25 invested yields \$4.50 income.

$$\begin{array}{r}
0.0419 \\
10725)450.00 \\
\underline{42900} \\
21000 \\
\underline{10725} \\
102750 \\
\underline{96525} \\
6225
\end{array}$$

29. When Mexican Central Ry. 1st mortgage 4% be at 62½, how much must be invested to produce an an \$200, brokerage ½? What per cent on his investme chaser receive?

Each bond of \$1000 yields \$40 income.

\$200 income requires $\frac{200}{40} = 5$ bonds.

$$\$62\frac{1}{4} + \$\frac{1}{4} = \$62\frac{1}{4} = \$62.75.$$

Each bond costs $10 \times $62.75 = 627.50 .

\$627.50 5 \$3137.50 Ans.

Each \$62.75 invested yields \$4 income.

0.0637

30. When West Shore R.R. 1st mortgage 4% bonds are selling at 1084, how much must be invested to produce an annual income of \$800, brokerage 1?

Each bond of \$1000 yields \$40 income.

\$800 income requires $\frac{$00}{40} = 20$ bonds.

$$\$ 108 \frac{1}{4} + \$ \frac{1}{8} = \$ 108 \frac{7}{8} = \$ 108.875.$$

Each bond costs $10 \times \$ 108.875 = \$ 1088.75$.

31. When New England Tel. and Tel. Co. 6% bonds are selling at 101; how much must be invested to produce an annual income of \$900, brokerage;

Each bond of \$1000 yields \$60 income.

\$ 900 income requires $\frac{900}{60} = 15$ bonds.

$$\$101\frac{1}{8} + \$\frac{1}{8} = \$101\frac{1}{4} = \$101.25.$$

Each bond costs $10 \times $101.25 = 1012.50 .

32. If a man buys a 6% bond at 120, what rate of interest does he receive on the money invested?

Each \$120 invested yields \$6 interest.

$$\begin{array}{r}
0.05 \\
120)6.00 \\
600
\end{array}$$

5 %. Ans.

33. If 3% bonds are at 88½, what rate per cent interest will a purchaser receive on his money?

Each \$88.50 invested yields \$3 interest.

S.390/a Ans.

34. If an 8% stock is at 150, what rate per cent interest will a purchaser receive on his money?

Each \$150 invested yields \$8 interest.

5.33 %. Ans.

35. If a 10% stock is at 175, what rate per cent interest will an investor receive on his money?

Each \$175 invested yields \$10 interest.

$$\begin{array}{r}
0.0571 \\
175)10.00 \\
\underline{875} \\
1250 \\
\underline{1225} \\
250 \\
\underline{175} \\
75
\end{array}$$

5.71%. Ans.

36. If a 4½% stock is at 85, what rate per cent interest will a purchaser receive on his money?

Each \$85 invested yields \$4.50 interest.

5.29 %. Ans.

37. If 7% bonds are at 114, what rate per cent interest will a purchaser receive on his money?

Each \$114 invested yields \$7 interest.

$$\begin{array}{r}
0.0614 \\
114)7.00 \\
\underline{684} \\
160 \\
\underline{114} \\
460 \\
\underline{456} \\
4
\end{array}$$

6.14%. Ans.

38. If 6% bonds are at 130, what rate per cent interest will a purchaser receive on his money?

Each \$130 invested yields \$6 interest.

$$\begin{array}{r}
0.0461 \\
130)6.00 \\
\underline{520} \\
800 \\
\underline{780} \\
200 \\
\underline{130} \\
70
\end{array}$$

4.62 %. Ans.

39. If \$8000 5% stocks are sold at 90 and the proceeds invested in 3½% stocks at 60, find the increase or decrease in income.

Income from 5% stock = 5% of \$8000 = \$400.

Proceeds from 5% stock = $80 \times $90 = 7200 .

\$0.60 is paid for \$1 of 3½% stock.

Therefore, \$7200 is paid for $\frac{$7200}{0.60}$ = \$12,000 of $3\frac{1}{2}$ % stock.

Income from $3\frac{1}{2}$ % stock = $3\frac{1}{2}$ % of \$12,000 = \$420.

\$420 - \$400 = \$20, increase in income. Ans.

40. If \$10,000 $3\frac{1}{2}$ % bonds are sold at 65, and the proceeds invested in 8% bonds at 130, find the increase or decrease in income.

Income from $3\frac{1}{2}\%$ bonds = $3\frac{1}{2}\%$ of \$10,000 = \$350.

Proceeds from $3\frac{1}{2}\%$ bonds = $100 \times $65 = 6500 .

\$1.30 is paid for \$1 of 8% bonds.

Therefore, \$6500 is paid for $\frac{$6500}{1.30}$ = \$5000 of 8% bonds.

Income from 8% bonds = 8% of \$5000 = \$400.

\$400 - \$350 = \$50, increase in income. Ans.

41. If \$8000 4½% stocks are sold at 70 and the proceeds invested in 10% stocks at 160, find the increase or decrease in income.

Income from $4\frac{1}{2}\%$ stock = $4\frac{1}{2}\%$ of \$8000 = \$360.

Proceeds from $4\frac{1}{2}\%$ stock = $80 \times $70 = 5600 .

\$1.60 is paid for \$1 of 10% stock.

Therefore, \$5600 is paid for $\frac{$5600}{1.60}$ = \$3500 of 10% stock.

Income from 10% stock = 10% of \$3500 = \$350.

\$360 - \$350 = \$10, decrease in income. Ans.

42. If \$6000 6% bonds are sold at 90, and the proceeds invested in 10% bonds at 135, find the increase or decrease in income.

Income from 6% bonds = 6% of \$6000 = \$360.

Proceeds from 6% bonds = $60 \times $90 = 5400 .

\$1.35 is paid for \$1 of 10 % bonds.

Therefore, \$5400 is paid for $\frac{$5400}{1.35}$ = \$4000 of 10% bonds.

Income from 10% bonds = 10% of \$4000 = \$400.

\$400 - \$360 = \$40, increase in income. Ans.

43. Find the rate of interest obtained by investing in a 5% bond at 124.

Each \$124 invested yields \$5 interest.

$$\begin{array}{r}
 0.0403 \\
 124)5.00 \\
 \underline{496} \\
 \hline
 400 \\
 \underline{872} \\
 \hline
 28
 \end{array}$$

4.03%. Ans.

44. What is the price of stock if \$7000 stock can be bought for \$5880?

\$7000 stock = 70 shares.

84. Ans.

45. Find the amount received for 100 mining shares issued at \$15 a share and sold at 2½ % discount.

0.0225	\$1 5.
15	0.3375
$\overline{1125}$	\$14.6625
225	
0.3375	\$1468.25 Ans.

46. How much 3½% stock must be sold at 75½ to buy \$5000 4% stock at 9½, brokerage ½ on each transaction?

1 share of 4% stock costs $$94\frac{3}{5} + $\frac{1}{5} = $94\frac{1}{2}$.

1 share of $3\frac{1}{4}$ % stock sells for \$75 $\frac{1}{4}$ - \$ $\frac{1}{4}$ = \$75.

Therefore, the amount of stock required

$$=\frac{94\frac{1}{1}\times\$5000}{75}=\frac{189}{2}\times\$\frac{5999}{75}=\$6300. \ Ans.$$

47. How much stock must be sold at $76\frac{1}{6}$ to raise a sum sufficient to discount a note for \$1075, due in 53 days, with grace, and discounted at $5\frac{1}{6}$ %?

The time of the note to run is 56 days.

The discount is the interest on \$1075 for 56 days at $5\frac{1}{2}\%$; or

$$\frac{11}{12} \times 9\frac{1}{12} \times \$1.075 = \$9.20.$$

The proceeds is \$1075 - \$9.20 = \$1065.80.

1 share of the stock sells for \$761.

Therefore, the number of shares of stock is $\frac{1065.80}{76.125} = 14$ shares; and the amount of the stock is $14 \times $100 = 1400 . Ans.

48. A broker bought five \$1000 bonds at 88½. At what price must he sell them to gain \$100, brokerage ½ on each transaction?

If the broker is to gain \$100 on the transaction, he must gain $\frac{1}{3}$ of \$100 = \$20 on each bond; that is, \$2 on each \$100 of the face value of the bonds. He must also pay $\frac{1}{3} + \frac{1}{3}$ for brokerage.

Therefore, the selling price must be $88\frac{1}{2} + 2 + \frac{1}{8} + \frac{1}{8} = 90\frac{3}{4}$. Ans.

49. If a broker buys bonds at 87%, at what price must be sell them to make 12½% profit, brokerage % on each transaction?

The price of the bonds is $87\frac{7}{8} + \frac{1}{8} = 88$.

$$88 + 12\frac{1}{2}\%$$
 of $88 = 88 + 11 = 99$.

The selling price of the bonds is, therefore, $99 + \frac{1}{2} = 99\frac{1}{2}$. Ans.

50. Which is the more profitable stock for investment, a 4% at 85 or a 3% at 63? a $3\frac{1}{2}$ % at $67\frac{1}{2}$ or a 4% at $81\frac{1}{2}$?

Each \$85 invested in the 4% stock yields \$4 interest; each \$63 in the 3% stock yields \$3 interest.

0.0470	0.0476
85)4.00	63)3.00
340	252
	480
600	441
595	390
	3 78
50	12

Therefore, the 4% stock yields 4.71% interest; and the 3%, 4.76%. Therefore, the 3% is the more profitable investment.

Each \$67.25 invested in the 3½% stock yields \$3.50 interest; each \$81.50 in the 4% stock yields \$4 interest.

$$\begin{array}{c|c}
0.0520 & 0.0490 \\
6725)350.00 & 815)40.00 \\
\underline{33625} & 3260 \\
\hline
13750 & 7400 \\
\underline{13450} & 7335 \\
\hline
3000 & 650
\end{array}$$

Therefore, the $3\frac{1}{2}$ % stock yields 5.20% interest; and the 4%, 4.91%. Therefore, the $3\frac{1}{2}$ % stock is the more profitable investment.

51. Find the price of a $4\frac{1}{2}$ % bond to be as profitable an investment as a $3\frac{1}{2}$ % bond at $88\frac{1}{2}$.

A $3\frac{1}{2}$ % bond at $88\frac{1}{2}$ yields $\frac{3\frac{1}{2}}{88\frac{1}{2}}$ of 100% interest.

The price of a $4\frac{1}{2}$ % bond to yield $\frac{3\frac{1}{2}}{88\frac{1}{2}}$ of 100% interest must be

$$4\frac{1}{2} \div \frac{3\frac{1}{4}}{88\frac{1}{4}} = \frac{9}{2} \times \frac{2}{7} \times \frac{177}{2} = \frac{1593}{14} = 113\frac{1}{14}$$
. Ans.

52. Find the price of a 5% bond to be as profitable an investment as a 3% bond at 89½.

A 3% bond at 89½ yields $\frac{3}{89½}$ of 100% interest.

The price of a 5% bond to yield $\frac{3}{89\frac{1}{2}}$ of 100% interest must be

$$5 \div \frac{3}{89\frac{1}{2}} = 5 \times \frac{1}{3} \times \frac{179}{2} = \frac{895}{6} = 149\frac{1}{6}$$
. Ans.

53. Find the price of a 3½% bond to be as profitable an investment as a 6% bond at par.

A 6% bond at par yields 6% interest.

The price of a 3½% bond to yield 6% interest must be

$$3\frac{1}{4} \div \frac{6}{100} = \frac{7}{2} \times \frac{\cancel{199}}{\cancel{6}} = \frac{175}{3} = 58\frac{1}{3}. \quad Ans.$$

54. Find the loss in buying \$80,000 worth of bonds at 91\{ and selling at 90, brokerage \{ \} on each transaction.

The cost for every \$ 100 of the bonds is $$91\frac{1}{2} + $\frac{1}{2} = $91\frac{1}{2}$.

The price to the seller for every \$100 of the bonds is

$$\$90 - \$\frac{1}{3} = \$89\frac{7}{3}$$
.

The loss on every \$ 100 of the bonds is $$91\frac{1}{4} - $89\frac{1}{8} = $1\frac{1}{8} = 1.875 .

55. Which is the better investment, a 5% stock at 137½ or a 3½% stock at 91½? What rate of interest will be received from each investment?

Each \$137.25 invested in the 5% stock yields \$5 interest; each \$91.50 in the 3½% stock yields \$3.50 interest.

0.0364	0.0382
13725)500.00	915)35.00
41175	2745
88250	7550
82350	7320
59000	2300
54900	1830
4100	470

Therefore, the 5% stock yields 3.64% interest; the $3\frac{1}{4}$ % stock yields 3.83%; and the $3\frac{1}{4}$ % stock is the better investment. Ans.

56. A person invests \$7370 in the purchase of a stock at 92. What will be his loss if he sells at 90, brokerage \(\frac{1}{4} \) on each transaction ?

The buying price is $92 + \frac{1}{8} = 92\frac{1}{8}$.

The number of shares is $\frac{7370}{921} = 80$.

The selling price is $90 - \frac{1}{3} = 89\frac{7}{3}$.

Therefore, the loss on each share is $$92\frac{1}{8} - $89\frac{7}{8} = $2\frac{1}{4}$.

Therefore, the loss on 80 shares is $80 \times $21 = 180 . Ans.

57. How much stock must be sold at 90\{ so that when the seller invests the proceeds in a mortgage at 6% he will receive \$543.75 annual income?

The face of the 6% mortgage is $$543.75 \div 0.06 = 9062.50 .

The number of shares of stock at $90\frac{1}{9}$ that must be sold to amount to \$9062.50 is $\frac{9062.50}{90.625} = 100$ shares.

100 shares amount to \$10,000. Ans.

58. A person invests 3 of his money at 6%, 3 at 41%, and the rest at 31%. What per cent does he receive on the whole amount?

$$\frac{2}{7} + \frac{2}{5} = \frac{10 + 14}{35} = \frac{24}{35}$$
. $\frac{35}{35} - \frac{24}{35} = \frac{11}{35}$.

On the whole amount he receives

$$\frac{3}{7}$$
 of $6\% + \frac{2}{5}$ of $4\frac{1}{2}\% + \frac{1}{3}\frac{1}{5}$ of $3\frac{1}{2}\% = 1\frac{5}{7}\% + 1\frac{1}{5}\% + 1\frac{1}{10}\%$
= $3\frac{5}{7}\frac{0}{7}\frac{5}{0} + \frac{7}{7}\% = 4\frac{1}{7}\frac{3}{5}\% = 4.61\%$. Ans.

59. How many shares of stock must a man sell at 1074, that when he invests the proceeds in 3% stock at 71½ he may receive an annual income of \$900?

Each share of the 3% yields \$3 income.

\$900 income requires 200 or 300 shares.

The cost of 300 shares at $71\frac{1}{2}$ is $300 \times \$71\frac{1}{2}$.

Therefore, the number of shares he must sell at 1071 is.

$$\frac{300 \times 71\frac{1}{4}}{107\frac{1}{4}} = \frac{100}{300} \times \frac{143}{2} \times \frac{\frac{2}{4}}{\frac{429}{3}} = 200. \quad Ans.$$

Exercise 133. Page 296.

1. Find the cost of a sight draft on New York of \$1100, exchange 1 % premium.

Exchange = $\frac{1}{4}$ % of \$ 1100 = \$2.75.

Cost of draft = \$1100 + \$2.75 = \$1102.75. Ans.

2. Find the cost of a sight draft on New Orleans of \$ 1350, exchange \$ % discount.

Exchange = $\frac{1}{4}$ % of \$1400 = \$3.50.

Cost of draft = \$1350 - \$3.50 = \$1346.50. Ans.

3. Find the cost of a draft on Boston of \$1600, payable 30 days after sight with grace, interest 6%, exchange ½% premium.

Discount on \$ 1600 for 33 dy. at $6\% = 5\frac{1}{2} \times $ 1.60 = $ 8.80$.

Proceeds = \$1600 - \$8.80 = \$1591.20.

Exchange $= \frac{1}{4}\%$ of \$ 1600 = \$4.

Cost of draft = \$1591.20 + \$4 = \$1595.20. Ans.

4. Find the cost of a draft of \$500, payable 60 days after sight with grace, interest 7%, exchange ½% discount.

Discount on \$500 for 63 dy. at $6\% = 10.5 \times $0.50 = 5.25 .

Exchange $= \frac{1}{2}$ % of \$500 = \$2.50.

Total discount = \$6.13 + \$2.50 = \$8.63.

Cost of draft = \$500 - \$8.63 = \$491.37. Ans.

5. Find the cost of a draft of \$1200, payable 90 days after sight with grace, interest 7%, exchange ½% premium.

Discount on \$1200 for 93 dy. at $6\% = 15.5 \times 1.20 ; at $7\% = 15.5 \times 1.40 .

$$\begin{array}{r}
 \$15.5 \\
 \hline
 1.40 \\
 \hline
 6200 \\
 \hline
 155 \\
 \hline
 \$21.700
\end{array}$$

Proceeds = \$1200 - \$21.70 = \$1178.30.

Exchange $= \frac{1}{2}$ % of \$1200 = \$6.00.

Cost of draft = \$1178.30 + \$6 = \$1184.30. Ans.

6. Find the cost of a draft of \$950, payable in 30 days with grace, interest 4½%, exchange at par.

Discount on \$950 for 33 dy. at $6\% = 5.5 \times 0.95 .

7. Find the cost of a draft of \$725, payable in 60 days with grace, interest 5%, exchange 1% discount.

Discount on \$725 for 63 dy. at $6\% = 10.5 \times 0.725 .

Exchange = $\frac{1}{4}$ % of \$800 = \$2.

Total discount = \$6.34 + \$2 = \$8.34.

Cost of draft = \$725 - \$8.34 = \$716.66. Ans.

8. Find the cost of a draft of \$810, payable in 90 days with grace, interest 5½%, exchange ½% premium.

Discount on \$810 for 93 dy. at $6\% = 15.5 \times 0.81 .

Exchange = $\frac{1}{4}$ % of \$900 = \$2.25.

Cost of draft = \$798.49 + \$2.25 = \$800.74. Ans.

9. Find the face of a draft, payable 30 days after sight with grace, that can be bought for \$274, interest 6%, exchange at par.

Discount on \$1 for 33 dy. at 6% = \$0.0055; and the proceeds of \$1 = \$1 - \$0.0055 = \$0.9945.

Face of draft =
$$\$\frac{274}{0.9945}$$
 = $\$275.52$. Ans.

$$\begin{array}{r} 275.51 \\ 9945)2740000. \\ \underline{19890} \\ 75100 \\ \underline{69615} \\ 54850 \\ \underline{49725} \\ 51250 \\ \underline{49725} \\ 15250 \\ \underline{9945} \\ 5305 \end{array}$$

10. Find the face of a draft, payable 60 days after sight with grace, that can be bought for \$ 1250, interest 7%, exchange ½% premium.

Discount on \$1 for 63 dy. at 6% = \$0.0105; at 7% = \$0.01225; and proceeds of \$1 = \$1 - \$0.01225 = \$0.98775.

Exchange on \$1 = \$0.0025; and cost of \$1 = \$0.98775 + \$0.0025 = \$0.99025.

Face of draft = $\$\frac{1250}{0.99025}$ = \$1262.31. Ans.

$$\begin{array}{r} 1262.30 \\ 99025 \hline 125000000. \\ \underline{99025} \\ \hline 259750 \\ \underline{198050} \\ \hline 617000 \\ \underline{594150} \\ \underline{228500} \\ \underline{198050} \\ \underline{304500} \\ \underline{297075} \\ \overline{74250} \end{array}$$

11. Find the face of a draft, payable 60 days after date with grace, that can be bought for \$1125, interest 5½%, exchange ½% discount.

Discount on \$1 for 63 dy. at 6% = 0.0105; at $5\frac{1}{2}\% = \$0.009625$; and proceeds of \$1 = \$1 - \$0.009625 = \$0.990375.

Exchange on \$1 = \$0.0025; and cost of \$1 = \$0.990375 - \$0.0025 = \$0.987875.

Face of draft =
$$\$\frac{1125}{0.987875}$$
 = $\$1138.81$. Ans.

12. Find the face of a draft, payable 30 days after date with grace, that can be bought for \$520, interest 4%, exchange ½% premium.

Discount on \$1 for 33 dy. at 6% = \$0.0055; at $4\% = \$0.0036\frac{1}{3}$; and proceeds of $\$1 = \$1 - \$0.0036\frac{1}{3} = \$0.9963\frac{1}{3}$.

Exchange on \$1 = \$0.005; and cost of $\$1 = \$0.9963\frac{1}{3} + \$0.005 = \$1.0013\frac{1}{3}$.

Face of draft = $\$\frac{520}{1.001\frac{1}{4}} = \$\frac{1560}{3.004} = \$519.31$. Ans.

$$\begin{array}{r}
519.30 \\
3004)1560000, \\
\underline{15020} \\
5800 \\
\underline{3004} \\
27960 \\
\underline{27960} \\
27036 \\
\underline{9240} \\
9012 \\
\underline{2280}
\end{array}$$

13. Find the face of a draft, payable 90 days after date with grace, that can be bought for \$10,000, interest $4\frac{1}{2}$ %, exchange at par.

Discount on \$1 for 93 dy. at 6% = \$0.0155; at $4\frac{1}{2}\% = \$0.011625$; and proceeds of \$1 = \$1 - \$0.011625 = \$0.988375.

Face of draft =
$$\frac{10000}{0.988375}$$
 = \$10,117.62. Ans.

$$\begin{array}{r} 10117.61 \\ 988375)100000000000. \\ \underline{988375} \\ 1162500 \\ \underline{988375} \\ 1741250 \\ \underline{988375} \\ 7528750 \\ \underline{6918625} \\ 6101250 \\ \underline{5930250} \\ 1710000 \\ \underline{988375} \\ 721625 \end{array}$$



TEACHERS' EDITION.

Exercise 134. Page 298.

1. Find the cost of a sight draft on London for £ 320 10 s. 6 d.

£ 320 10 s. 6 d. = £ 320.525.

 $320.525 \times 44.865 = 1559.85$. Ans.

320.525 4.865 1602625 1923150 2564200 1282100 1559.354125

2. Find the cost of a sight draft on Paris for 8000 francs.

3. Find the cost of a sight draft on Hamburg for 2876 reichsmarks.

4 reichamarks = \$0.965.

... 1 reichsmark = \$0.23875.

\$686.64500 \$686.65. Ans.

 Find the cost of a sight draft on Amsterdam for 6486 guilders.

\$ 2618.72. Ans.

Find the cost of a sight draft on Glasgow for £ 5876 10 s.
 £ 5876 10 s. = £ 5876.5.

5876.5×\$4.865=\$28,589.17. Ans.

5876.5 4.865 293825 352590 470120 235060 28589.1725

6. Find the cost of a sight draft on Paris for 12,842 francs.

12,842 fr. =
$$\frac{12842}{5.181}$$

= $\frac{2478.55}{2478.55}$. Ans.

158150

7. Find the cost of a sight draft on Berlin for 4885 reichsmarks.

1 reichsmark = \$0.23875.

\$ 1166.29. Ans.

8. Find the cost of a sight draft on Rotterdam for 8282 guilders.

\$0.40375 8282 80750 323000 80750 323000 \$3343.85750 \$3343.86. Ans.

9. Find the cost of a sight draft on Liverpool for £ 1242 12 s. 6 d.

£ 1242 12 s. 6 d. = £ 1242.625.

 $1242.625 \times 4.865

= \$6045.37. Ans.

1242.625 4.865 6213125 7455750 9941000 4970500 6045.370625 10. Find the cost of a sight draft on Paris for 2685 francs.

2685 fr. =
$$\$\frac{2685}{5.18\frac{1}{3}}$$
 = \$ 518.21. Ans.

11. Find the face of a sight draft on Glasgow that can be bought for \$2000.

$$\$2000 = £\frac{2000}{4.865} = £411.0997$$

= £411 2 s. Ans.

4460

12. Find the face of a sight draft on London that can be bought for \$4000.

Twice as large a draft can be bought for \$4000 as for \$2000.

\$2000 will buy a draft (from Ex. 11) of £411 1s. 11.928 d.

13. Find the cost of a sixty-day draft on London for £ 150, when sixty-day bills are quoted at 4.81\frac{1}{4}, and the broker's commission is \frac{1}{4}% of the cost of the draft.

$$150 \times \$4.81\frac{1}{4} = \$721.88.$$

$$\frac{1}{8}\% \text{ of } \$721.88 = \$0.90.$$

$$\frac{\$4.8125}{2406250}$$

$$\frac{150}{2406250}$$

$$\$721.88$$

$$48125$$

$$0.90$$

14. How large a sight draft on Paris can be bought for \$2840? 2840×5.18 fr. = 14,714.75 fr. Ans.

\$721.8750

3 722.78 Ans.

15. How large a sixty-day draft on Paris can be bought for \$1500, when sixty-day bills are quoted at 5.17‡?

 1500×5.17 fr. = 7760.625 fr. Ans.

16. How large a sight draft on Berlin can be bought for \$8000?

4 reichsmarks = \$0.955.

 \therefore 1 reichsmark = \$0.23875.

$$$8000 = \frac{8000}{0.23875} \text{ reichsmarks}$$

$$= \frac{8000}{0.23\frac{7}{4}} \text{ reichsmarks}$$

$$= \frac{64000}{1.91} \text{ reichsmarks}$$

=33,507.85 reichsmarks. Ans.

17. How large a sixty-day draft on Hamburg can be bought for \$2500, when German sixty-day drafts are quoted at 0.95?

4 reichsmarks = \$0.95.

 \therefore 1 reichsmark = \$0.23\frac{1}{2}.

\$2500 =
$$\frac{2500}{0.23\frac{3}{4}}$$
 reichsmarks
= $\frac{10000}{0.95}$ reichsmarks
= 10,526.32 reichsmarks.
Ans.

18. How large a sight draft on Amsterdam can be bought for \$2200?

55

$$$2200 = \frac{2200}{0.40\frac{3}{8}}$$
 guilders
= $\frac{17600}{3.23}$ guilders
= 5448.92 guilders. Ans.

19. How large a sixty-day draft on Rotterdam can be bought for \$1200, when a sixty-day draft on Holland is quoted at 0.401?

\$ 1200 =
$$\frac{1200}{0.40\frac{1}{8}}$$
 guilders
= $\frac{9600}{3.21}$ guilders
= 2990.65 guilders. Ans.

Exercise 135. Page 300.

1. Find the equated time for the payment of \$250 due in 3 mo., \$400 due in 6 mo., \$700 due in 8 mo.

\$
$$250 \times 0 =$$
\$ $400 \times 3 = 1200
\$ $700 \times 5 = 3500$
\$ 1350
\$ 4700
\$ $3\frac{1}{2}$
\$ $3\frac{1}{2}$ mo. = 3 mo. 14 dy.

Hence, the equated time is 3 mo. 14 dy. after 3 mo.; that is, 6 mo. 14 dy. Ans.

2. Find the equated time for the payment of \$300 due in 30 days, \$500 due in 60 days, and \$200 due in 90 days.

$$\$300 \times 00 =$$
 $\$500 \times 30 = \15000
 $\$200 \times 60 = 12000$
 $\$1000$
 $\$27000$

Hence, the equated time is 27 dy. after 30 dy.; that is, 57 dy. Ans.

3. Find the equated time for the payment of \$325 due now, \$200 due in 30 days, \$460 due in 60 days, and \$150 due in 90 days.

$$\$325 \times 00 =$$
 $\$200 \times 30 = \6000
 $\$460 \times 60 = 27600$
 $\$150 \times 90 = 13500$
 $\$1135$
 $\$47100$

Hence, the equated time is 41 dy. Ans.

4. Find the equated time for the payment of \$240 due May 10, \$420 due July 2, \$310 due Sept. 14, and \$600 due Oct. 1.

$$\$240 \times 00 =$$
 $\$420 \times 53 = \22260
 $\$310 \times 127 = 39370$
 $\$600 \times 144 = 86400$
 $\$1570$
 $\$148030$
 94.3

Hence, the equated time is 94 dy. after May 10; that is, Aug. 12. Ans.

5. Find the equated time for the payment of \$275 due June 21, \$175 due July 16, \$2.0 due Aug. 6, and \$150 due Sept. 3.

Hence, the equated time is 31 dy. after June 21; that is, July 22. Ans.

6. Find the equated time for the payment of \$112.30 due July 6, \$115.25 due July 30, \$252.15 due Sept. 4, and \$102.36 due Oct. 1.

$$$112.30 \times 00 =$$
 $$115.25 \times 24 = 2766.00
 $$232.15 \times 60 = 13929.00$
 $$102.36 \times 87 = 8905.32$
 $$562.06$
 $$25600.32$

Hence, the equated time is 46 dy. after July 6; that is, Aug. 21. Ans.

7. A owes B \$200 due in 10 mo. If he pays \$120 in 4 mo., when should he pay the balance?

By paying \$120 in 4 mo. A loses the use of \$120 for 6 mo., which is equal to the use of \$720 for 1 mo. Therefore, he is entitled to keep the balance $($80)^{-29}$ mo. = 9 mo. after its maturity.

Hence, he should pay the balance in 19 mo. Ans.

8. A owed B \$2000 payable in 4 mo., but at the end of 1 mo. he paid him \$500, at the end of 2 mo. \$500, and at the end of 3 mo. \$500. In how many months is the balance due?

$$\$500 \times 3 = \$1500$$

 $\$500 \times 2 = 1000$
 $\$500 \times 1 = 500$
 $\$1500$

Therefore, he is entitled to keep the balance (\$500) $\frac{$000}{500}$ mo. = 6 mo. after its maturity.

Hence, the balance is due in 10 mo. Ans.

9. A man, Feb. 11, 1898, gave a note for \$1700 payable in 4 mo.; but he paid Mar. 22, \$400, Apr. 20, \$220, May 10, \$300. When was the balance due?

Note was due June 11, 1898.

$$\$400 \times 81 = \$32400$$

 $\$220 \times 52 = 11440$
 $\$300 \times 32 = 9600$
 $\$53440$

Therefore, he is entitled to keep the balance (\$780) $\frac{5}{7}$ dy.=69 dy. after its maturity.

Hence, the balance was due 69 dy. after June 11, 1898; that is, Aug. 19, 1898. Ans.

10. A man, Jan. 4, 1898, gave a note for \$2500 payable in 6 mo.; but he paid Feb. 4, \$200, Mar. 4, \$400, Apr. 4, \$600, May 4, \$500, and June 4, \$300. When was the balance due?

Note was due July 4, 1898.

$$\$200 \times 5 = \$1000$$
 $\$400 \times 4 = 1600$
 $\$600 \times 3 = 1800$
 $\$500 \times 2 = 1000$
 $\$300 \times 1 = 300$
 $\$2000$

Therefore, he is entitled to keep the balance (\$500) $\frac{5700}{500}$ mo. = 11.4 mo. after its maturity.

Hence, the balance was due 11.4 mo. = 11 mo. 12 dy. after July 4, 1898; that is, June 16, 1899. Ans.

Exercise 136. Page 302.

1. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 35 dy.

The balance of account is \$1000 - \$950 = \$50.

If the account were settled at the later date, May 17, 1897, the \$1000 would have been on interest 35 dy., which is equivalent to having the balance, \$50, on interest $\frac{1980}{2}$ of 35 dy. = 700 dy.

Hence, the balance should begin to draw interest 700 dy. before May 17, 1897; that is, June 17, 1895. Ans.

2. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 35 dy.

The balance of account is \$1000 - \$950 = \$50.

If the account were settled at the later date, May 17, 1897, the \$950 would have been on interest 35 dy., which is equivalent to having the balance, \$50, on interest $\frac{950}{50}$ of 35 dy. = 665 dy.

Hence, the balance should remain unpaid 665 dy. after May 17, 1897; that is, until Mar. 13, 1899. Ans.

3. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 24 dy.

The balance of account is \$1000 - \$920 = \$80.

If the account were settled at the later date, June 23, 1898, the \$1000 would have been on interest 24 dy., which is equivalent to having the balance, \$80, on interest $\frac{1980}{8}$ of 24 dy. = 300 dy.

Hence, the balance should begin to draw interest 300 dy. before June 23, 1898; that is, Aug. 27, 1897. Ans.

4. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 83 dy.

The balance of account is \$500 - \$480 = \$20.

If the account were settled at the later date, July 6, 1897, the \$480 would have been on interest 83 dy., which is equivalent to having the balance, \$20, on interest $\frac{480}{20}$ of 83 dy. = 1992 dy.

Hence, the balance should remain unpaid 1992 dy. after July 6, 1897; that is, until Dec. 20, 1902. Ans.

5. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 31 dy.

The balance of account is \$875 - \$600 = \$275.

If the account were settled at the later date, Sept. 13, 1897, the \$875 would have been on interest 31 dy., which is equivalent to having the balance, \$275, on interest $\frac{475}{7}$ of 31 dy. = 99 dy.

Hence, the balance should begin to draw interest 99 dy. before Sept. 13, 1897; that is, June 6, 1897. Ans.

6. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 7 dy.

The balance of account is \$550 - \$500 = \$50.

If the account were settled at the later date, June 4, 1898, the \$500 would have been on interest 7 dy., which is equivalent to having the balance, \$50, on interest $\frac{500}{50}$ of 7 dy. = 70 dy.

Hence, the balance should remain unpaid 70 dy. after June 4, 1898; that is, until Aug. 13, 1898. Ans.

7. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 63 dy.

The balance of account is \$400 - \$300 = \$100.

If the account were settled at the later date, June 6, 1898, the \$400 would have been on interest 63 dy., which is equivalent to having the balance, \$100, on interest $\frac{488}{100}$ of 63 dy. = 252 dy.

Hence, the balance should begin to draw interest 252 dy. before June 6, 1898; that is, Sept. 27, 1897. Ans.

8. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 36 dy.

The balance of account is \$750 - \$500 = \$250.

If the account were settled at the later date, Mar. 12, 1898, the \$500 would have been on interest 36 dy., which is equivalent to having the balance, \$250, on interest $\frac{590}{190}$ of 36 dy. = 72 dy.

Hence, the balance should remain unpaid 72 dy. after Mar. 12, 1898; that is, until May 23, 1898. Ans.

9. Find the time for the payment of the balance of an account if the debit and credit sides, when equated, stand

The difference between the equated times is 36 dy.

The balance of account is \$750 - \$500 = \$250.

If the account were settled at the later date, Mar. 12, 1898, the \$750 would have been on interest 36 dy., which is equivalent to having the balance, \$250, on interest $\frac{750}{250}$ of 36 dy. = 108 dy.

Hence, the balance should begin to draw interest 108 dy. before Mar. 12, 1898; that is, Nov. 24, 1897. Ans.

Exercise 137. Page 303.

1. Find the cash balance of the following account, reckoning interest at 6%:

1897.	DB.	INT.	1897.		Cm.	Int.
Apr. 5. To mdse.,	\$ 250.00	\$8.18	Apr. 20.	By cash,	\$ 200.00	\$ 2.00
Apr. 27. To mdse.,	610.00	5.89	Apr. 80.	By cash,	500.00	4.17
June 1. To mdse.,	200.00	0.60	June 4.	By cash,	400,00	1.00
June 19. To bal. acct.,	40.00	'	June 19.	By bal. int.,		1.95
	\$ 1100.00	\$ 9.12	1		\$ 1100.00	\$ 9.12

Hence, the cash balance is \$40.00 - \$1.95 = \$38.05. Ans.

2. Find the cash balance of the following account, reckoning interest at 6%:

1 89 7.	Dr.	INT.	1897.		Cr.	Int.
Jan. 15. To mdse. 8 mo	., \$ 250.00	\$7.46	Apr. 26.	By cash,	\$ 150.00	\$ 4.20
Feb. 25. To mdse. 8 mo	98.50	2.28	May 17.	By cash,	150.00	8.68
Mar. 8. To mdse, 8 mo	800.00	6.25	July 7.	By cash,	200.00	8.20
	•		Oct. 11.	By bal. acct.,	148.50	
		<u> </u>	Oct. 11.	By bal. int.,		4.91
	\$ 648.50	\$ 15.99		•	8 648.50	\$ 15.99

Hence, the cash balance is \$148.50 + \$4.91 = \$153.41. Ans.

3. Find the cash balance of the following account, reckoning interest at 6%:

	• • • • • • • • • • • • • • • • • • • •						
1897.		Dr.	Int.	1897.		Cr.	Int.
Jan. 2.	To mdse. 60 dy.,	\$ 100.00	\$ 2.58	Feb. 25.	By cash,	\$ 100.00	\$ 2.68
Mar. 8.	To mdse. 60 dy.,	200.00	2.90	Mar. 22.	By cash,	150.00	8.88
May 10.	To mdse. 80 dy.,	150.00	1.85	June 21.	By cash,	200.00	1.40
June 2.	To mdse.,	95.00	0.97	Aug. 2.	By bal. acct.,	95.00	
				Aug. 2.	By bal. int.,		0.89
		\$ 545.00	\$7.75			\$ 545.00	\$ 7.75

Hence, the cash balance is \$95.00 + \$0.39 = \$95.39. Ans.

Exercise 138. Page 305.

Find the balance on deposit Jan. 1, 1898, on the following account:

1. Interest being 4%, computed quarterly. Deposited Jan. 1, 1897, \$125; Mar. 22, 1897, \$40; June 8, 1897, \$35; July 30, 1897, \$85; Sept. 24, 1897, \$65. Withdrawn Apr. 2, 1897, \$110; June 30, 1897, \$40; Oct. 22, 1897, \$10; Dec. 17, 1897, \$25.

DATE.	DEPOSIT	ED.	WITHDRA	WN.	Interes	ьт.	Balanc	E.
1897.								
Jan. 1,	\$ 125	00		1 11			\$ 125	00
Mar. 22,	40	00					165	00
Apr. 1,		}			\$ 1	25	166	25
Apr. 2,			\$ 110	00	-		56	25
June 8,	35	00	•				91	25
June 30,			40	00			51	25
July 1,				•••	0	51	51	76
July 30,	85	00			•	-	136	76
Sept. 24,	65	00]]]	201	76
Oct. 1,	00] }	0	52	202	28
Oct. 22,			10	00	· ·		192	28
• 1					İ			-
Dec. 17,			25	00			167	28
1898.								ļ
Jan. 1,				1 11	1	67	168	86

2. Interest being 3%, computed quarterly. Deposited Jan. 1, 1897, \$200; Feb. 14, 1897, \$125; Mar. 10, 1897, \$75; May 31, 1897, \$50; Aug. 2, 1897, \$100. Withdrawn May 7, 1897, \$25; June 22, 1897, \$40; Oct. 2, 1897, \$50; Nov. 4, 1897, \$65; Dec. 14, 1897, \$75.

DATE.	DEPOSIT	ED.	WITHDRA	WW.	Interes	FT.	BALAN	CR.
1897.				Ī .			•	i
Jan. 1,	\$ 200	00	I				\$ 200	00
Feb. 14,	125	∣ 00]			325	00
Mar. 10,	75	00		[]			400	00
Apr. 1,		i İ		'	\$1	50	401	50
May 7,		l l	\$25	00	-		376	50
May 31,	50	00	-	[]			426	50
June 22,		·	40	00			586	50
July 1,				!	2	82	389	32
Aug. 2,	100	00					489	32
Oct. 1,					2	92	492	24
Oct. 2,			50	00			442	24
Nov. 4,			65	00			377	24
Dec. 14,			75	00			302	24
1898.				!				
Jan. 1,		' <u> </u>			2	27	304	51

3. Interest being 3%, computed semi-annually. Deposited Jan. 1, 1897, \$425; May 10, 1897, \$15; Sept. 24, 1897, \$200; Oct. 5, 1897, \$25; Nov. 15, 1897, \$65. Withdrawn Feb. 1, 1897, \$25; Mar. 20, 1897, \$45; Aug. 2, 1897, \$50; Aug. 28, 1897, \$125; Dec. 10, 1897, \$100.

DATE.	DEPOSIT	ED.	WITHDRA	WN.	INTERE	вт.	BALANC	TR.
1897. Jan. 1, Feb. 1, Mar. 20,	\$ 425	00	\$ 25 45	00			\$ 425 400 355	00
May 10, July 1,	15	00	40		\$ 5	32	370 375	00 00 32
Aug. 2, Aug. 28,	200		50 125	00			325 200	32 32
Sept. 24, Oct. 5,	200 25 65	00					400 425	32 32
Nov. 15, Dec. 10, 1898.	00	00	100	00			490 390	32 32
Jan. 1,					3	00	393	32

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4. Interest being 3%, computed annually. Deposited Jan. 1, 1897, \$266.50; May 3, 1897, \$122.50; Aug. 2, 1897, \$57; Aug. 9, 1897, \$108; Sept. 4, 1897, \$64.50. Withdrawn June 15, 1897, \$40; Oct. 8, 1897, \$75; Nov. 1, 1897, \$60; Dec. 4, 1897, \$85; Dec. 20, 1897, \$142.

DATE.	DEPOSIT	ED,	WITHDRA	wn.	Interes	т.	Balanc	JE.
1897.	 							
Jan. 1,	\$ 266	50					\$ 266	50
May 3,	122	50					389	00
June 15,			\$40	00			349	00
Aug. 2,	57	00					406	00
Aug. 9,	108	00					514	00
Sept. 4,	64	50	II				578	50
Oct. 8,			75	00			50 3	50
Nov. 1,			60	00			44 3	50
Dec. 4,			85	00			358	50
Dec. 20,			142	00			216	50
1898.								
Jan. 1,					\$ 6	49	222	99

Exercise 139. Page 309.

1. Find the square root of 2916.

2. Find the square root of 7921.

3. Find the square root of 494,209.

4. Find the square root of 20,164.

$$\begin{array}{r}
2\ 01\ 64(142) \\
 \underline{1} \\
24)101 \\
 \underline{96} \\
282)564 \\
584
\end{array}$$

5. Find the square root of 3,345,241.

6. Find the square root of 125,457.64.

7. Find the square root of 47,320,641.

8. Find the square root of 21,609.

9. Find the square root of 53.7289.

10. Find the square root of 883.2784.

11. Find the square root of 1.97262025.

12. Find the square root of 0.0002090916.

13. Find the square root of 2.

14. Find the square root of 5.

15. Find the square root of 0.3.

$$0.30\ 00\ 00\ 00 (0.547722$$

16. Find the square root of 31.

$$\begin{array}{r} 3.25\ 00\ 00(1.802775\\ \underline{1}\\ 28)225\\ \underline{224}\\ 3602)10000\\ \underline{7204}\\ 3604)27960\\ \underline{25228}\\ \underline{27320}\\ \underline{25228}\\ \underline{20920}\\ 18020\\ \end{array}$$

17. Find the square root of 8\{\frac{1}{2}}.
8.83 33 33(2.972092

- 18. Find the square root of 0.9.
 - 0.90 00 00 00 (0.948683 81 184)900 736 1888)16400 15104 18966)129600 113796 18972)158040 151776 62640 56916
- 19. Find the square root of $\frac{4}{3}$. $\sqrt{\frac{1}{3}} = \frac{2}{3} = 0.666667$.
- 20. Find the square root of §.

 0.55 55 55 55 (0.745355

 49

 144)655
 576

 1485)7955
 7425

 14903)53055
 44709

 14906)83465
 74530

 89355
 74530
- 21. Find the square root of \(\frac{1}{4}\).

 0.50 00 00 00 (0.707108
 \(\frac{49}{49}\)

 1407)10000
 \(\frac{9849}{14141}\)

 14141)15100
 \(\frac{14141}{14141}\)

 14142)95900
 \(\frac{84852}{84852}\)

22. Find the square root of §.

0.60 00 00 00 (0.774596

49

147)1100

1029

1544)7100

6176

15485)92400

77425

15490)149750

139410

103400

92940

- 23. Find the square root of \(\frac{3}{4}\).

 0.75 00 00 00(0.866025\)
 \(\frac{64}{4}\)

 166)1100
 \(\frac{996}{10356}\)

 1726)10400
 \(\frac{10356}{34640}\)
 \(\frac{34640}{93600}\)

 86600
- 24. Find the square root of \(\frac{3}{4}\).

 0.66 66 66 66 (0.816496)
 \(\frac{64}{161}\)

 161)266
 \(\frac{161}{161}\)

 1626)10566
 \(\frac{9756}{9756}\)

 16324)81066
 \(\frac{65296}{146952}\)
 \(\frac{146952}{107546}\)
 \(\frac{97968}{97968}\)

Exercise 140. Page 315.

1. Find the cube root of 1331.

$$\begin{array}{c|c}
 & 1331(11) \\
 & 3 \times 10^{2} = 300 \\
 & 3 \times (10 \times 1) = 30 \\
 & 1^{2} = 1 \\
 & 331
 \end{array}$$

2. Find the cube root of 1728.

$$\begin{array}{c|c}
 & 1728(12) \\
 & 3 \times 10^{2} = 300 \\
 & 3 \times (10 \times 2) = 60 \\
 & 2^{2} = 4 \\
 & 364 \\
 \hline
 & 728
 \end{array}$$

3. Find the cube root of 12.167.

$$3 \times 20^{2} = 1200 \\
3 \times (20 \times 3) = 180 \\
3^{2} = 9 \\
\hline
1389$$

$$4167$$

4. Find the cube root of 300.763.

$$300.763(6.7)$$

$$3 \times 60^{2} = 10800$$

$$3 \times (60 \times 7) = 1260$$

$$7^{2} = 49$$

$$12109$$

$$84763$$

5. Find the cube root of 148,877.

6. Find the cube root of 2,048,383.

7. Find the cube root of 59.776471.

$$3 \times 30^{2} = 2700$$

$$3 \times (30 \times 9) = 810$$

$$9^{2} = 81$$

$$3591$$

$$891$$

$$3 \times 390^{2} = 456300$$

$$3 \times (390 \times 1) = 1170$$

$$1^{2} = 1$$

$$457471$$

$$457471$$

8. Find the cube root of 304,957.115891.

$$3 \times 60^{2} = 10800$$

$$3 \times (60 \times 7) = 1260$$

$$7^{2} = 49$$

$$1309$$

$$3 \times 670^{2} = 1346700$$

$$3 \times (670 \times 3) = 6030$$

$$3^{2} = 9$$

$$1352739$$

$$6039$$

$$3 \times 6730^{2} = 135878700$$

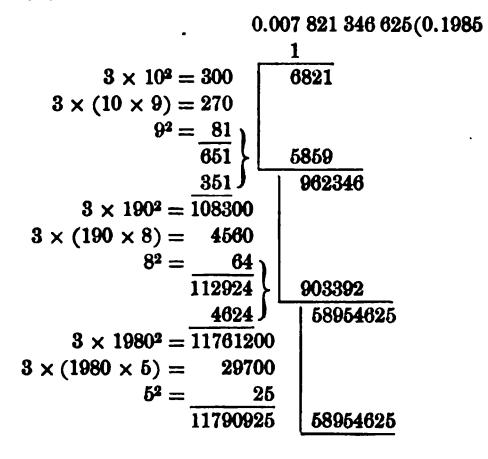
$$3 \times (6730 \times 1) = 20190$$

$$1^{2} = 1$$

$$135898891$$

$$135898891$$

9. Find the cube root of 0.007821346625.



10. Find the cube root of 104.600290750613.

11. Find the cube root of 17,183,498,535,125.

$$3 \times 20^{2} = 1200 \\
8 \times (20 \times 5) = 300 \\
5^{2} = \frac{25}{1525} \\
3 \times 250^{2} = 187500 \\
3 \times (250 \times 8) = 6000 \\
8^{2} = \frac{64}{193564} \\
3 \times 25800^{2} = 1996920000 \\
3 \times (25800 \times 5) = 387000 \\
5^{2} = \frac{25}{1997307025}$$

$$17 183 498 535 125 (25805)

9183

7625

1558498

1548512

9986535125$$

12. Find the cube root of 122,615.327232.

$$3 \times 40^{2} = 4800 \\
3 \times (40 \times 9) = 1080 \\
9^{2} = \frac{81}{5961} \\
3 \times 490^{2} = 720300 \\
3 \times (490 \times 6) = 8820 \\
6^{2} = \frac{36}{729156} \\
8856 \\
3 \times 4960^{2} = 73804800 \\
3 \times (4960 \times 8) = 119040 \\
8^{2} = \frac{64}{73923904}$$

$$58615$$

$$4966327$$

$$4966327$$

$$4374936$$

$$591391232$$

13. Find the cube root of 116,400.

14. Find the cube root of 22,406,807.

15. Find the cube root of 10.

$$3 \times 20^{2} = 1200 \\
3 \times (20 \times 1) = 60 \\
1^{2} = \frac{1}{1261} \\
3 \times 210^{2} = \overline{132300} \\
3 \times (210 \times 5) = 3150 \\
5^{2} = \underline{25} \\
135475 \\
3 \times 2150^{2} = \overline{13867500} \\
3 \times (2150 \times 4) = 25800 \\
4^{2} = \underline{16} \\
13893316 \\
25816 \\
3 \times 2154^{2} = \overline{13919148}$$

$$10.000(2.1544) \\
8 \\
1261 \\
739000$$

$$677375 \\
61625000$$

$$61625000$$

$$55573264 \\
60517360 \\
55676592$$

16. Find the cube root of 3\{\frac{1}{2}}.

$$\sqrt[3]{3\frac{5}{8}} = \sqrt[3]{\frac{29}{8}} = \frac{\sqrt[3]{29}}{2} = \frac{3.0723}{2} = 1.5362. \quad Ans.$$

$$29.000(3.0723)$$

$$27$$

$$3 \times 300^{2} = 270000$$

$$3 \times (300 \times 7) = 6300$$

$$7^{2} = \frac{49}{276349}$$

$$\frac{6349}{276349}$$

$$3 \times 3070^{2} = \frac{28274700}{28293124}$$

$$3 \times (3070 \times 2) = 18420$$

$$2^{2} = \frac{4}{28293124}$$

$$\frac{18424}{28293124}$$

$$3 \times 3072^{2} = \frac{28311552}{28311552}$$

$$\frac{56586248}{89707520}$$

$$84934658$$

17. Find the cube root of 81.

$$3 \times 200^{2} = 120000$$

$$3 \times (200 \times 2) = 1200$$

$$2^{2} = 4$$

$$121204$$

$$3 \times 2020^{2} = 12241200$$

$$3 \times (2020 \times 7) = 42420$$

$$7^{2} = 49$$

$$12283669$$

$$42469$$

$$3 \times 2027^{2} = 12326187$$

$$8.333 333(2.0274$$

$$242408$$

$$90925333$$

$$85985683$$

$$49396503$$

$$49304748$$

18. Find the cube root of 5.

19. Find the cube root of §.

 $3 \times 80^{2} = 19200$ $3 \times (80 \times 2) = 480$ $2^{2} = \frac{4}{19684}$ $3 \times 82^{2} = 20172$ $3 \times 82^{2} = 20172$ $3 \times 82^{3} = 20172$ $3 \times 82^{2} = 20172$

21. Find the cube root of \\ \frac{1}{2}.

$$3 \times 900^{2} = 2430000$$

$$3 \times (900 \times 8) = 21600$$

$$8^{2} = \frac{64}{2451664}$$

$$3 \times 908^{2} = \frac{21664}{2473392}$$

$$19613312$$

$$13866880$$

$$12366960$$

Exercise 141. Page 321.

- 1. Find the area of a parallelogram, base 18 in., altitude 11 in. Area = (18×11) sq. in. = 198 sq. in. Ans.
- 2. Find the area of a triangle, base 16 in., altitude 12 in. Area = $\frac{1}{2}(16 \times 12)$ sq. in. = 96 sq. in. Ans.
- 3. Find the area of a rectangle, base 24 in., altitude 18 in. Area = (24×18) sq. in. = 432 sq. in. Ans.
- 4. Find the area of a square, side 18 in. Area = (18×18) sq. in. = 324 sq. in. Ans.
- 5. Find the area of a rhombus, diagonals 8 in. and 10 in. Area = $\frac{1}{4}(8 \times 10)$ sq. in. = 40 sq. in. Ans.

6. Find the area of a triangle, sides 12 in., 11 in., and 10 in., respectively.

The half sum of the sides is $\frac{1}{4}(12 + 11 + 10)$ in. = 16.5 in.

Area =
$$\sqrt{16.5 \times 4.5 \times 5.5 \times 6.5}$$
 sq. in.
= $\sqrt{2654.4375}$ sq. in. = 51.52 sq. in. Ans.

7. Find the area of a regular hexagon, side 4 in.

Apothem = 0.8660×4 in. = 3.464 in.

Perimeter = 6×4 in. = 24 in.

Area = $\frac{1}{4}$ (24 × 3.464) sq. in. = 41.568 sq. in. Ans.

8. Find the area of a regular octagon, side 2 in.

Apothem = 1.2071×2 in. = 2.4142 in.

Perimeter = 8×2 in. = 16 in.

Area = $\frac{1}{4}$ (16 × 2.4142) sq. in. = 19.3136 sq. in. Ans.

9. Find the area of a triangle, base 185 yd., altitude 154 yd.

Area =
$$\frac{1}{2}$$
 (185 × 154) sq. yd. = 14,245 sq. yd. Ans.

$$\begin{array}{r}
185 \\
 \hline
2 \boxed{154} \\
 \hline
77 \\
 \hline
1295 \\
 \hline
14245
\end{array}$$

10. Find the area of a square, side 212 yd.

Area =
$$(212 \times 212)$$
 sq. yd. = 44,944 sq. yd. Ans.

 $\begin{array}{r}
 212 \\
 \hline
 212 \\
 \hline
 424 \\
 212 \\
 \hline
 424 \\
 \hline
 44944 \\
\end{array}$

11. Find the area of a rectangle, base 106 yd., altitude 66 yd. Area = (106×66) sq. yd. = 6996 sq. yd. Ans.

$$\begin{array}{r}
 106 \\
 \hline
 636 \\
 \hline
 636 \\
 \hline
 6996
 \end{array}$$

12. Find the area of a parallelogram, base 24 ft., altitude 18 ft.

Area =
$$(24 \times 18)$$
 sq. ft. = 432 sq. ft. Ans.

13. Find the area of an equilateral triangle, side 132 yd.

Apothem = $0.2887 \times 132 \text{ yd.} = 38.1084 \text{ yd.}$

Perimeter = 3×132 yd. = 396 yd.

Area =
$$\frac{1}{4}$$
 (396 × 38.1084) sq. yd. = 7545.4632 sq. yd. Ans.

0.2887	2 396	38.1084
132	198	198
5774		3048672
8661		3429756
2887		381084
38.1084		7545.4632

14. Find the area of a right triangle, base 164 ft., perpendicular 150 ft.

Area =
$$\frac{1}{4}$$
 (164 × 150) sq. ft. = 12,300 sq. ft. Ans.

15. Find the area of a regular pentagon, side 51 in.

Apothem = $0.6882 \times 5\frac{1}{3}$ in. = 3.7851 in.

Perimeter = 5×5.5 in. = 27.5 in.

Area = $\frac{1}{4}(27.5 \times 3.7851)$ sq. in. = 52.0451 sq. in. Ans.

• –	-
0.6882	3.7851
5.5	27.5
34410	189255
34410	264957
3.78510	75702
	2 104.09025
	52.0451

16. Find the area of a parallelogram, base 122 yd., altitude 76 yd. Area = (122×76) sq. yd. = 9272 sq. yd. Ans.

17. Find the area of a regular decagon, side 21 in.

Apothem = 1.5388×2.5 in. = 3.847 in.

Perimeter = 10×2.5 in. = 25 in.

Area = $\frac{1}{2}(25 \times 3.847)$ sq. in. = 48.0875 sq. in. Ans.

18. Find the area of a triangle, base 82cm, altitude 51cm.

Area =
$$\frac{1}{4}(82 \times 51)^{\text{qem}} = 2091^{\text{qem}}$$
. Ans.
$$\begin{array}{ccc}
2 & & & 51 \\
41 & & & \frac{41}{51} \\
& & & \frac{204}{2091}
\end{array}$$

19. Find the area of a rhombus, diagonals 16 ft. and 12 ft. Area = $\frac{1}{2}(16 \times 12)$ sq. ft. = 96 sq. ft. Ans.

20. Find the area of a circle, diameter 72 ft.

Area = $(3.1416 \times 36 \times 36)$ sq. ft. = 4071.5136 sq. ft. Ans.

36	3.1416
36	1296
216	188496
108	282744
1296	62832
	31416
	4071.5136

21. Find the area of a trapezoid, parallel sides 108 ft. and 56 ft., respectively, altitude 48 ft.

Sum of bases = 106 ft. + 56 ft. = 162 ft.

Area = $\frac{1}{2}$ (48 × 162) sq. ft. = 3888 sq. ft. Ans.

22. Find the number of hektars in a triangular field, one side of which is 82.1^m, and the distance to this side from the opposite corner 47.3^m.

Area = $\frac{1}{2}(82.1 \times 47.3)^{qm} = 1941.665^{qm} = 0.1942^{hs}$. Ans.

23. Find the number of acres in a triangular field, one side of which is 343.6 ft., and the distance to this side from the opposite corner 163.2 ft.

Area = $\frac{1}{4}$ (343.6 × 163.2) sq. ft. = 28,037.76 sq. ft. = 0.644 A. Ans.

24. Find the area of a circle that has a radius of 10 in.; of a circle that has a diameter of 10 ft.; of a circle that has a circumference of 30 in.

Area =
$$(3.1416 \times 10 \times 10)$$
 sq. in. = 314.16 sq. in. Ans.

Area =
$$(0.7854 \times 10 \times 10)$$
 sq. ft. = 78.54 sq. ft. Ans.

Area =
$$\left(0.7854 \times \frac{30}{3.1416} \times \frac{30}{3.1416}\right)$$
 sq. in. = 71.620 sq. in. Ans.
9.7854 × $\frac{15}{30}$ × $\frac{15}{30}$ × $\frac{15}{3.1416}$ = $\frac{225}{3.1416}$ = 225 × 0.31831.
 $\frac{225}{159155}$
63662
 $\frac{63662}{71.61975}$

25. A horse is tied by a rope 27.8^m long; over what part of a hektar can he graze?

Area =
$$(3.1416 \times 27.8 \times 27.8)^{qm} = 2427.95^{qm} = 0.2428^{ha}$$
. Ans.

$$\begin{array}{c} 27.8 \\ \hline 27.8 \\ \hline 2224 \\ \hline 1946 \\ \hline 556 \\ \hline 772.84 \\ \hline \hline 231852 \\ \hline \end{array}$$

26. How many square feet in a circle that has a diameter of 173 yd. 1

$$17\frac{2}{3}$$
 yd. = 53 ft.

Area =
$$(0.7854 \times 53 \times 53)$$
 sq. ft. = 2206.1886 sq. ft. Ans.

53	0.7854	
53	2809	
159	70686	
265	62832	
2809	15708	
	2206.1886	

27. How many square feet in a circle that has a circumference of 117 yd.?

$$117 \text{ yd.} = 351 \text{ ft.}$$

$$Diameter = \frac{351}{3.1416} \text{ ft.}$$

$$Area = \left(0.7854 \times \frac{351}{3.1416} \times \frac{351}{3.1416}\right) \text{ sq. ft.} = 9804.0276 \text{ sq. ft.} \quad Ans.$$

$$9.7854 \times \frac{351}{3.1416} \times \frac{351}{3.1416} = \frac{123201}{4} \times \frac{1}{3.1416} = 30800.25 \times 0.31831.$$

$$\frac{0.31831}{30800.25}$$

$$\frac{0.31831}{159155}$$

$$63662$$

$$254648$$

$$\frac{95493}{9804.0275775}$$

28. Find the area of a triangle whose sides are 73 ft., 57 ft., and 48 ft.

The half sum of the sides = $\frac{1}{4}(73 + 57 + 48)$ ft. = 89 ft.

Area =
$$\sqrt{89 \times 16 \times 32 \times 41}$$
 sq. ft. = $\sqrt{1868288}$ sq. ft. = 1366.853 sq. ft. Ans.

1 86 82 88 (1366.853 1____

29. Find the number of hektars in a triangular field whose sides are 37.5^m, 91.7^m, and 78.9^m.

The half sum of the sides = $\frac{1}{4}(37.5 + 91.7 + 78.9)^m = 104.05^m$.

Area =
$$\sqrt{104.05 \times 66.55 \times 12.35 \times 25.15^{qm}} = \sqrt{2150775.55281875^{qm}}$$

= $1466.5^{qm} = 0.1467^{ha}$. Ans.

104.05 85517.914625 66.55 **25**.15 427589573125 52025 85517914625 **52025** 427589573125 62430 62430 171035829250 2150775.55281875 6924.5275 12.35 346226375 2 15 07 75.55 28 18 75(1406.5 207735825 1 138490550 24)115 **6924**5275 96 85517.914625 286) 1907 1716 2926) 19175 17556

30. Find the number of hektars in a triangular field whose sides are 67.5^m, 81.2^m, and 102.7^m.

29325) 161955

146625

The half sum of the sides = $\frac{1}{2}(67.5 + 81.2 + 102.7)^m = 125.7m$. Area = $\sqrt{125.7 \times 58.2 \times 44.5 \times 23^{qm}} = \sqrt{7487659.89^{qm}}$

$$= 2736.3^{qm} = 0.2736^{ha}. Ans.$$

125.7
58.2
2514
10056
6 285
7315.74
44.5
3657870
2926296
2926296
325550.43
23
97665129
65110086

7487659.89

7 48 76 59.89(2736.3 4 47)348 329 543)1976 1629 5466)34759 32796 54723)196389 164169 31. Find the number of acres in a triangular field whose sides are 227 ft., 342 ft., and 416 ft.

The half sum of the sides = $\frac{1}{4}(227 + 342 + 416)$ ft. = 492.5 ft.

Area = $\sqrt{492.5 \times 265.5 \times 150.5 \times 76.5}$ sq. ft. = $\sqrt{1505458178.4375}$ sq. ft.

= 38,800.23 sq. ft. =
$$\frac{38800.23}{43560}$$
 A. = 0.8907 A. Ans.

32. Find the number of acres in a triangular field whose sides are 79.08 ch., 57.03 ch., and 102.19 ch.

The half sum of the sides = $\frac{1}{2}$ (79.08+57.03+102.19) ch. = 119.15 ch.

Area = $\sqrt{119.15 \times 40.07 \times 62.12 \times 16.96}$ sq. ch.

 $=\sqrt{5030031.2603456}$ sq. ch. =2242.77 sq. ch. =224.277 A. Ans.

30492

33. Find the number of square rods in a triangle whose sides at 7 rd. 2 yd.; 6 rd. 5 yd.; and 9 rd. 4½ ft.

7 rd. 2 yd. = 40.5 yd.; 6 rd. 5 yd. = 38 yd.; 9 rd. 4½ ft. = 51 yd.

The half sum of the sides = $\frac{1}{2}(40.5 + 38 + 51)$ yd. = 64.75 yd.

Area =
$$\sqrt{64.75 \times 24.25 \times 26.75 \times 13.75}$$
 sq. yd.
= $\sqrt{577534.58984375}$ sq. yd. = 759.9569 sq. yd.
= $\frac{759.9569}{30.25}$ sq. rd. = 25.12 sq. rd. Ans.

64.75 24.25	57 75 34.58 98 43 75 (759.956 9 49
32375 12950 25900 12950	145)875 725 1509)15034 13581
1670.1875 26.75	15189)145358 136701
78509375 109013125 94211250 81403750	151985)865798 759925 1519906)10587343
42002.515625 13.75	9119436 15199129)146790775
210012578125 294017609375 120007546875 42002515025	136792161 25.12 3025)75995.69 6050
577534.58984375	15495 15125
	3706 3025
	6819 6050
	769

34. One diagonal of a trapezium is 10 rd., and the perpendiculars upon it from the opposite corners are 6 rd. and 8 rd. Find the area.

Area of 1st triangle = $\frac{1}{4}$ (10 × 6) sq. rd. = 30 sq. rd.

Area of 2d triangle = $\frac{1}{4}$ (10 × 8) sq. rd. = 40 sq. rd.

Area of trapezium = 30 sq. rd. + 40 sq. rd. = 70 sq. rd. Ans.

35. Find the area of a lot of land in the shape of a trapezium, if one diagonal is 108 ft., and the perpendiculars upon it from the opposite corners are 55 ft. and 60 ft.

Area of 1st triangle = $\frac{1}{4}$ (108 × 55) sq. ft. = 2970 sq. ft.

Area of 2d triangle = $\frac{1}{4}$ (108 × 60) sq. ft. = 3240 sq. ft.

Area of trapezium = 2970 sq. ft. + 3240 sq. ft. = 6210 sq. ft. Ans.

36. What is the area of the ground covered by a tent, the base of which is a regular heptagon 25 ft. on a side?

Apothem = 1.0382×25 ft. = 25.955 ft.

Perimeter = 7×25 ft. = 175 ft.

Area = $\frac{1}{4}$ (175 × 25.955) sq. ft. = 2271.0625 sq. ft. Ans.

37. How many paving stones will be required to pave a rectangular court 60 ft. long and 40 ft. wide, if each stone is in the shape of a regular hexagon 5 in. on a side?

Area of court = (60×40) sq. ft. = 2400 sq. ft.

Apothem = 0.8660×5 in. = 4.33 in.

Perimeter = 6×5 in. = 30 in.

Area of stone = $\frac{1}{2}$ (30 × 4.33) sq. in. = 64.95 sq. in.

Number of stones =
$$\frac{2400 \times 144}{64.95}$$
 = 5322. Ans.

03.00	
144	5321.
2400	6495)34560000.
57600	32475
288	20850
345600	19485_
	13650
	12990
	6600
	<u>8495</u>

38. At \$225 an acre, what is the value of a field in the shape of a regular pentagon 250 yd. on a side?

Apothem = 0.6882×250 yd. = 172.05 yd.

Perimeter = 5×250 yd. = 1250 yd.

Area = $\frac{1}{4}$ (1250 × 172.05) sq. yd. = 107,531.25 sq. yd. = 22.217 A.

 $1 A. = 160 \times 301 \text{ sq. yd.} = 4840 \text{ sq. yd.}$

39. A rectangular field 100 yd. wide contains 3 A. What is its length?

$$\frac{3\frac{1}{1} \times 4840}{100} = \frac{2\cancel{3} \times \cancel{4840}}{\cancel{8} \times \cancel{100}} = \frac{605}{4} = 151\frac{1}{4}.$$
 151\frac{1}{4} yd. Ans.

 $3\frac{1}{4}$ A. = $3\frac{1}{4}$ × 4840 sq. yd.

40. The dimensions of a rectangle are 45 yd. and 28 yd. What is the length of its diagonal?

$$\sqrt{45^2 + 28^2} = \sqrt{2025 + 784} = \sqrt{2809} = 53.$$

$$28.09(53)$$

$$25$$

$$103)309$$

$$809$$

$$53 \text{ yd. } Ans.$$

41. A field has the shape of a right triangle, and the two legs are 75 yd. and 60 yd., respectively. What decimal of an acre does the field contain?

Area =
$$\frac{1}{4}$$
 (75 × 60) sq. yd. = $\frac{1}{4} \times \frac{75 \times 60}{4840}$ A.
 $\frac{1}{2} \times \frac{15}{75} \times \frac{15}{50} \times \frac{1}{4840} = \frac{225}{484} = 0.46488$. 0.46488 A. Ans.

42. Compare the areas of a square and an equilateral triangle, if the perimeter of each is 60 ft.

Side of square $= \frac{1}{4}$ of 60 ft. = 15 ft.

Area of square = (15×15) sq. ft.

Side of triangle = 20 ft.

Apothem = 0.2887×20 ft.

· Area of triangle = $\frac{1}{4}$ (60 × 0.2887 × 20) sq. ft.

.. area square: area triangle

$$= 15 \times 15 : \frac{1}{2} (60 \times 0.2887 \times 20) = 3 : 2.3096$$
. Ans.

$$\frac{\cancel{13} \times \cancel{15}}{\cancel{39} \times 0.2887 \times \cancel{29}} = \frac{3}{2.3096}.$$

43. Find the area of a field in the shape of a trapezoid, if the altitude is 240 yd., and the parallel sides are 510 yd. and 725 yd., respectively.

Sum of bases = 510 yd. + 725 yd. = 1235 yd.

Area = $\frac{1}{2}$ (1235 × 240) sq. yd. = 148,200 sq. yd. Ans.

44. The legs of a right triangle are each equal to 12 ft. Find the appotential.

45. A city lot in the shape of a right triangle has for its base 119 ft., and for its perpendicular 120 ft. Find the area and the hypotenuse of the lot.

Area = $\frac{1}{2}$ '119 × 120; sq. ft. = 7140 sq. ft. Ans. Hypotenuse = $\sqrt{119^2 + 120^2}$ ft. = $\sqrt{14161 + 14400}$ ft. = $\sqrt{28561}$ ft. = 169 ft. Ans. 2 85 61(169)

46. Find the base and the area of a right triangle, hypotenuse 130 yd., and perpendicular 112 yd.

Base =
$$\sqrt{130^2 - 112^2}$$
 yd. = $\sqrt{16900 - 12544}$ yd. = $\sqrt{4356}$ yd. = 66 yd. Ans.
$$\frac{4356(66)}{36}$$

$$\frac{36}{126)756}$$
756

47. Find the perpendicular and the area of a right triangle, hypotenuse 164 ft., and base 160 ft.

Perpendicular =
$$\sqrt{164^2 - 160^2}$$
 ft. = $\sqrt{26896 - 25600}$ ft. = $\sqrt{1296}$ ft. = 36 ft. Ans.
 $12.96(36)$ $\frac{9}{396}$ $\frac{9}{396}$

Area = $\frac{1}{4}$ (160 × 36) sq. ft. = 2880 sq. ft. Ans.

48. Find the hypotenuse and the area of a right triangle, base 100 yd., and perpendicular 105 yd.

Area = $\frac{1}{2}$ (100 × 105) sq. yd. = 5250 sq. yd. Ans.

49. Find the hypotenuse and the area of a right triangle, base 96 ft., and perpendicular 110 ft.

Area = $\frac{1}{2}$ (259 × 660) sq. yd. = 85,470 sq. yd.

51. A rectangular field is 345 yd. long an is the length of its diagonal?

Diagonal =
$$\sqrt{345^2 + 152^2}$$
 yd. = $\sqrt{119025 + 142129}$ yc 14 21 29(377

52. The legs of a right triangle are 44 ft. 4 in. and 13 ft. 9 in., respectively. Find the length of its hypotenuse.

44 ft. 4 in. =
$$532$$
 in.; 13 ft. 9 in. = 165 in.

Hypotenuse =
$$\sqrt{532^2 + 165^2}$$
 in. = $\sqrt{283024 + 27225}$ in.
= $\sqrt{310249}$ in. = 557 in. = 46 ft. 5 in. Ans.
 $\frac{31\ 02\ 49(557}{25}$
 $\frac{25}{1107)7749}$

53. The hypotenuse of a right triangle is 7 ft. 1 in., and one leg is 6 ft. 5 in. Find the other leg and the area.

7749

7 ft. 1 in. = 85 in.; 6 ft. 5 in. = 77 in.
Leg =
$$\sqrt{85^2 - 77^2}$$
 in. = $\sqrt{7225 - 5929}$ in.
= $\sqrt{1296}$ in. = 36 in. = 3 ft. Ans.
12 96(36
9
66)396
396

Area = $\frac{1}{2}$ (3 × $6\frac{5}{12}$) sq. ft. = 9 \(\frac{5}{8}\) sq. ft. = 9 sq. ft. 90 sq. in. Ans.

54. The hypotenuse of a right triangle is 3 ft. 1 in., and one leg is 2 ft. 11 in. Find the other leg and the area.

3 ft. 1 in.
$$= 37$$
 in.; 2 ft. 11 in. $= 35$ in.

Leg =
$$\sqrt{37^2-35^2}$$
 in. = $\sqrt{1396-1225}$ in. = $\sqrt{144}$ in. = 12 in. = 1 ft. Ans.
Area = $\frac{1}{4}(2\frac{11}{12} \times 1)$ sq. ft. = $1\frac{11}{14}$ sq. ft. = 1 sq. ft. 66 sq. in. Ans.

55. The area of a lot in the shape of a right triangle is 1560 sq. yd., and the base is 80 yd. Find the perpendicular and the hypotenuse.

Perpendicular =
$$\frac{2 \times 1569}{80}$$
 yd. = 39 yd. Ans.

56. The area of a right triangle is 60 sq. in., and one leg is 8 in. Find the hypotenuse and the other leg.

$$Leg = \frac{2 \times \frac{15}{99}}{\frac{9}{2}} in. = 15 in. Ans.$$

Hypotenuse = $\sqrt{16^2 + 8^2}$ in. = $\sqrt{225 + 64}$ in. = $\sqrt{289}$ in. = 17 in. Ans.

57. The length and diagonal of a rectangular field are 60 rd. and 65 rd., respectively. What is its area?

Breadth =
$$\sqrt{65^2 - 60^2}$$
 rd. = $\sqrt{4225 - 3600}$ rd. = $\sqrt{625}$ rd. = 25 rd. Area = (80×25) sq. rd. = 1500 sq. rd. = 9 $\frac{1}{2}$ A. Area.

56. What is the length of a side of a square that contains 390,625 sq ft.?

Side =
$$\sqrt{390625}$$
 ft. = 625 ft. Ans.
39 06 25 (625
36
122)306
244
1245)6225
6225

59. Express to six places of decimals the length of the diagonal of a square in terms of a side.

Diagonal =
$$\sqrt{1^2 + 1^2} = \sqrt{1 + 1} = \sqrt{2} = 1.414213$$
. Ans.

2.00(1.414213

1
24)100
2828)6040
96
5656
281)400
3840
281
2824)11900
10120
11296
8484

60. The hypotenuse of a right triangle is 95 ft., and the two legs are as 3 to 4. Find the legs and the area.

1636

 $(Base)^2 : (Perpendicular)^2 = 3^2 : 4^2 = 9 : 16.$

6040

 $(Base)^2 + (Perpendicular)^2 = 95^2 = 9025.$

$$(Base)^2 = \frac{9}{25}$$
 of $9925 = 3249$. Base = $\sqrt{3249}$ ft. = 57 ft. Ans.

$$(Perpendicular)^2 = \frac{16}{25} \times \frac{361}{9925} = 5776.$$

Perpendicular = $\sqrt{5776}$ ft. = 76 ft. Ans.

Area = $\frac{1}{4}$ (76 × 57) sq. ft. = 2166 sq. ft. Ans.

$$\begin{array}{r}
 2 | 76 \\
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61. St. Mark's Square in Venice has the shape of a trapezoid. The parallel sides are 61 yd. and 90 yd., respectively, and the altitude is 192 yd. What is its area?

Sum of bases = 61 yd. + 90 yd. = 151 yd.

Area = $\frac{1}{4}$ (192 × 151) sq. yd. = 14,496 sq. yd. = 2.995 A. Ans.

12 The perimeter of a regular because in 45 in. Find its area Side (4) 15 in. 7.5 in. Apitiem = 0.2000 a 7.5 in. = 5.406 in. Area - 4/15 / 6/195, wp. in. = 148.1375 mg. in. das

63 A circular pond contains 12 acres. Express its diameter in Inat.

12 / 13,560 sq. ft. Area $\sqrt{0.31831} \times 12 \times 43560$ ft. Hadius $\sqrt{166.387.0032}$ ft. = 407.905 ft. 2×407.905 ft. = 815.81 ft. Ans. Districtor 4235430 12 16 63 87.00 32(407.905 H7120 AHBAH) 16 622720 807)6387 5649 0.31831 8149)73800 622720 73341 636620 815805)4593200 222817 4079025 03002 514175 63662

159166

100387.00320

64. What is the diameter of a circle whose radius is 1262 sq. ft. ? Radius = $\sqrt{0.31831 \times 1262}$ ft. = $\sqrt{401.70722}$ ft. = 20.0426 ft. Diameter = 2 × 20.0426 ft. = 40.085 ft. Ans.

65. What is the diameter of a circle whose area is 2206 sq. ft. ? Radius = $\sqrt{0.31831 \times 2206}$ ft. = $\sqrt{702.19186}$ ft. = 26.4989 ft. Diameter = 2 × 26.4989 ft. = 52.998 ft. Ans.

7 02.19 18 60(26.4989 0.31831 2206 46)302 190986 276 63662 524)2619 63662 702.19186 **2096 5289**)52318 47601 52988)471760 423904 **529969)4785600** 4769721 15879

Exercise 142. Page 327.

1. Find the volume of a triangular prism, height 11 in., and sides of the ends 2 in., 3 in., and 4 in., respectively.

Half sum of sides of base $= \frac{1}{2}(2+3+4)$ in. = 4.5 in.

Area of base = $\sqrt{4.5 \times 2.5 \times 1.5 \times 0.5}$ sq. in = $\sqrt{8.4375}$ sq. in. = 2.9047 sq. in.

Volume = (11×2.9047) cu. in. = 31.9517 cu. in. Ans.

4.5	8.43 75(2.9047
2.5	4
 225	49)443
90	441
•	580 <u>4)27500</u>
11.25	23216
1.5	58087)428400
5625	406609
1125	21791
16.875	
0.5	
8.4375	

2. Find the capacity in bushels of a bin 6 ft. long, the end of which is a square 3 ft. 3 in. on a side.

$$3 \text{ ft. 3 in.} = 3\frac{1}{4} \text{ ft.}$$

$$Volume = (6 \times 3\frac{1}{4} \times 3\frac{1}{4}) \text{ cu. ft.} = \left(\frac{3}{8} \times \frac{13}{4} \times \frac{13}{4}\right) \text{ cu. ft.}$$

$$= \frac{507}{8} \text{ cu. ft.} = 63.375 \text{ cu. ft.}$$

$$\frac{4}{3} \text{ of } 63.375 = 50.7$$

$$\frac{1}{4} \text{ of } 0.01 \text{ of } 50.7 = \frac{0.2535}{50.9535}$$

$$50.9535 \text{ bu. } Ans.$$

3. Find the lateral surface and the volume of a regular pyramid, base a regular hexagon 9 in. on a side, altitude 40 in., and slant height 40.75 in.

Perimeter of base = 6×9 in. = 54 in.

Lateral surface = $\frac{1}{2}$ (54 × 40.75) sq. in. = 1100.25 sq. in. Ans.

Apothem of base = 0.8660×9 in. = 7.794 in.

Area of base = $\frac{1}{2}$ (54 × 7.794) sq. in. = 210.438 sq. in.

$$\begin{array}{r}
2 \boxed{54} \\
27 \\
\hline
27 \\
\hline
54558 \\
\hline
210.438
\end{array}$$

Volume = $\frac{1}{8}$ (210.438 × 40) cu. in. = 2805.84 cu. in. Ans.

4. Find the number of cubic yards in a prism, base a square 200 ft. on a side, height 40 ft.

Volume =
$$(200 \times 200 \times 40)$$
 cu. ft. = 1,600,000 cu. ft.
= $\frac{1600000}{27}$ cu. yd. = $59,259\frac{7}{27}$ cu. yd. Ans.
 59259

5. How many square yards of canvas are required for a conical tent 9 ft. 11 in. high, diameter of base 20 ft.?

9 ft. 11 in.=119 in.; 20 ft.=240 in. Radius=
$$\frac{1}{2}$$
 of 240 in.=120 in. Slant height = $\sqrt{119^2 + 120^2}$ in. = $\sqrt{14161 + 14400}$ in. = $\sqrt{28561}$ in. = 169 in.

Lateral surface = $\frac{1}{4}(3.1416 \times 240 \times 169)$ sq. in. = 63,711.648 sq. in. = $\frac{63711.648}{9 \times 144}$ sq. yd. = 49.16 sq. yd. Ans.

2 240	3.1416	144	49.160
120	120	9	1296)63711.648
	628320	1296	<u>5184</u>
	31416		11871
	376.992		11664
	169		2076
	3392928		1296
	2261952		7804
	376992		7776
•	63711.648		288

6. Find the volume and the lateral surface of a frustum of a regular pyramid, bases squares 24 in. and 12 in. on a side, respectively, altitude 174 in., slant height 184 in.

Area of lower base = (2×2) sq. ft. = 4 sq. ft.

Area of upper base = (1×1) sq. ft. = 1 sq. ft.

$$\sqrt{4\times 1}=\sqrt{4}=2.$$

Volume = $\frac{1}{3} \times \frac{17\frac{1}{2}}{12} (4 + 1 + 2)$ cu. ft. = $\left(\frac{1}{3} \times \frac{17\frac{1}{2}}{12} \times 7\right)$ cu. ft. = $3\frac{29}{72}$ cu. ft. = 3 cu. ft. 696 cu. in. Ans.

$$\frac{1}{8} \times \frac{35}{2} \times \frac{1}{12} \times 7 = \frac{245}{72} = 3\frac{39}{2}.$$

Perimeter of lower base $= 4 \times 2$ ft. = 8 ft.

Perimeter of upper base $= 4 \times 1$ ft. = 4 ft.

Half sum of perimeters of bases = $\frac{1}{4}(8+4)$ ft. = 6 ft.

Lateral surface
$$=\frac{1}{2}\left(6 \times \frac{18\frac{1}{2}}{12}\right)$$
 sq. ft. =4 sq. ft. 90 sq. in. Ans. $\frac{1}{2} \times 6 \times \frac{18\frac{1}{2}}{12} = \frac{1}{2} \times \beta \times \frac{37}{2} \times \frac{1}{12} = \frac{37}{8} = 4\frac{5}{4}$.

7. Find the volume and the lateral surface of a frustum of a right cone, radii of bases 50cm and 30cm, respectively, altitude 48cm, and slant height 52cm.

Area of lower base = $(3.1416 \times 50^2)^{\text{qcm}}$. Area of upper base = $(3.1416 \times 30^2)^{\text{qcm}}$. Square root of product of areas of bases

$$=\sqrt{3.1416\times50^2\times3.1416\times30^2}=3.1416\times50\times30=3.1416\times1500.$$

Volume =
$$\frac{1}{8} \times 48 \times (3.1416 \times 2500 + 3.1416 \times 900 + 3.1416 \times 1500)^{\text{ccm}}$$

= $\left[\frac{1}{8} \times 48 \times 3.1416 \times (2500 + 900 + 1500)\right]^{\text{ccm}}$
= $\left(\frac{1}{8} \times 48 \times 3.1416 \times 4900\right)^{\text{ccm}} = 24,630.144^{\text{ccm}}$. Ans.

Perimeter of lower base = $3.1416 \times 100^{\text{cm}} = 314.16^{\text{cm}}$. Perimeter of upper base = $3.1416 \times 60^{\text{cm}} = 188.496^{\text{cm}}$. Half sum of perimeters of bases = $\frac{1}{4}(314.16 + 188.496)^{\text{cm}} = 251.328^{\text{cm}}$. Lateral surface = $\frac{1}{4}(251.328 \times 52)^{\text{qcm}} = 6534.528^{\text{qcm}}$. Ans.

8. Find the volume and the surface of a sphere whose diameter is 17.2cm.

Surface = $(3.1416 \times 17.2 \times 17.2)^{\text{qcm}} = 929.411^{\text{qcm}}$. Ans.

Volume = $(\frac{1}{6} \times 3.1416 \times 17.2 \times 17.2 \times 17.2)^{ccm} = 26,643.114^{ccm}$. Ans.

· ·		
17.2	295.84	
17.2	3.1416	
344	177504	
1204	29584	
	118336	
172	29584	
295.84	88752	
	929.410944	
	28	
<i>0</i> 1 1 7 0	619607296	
6 <u>172</u>	7435287552	
283	1858821888	
	26643,118728	

9. A right cylinder is 3 ft. 2 in. in diameter and 4 ft. 6 in. high Find its volume and its lateral surface.

3 ft. 2 in. =
$$3\frac{1}{6}$$
 ft.; 4 ft. 6 in. = $4\frac{1}{4}$ ft.

Radius = $\frac{1}{4}$ of $3\frac{1}{6}$ ft. = $1\frac{7}{11}$ ft.

Volume = $(4\frac{1}{4} \times 3.1416 \times 1\frac{7}{12} \times 1\frac{7}{12})$ cu. ft.

$$= \left(\frac{3}{2} \times 3.1418 \times \frac{19}{12} \times \frac{19}{12}\right) \text{ cu. ft.} = 35.4412 \text{ cu. ft.} \text{ Ans.}$$

Lateral surface = $(4\frac{1}{2} \times 3.1416 \times 3\frac{1}{6})$ sq. ft.

$$= \left(\frac{9}{2} \times 3.1416 \times \frac{19}{6}\right) \text{ sq. ft.} = 44.7678 \text{ sq. ft.} \text{ Ans.}$$

\ <i>F</i>	y /	
19	19	0.2618
19	9	171
171	171	2618
19		18326
361		2618
3		44.7678
1083		
0.1309		
9747		
3249		
1083		
4 141.7647		

10. Find the length of an edge of a cubical vessel that will hold a ton of water.

1 cu. ft. of water weighs 621 lb.

35.4412

Therefore, 1 lb. of water occupies $\frac{1}{62\frac{1}{4}}$ cu. ft. and 2000 lb. occupy $\left(2000 \times \frac{1}{62\frac{1}{4}}\right)$ cu. ft. $= \left(\frac{16}{2999} \times \frac{2}{125}\right)$ cu. ft. = 32 cu. ft.

An edge of the vessel therefore = $\sqrt[8]{32}$ ft. = 3.17480 ft. Ans.

$$32.000(3.17480)$$

$$3 \times 30^{2} = 2700$$

$$3 \times (30 \times 1) = 90$$

$$1^{2} = \frac{1}{2791}$$

$$3 \times 310^{2} = 288300$$

$$3 \times (310 \times 7) = 6510$$

$$7^{2} = \frac{49}{294859}$$

$$\frac{6559}{294859}$$

$$3 \times 3170^{2} = 30146700$$

$$3 \times (3170 \times 4) = 38040$$

$$4^{2} = \frac{16}{30184756}$$

$$\frac{38056}{38056}$$

$$2 \times 3174^{2} = 30222828$$

$$\frac{120739024}{242479760}$$

$$\frac{120739024}{242479760}$$

11. A rectangular tank 6 ft. long and 4½ ft. wide holds 108 cu. ft. of water. What is the height of the tank?

Height =
$$\left(\frac{108}{6 \times 4\frac{1}{2}}\right)$$
 ft. = $\frac{\cancel{108} \times \cancel{2}}{\cancel{6} \times \cancel{9}}$ ft. = 4 ft. Ans.

12. Find the total surface of a regular pyramid, base a square 5 ft. on a side, and slant height 20 ft.

Perimeter of base = 4×5 ft. = 20 ft.

Lateral surface = $\frac{1}{4}$ (20 × 20) sq. ft. = 200 sq. ft.

Area of base = (5×5) sq. ft. = 25 sq. ft.

Total surface = 200 sq. ft. + 25 sq. ft. = 225 sq. ft. Ans.

13. The circumference of the base of a right cone is 12 ft., and the height of the cone is 12 ft. Find the volume.

Radius of base =
$$\frac{12}{2 \times 3.1416}$$

Area of base =
$$\left(3.1416 \times \frac{12}{2 \times 3.1416} \times \frac{12}{2 \times 3.1416}\right)$$
 sq. ft.

Volume =
$$\left(\frac{1}{3} \times 12 \times 3.1416 \times \frac{12}{2 \times 3.1416} \times \frac{12}{2 \times 3.1416}\right)$$
 cu. ft.
= 45.83664 cu. ft. Ans.
 $\frac{2}{4}$
 $\frac{1}{3} \times 12 \times 3.1416 \times \frac{12}{2 \times 3.1416} \times \frac{12}{2 \times 3.1416} = \frac{144}{3.1416}$
= $144 \times 0.31831 = 45.83664$.
0.31831
 $\frac{144}{127324}$
 $\frac{127324}{4}$
 $\frac{31831}{45.83664}$

14. Find the surface of a megaphone in the shape of a frustum of a right cone, diameters of the upper and lower bases 24 in. and 3 in., respectively, slant height 30 in.

Perimeter of upper base = 3.1416×3 in.

Perimeter of lower base = 3.1416×24 in.

Sum of perimeters of bases = 3.1416×27 in.

Lateral surface = $\frac{1}{2}(3.1416 \times 27 \times 30)$ sq. in.

= 1272.348 sq. in. = 8 sq. ft. 120.348 sq. in. Ans.

$$\begin{array}{ccc}
27 & 3.1416 \\
30 & 405 \\
2 \overline{\smash{\big)}\,810} & 157080 \\
405 & \underline{125664} \\
1272.3480
\end{array}$$

15. Find the difference between the volume of a frustum of a regular pyramid, bases squares 8 ft. and 6 ft., respectively, on a side, and altitude 9 ft., and the volume of a right prism, base a square 7 ft. on a side, altitude 9 ft.

Area of upper base = (6×6) sq. ft. = 36 sq. ft.

Area of lower base = (8×8) sq. ft. = 64 sq. ft.

Square root of product of areas of bases = $\sqrt{36 \times 64} = 6 \times 8 = 48$. Volume of frustum of pyramid

$$=\frac{1}{3} \times 9 \times (36 + 64 + 48)$$
 cu. ft. $=\left(\frac{1}{3} \times 9 \times 148\right)$ cu. ft. $=$ 444 cu. ft.

Volume of prism = $(9 \times 7 \times 7)$ cu. ft. = 441 cu. ft.

Therefore, the frustum of the pyramid is the larger by

444 cu. ft. - 441 cu. ft. = 3 cu. ft. Ans.

16. Find the surface and the volume of a sphere whose diameter is 28 in.

Surface = $(3.1416 \times 28 \times 28)$ sq. in. = $\cdot 2463.0144$ sq. in. Ans. Volume = $(\frac{1}{4} \times 3.1416 \times 28 \times 28 \times 28)$ cu. in. = 11,494.0672 cu. in. Ans.

28	3,1416
28	784
$\overline{224}$	125664
56	251328
784	219912
,,,,	2463.0144
	43
6 28	16420096
43	98520576
•	11494,0672

17. Find the ratio of the volume of a cube of wood 15 in. on an edge to the volume of the largest sphere that can be turned from it. Find the ratio of their surfaces.

$$\frac{\text{Volume of cube}}{\text{Volume of sphere}} = \frac{15^8}{0.5236 \times 15^8} = \frac{1}{0.5236}. \quad Ans.$$

$$\frac{\text{Surface of cube}}{\text{Surface of sphere}} = \frac{6 \times 15^2}{3.1416 \times 15^2} = \frac{6}{3.1416} = \frac{1}{0.5236}. \quad Ans.$$

18. Find the ratio of the volume of a cube of wood to the volume of the largest right cylinder that can be turned from it. Find the ratio of their surfaces.

$$\frac{\text{Volume of cube}}{\text{Volume of cylinder}} = \frac{18}{1 \times 3.1416 \times \frac{1}{2} \times \frac{1}{2}} = \frac{1}{0.7854}. \quad Ans.$$

$$\frac{\text{Surface of cube}}{\text{Surface of cylinder}} = \frac{6 \times 1^{2}}{2 \times 3.1416 \times (\frac{1}{2})^{2} + 3.1416 \times 1}$$

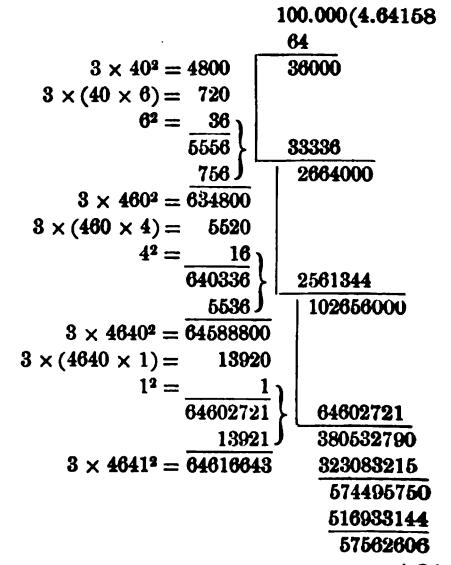
$$= \frac{6}{\frac{1}{2} \times 3.1416} = \frac{1}{\frac{1}{4} \times 3.1416} = \frac{1}{0.7854}. \quad Ans.$$

19. Find the ratio of the volume of a right cylinder of wood to the volume of the largest right cone that can be turned from it. Find the ratio of their lateral surfaces.

$$\frac{\text{Volume of cylinder}}{\text{Volume of cone}} = \frac{1 \times 3.1416 \times 1^2}{\frac{1}{8} \times 1 \times 3.1416 \times 1^2} = \frac{1}{3}. \text{ Ans.}$$

$$\frac{\text{Lateral surface of cylinder}}{\text{Lateral surface of cone}} = \frac{1 \times 3.1416 \times 1}{\frac{1}{8} \times 1 \times 3.1416 \times 1} = \frac{1}{2}. \text{ Ans.}$$

20. Find the length of an edge of a cube that contains 100 cu. in.



4.64159 in. Ans.

21. The Great Pyramid of Egypt was originally made in the form of a regular pyramid, altitude 480½ ft., and base a square 764 ft. on a side. Find in acres the area of the ground covered by the pyramid. Find in cubic yards the volume, and in square yards the lateral surface of the pyramid.

Area of base =
$$(764 \times 764)$$
 sq. ft. = $\frac{191 \quad 382}{194 \times 764}$ A. = $\frac{72962}{5445}$ A. = $\frac{132177}{5445}$ A. = 13.4 A. Ans. Volume = $(\frac{1}{8} \times 764 \times 764 \times 480\frac{3}{4})$ cu. ft. = $\frac{1}{8} \times \frac{764 \times 764 \times 480\frac{3}{4}}{27}$ cu. yd. = $\frac{191 \quad 641}{3 \times 27 \times 4}$ cu. yd. = $\frac{93537284}{27}$ cu. yd. = $\frac{3,464,343\frac{3}{27}}{27}$ cu. yd. Ans.

Slant height =
$$\sqrt{480.75^2 + 382^2}$$
 ft. = $\sqrt{231120.5625 + 145924}$ ft. = $\sqrt{377044.5625}$ ft. = 614.04 ft.

Lateral surface =
$$(\frac{1}{4} \times 4 \times 764 \times 614.04)$$
 sq. ft. = $\frac{2 \times 764 \times 614.04}{9}$ sq. yd. = $\frac{312751.04}{3}$ sq. yd. = 104,250.35 sq. yd. Ans.

22. The mast of a ship is 80 ft. high, and the diameters of its ends are 4 ft. 6 in. and 2 ft., respectively. Find its value at 75 cents a cubic foot.

Area of lower base = (0.7854×4.5^2) sq. ft. = (0.7854×20.25) sq. ft. Area of upper base = (0.7854×2^2) sq. ft. = (0.7854×4) sq. ft. Square root of product of areas of bases

$$= \sqrt{0.7854 \times 20.25 \times 0.7854 \times 4} \text{ sq. ft.} = (0.7854 \times 4.5 \times 2) \text{ sq. ft.}$$
$$= (0.7854 \times 9) \text{ sq. ft.}$$

Sum of areas of bases plus square root of their product

=
$$(0.7854 \times 20.25 + 0.7854 \times 4 + 0.7854 \times 9)$$
 sq. ft.
= $0.7854 \times (20.25 + 4 + 9)$ sq. ft. = (0.7854×33.25) sq. ft.

Volume = $(\frac{1}{3} \times 80 \times 0.7854 \times 33.25)$ cu. ft. = 696.388 cu. ft.

$$\begin{array}{r}
33.25 \\
80 \\
\hline
2660.00 \\
\hline
2660 \\
\hline
157080 \\
\underline{5236} \\
696.388
\end{array}$$

Value = $696.388 \times \$0.75 = \522.29 . Ans.

$$696.388 \\
0.75 \\
\hline
3481940 \\
4874716 \\
\hline
522.29100$$

23. A spherical shot 6 in. in diameter is melted and cast into a cylinder 3 in. in diameter. What is the height of this cylinder?

Volume of shot $=(0.5236 \times 6^8)$ cu. in.

Volume of cylinder = (height $\times 0.7854 \times 3^2$) cu. in.

Height of cylinder $=\frac{0.5236 \times 6^3}{0.7854 \times 3^2}$ in. = 16 in. Ans.

$$\frac{\cancel{9.5236} \times \cancel{9} \times \cancel{9} \times \cancel{9}}{\cancel{9.7854} \times \cancel{3} \times \cancel{3}} = 16.$$

24. A cylindrical pail 14 in. high holds 2 cu. ft. of water. What is the diameter of its base?

Volume = 2 cu. ft. = (2×1728) cu. in.

Volume = $[14 \times 0.7854 \times (diameter)^2]$ cu. in.

Diameter = $\sqrt{\frac{2 \times 1728}{14 \times 0.7854}}$ in. = $\sqrt{314.3075}$ in. = 17.73 in. Ans.

$$\frac{2 \times 1728}{14 \times 0.7854} = \frac{2 \times 1728 \times 10000}{\cancel{14} \times \cancel{7854}} = \frac{2880000}{9163} = 314.3075.$$

35448)309100 283584

25516

25. A regular pyramid 14 in. high has for its base an equilateral triangle 6 in. on a side. What is its volume?

Half sum of sides of base $= \frac{1}{2}(6+6+6)$ in. = 9 in.

Area of base = $\sqrt{9 \times 3 \times 3 \times 3}$ sq. in. = $\sqrt{243}$ sq. in. = 15.588 sq. in. Volume = ($\frac{1}{4} \times 14 \times 15.588$) cu. in. = 72.744 cu. in. Ans.

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26. A right prism 8 in. high has for its base a trapezoid whose altitude is 4 in., and whose parallel sides are 5 in. and 3 in., respectively. What is the volume of the prism in cubic inches?

Sum of bases of trapezoid = 5 in. + 3 in. = 8 in. Area of base = $\frac{1}{2}(8 \times 4)$ sq. in. = 16 sq. in. Volume = (8×16) cu. in. = 128 cu. in. Ans.

27. A rectangular room is 18 ft. long, 16 ft. wide, and 12 ft. high. What is the distance from the upper right-hand corner to the opposite lower left-hand corner?

Diagonal of floor = $\sqrt{18^2 + 16^2}$ ft.

Diagonal of room =
$$\sqrt{(\sqrt{18^2 + 16^2})^2 + 12^2}$$
 ft. = $\sqrt{18^2 + 16^2 + 12^2}$ ft. = $\sqrt{324 + 256 + 144}$ ft. = $\sqrt{724}$ ft. = 26.907 ft. Ans.

28. A conical spire 40 ft. high has a base 15 ft. in diameter. Find the cost at 5 cents a square inch of gilding the spire.

Slant height =
$$\sqrt{40^2 + 7.5^2}$$
 ft. = $\sqrt{1600 + 56.25}$ ft. = $\sqrt{1656.25}$ ft. = 40.7 ft. = 40.7 ft. $\frac{16}{807)5625}$

Circumference of base = 3.1416×15 ft.

Lateral surface = $(\frac{1}{4} \times 40.7 \times 3.1416 \times 15)$ sq. ft. = 958.9734 sq. ft.

2 3.14	40.7
1.570	15
610	2035
785	407
15708	610.5
9424 8	010.0
958.973	

0.05 per sq. in. = 144×0.05 per sq. ft. = 7.20 per sq. ft.

\$ 6904.61. Ans.

Exercise 143. Page 330.

1. If the diameter of the moon is reckoned at 2000 mi., and that of the earth at 8000 mi., find the ratio of their surfaces and the ratio of their volumes.

 $2000^2:8000^2=1^2:4^2=1:16$. Ans. $2000^8:8000^8=1^8:4^8=1:64$. Ans.

2. If the diameters of two circles are 20 in. and 40 in., find the ratio of their circumferences and of their areas.

$$20:40=1:2.$$
 Ans. $20^2:40^2=1^2:2^2=1:4.$ Ans.

3. If the areas of two circles are 8000 sq. in. and 36,000 sq. in., respectively, find the ratio of their diameters.

$$\sqrt{8000}: \sqrt{36000} = \sqrt{4}: \sqrt{18} = 2:4.242 = 1:2.121$$
. Ans.
$$18.00(4.242)$$

$$16$$

$$82)200$$

$$164$$

$$844)3600$$

$$8376$$

$$8482)22400$$

$$16964$$

$$5436$$

4. If the volumes of two spheres are 100 cu. in. and 1000 cu. in., respectively, find the ratio of their diameters.

$$\sqrt[8]{100} : \sqrt[8]{1000} = \sqrt[8]{1} : \sqrt[8]{10} = 1 : 2.154. \ Ans.$$

$$10.000(2.154)$$

$$8$$

$$2000$$

$$3 \times (20 \times 1) = 60$$

$$1^2 = \frac{1}{1261}$$

$$\frac{61}{1261}$$

$$3 \times 210^2 = 132300$$

$$3 \times (210 \times 5) = 3150$$

$$5^2 = \frac{25}{135475}$$

$$\frac{3175}{3175}$$

$$3 \times 215^2 = 138675$$

$$\frac{677375}{616250}$$

$$\frac{61550}{61550}$$

5. If an ox 7 ft. in girth weighs 1500 lb., what will be the girth of a similar ox that weighs 2500 lb.?

$$\sqrt[3]{1500}$$
: $\sqrt[3]{2500}$ = 7 ft. : ?.
 $\sqrt[3]{1}$: $\sqrt[3]{\frac{1500}{1500}}$ = 7 ft. : ?.
 $\sqrt[3]{1}$: $\sqrt[3]{1\frac{3}{2}}$ = 7 ft. : ?.
1:1.185 = 7 ft. : ?.
1.185 × 7 ft. = 8.295 ft. 8.3 ft. Ans.

$$3 \times 10^{2} = 300$$

$$3 \times (10 \times 1) = 30$$

$$1^{2} = \frac{1}{331}$$

$$3 \times 110^{2} = 36300$$

$$3 \times (110 \times 8) = 2640$$

$$8^{2} = \frac{64}{39004}$$

$$3 \times 118^{2} = 41772$$

$$3 \times 118^{2} = 41772$$

$$208860$$

$$27486$$

6. The surface of a pyramid is 560 sq. in. What is the surface of a similar pyramid whose volume is 27 times as great?

$$\sqrt[3]{1}: \sqrt[3]{27} = 1:3.$$

 $1^2:3^2=560$ sq. in. :?.

1:9=560 sq. in.:?. $9\times 560 \text{ sq. in.}=5040 \text{ sq. in.}$ Ans.

7. The volume of a pyramid is 1331 cu. in. What is the volume of a similar pyramid whose surface is 4 times as great?

$$\sqrt{1}:\sqrt{4}=1:2.$$

 $1^8:2^8=1331$ cu. in. :?.

1:8=1331 cu. in.: ?. 8×1331 cu. in. = 10,648 cu. in. Ans.

8. If a well-proportioned man 5 ft. 10 in. high weighs 160 lb., what should a man 6 ft. high weigh, to the nearest tenth of a pound? What should be the height, to the nearest tenth of an inch, of a man who weighs 210 lb.?

$$70^8:72^8=160$$
 lb. :?.

343000:373248=160 lb.:?

$$\frac{373248 \times 160 \text{ lb.}}{343000} = \frac{1492992}{8575} \text{ lb.} = 174.1 \text{ lb.} \quad Ans.$$

$$\sqrt[3]{160}$$
: $\sqrt[3]{210}$ = 70 in. :?.
 $\sqrt[3]{1}$: $\sqrt[3]{1.3125}$ = 70 in. :?.
 $1:1.095$ = 70 in. :?.
 $\frac{1.095 \times 70 \text{ in.}}{1}$ = 76.65 in.

76.6 in. = 6 ft. 4.6 in. Ans.

$$3 \times 100^{2} = 30000$$

$$3 \times (100 \times 9) = 2700$$

$$9^{2} = \frac{81}{32781}$$

$$\frac{2781}{35643}$$

$$3 \times 109^{2} = \frac{35643}{35643}$$

9. A three-gallon jug and a one-gallon jug are similar. Find to three decimals the ratio of their diameters.

$$\sqrt[3]{3} : \sqrt[3]{1} = \sqrt[3]{1} : \sqrt[3]{\frac{1}{3}} = 1 : 0.693. \text{ Ans.}$$

$$0.333 \ 333 \ 333 \ (0.693)$$

$$216$$

$$3 \times (60 \times 9) = 1620$$

$$9^{2} = \underbrace{81}_{12501}$$

$$112509$$

$$3 \times (690 \times 3) = 6210$$

$$3^{2} = \underbrace{9}_{1434519}$$

$$4303557$$

$$520776$$

10. Two hills have exactly the same shape; one is 900 ft. high, the other 1200 ft. Find the ratio of their surfaces, and also the ratio of their volumes.

 $900^2:1200^2=3^2:4^2=9:16$. Ans.

 $900^8:1200^8=3^8:4^8=27:64$. Ans.

11. A ball 3 in. in diameter weighs 4 lb.; another ball of the same metal weighs 9 lb. Find the diameter of the second ball to the nearest thousandth of an inch.

$$\sqrt[8]{4}$$
: $\sqrt[8]{9} = 3$ in. : ?. $\sqrt[8]{1}$: $\sqrt[8]{2.25} = 3$ in. : ?.

1:1.3103=3 in.:?.

 1.3103×3 in. = 3.9309 in.

3.931 in. Ars.

$$3 \times 10^{2} = 300$$

$$3 \times (10 \times 3) = 90$$

$$3^{2} = \frac{9}{399}$$

$$3 \times 130^{2} = 50700$$

$$3 \times (130 \times 1) = 390$$

$$1^{2} = \frac{1}{51091}$$

$$3 \times 13100^{2} = 514830000$$

$$3 \times (13100 \times 3) = 117900$$

$$3^{2} = \frac{9}{514947909}$$

$$1544843727$$

$$364156273$$

12. If Apollo's altar were a perfect cube 10 ft. on an edge, what would be the edge of a new cubical altar containing twice as much stone?

$$\sqrt[3]{1}:\sqrt[3]{2}=10 \text{ ft.}:?.$$

1:1.2599=10 ft.:?.

 1.2599×10 ft. = 12.599 ft. = 12 ft. 7.188 in. Ans.

13. A man standing 40 ft. from a building 24 ft. wide observed that, when he closed one eye, the width of the building hid from view 90 rd. of fence which was parallel to the width of the building. Find the distance from the eye of the observer to the fence.

24: 40 = 90 rd.:?
$$\frac{\frac{5}{40} \times \frac{30}{90} \text{ rd.}}{\frac{24}{3}} = 150 \text{ rd. } Ans.$$

14. A bushel measure and a peck measure are of the same shape. Find the ratio of their heights.

1 bu. = 4 pk.
$$\sqrt[3]{4} : \sqrt[3]{1} = \sqrt[3]{1} : \sqrt[3]{0.25} = 1 : 0.63$$
. Ans.
$$0.250\ 000\ (0.63)$$

$$216$$

$$3 \times 60^{2} = 10800$$

$$3 \times (60 \times 3) = 540$$

$$3^{2} = 9$$

$$11349$$

$$34047$$

15. If the height and the diameter of a cylinder are both doubled, in what ratio is the volume altered?

Volume = height \times 0.7854 \times diameter \times diameter.

()f the larger cylinder the volume = twice the height \times 0.7854 \times twice the diameter \times twice the diameter.

Therefore, the larger cylinder is 8 times the smaller.

Exercise 144. Page 334.

1. Change 1^8 , 1^8 , 1^{29} , 1^{35} to continued fractions.

ge
$$\frac{3}{11}$$
, $\frac{1}{13}$, $\frac{1}{13}$, $\frac{1}{13}$, $\frac{2}{13}$, $\frac{9}{2}$)3(1 $\frac{2}{1}$)2(2 $\frac{2}{2}$

$$\therefore \frac{1}{11} = \frac{1}{3 + \frac{1}{1 + \frac{1}{2}}} Ans.$$

$$\therefore \frac{1}{3} = \frac{1}{5 + \frac{1}{1 + \frac{1}{3 + \frac{1}{3}}}} Ans.$$

$$\begin{array}{c}
20)127(4) \\
116 \\
\hline
11)29(2) \\
\underline{22} \\
7)11(1) \\
\underline{7} \\
4)7(1) \\
\underline{4} \\
3)4(1) \\
\underline{3} \\
1)3(3) \\
\underline{3} \\
2
\end{array}$$

$$\therefore \frac{29}{127} = \frac{1}{4 + \frac{1}{2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{3}}}}} Ans.$$

$$\begin{array}{l} {}^{135}_{64} = 2\frac{7}{64}.\\ \\ {}^{135}_{64} = 2 + \frac{1}{9 + \frac{1}{7}} \text{ Ans.} \end{array}$$

2. Find the approximate values of $\frac{29}{29}$; $\frac{28}{47}$; $\frac{78}{85}$.

$$\frac{1}{1})6(6)$$

$$\frac{6}{2}$$

$$\frac{5}{47} = 1\frac{5}{47}.$$

$$1 = 1.$$

$$\frac{6)47}{42}$$

$$\frac{42}{5})6(1$$

$$\frac{5}{1})5(5$$

$$\frac{5}{1})5(5$$

$$\frac{5}{1})\frac{5}{5}$$

$$\frac{5}{1}$$

$$\frac{\frac{1}{1} = 1}{\frac{1}{1 + \frac{1}{6}}} = \frac{6}{7}$$

$$\frac{\frac{1}{1 + \frac{1}{6}} = \frac{6}{7}}{\frac{1}{1 + \frac{1}{6 + \frac{1}{1}}}} = \frac{\frac{44}{51}}{\frac{1}{1 + \frac{1}{1}}} = \frac{\frac{19}{22}}{\frac{1}{1 + \frac{1}{1}}}$$

$$\frac{1}{1 + \frac{1}{6 + \frac{1}{3}}} = \frac{22}{22}.$$

$$\frac{1}{1 + \frac{1}{6 + \frac{1}{3}}} = \frac{25}{29}.$$

$$\frac{1}{1 + \frac{1}{6 + \frac{1}{3 + \frac{1}{1}}}} = \frac{25}{29}.$$

$$1, \frac{2}{3}, \frac{19}{23}, \frac{25}{35}, \frac{44}{51}, \frac{69}{55}. Ans.$$

$$1, \frac{1}{3}, \frac{19}{22}, \frac{25}{35}, \frac{44}{51}, \frac{69}{55}. Ans.$$

Find a series of fractions approximating to 0.236; 0.2361; 1.609.

$$0.236 = \frac{236}{1000} = \frac{59}{250}.$$

$$\begin{array}{c} \frac{50}{10} = \frac{59}{150}, \\ \therefore \frac{59}{150} = \frac{1}{4 + \frac{1}{4 + \frac{1}{1 + \frac{1}{2}}}} \\ & \frac{1}{1 + \frac{1}{2}} \end{array}$$

$$\frac{1}{4} = \frac{1}{4}$$

$$\frac{1}{4+\frac{1}{4}} = \frac{4}{17}$$

$$\frac{1}{4 + \frac{1}{4 + \frac{1}{1}}} = \frac{21}{89}$$

$$\frac{1}{4+\frac{1}{4+\frac{1}{4}}}=\frac{17}{72}.$$

$$\frac{1}{4}, \frac{1}{17}, \frac{1}{12}, \frac{1}{12}. \quad Ans.$$

$$0.2361 = \frac{10000}{10000}.$$

$$\frac{1}{10000} = \frac{1}{4 + \frac{1}{4 + \frac{1}{17 + \frac{1}{8}}}}$$
17

$$\frac{\frac{1}{4} = \frac{1}{4}}{\frac{1}{4} + \frac{1}{4}} = \frac{4}{17}.$$

$$\frac{1}{4 + \frac{1}{4 + \frac{1}{4 + \frac{1}{17}}}} = \frac{293}{1241}$$

$$\frac{1}{4+\frac{1}{4+\frac{1}{4}}}=\frac{17}{72}.$$

$$1.609 = 1 + \frac{609}{1000}.$$

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$$1.609 = 1 + \frac{405}{1000}.$$

$$609)1000(1 \\ 0.09 = 1 + \frac{405}{1000}.$$

$$1 + \frac{409}{1000} = 1 + \frac{1}{1 + \frac{1$$

$$1 + \frac{1}{1} = 2.$$

$$1 + \frac{1}{1 + \frac{1}{1}} = \frac{3}{2}.$$

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{5}{3}$$

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}} = \frac{8}{5}.$$

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{0}}}}} = \frac{29}{18}.$$

$$1 + \frac{1}{1 + \frac{1}{3}}$$

$$1 + \frac{1}{1 +$$

$$1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{5}}}}} = \frac{214}{133}. \qquad 1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{5}}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{5}}}$$

$$1 + \frac{1}{1$$

Find a series of fractions approximating to 0.382; 1.732; 0.6253.

$$0.382 = \frac{143}{1835} = \frac{11}{11}$$

$$\frac{\frac{1}{2} = \frac{1}{2}}{\frac{1}{2 + \frac{1}{1}}} = \frac{1}{3}$$

$$\frac{\frac{1}{2 + \frac{1}{1}} = \frac{2}{5}}{\frac{1}{2 + \frac{1}{1}}} = \frac{3}{8}$$

$$\frac{\frac{1}{2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}} = \frac{5}{13}.$$

$$\frac{\frac{1}{2 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}}} = \frac{8}{21}.$$



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$$\frac{1}{2 + \frac{1}{1 +$$

1, 1, 5, 1, 4, 4, 11, 11, 14. Ans.

$$1.732 = 1\frac{183}{183}.$$

$$183)250(1)$$

$$\frac{183}{67)183(2)}$$

$$\frac{134}{49)67(1)}$$

$$\frac{49}{18)49(2)}$$

$$\frac{36}{13)18(1)}$$

$$\frac{13}{5)13(2)}$$

$$\frac{10}{3)5(1)}$$

$$\frac{3}{2})3(1)$$

$$\frac{2}{1}(2)$$

$$\frac{2}{2}$$

$$1 + \frac{1}{1} = 2. \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}} = \frac{71}{41}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{5}{3}. \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}}$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1}}} = \frac{7}{4} \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}} = \frac{97}{56}.$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}} = \frac{19}{11}. \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}} = \frac{168}{97}.$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}}}} = \frac{26}{15}. \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}} = \frac{168}{97}.$$

$$1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2}}}}}} = \frac{26}{15}. \qquad 1 + \frac{1}{1 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 +$$

$$\frac{\frac{1}{1}}{1 + \frac{1}{1}} = \frac{1}{2}.$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{1}}}=\frac{2}{3}.$$

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{2}}}} = \frac{5}{8}.$$

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{2+\frac{1}{51}}}}} = \frac{\frac{257}{411}}{\frac{2}{1+\frac{1}{51}}}$$

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{2+\frac{1}{51+\frac{1}{1}}}}}} = \frac{262}{419}.$$

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{2+\frac{1}{51+\frac{1}{1+\frac{1}{2}}}}}} = \frac{781}{1249}.$$

$$\frac{1}{1+\frac{1}{2}} = \frac{257}{411}.$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{2}}} = \frac{257}{411}.$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{2}}} = \frac{1824}{2917}.$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{2}}} = \frac{1824}{2917}.$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{2}}} = \frac{1}{1+\frac{1}{2}}$$

1, \frac{1}{2}, \frac{2}{3}, \frac{2}{6}, \frac{257}{417}, \frac{262}{419}, \frac{751}{1249}, \frac{1624}{2677}. Ans.

5. Find the approximate values of $\frac{17}{45}$; $\frac{917}{557}$; $\frac{711}{513}$; $\frac{987}{113}$.

of
$$\frac{171}{457}$$
; $\frac{618}{757}$; $\frac{711}{818}$; $\frac{987}{118}$.

$$\therefore \frac{177}{457} = \frac{1}{2 + \frac{1}{1 + \frac{1}{2} + \frac{1}{18 + \frac{1}{1 + \frac{1}{2}}}}$$

$$\frac{1}{2} = \frac{1}{2}.$$

$$\frac{1}{2+\frac{1}{3}}=\frac{1}{3}$$

$$\frac{\frac{1}{2 + \frac{1}{1 + \frac{1}{2}}} = \frac{3}{8}.$$

$$\frac{\frac{1}{2 + \frac{1}{1 + \frac{1}{2}}} = \frac{55}{147}.$$

$$\frac{\frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{18 + \frac{1}{1}}}}} = \frac{58}{155}$$

1, 1, 1, 1, 147, 155. Ans.

$$\therefore \frac{313}{757} = \frac{1}{1 + \frac{1}{4 + \frac{1}{3 + \frac{1}{4}}}}$$

$$3 + \frac{1}{1 + \frac{1}{8 + \frac{1}{4}}}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{3}}} = \frac{13}{16}.$$

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{4}} = \frac{4}{5}.$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{3 + \frac{1}{1}}}} = \frac{17}{21}$$

$$\frac{\frac{1}{1+\frac{1}{4+\frac{1}{3+\frac{1}{1+\frac{1}{8}}}}} = \frac{\frac{149}{184}}{1}$$

 $\frac{711}{818} = \frac{287}{271}$

1, \$, \frac{1}{6}, \frac{1}{27}, \frac{1}{28}. Ans.

$$\therefore \frac{337}{277} = \frac{1}{1 + \frac{1}{6 + \frac{1}{1 + \frac{1}{33}}}}$$

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{6}} = \frac{7}{8}$$

$$\frac{1}{1 + \frac{1}{6}} = \frac{6}{7}$$

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$$\frac{987}{1118} = 8\frac{38}{1118}.$$

$$33)113(3)$$

$$\frac{99}{14})33(2)$$

$$\frac{28}{5})14(2)$$

$$8 = 8.$$

$$8 + \frac{1}{3} = 8\frac{1}{3} = \frac{25}{3}.$$

$$8 + \frac{1}{3 + \frac{1}{2}} = 8\frac{5}{3} = \frac{58}{7}.$$

$$8 + \frac{1}{3 + \frac{1}{2}} = 8\frac{5}{17} = \frac{141}{17}.$$

$$8 + \frac{1}{3 + \frac{1}{2}} = 8\frac{7}{12} = \frac{199}{24}.$$

$$8, \frac{1}{3}, \frac{54}{1}, \frac{141}{12}, \frac{199}{24}. \text{ Ans.}$$

6. Find the proper fraction that, when changed to a continued fraction, will have 2, 3, 5, 6, 7 as quotients.

$$\frac{1}{2 + \frac{1}{3 + \frac{1}{5 + \frac{1}{6 + \frac{1}{7}}}} = \frac{709}{1640} \cdot Ans. \qquad \frac{1}{6\frac{1}{7}} = \frac{7}{43}; \qquad \frac{1}{5\frac{7}{43}} = \frac{43}{222}; \\ \frac{1}{3\frac{43}{232}} = \frac{222}{709}; \qquad \frac{1}{2\frac{732}{769}} = \frac{709}{1640}.$$

7. Find a series of fractions approximating to the ratio of the pound troy (5760 gr.) to the pound avoirdupois (7000 gr.).

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{4 + \frac{1}{1}}} = \frac{5}{6}.$$

$$\frac{1}{1 + \frac{1}{4}} = \frac{4}{5}.$$

$$\frac{1}{1 + \frac{1}{4}} = \frac{1}{1 + \frac{1}{1}}$$

$$= \frac{14}{17}.$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1}}} = \frac{65}{79}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{1}}}} = \frac{65}{79}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{1}}}} = \frac{65}{79}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{1 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}{4 + \frac{1}{4 + \frac{1}{4}}}} = \frac{9}{11}$$

$$\frac{1}{1 + \frac{1}$$

8. Find a series of fractions approximating to the ratio of the side of a square to its diagonal; that ratio being 1:1.414214 nearly.

$$\frac{1}{1.414214} = \frac{1000000}{1414214} = \frac{7071}{10000}.$$

$$7071)10000(1) \frac{7071}{2929)7071(2} \Rightarrow \frac{1}{100000} = \frac{1}{1 + \frac{1}{2 +$$

$$\frac{1}{1} = 1.$$

$$\frac{1}{1 + \frac{1}{2}} = \frac{2}{3}.$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{5}{7}.$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{12}{17}$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{12}{17}$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{3416}{4831}.$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{3416}{4831}.$$

$$\frac{1}{1 + \frac{1}{2 + \frac{1}{2}}} = \frac{3416}{4831}.$$

9. Find a series of fractions approximating to the ratio of the ar to the square chain, from the equality 1 ar = 0.2471 sq. ch.

$$0.2471 = \frac{2471}{100000}.$$

$$2471)10000(4)$$

$$\frac{9884}{116)2471(21)}$$

$$\frac{2436}{35)116(3)}$$

$$\frac{105}{11)35(3)}$$

$$\frac{33}{2)11(5)}$$

$$\frac{10}{10}$$

$$\frac{10}{1})2(2$$

$$\frac{1}{4} = \frac{1}{4}. \qquad \frac{1}{4 + \frac{1}{21}} = \frac{21}{85}. \qquad \frac{1}{4 + \frac{1}{21 + \frac{1}{3}}} = \frac{64}{259}.$$

$$\frac{1}{4 + \frac{1}{21 + \frac{1}{3}}} = \frac{213}{862}. \qquad \frac{1}{4 + \frac{1}{21 + \frac{1}{3}}} = \frac{1129}{4569}.$$

$$\frac{1}{4 + \frac{1}{21 + \frac{1}{3}}} = \frac{1129}{4569}.$$

10. Find a series of fractions approximating to the ratio of the weight of the 48-pound shot to the weight of the French shot of 24 kg.

$$48 \text{ lb.} = 48 \times 0.45359^{\text{kg}} = 21.77232^{\text{kg}}.$$

$$907) 1000(1) \frac{21.77232}{907} = \frac{907}{1000}.$$

$$\frac{837}{70)93(1} \cdot \cdot \cdot \frac{907}{1000} = \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{3}}}}}}}$$

$$\frac{69}{1)23(23}$$

$$\frac{1}{1} = 1. \quad \frac{1}{1 + \frac{1}{9}} = \frac{9}{10}. \quad \frac{1}{1 + \frac{1}{9 + \frac{1}{1}}} = \frac{10}{11}. \quad \frac{1}{1 + \frac{1}{9 + \frac{1}{1 + \frac{1}{3}}}} = \frac{39}{43}.$$

$$1, \frac{9}{10}, \frac{10}{11}, \frac{39}{43}. \quad Ans.$$

11. If the mean diameter of the Earth is reckoned at 7912 mi., and that of Mars 4189 mi., find a series of fractions approximating to the ratio of the mean diameters of these two planets.

ratio of the mean diameters of these two planets.
$$\frac{4189)7912(1}{4189} \qquad \qquad \cdots \qquad \frac{4189}{512} = \frac{1}{1 + \frac{1}{$$

$$\frac{1}{1} = 1.$$

$$\frac{1}{1 + \frac{1}{1}} = \frac{1}{2}.$$

$$\frac{1}{1 + \frac{1}{1}} = \frac{8}{15}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{836}{1579}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{836}{1579}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1}}} = \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{1 + \frac{1}{1}}}.$$

12. Find a series of fractions approximating to the ratio of a cubic yard to a cubic meter from the equality

1 cu. yd. =
$$0.76453^{\text{cbm}}$$
.
 $0.76453 = \frac{76458}{100000}$.

yard to a cubic meter from the equality
$$1 \text{ cu. yd.} = 0.76453^{\text{cbm.}}$$

$$0.76453 = \frac{76453}{1000005}.$$

$$76453)1000000(1) \\ \frac{76453}{23547})76453(3) \\ \frac{70641}{5812})23547(4) \\ \frac{23248}{299})5812(19) \\ \frac{5681}{131})299(2) \\ \frac{262}{37})131(3) \\ \frac{111}{20})37(1) \\ \frac{20}{17})20(1) \\ \frac{17}{3})17(5) \\ \frac{15}{2})3(1) \\ \frac{2}{2}(2) \\ \frac{2}{1})2(2) \\ \frac{2}{2}(2)$$

$$\frac{1}{1} = 1.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{3}{4}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{19}}} = \frac{250}{327}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4}}} = \frac{13}{17}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4 + \frac{1}{19 + \frac{1}{2}}}}} = \frac{513}{671}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4 + \frac{1}{19 + \frac{1}{2}}}}} = \frac{1789}{2340}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4 + \frac{1}{19 + \frac{1}{2}}}}} = \frac{2002}{3011}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{4 + \frac{1}{19 + \frac{1}{4 + \frac{1}{4 + \frac{1}{19 + \frac{1}{4 + \frac$$

1, \$, \frac{15}{4}, \frac{250}{527}, \frac{513}{571}, \frac{1750}{2340}, \frac{2302}{5351}, \frac{4091}{5351}, \frac{25757}{35757}, \frac{35845}{35745}. Ans.

 $1 + \frac{1}{1 + \frac{1}{5 + \frac{1}{1}}}$

13. Find a series of fractions approximating to the ratio of the kilometer to the mile, from the equality $1^m = 1.09362$ yd.

$$1^{m} = 1.09362 \text{ yd.}$$
 $1^{km} = 1093.62 \text{ yd.}$

$$\therefore 1^{km} = 0.621 \text{ mi.}$$

kilometer to the mile, from the equality
$$1^{m} = 1.09362$$
 yd. $1^{km} = 1093.62$ yd. $0.621 = \frac{621}{1000}$. $0.621 = \frac{621}$

$$\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}{3+\frac{1}{1}}}}}} = \frac{\frac{77}{124}}{1+\frac{1}}1+\frac{1}{1+\frac{1}{1+\frac{1}{1+\frac{1}1+\frac{1}1+\frac{1}1+\frac{1}{1+\frac{1}{1+\frac{1}{1+$$

 $1, \frac{1}{2}, \frac{3}{8}, \frac{3}{8}, \frac{5}{8}, \frac{10}{8}, \frac{59}{95}, \frac{77}{124}, \frac{136}{278}$. Ans.

14. Find the proper fraction that, if changed to a continued fraction, will have as quotients 1, 7, 5, 2.

$$\frac{1}{1+\frac{1}{7+\frac{1}{5+\frac{1}{2}}}} = \frac{79}{90} \cdot Ans.$$

$$\frac{1}{5+\frac{1}{2}} = \frac{2}{11}; \quad \frac{1}{7+\frac{1}{2}} = \frac{11}{79}; \quad \frac{1}{1+\frac{1}{2}} = \frac{79}{90}.$$

15. Find a series of fractions approximating to 0.5236; approximating to 0.7854.

$$0.5236 = \frac{5236}{10000} = \frac{1309}{2500}.$$

$$0.5236 = \frac{523}{10000} = \frac{1308}{2500}.$$

$$1309)2500(1)$$

$$\frac{1309}{1191})1309(1)$$

$$\frac{1191}{118})1191(10)$$

$$\frac{1180}{11})118(10)$$

$$\frac{110}{8})11(1)$$

$$\frac{8}{3})8(2)$$

$$\frac{6}{2})3(1)$$

$$\frac{2}{1}(2)2$$

$$\frac{1}{1}=1.$$

$$\frac{1}{1+\frac{1}{1}}=\frac{1}{2}$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{10}}} = \frac{11}{21}$$

$$\frac{\frac{1}{1+\frac{1}{1+\frac{1}{10+\frac{1}{10}}}}$$

$$\frac{1}{1 + \frac{1}{1 + \frac{1}{10 + \frac{1}{10}}}} = \frac{111}{212} \qquad \frac{1}{1 + \frac{1}{1 + \frac{1}{10 + \frac{1}{1}}}} = \frac{122}{233}$$

$$\frac{\frac{1}{1 + \frac{1}{1 + \frac{1}{10 + \frac{1}{10 + \frac{1}{1 + \frac{1}{2}}}}}}$$

$$\frac{1}{1+\frac{1}{1+\frac{1}{10+\frac{1}{10+\frac{1}{1}}}}} = \frac{355}{678}. \qquad \frac{1}{1+\frac{1}{1+\frac{1}{10+\frac{1}{10+\frac{1}{1}}}}} = \frac{477}{911}.$$

 $1, \frac{1}{2}, \frac{1}{21}, \frac{1}{212}, \frac{1}{233}, \frac{353}{575}, \frac{677}{577}$. Ans.

$$0.7854 = \frac{7854}{10000} = \frac{8927}{5000}$$

$$\begin{array}{r}
3927)5000(1)\\
\underline{3927}\\
1073)3927(3)\\
\underline{3219}\\
708)1073(1)
\end{array}$$

$$=\frac{1}{1+\frac{1}{3+\frac{1}}{3+\frac{1}{$$

1,
$$\frac{1}{2}$$
, $\frac{1}{21}$, $\frac{1}{212}$, $\frac{1}{233}$, $\frac{355}{675}$, $\frac{477}{675}$. Ans.

$$0.7854 = \frac{7854}{100000} = \frac{3927}{8000}$$

$$\therefore \frac{3927}{5000} = \frac{1}{1 + \frac{1}{3 + \frac{1}{1 + \frac{1}{$$

$$\begin{array}{c} 13 \\ 13 \\ \hline 9)13(1 \\ \hline 9 \\ \hline 4)9(2 \\ \hline 8 \\ \hline 1)4(4 \\ \hline 4 \\ \end{array}$$

$$\frac{1}{1} = 1.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{3}{4}.$$

$$\frac{1}{1 + \frac{1}{3}} = \frac{3}{4}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{1}}} = \frac{4}{5}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{1}}} = \frac{7}{9}.$$

$$\frac{1}{1 + \frac{1}{3 + \frac{1}{1 + \frac{1}$$

1, \(\frac{2}{4}\), \(\frac{1}{5}\), \(\frac{1}{14}\), \(\frac{1}{275}\), \(\frac{133}{233}\), \(\frac{855}{452}\), \(\frac{893}{1787}\). Ans.

16. Find a series of fractions approximating to the continued fraction that has as quotients 7, 2, 1, 2, 6, 4; that has as quotients 1, 2, 3, 4, 5, 6.

$$\frac{1}{7} = \frac{1}{7}. \qquad \frac{1}{7 + \frac{1}{2}} = \frac{2}{15}. \qquad \frac{1}{7 + \frac{1}{2}} = \frac{3}{22}. \qquad \frac{1}{7 + \frac{1}{2 + \frac{1}{1}}} = \frac{8}{59}.$$

$$\frac{1}{7 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{6}}}} = \frac{51}{376}. \qquad \frac{1}{7 + \frac{1}{2 + \frac{1}{1 + \frac{1}{2 + \frac{1}{6}}}} = \frac{212}{1563}.$$

1, 15, 12, 59, 176, 212. Ans.

$$\frac{1}{1} = 1. \qquad \frac{1}{1 + \frac{1}{2}} = \frac{2}{3}. \qquad \frac{1}{1 + \frac{1}{2 + \frac{1}{3}}} = \frac{7}{10}. \qquad \frac{1}{1 + \frac{1}{2 + \frac{1}{3}}} = \frac{30}{43}.$$

$$\frac{1}{1+\frac{1}{2+\frac{1}{3+\frac{1}{4+\frac{1}{6}}}}} = \frac{157}{225}. \qquad \frac{1}{1+\frac{1}{2+\frac{1}{3+\frac{1}{4+\frac{1}{5+\frac{1}{6}}}}}} = \frac{972}{1393}.$$

 $1, \frac{2}{3}, \frac{7}{10}, \frac{80}{43}, \frac{157}{123}, \frac{972}{1233}$. Ans.

Exercise 145. Page 337.

1. Change 4852 of the common scale to the scale of 7.

7 4852 7 693 remainder 1. 7 99 remainder 0. 7 14 remainder 1. 2 remainder 0.

20,101. Ans.

2. Change 4852 of the common scale to the scale of 2.

214852 2|2426 remainder 0. $2 \mid 1213$ remainder 0. 606 remainder 1. 2 303 remainder 0. 2 151 remainder 1. 2 75 remainder 1. 2 2 37 remainder 1. 2 18 remainder 1. 9 remainder 0. 2 4 remainder 1. 2 2 remainder 0. 1 remainder 0.

1,001,011,110,100. Ans.

3. Change 4852 of the common scale to the scale of 9.

9 4852 9 539 remainder 1. 9 59 remainder 8. 6 remainder 5.

6581. Ans.

4. Change 4852 of the common scale to the scale of 3.

3 4852 3 1617 remainder 1. 3 539 remainder 0. 3 179 remainder 2. 3 59 remainder 2. 3 19 remainder 2. 3 6 remainder 1. 2 remainder 0. 20,122,201. Ass.

5. Change 4852 of the common scale to the scale of 6.

6 4852 6 808 remainder 4. 6 134 remainder 4. 6 22 remainder 2. 3 remainder 4.

34,244. Ans.

6. Change 4852 of the common scale to the scale of 5.

5 4852 5 970 remainder 2. 5 194 remainder 0. 5 38 remainder 4. 5 7 remainder 3. 1 remainder 2.

123,402. Ans.

7. Change 4852 of the common scale to the scale of 8.

8 4852 8 606 remainder 4. 8 75 remainder 6. 8 9 remainder 3. 1 remainder 1.

11,364. Ans.

8. Change 4852 of the common scale to the scale of 4.

4 4852 4 1213 remainder 0. 4 303 remainder 1. 4 75 remainder 3. 4 18 remainder 3. 4 4 remainder 2. 1 remainder 0.

1,023,310. Ans.

9. Change 54,231 of the scale of 6 to the common scale.

10	54231		
10	3235	remainder	5 .
10	202	remainder	3.
10	11	remainder	4.
	0	remainder	7.

7435. Ans.

10. Change 54,231 of the scale of 7 to the common scale.

13,497. Ans.

11. Change 54,231 of the scale of 8 to the common scale.

12. Change 54,231 of the scale of 9 to the common scale.

10	54231	
10	4830	remainder 1.
10	438	remainder 1.
10	38	remainder 9.
	3	remainder 5.
		35,911. Ans.

Perform the following arithmetical processes:

13. Add 67,814; 76,406; 88,718 (scale of 9).

67814 76406 88718 255140 Ans.

14. Add 44,231; 13,432; 12,304 (scale of 5).

44231 13432 12304 131022 Ans.

15. Subtract 77,614 from 114,672 (scale of 8).

114672 77614 15056 Ans.

16. Subtract 52,515 from 112,252 (scale of 6).

112252 52515 15333 Ans.

17. Multiply 14,612 by 6502 (scale of 7).

18. Multiply 72,645 by 46,723 (scale of 8).

19. Divide 162,542 by 6522 (scale of 7).

$$\begin{array}{r}
 16 \\
 6522 \overline{\smash{\big)}\,162542} \\
 \underline{6522} \\
 64322 \\
 \underline{55365} \\
 \underline{5624}
\end{array}$$

165524. Ans.

20. Divide 468,722 by 5432 (scale of 9).

778818. Ans.

Exercise 146. Page 339.

1. Find the seventh term of the series 3, 5, 7, etc.

$$3 + (6 \times 2) = 3 + 12 = 15$$
. Ans.

2. Find the fifteenth term of the series 2, 7, 12, etc.

$$2 + (14 \times 5) = 2 + 70 = 72$$
. Ans.

3. Find the sixth term of the series 2, 24, 34, etc.

$$2 + (5 \times 5) = 2 + 35 = 55$$
. Ans.

4. Find the twentieth term of the series 2, $3\frac{1}{4}$, $4\frac{1}{2}$, etc.

$$2+(19\times1\frac{1}{4})=2+23\frac{3}{4}=25\frac{3}{4}$$
. Ans.

5. Find the seventh term of the series 21, 19, 17, etc.

$$21 - (6 \times 2) = 21 - 12 = 9$$
. Ans.

6. Find the twelfth term of the series 18, 17, 16, etc.

$$18-(11\times\frac{2}{3})=18-7\frac{1}{3}=10\frac{2}{3}$$
. Ans.

7. If the first term of a series is 5, and the common difference 21, find the thirteenth and the eighteenth terms.

13th term =
$$5 + (12 \times 2\frac{1}{4})$$

= $5 + 27 = 32$.
18th term = $5 + (17 \times 2\frac{1}{4})$
= $5 + 38\frac{1}{4} = 43\frac{1}{4}$.

8. If the fourth term of a series is 18, and the common difference 3, find the seventh and eleventh terms.

The seventh term is the fourth term of the series whose first term is 18; the eleventh term is the eighth term of this series.

7th term =
$$18 + (3 \times 3)$$

= $18 + 9 = 27$.
11th term = $18 + (7 \times 3)$
= $18 + 21 = 39$.

9. If the fifth term of a decreasing series is 52, and the common difference 3½, find the twelfth and eighteenth terms.

The twelfth term is the eighth term of the series whose first term is 52; the eighteenth term is the fourteenth term of this series.

12th term =
$$52 - (7 \times 3\frac{1}{2})$$

= $52 - 24\frac{1}{2} = 27\frac{1}{2}$.
18th term = $52 - (13 \times 3\frac{1}{2})$
= $52 - 45\frac{1}{2} = 6\frac{1}{2}$.

10. If the fourth term of a series is 14, and the twelfth term 38, what is the common difference?

$$\frac{38-14}{8}=3$$
. Ans.

11. Find the common difference in a series if the fourth term is 12 and the seventh term 27.

$$\frac{27-12}{3}=5$$
. Ans.

12. Find the common difference in a series if the first term is 20 and the fourth term 40.

$$\frac{40-20}{3}=6\frac{2}{3}$$
. Ans.

13. Find the common difference in a series if the first term is 2 and the eleventh term 20.

$$\frac{20-2}{10}=1\frac{4}{5}. \ Ans.$$

14. Find the common difference in a series if the third term is 7 and the eighth term 12½.

$$\frac{12\frac{1}{2}-7}{5}=1_{10}. \ Ans.$$

15. Find the common difference in a series if the first term is 1 and the fourth term 19.

$$\frac{19-1}{9}=6$$
. Ans.

Exercise 147. Page 340.

1. Find the sum of 1, 5, 9, etc., to twenty terms. 20th term = $1 + (19 \times 4) = 1 + 76 = 77$. Sum = $20 \times \frac{1}{4}(1 + 77) = 20 \times 39 = 780$. Ans.

2. Find the sum of 4, $5\frac{1}{2}$, 7, etc., to eight terms. 8th term = $4 + (7 \times 1\frac{1}{2}) = 4 + 10\frac{1}{2} = 14\frac{1}{2}$. Sum = $8 \times \frac{1}{2}(4 + 14\frac{1}{2}) = 8 \times 9\frac{1}{2} = 74$. Ans.

3. Find the sum of 8, $7\frac{2}{3}$, $7\frac{1}{3}$, etc., to sixteen terms. 16th term = $8 - (15 \times \frac{1}{3}) = 8 - 5 = 3$. Sum = $16 \times \frac{1}{2}(8+3) = 16 \times 5\frac{1}{2} = 88$. Ans.

4. Find the sum of 20, 181, 161, etc., to seven terms.

7th term =
$$20 - (6 \times 1\frac{1}{4}) = 20 - 10\frac{1}{4} = 9\frac{1}{4}$$
.

Sum =
$$7 \times \frac{1}{2}(20 + 9\frac{1}{2}) = 7 \times 14\frac{1}{2} = 103\frac{1}{2}$$
. Ans.

5. Find the sum of the first twenty natural numbers.

Sum =
$$20 \times \frac{1}{4}(1+20) = 20 \times 10\frac{1}{4} = 210$$
. Ans.

6. Find the sum of the natural numbers from 37 to 53 both inclusive.

Sum =
$$17 \times \frac{1}{2}(37 + 53) = 17 \times 45 = 765$$
. Ans.

7. Find the sum of a series of thirty terms, if the first term is 21 and the last 59.

Sum =
$$30 \times \frac{1}{2}(21 + 59) = 30 \times 40 = 1200$$
. Ans.

8. Find the sum of the series whose first two terms are 3 and 9 and the last term 75.

Number of terms =
$$1 + \frac{75 - 3}{6} = 1 + 12 = 13$$
.

Sum =
$$13 \times \frac{1}{2}(3 + 75) = 13 \times 39 = 507$$
. Ans.

9. Find the sum of a series of twenty terms whose third and fifth terms are 10 and 15, respectively.

Common difference
$$=\frac{15-10}{2}=2\frac{1}{2}$$
.

1st term =
$$10 - (2 \times 2\frac{1}{2}) = 10 - 5 = 5$$
.

20th term =
$$5 + (19 \times 2\frac{1}{2}) = 5 + 47\frac{1}{2} = 52\frac{1}{2}$$
.

Sum =
$$20 \times \frac{1}{2}(5 + 52\frac{1}{2}) = 20 \times 28\frac{3}{4} = 575$$
. Ans.

10. A body falls through a space of $16\frac{1}{12}$ ft. in the first second of its fall, and in each succeeding second $32\frac{1}{6}$ ft. more than in the second just before. How far will a stone fall in the seventh second? How far in seven seconds?

7th term =
$$16\frac{1}{12}$$
 ft. + $(6 \times 32\frac{1}{6}$ ft.) = $16\frac{1}{12}$ ft. + 193 ft. = $209\frac{1}{12}$ ft. Ans. Sum = $7 \times \frac{1}{2}(16\frac{1}{12} + 209\frac{1}{12})$ ft. = $7 \times 112\frac{7}{12}$ ft. = $788\frac{1}{12}$ ft. Ans.

11. A travels 8 miles the first day, 11 miles the second, 14 miles the third, and so on, and overtakes in 17 days B who started at the same time, and traveled at a uniform rate. What is B's rate per day?

17th term =
$$8 \text{ mi.} + (16 \times 3 \text{ mi.}) = 8 \text{ mi.} + 48 \text{ mi.} = 56 \text{ mi.}$$

Sum =
$$17 \times \frac{1}{2}(8 + 56)$$
 mi. = 17×32 mi.

$$\frac{17 \times 32}{17}$$
 mi. = 32 mi. Ans.

12. In a potato race 100 potatoes are placed in a straight line 3 ft. distant from each other. A boy, starting from a basket 3 ft. from the first potato, is required to pick them up one by one and carry them to the basket. To finish the race how far must the boy run?

First term is 6 ft., common difference 6 ft., and number of terms 100.

100th term = 6 ft.
$$+(99 \times 6 \text{ ft.}) = 100 \times 6 \text{ ft.} = 600 \text{ ft.}$$

Sum =
$$100 \times \frac{1}{2}(6 + 600)$$
 ft. = 100×303 ft. = $30,300$ ft. Ans.

13. How many times a day does a clock strike that strikes the hours only?

For half a day, sum = $12 \times \frac{1}{2}(1 + 12) = 12 \times 6\frac{1}{2} = 78$.

For whole day, $2 \times 78 = 156$. Ans.

14. A body falls through a space of 4.9^m in the first second of its fall, and in each succeeding second 9.8^m more than in the second just before. A stone dropped from a balloon was 35 seconds in reaching the ground. How high was the balloon?

35th term =
$$4.9^{\text{m}} + (34 \times 9.8)^{\text{m}} = 4.9^{\text{m}} + 333.2^{\text{m}} = 338.1^{\text{m}}$$
.

Sum =
$$35 \times \frac{1}{2} (4.9^{m} + 338.1^{m}) = 35 \times 171.5^{m} = 6002.5^{m}$$
. Ans.

Exercise 148. Page 342.

1. Find the eighth term of the series 2, 6, 18, etc.

$$2 \times 3^7 = 2 \times 2187 = 4374$$
. Ans.

2. Find the fifth term of the series 8, 4, 2, etc.

$$8 \times (\frac{1}{2})^4 = 8 \times \frac{1}{16} = \frac{1}{2}$$
. Ans.

3. Find the seventh term of the series 2, 3, $4\frac{1}{2}$, etc.

$$2 \times (\frac{3}{2})^6 = 2 \times \frac{729}{64} = \frac{729}{32} = 22\frac{25}{32}$$
. Ans.

4. Find the sixth term of the series 4, 23, 17, etc.

$$4 \times (\frac{2}{3})^5 = 4 \times \frac{32}{243} = \frac{128}{243}$$
. Ans.

5. Find the eighth term of the series 4, 10, 25, etc.

$$4 \times (\frac{5}{2})^7 = 4 \times \frac{78125}{128} = \frac{78125}{32} = 2441\frac{13}{32}$$
. Ans.

6. Find the fifth term of the series $\frac{1}{4}$, $\frac{1}{16}$, $\frac{1}{64}$, etc.

$$\frac{1}{4} \times (\frac{1}{4})^4 = \frac{1}{4} \times \frac{1}{256} = \frac{1}{1024}$$
. Ans.

7. Find the ninth term of the series 4, 2, 1, etc.

$$4 \times \left(\frac{1}{2}\right)^8 = 2^2 \times \frac{1}{2^8} = \frac{1}{2^6} = \frac{1}{64}$$
 Ans.

8. Find the sixth term of the series 6, 9, 131, etc.

$$6 \times (\frac{3}{2})^5 = 6 \times \frac{243}{52} = \frac{729}{16} = 45\frac{9}{16}$$
. Ans.

9. Write the first six terms of the geometrical series whose fit and sixth terms are 112 and 224, respectively.

Ratio = 2. 1st term =
$$\frac{112}{2^4}$$
 = 7.

Therefore, the series is 7, 14, 28, 56, 112, 224. Ans.

10. The seventh and ninth terms of a geometrical series are 1 and 144, respectively. Find the twelfth term.

9th term = 7th term × (ratio)².
∴ (ratio)² =
$$\frac{144}{100}$$
. ∴ ratio = $\frac{12}{10} = \frac{6}{5}$.
12th term = $144 \times (\frac{6}{5})^8 = 144 \times \frac{216}{125} = 248.832$. Ans.

11. A capital of \$1000 is increased by $\frac{1}{10}$ of itself each year. Where will it be at the beginning of the fifth year?

$$1000 \times \$(\frac{1}{10})^4 = 1000 \times \$\frac{14841}{10000} = \$1464.10$$
. Ans.

12. A capital of \$1000 is increased by $_{100}$ of itself each year. Where will it be at the beginning of the sixth year?

$$1000 \times \$(\frac{186}{180})^5 = 1000 \times \$\frac{133832355778}{1000} = \$1338.23$$
. Ans.

Exercise 149. Page 343.

1. Find the sum of 2, 6, 18, etc., to six terms.

6th term =
$$2 \times 3^5 = 2 \times 243 = 486$$
.

Sum =
$$\frac{3 \times 486 - 2}{3 - 1} = \frac{1458 - 2}{2} = \frac{1456}{2} = 728$$
. Ans.

2. Find the sum of 1, 2, 4, etc., to nine terms.

9th term =
$$1 \times 2^6 = 1 \times 256 = 256$$
.

Sum =
$$\frac{2 \times 256 - 1}{2 - 1} = \frac{512 - 1}{1} = 511$$
. Ans.

3. Find the sum of 3, 9, 27, etc., to five terms.

5th term =
$$3 \times 3^4 = 3 \times 81 = 243$$
.

Sum =
$$\frac{3 \times 243 - 3}{3 - 1} = \frac{729 - 3}{2} = \frac{726}{2} = 363$$
. Ans.

4. Find the sum of 2, 3, $4\frac{1}{2}$, etc., to eight terms.

8th term =
$$2 \times (\frac{3}{2})^7 = 2 \times \frac{2187}{128} = \frac{2187}{64} = 34\frac{1}{64}$$
.

Sum =
$$\frac{\frac{3}{4} \times 34\frac{11}{64} - 2}{\frac{3}{4} - 1} = \frac{51\frac{33}{128} - 2}{\frac{1}{4}} = 2 \times 49\frac{33}{128} = 98\frac{34}{64}$$
. Ans.

5. Find the sum of 1, $\frac{1}{3}$, $\frac{1}{6}$, etc., to eight terms.

8th term =
$$1 \times (\frac{1}{8})^7 = \frac{1}{2187}$$
.

Sum =
$$\frac{1 - \frac{1}{4} \times \frac{1}{2187}}{1 - \frac{1}{8}} = \frac{1 - \frac{1}{5561}}{\frac{2}{8}} = \frac{\frac{3280}{6560}}{\frac{6560}{6561}} \times \frac{3}{2} = \frac{3280}{2187} = 1\frac{1}{2}\frac{9}{187}.$$
 Ans.

6. Find the sum of 1, $\frac{1}{2}$, $\frac{1}{4}$, etc., to ten terms.

10th term =
$$1 \times (\frac{1}{2})^9 = \frac{1}{512}$$
.

Sum =
$$\frac{1 - \frac{1}{2} \times \frac{1}{517}}{1 - \frac{1}{2}} = \frac{1 - \frac{1}{1024}}{\frac{1}{2}} = 2 \times \frac{1023}{1024} = \frac{1023}{512} = 1\frac{511}{512}$$
. Ans.

7. Find the sum of $\frac{1}{2}$, $\frac{1}{3}$, $\frac{2}{3}$, etc., to eight terms.

7th term =
$$\frac{1}{2} \times (\frac{2}{3})^7 = \frac{1}{2} \times \frac{128}{2187} = \frac{34}{2187}$$
.

Sum =
$$\frac{\frac{1}{4} - \frac{2}{3} \times \frac{64}{2181}}{1 - \frac{2}{3}} = \frac{\frac{1}{4} - \frac{128}{6561}}{\frac{1}{3}} = 3 \times \frac{6305}{13122} = \frac{6305}{4374} = 1\frac{123}{1374}$$
. Ans.

8. Find the sum of the first six terms of the series whose first term is 3 and ratio 5.

6th term =
$$3 \times 5^5 = 3 \times 3125 = 9375$$
.

Sum =
$$\frac{5 \times 9375 - 3}{5 - 1} = \frac{46875 - 3}{4} = \frac{46872}{4} = 11,718$$
. Ans.

9. Find the sum of the first eight terms of the series whose first term is 3 and ratio \(\frac{1}{4}\).

8th term =
$$3 \times (\frac{1}{8})^7 = 3 \times \frac{1}{2187} = \frac{1}{729}$$
.

$$Sum = \frac{3 - \frac{1}{1} \times \frac{1}{729}}{1 - \frac{1}{3}} = \frac{3 - \frac{1}{2117}}{\frac{2}{3}} = \frac{3}{2} \times 2\frac{2\frac{1}{2}\frac{1}{18}}{2\frac{1}{18}} = \frac{3}{2} \times \frac{\frac{3280}{6569}}{2187} = \frac{3280}{729} = 4\frac{32}{2}\frac{2}{3}.$$
Ans.

10. A man saved in one year \$64, and in each succeeding year, for 9 years more, 1½ times as much as in the preceding year. Find the whole amount he saved.

Number of terms is 10.

10th term =
$$64 \times (\frac{3}{4})^9 = 2^6 \times \frac{3^9}{2^9} = \frac{3^9}{2^3} = \frac{19683}{8} = 2460\frac{3}{4}$$
.

Sum =
$$\frac{\frac{3}{4} \times 2460\frac{3}{4} - 64}{\frac{3}{4} - 1} = \frac{3690\frac{3}{16} - 64}{\frac{1}{4}} = 2 \times 3626\frac{9}{16} = 7253\frac{1}{4}.$$

\$7253\frac{1}{4} = \$7253.13. Ans.

$$s = \frac{3}{1-\frac{1}{3}} = \frac{3}{\frac{1}{3}} = 2.$$

3. Find the sum of the infinite series 1

$$s = \frac{\frac{1}{4}}{1 - \frac{1}{4}} = \frac{\frac{1}{4}}{\frac{1}{2}} = \frac{1}{4}$$
. Δ

4. Find the sum of the infinite series 1,

$$s = \frac{1}{1 - \frac{1}{3}} = \frac{\frac{1}{3}}{\frac{1}{3}} = \frac{1}{4}$$
. A

5. Find the sum of the infinite series 0.

$$s = \frac{0.17}{1 - 0.01} = \frac{0.17}{0.99} =$$

6. Find the sum of the infinite series 0.2

$$s = \frac{0.21}{1 - 0.01} = \frac{0.21}{0.99} =$$

7. Find the sum of the infinite series 0.9

$$s = \frac{0.9}{1 - 0.1} = \frac{0.9}{0.9} = 1$$

8. Find the sum of the infinite series 0.5

$$s = \frac{0.23}{1 - 0.01} = \frac{0.23}{0.99} =$$

TEACHERS' EDITION.

Exercise 151. Page 349.

- 1. $\log 70 = 1.8451$. Ans.
- 2. $\log 101 = 2.0043$. Ans.
- 3. $\log 333 = 2.5224$. Ans.
- 4. $\log 3491 = 3.5428 + (\frac{1}{10} \text{ of } 13) = 3.5429$. Ans.
- 5. $\log 1866 = 3.2695 + \binom{6}{10}$ of 23) = 3.2709. Ans.
- 6. $\log 6897 = 3.8382 + (\frac{7}{10} \text{ of } 6) = 3.8386$. Ans.
- 7. $\log 9901 = 3.9956 + (\frac{1}{10} \text{ of } 5) = 3.9957$. Ans.
- 8. $\log 4389 = 3.6415 + (\frac{9}{10} \text{ of } 10) = 3.6424$. Ans.
- **9.** $\log 1111 = 3.0453 + (\frac{1}{10} \text{ of } 39) = 3.0457$. Ans.
- **10**. $\log 58,343 = 4.7657 + (\frac{43}{100} \text{ of } 7) = 4.7660$. Ans.
- **11.** $\log 77,860 = 4.8910 + (\frac{60}{100} \text{ of } 5) = 4.8913$. Ans.
- **12.** $\log 30,127 = 4.4786 + (\frac{27}{100} \text{ of } 14) = 4.4790.$ Ans.
- **13**. $\log 730.84 = 2.8633 + (\frac{84}{100} \text{ of } 6) = 2.8638$. Ans.
- **14.** $\log 0.008765 = 7.9425 + (\frac{5}{10} \text{ of } 5) 10 = 7.9428 10$. Ans.
- **15.** $\log 8.0808 = 0.9074 + (\frac{8}{100} \text{ of } 5) = 0.9074$. Ans.
- **16.** $\log 5.0009 = 0.6990 + (\frac{9}{100} \text{ of } 8) = 0.6991$. Ans.
- 17. $\log 0.3769 = 9.5752 + (\frac{9}{10} \text{ of } 11) 10 = 9.5762 10$. Ans.
- **18.** $\log 0.070707 = 8.8494 + (\frac{7}{100} \text{ of } 6) 10 = 8.8494 10$. Ans.
- **19.** $\log 0.03723 = 8.5705 + \binom{8}{10} \text{ of } 12) 10 = 8.5709 10.$ Ans.
- **20.** $\log 98.871 = 1.9948 + (\frac{71}{100} \text{ of } 4) = 1.9951$. Ans.

Exercise 152. Page 353.

1. Find antilog 3.9017.

The number corresponding to the mantissa 9015 is 7970. The number corresponding to the mantissa 9020 is 7980. The difference between these numbers is 10, and $7970 + \frac{2}{3}$ of 10 = 7974. Ans.

2. Find antilog 1.2076.

The number corresponding to the mantissa 2068 is 1610. The number corresponding to the mantissa 2095 is 1620. The difference between these numbers is 10,

and $1610 + \frac{3}{27}$ of 10 = 1613. Therefore, the number required is 16.13. Ans.

3. Find antilog 0.4442.

The number corresponding to the mantissa 4440 is 2780. The number corresponding to the mantissa 4456 is 2790. The difference between these numbers is 10

The difference between these numbers is 10, and $2780 + \frac{2}{18}$ of 10 = 2781.

Therefore, the number required is 2.781. Ans.

4. Find antilog 1.0090.

The number corresponding to the mantissa 0086 is 1020. The number corresponding to the mantissa 0128 is 1030.

The difference between these numbers is 10,

and 1020 + 4 of 10 = 1021.

Therefore, the number required is 10.21. Ans.

5. Find antilog 4.8697.

The number corresponding to the mantissa 8692 is 7400. The number corresponding to the mantissa 8698 is 7410.

The difference between these numbers is 10,

and $7400 + \frac{2}{3}$ of 10 = 7408.

Therefore, the number required is 74,080. Ans.

6. Find antilog 1.9214.

The number corresponding to the mantissa 9212 is 8340.

The number corresponding to the mantissa 9217 is 8350.

The difference between these numbers is 10,

and $8340 + \frac{2}{3}$ of 10 = 8344.

Therefore, the number required is 83.44. Ans.

7. Find antilog 2.9850.

The number corresponding to the mantissa 9850 is 9660. Therefore, the number required is 966. Ans.

8. Find antilog 4.5388.

The number corresponding to the mantissa 5378 is 3450.

The number corresponding to the mantissa 5391 is 3460.

The difference between these numbers is 10,

and $3450 + \frac{1}{2}$ of 10 = 3458.

Therefore, the number required is 34,580. Ans.

9. Find antilog 0.8550.

The number corresponding to the mantissa 8549 is 7160.

The number corresponding to the mantissa 8555 is 7170.

The difference between these numbers is 10,

and $7160 + \frac{1}{3}$ of 10 = 7162.

Therefore, the number required is 7.162. Ans.

10. Find antilog 9.9992 - 10.

The number corresponding to the mantissa 9991 is 9980.

The number corresponding to the mantissa 9996 is 9990.

The difference between these numbers is 10,

and

 $9980 + \frac{1}{3}$ of 10 = 9982.

Therefore, the number required is 0.9982. Ans.

11. Find antilog 7.0016 - 10.

The number corresponding to the mantissa 0000 is 1000.

The number corresponding to the mantissa 0043 is 1010.

The difference between these numbers is 10,

and

 $1000 + \frac{14}{3}$ of 10 = 1004.

Therefore, the number required is 0.001004. Ans.

12. Find antilog 9.2618 - 10.

The number corresponding to the mantissa 2601 is 1820.

The number corresponding to the mantissa 2625 is 1830.

The difference between these numbers is 10,

and

 $1820 + \frac{17}{27}$ of 10 = 1827.

Therefore, the number required is 0.1827. Ans.

13. Find antilog 8.7324 - 10.

The number corresponding to the mantissa 7324 is 5400.

Therefore, the number required is 0.054. Ans.

14. Find antilog 9.5555 - 10.

The number corresponding to the mantissa 5551 is 3590.

The number corresponding to the mantissa 5563 is 3600.

The difference between these numbers is 10,

and

 $3590 + \frac{4}{12}$ of 10 = 3593.

Therefore, the number required is 0.3593. Ans.

15. Find antilog 6.0216 - 10.

The number corresponding to the mantissa 0212 is 1050.

The number corresponding to the mantissa 0253 is 1060.

The difference between these numbers is 10,

and

1050 + 4 of 10 = 1051.

Therefore, the number required is 0.0001051. Ans.

16. Find antilog 7.0080 - 10.

The number corresponding to the mantissa 0043 is 1010.

The number corresponding to the mantissa 0086 is 1020.

The difference between these numbers is 10,

and

 $1010 + \frac{27}{3}$ of 10 = 1019.

Therefore, the number required is 0.001019. Ans.

17. Find antilog 8.2361 - 10.

The number corresponding to the mantissa 2355 is 1720.

The number corresponding to the mantissa 2380 is 1730.

The difference between these numbers is 10,

and

$$1720 + \frac{4}{15}$$
 of $10 = 1722$.

Therefore, the number required is 0.01722. Ans.

18. Find antilog 9.4513 - 10.

The number corresponding to the mantissa 4502 is 2820.

The number corresponding to the mantissa 4518 is 2830.

The difference between these numbers is 10,

and

$$2820 + \frac{11}{12}$$
 of $10 = 2827$.

Therefore, the number required is 0.2827. Ans.

Exercise 153. Page 353.

1. Find by logarithms the value of 948.22×0.4387 .

$$\log 948.22 = 2.9769$$

$$\log \ 0.4387 = \underline{9.6422 - 10}$$

$$2.6191 = \log 416$$
. Ans.

2. Find by logarithms the value of 1.9704×0.0786 .

$$\log 1.9704 = 0.2946$$

$$\log 0.0786 = 8.8954 - 10$$

$$9.1900 - 10 = \log 0.1549$$
. Ans.

3. Find by logarithms the value of 380.25×0.00673 .

$$\log 380.25 = 2.5801$$

$$\log 0.00673 = 7.8280 - 10$$

$$0.4081 = \log 2.559$$
. Ans.

4. Find by logarithms the value of 270.05×0.0087 .

$$\log 270.05 = 2.4315$$

$$\log \ 0.0087 = \underline{7.9395 - 10}$$

$$0.3710 = \log 2.349$$
. Ans.

5. Find by logarithms the value of 11.163×0.3333 .

$$\log 11.163 = 1.0478$$

$$\log \ 0.3333 = 9.5228 - 10$$

$$0.5706 = \log 3.721$$
. Ans.

6. Find by logarithms the value of 777.78×0.0787 .

$$\log 777.78 = 2.8909$$

$$\log 0.0787 = 8.8960 - 10$$

$$1.7869 = \log 61.21. Ans.$$

7. Find by logarithms the value of 216.21×0.76312 .

$$\log 216.21 = 2.3349$$

$$\log 0.76312 = 9.8826 - 10$$

$$2.2175 = \log 165. Ans.$$

8. Find by logarithms the value of 0.56127×1.2312 .

$$\log 0.56127 = 9.7492 - 10$$

$$\log 1.2312 = \underbrace{0.0903}_{9.8395 - 10} = \log 0.691. \ \textit{Ans.}$$

9. Find by logarithms the value of 0.86311×56.371 .

$$\log 0.86311 = 9.9361 - 10
\log 56.371 = 1.7511
1.6872 = \log 48.67. Ans.$$

10. Find by logarithms the value of 59.795×0.7955 .

$$\log 59.795 = 1.7767
\log 0.7955 = \frac{9.9007 - 10}{1.6774} = \log 47.58. Ans.$$

11. Find by logarithms the value of 2.6537×0.2313 .

$$\log 2.6537 = 0.4238$$

$$\log 0.2313 = 9.3642 - 10$$

$$9.7880 - 10 = \log 0.6137$$
. Ans.

12. Find by logarithms the value of 37.587×12.371 .

$$\log 37.587 = 1.5750$$

$$\log 12.371 = \underbrace{1.0924}_{2.6674} = \log 464.9. Ans.$$

13. Find by logarithms the value of 89.313×2.3781 .

$$\log 89.313 = 1.9510
\log 2.3781 = \underbrace{0.3762}_{2.3272} = \log 212.4. \text{ Ans.}$$

14. Find by logarithms the value of 9.1765×0.089 .

$$\begin{array}{c} \log & 9.1765 = 0.9627 \\ \log & 0.089 = \frac{8.9494 - 10}{9.9121 - 10} = \log 0.8168. \ \textit{Ans.} \end{array}$$

15. Find by logarithms the value of $4786 \times 54187 \times 0.00218 \times 0.8652$

$$\log 4786 = 3.6799$$

$$\log 5.4187 = 0.7339$$

$$\log 0.00218 = 7.3085 - 10$$

$$\log 0.8852 = 9.9371 - 10$$

$$1.6894 = \log 48.91. Ans.$$

16. Find by logarithms the value of 3.1416 \times 7.77 \times 184 \times 0.01865.

$$\begin{array}{rcl} \log 3.1416 &= 0.4971 \\ \log 7.77 &= 0.8404 \\ \log 184 &= 2.2648 \\ \log 0.01865 &= 8.2707 - 10 \\ \hline 1.9230 &= \log 83.76. \ \textit{Ans.} \end{array}$$

17. Find by logarithms the value of $0.7854 \times 129.6 \times 63.45 \times 0.0021$.

$$\log 0.7854 = 9.8951 - 10
\log 129.6 = 2.1126
\log 63.45 = 1.8025
\log 0.0021 = \frac{7.3222 - 10}{1.1324} = \log 13.57. Ans.$$

18. Find by logarithms the value of $1842.65 \times 9.876 \times 0.843 \times 0.0265$.

$$log 1842.65 = 3.2654
log 9.876 = 0.9946
log 0.843 = 9.9258 - 10
log 0.0265 = 8.4232 - 10
2.6090 = log 406.5. Ans.$$

19. Find by logarithms the value of $12.48 \times 44.63 \times 32.78 \times 0.004587$.

$$log 12.48 = 1.0962
log 44.63 = 1.6496
log 32.78 = 1.5156
log 0.004587 = $\frac{7.6615 - 10}{1.9229}$ = log 83.74. Ans.$$

20. Find by logarithms the value of $0.9876 \times 0.8765 \times 0.7654 \times 0.6543$.

$$\log 0.9876 = 9.9946 - 10$$

$$\log 0.8765 = 9.9428 - 10$$

$$\log 0.7654 = 9.8839 - 10$$

$$\log 0.6543 = 9.8158 - 10$$

$$9.6371 - 10 = \log 0.4336. Ans.$$

Exercise 154. Page 354.

1. Find by logarithms the value of 5.068.

$$\log 5.06 = 0.7042$$

$$\frac{3}{2.1126} = \log 129.6. \text{ Ans.}$$

2. Find by logarithms the value of 2.5015.

$$\log 2.501 = 0.3981$$

$$\frac{5}{1.9905} = \log 97.84. \ Ans.$$

3. Find by logarithms the value of 1.7167.

$$\log 1.716 = 0.2345$$

$$\frac{7}{1.6415} = \log 43.8. \ Ans.$$

4. Find by logarithms the value of 1.17810.

$$\log 1.178 = 0.0712$$

$$\frac{10}{0.7120} = \log 5.153. \ Ans.$$

5. Find by logarithms the value of 7.68216.

6. Find by logarithms the value of 0.76856.

$$\log 0.7685 = 9.8857 - 10$$

$$\frac{6}{9.3142 - 10} = \log 0.2061. \ \textit{Ans.}$$

7. Find by logarithms the value of 0.96118.

$$\log 0.9611 = 9.9828 - 10$$

$$\frac{8}{9.8624 - 10} = \log 0.7285.$$
 Ans.

8. Find by logarithms the value of 0.02312.

$$\log 0.0231 = 8.3636 - 10$$

$$\frac{2}{6.7272 - 10} = \log 0.0005336. \text{ Ans.}$$

9. Find by logarithms the value of 0.8567*.

$$\log 0.8567 = 9.9329 - 10$$

$$\frac{3}{9.7987 - 10} = \log 0.629. \quad Ans.$$

10. Find by logarithms the value of 0.54385.

$$\log 0.5438 = 9.7354 - 10$$

$$\frac{5}{8.6770 - 10} = \log 0.04753. \quad Ans.$$

11. Find by logarithms the value of 2.8614154.

$$\log 2.861415 = 0.4566$$

$$\frac{4}{1.8264} = \log 67.05. \quad Ans.$$

12. Find by logarithms the value of 3.791256.

13. Find by logarithms the value of 0.021875.

14. Find by logarithms the value of 0.871527.

$$\log 0.87152 = 9.9403 - 10$$

$$\frac{7}{9.5821 - 10} = \log 0.382.$$
 Ans.

15. Find by logarithms the value of 0.959568.

$$\log 0.95956 = 9.9821 - 10$$

$$\frac{8}{9.8568 - 10} = \log 0.7192. \text{ Ans.}$$

Exercise 155. Page 355.

1. Find by logarithms the value of $13^{\frac{1}{3}}$.

$$\log 13 = 1.1139$$

$$3 | 1.1139$$

$$0.3713$$

$$= \log 2.351. \ Ans.$$

2. Find by logarithms the value of $29^{\frac{1}{5}}$.

$$\log 29 = 1.4624$$

$$5 | 1.4624$$

$$0.2925$$

$$= \log 1.961. Ans.$$

3. Find by logarithms the value of $471^{\frac{1}{4}}$.

$$\log 471 = 2.6730$$

$$4 | \underline{2.6730}$$

$$0.6683$$

$$= \log 4.659. Ans.$$

4. Find by logarithms the value of 288.

$$\log 288 = 2.4594$$

$$6 \underbrace{|2.4594|}_{0.4099}$$

$$= \log 2.57. \ Ans.$$

5. Find by logarithms the value of $1019^{\frac{1}{7}}$.

$$\log 1019 = 3.0082$$

$$7 \underbrace{|3.0082|}_{0.4297}$$

$$= \log 2.689. Ans.$$

6. Find by logarithms the value of 1281.

$$\log 1281 = 3.1075 \\
8 | 3.1075 \\
0.3884 \\
= \log 2.446. \text{ Ans.}$$

7. Find by logarithms the value of 1862.

$$\log 1862 = 3.2700$$

$$9 \underbrace{|3.2700|}_{0.3633}$$

$$= \log 2.308. \ \textit{Ans.}$$

8. Find by logarithms the value of 87916.

$$\log 879 = 2.9440 \\
10 | 2.9440 \\
0.2944 \\
= \log 1.97. Ans.$$

9. Find by logarithms the value of $0.609^{\frac{1}{4}}$.

$$\log 0.609 = 9.7846 - 10$$

$$30. -30$$

$$4 \overline{\smash{\big)}39.7846 - 40}$$

$$9.9462 - 10$$

$$= \log 0.8834. Ans.$$

10. Find by logarithms the value of $0.8716^{\frac{1}{5}}$.

$$\log 0.8716 = 9.9403 - 10$$

$$40. -40$$

$$5 \overline{49.9403 - 50}$$

$$9.9881 - 10$$

$$= \log 0.973. Ans.$$

11. Find by logarithms the value of $0.021641^{\frac{1}{6}}$.

$$\log 0.021641 = 8.3353 - 10$$

$$50. -50$$

$$6 \overline{\smash{\big)}58.3353 - 60}$$

$$9.7226 - 10$$

$$= \log 0.528. Ans.$$

12. Find by logarithms the value of $0.9825^{\frac{1}{7}}$.

$$\log 0.9825 = 9.9924 - 10$$

$$60. -60$$

$$7 \overline{69.9924 - 70}$$

$$9.9989 - 10$$

$$= \log 0.9975. Ans.$$

13. Find by logarithms the value of 0.42184.

$$\log 0.42184 = 9.6251 - 10$$

$$70. -70$$

$$8 \overline{\smash{\big)}79.6251 - 80}$$

$$9.9531 - 10$$

$$= \log 0.8976. Ans.$$

14. Find by logarithms the value of 0.02187 .

$$\log 0.02187 = 8.3398 - 10$$

$$80. -80$$

$$9 \overline{88.3398 - 90}$$

$$9.8155 - 10$$

$$= \log 0.6539. Ans.$$

15. Find by logarithms the value of $93.73^{\frac{1}{2}}$.

$$\log 93.73 = 1.9719$$

$$2 | 1.9719$$

$$0.9860$$

$$= \log 9.683. Ans.$$

16. Find by logarithms the value of $21.97^{\frac{5}{6}}$.

$$\log 21.97 = 1.3418$$

$$6 \overline{\smash{\big)}\, 6.7090}$$

$$1.1182$$

$$= \log 13.13. Ans.$$

17. Find by logarithms the value of $7.935^{\frac{5}{7}}$.

$$\log 7.935 = 0.8996$$

$$7 \overline{)4.4980}$$

$$0.6426$$

$$= \log 4.391. Ans.$$

18. Find by logarithms the value of $0.815^{\frac{8}{4}}$.

$$\log 0.815 = 9.9112 - 10$$

$$\frac{3}{9.7336 - 10}$$

$$30. \quad -30$$

$$4 \overline{\smash{\big)}39.7336 - 40}$$

$$9.9334 - 10$$

$$= \log 0.8578. \text{ Ans.}$$

19. Find by logarithms the value of $2.8145^{\frac{2}{3}}$.

$$\log 2.8145 = 0.4494$$

$$2$$

$$3 0.8988$$

$$0.2996$$

$$= \log 1.993. Ans.$$

20. Find by logarithms the value of $0.04165^{\frac{9}{14}}$.

$$\log 0.04165 = 8.6196 - 10$$

$$\frac{9}{7.5764 - 10}$$

$$\frac{130. -130}{14\overline{\smash)137.5764 - 140}}$$

$$9.8269 - 10$$

$$= \log 0.6713. Ans.$$

21. Find by logarithms the value of 4,516,298¹³.

Exercise 156. Page 357.

1. Find by logarithms the value of $\frac{56.407}{13.045}$.

2. Find by logarithms the value of $\frac{857.06}{3079.8}$.

$$\log 857.06 = 2.9330$$

$$\operatorname{colog} 3079.8 = \underbrace{6.5114 - 10}_{9.4444 - 10}$$

$$= \log 0.2783. \ \textit{Ans.}$$

3. Find by logarithms the value of $\frac{0.9387}{598.6}$.

$$\log 0.9387 = 9.9726 - 10$$

$$colog 598.6 = 7.2229 - 10$$

$$7.1955 - 10$$

$$= \log 0.001569. Ans.$$

4. Find by logarithms the value of $\frac{3069}{0.7891}$.

5. Find by logarithms the value of $\frac{75.46 \times 0.0765}{93.08 \times 98.071}$.

$$\log 75.46 = 1.8777$$

$$\log 0.0765 = 8.8837 - 10$$

$$\operatorname{colog} 93.08 = 8.0312 - 10$$

$$\operatorname{colog} 98.071 = \underbrace{8.0084 - 10}_{6.8010 - 10}$$

$$= \log 0.0006324. \text{ Ans.}$$

6. Find by logarithms the value of $\frac{98 \times 537 \times 0.0079}{67309 \times 0.0947}$.

$$\begin{array}{ll} \log & 98 = 1.9912 \\ \log & 537 = 2.7300 \\ \log 0.0079 = 7.8976 - 10 \\ \operatorname{colog} 67309 = 5.1719 - 10 \\ \operatorname{colog} 0.0947 = \underbrace{1.0237}_{8.8144 - 10} \\ = \log 0.06523. \ \textit{Ans.} \end{array}$$

7. Find by logarithms the value of $\frac{314 \times 7.18 \times 8132}{519 \times 827 \times 3.215}$.

$$\begin{array}{c} \log & 314 = 2.4969 \\ \log & 7.18 = 0.8561 \\ \log & 8132 = 3.9102 \\ \operatorname{colog} & 519 = 7.2848 - 10 \\ \operatorname{colog} & 827 = 7.0825 - 10 \\ \operatorname{colog} & 3.215 = \underbrace{9.4928 - 10}_{1.1233} \\ & = \log 13.28. \ \textit{Ans.} \end{array}$$

8. Find by logarithms the value of $\frac{212 \times 2.16 \times 8002}{536 \times 351 \times 7.256}$.

$$\log 212 = 2.3263$$

$$\log 2.16 = 0.3345$$

$$\log 8002 = 3.9032$$

$$\operatorname{colog} 536 = 7.2708 - 10$$

$$\operatorname{colog} 351 = 7.4547 - 10$$

$$\operatorname{colog} 7.256 = 9.1393 - 10$$

$$0.4288$$

$$= \log 2.684. \text{ Ans.}$$

9. Find by logarithms the value of $(\frac{4}{1})^4$.

$$\log 61 = 1.7853$$

$$colog 73 = 8.1367 - 10$$

$$9.9220 - 10$$

$$4$$

$$9.6880 - 10$$

$$= \log 0.4876. Ans.$$

10. Find by logarithms the value of $(\frac{14}{3})^3$.

$$\log 13 = 1.1139$$

$$\operatorname{colog} 71 = \underbrace{8.1487 - 10}_{9.2626 - 10}$$

$$\underbrace{\frac{3}{7.7878 - 10}}_{= \log 0.006134. Ans.}$$

11. Find by logarithms the value of $(5^{5}_{11})^{2}$.

12. Find by logarithms the value of $(4\frac{4}{31})^8$.

$$4\frac{4}{31} = \frac{128}{31}.$$

$$\log 128 = 2.1072$$

$$\cosh 31 = \frac{8.5086 - 10}{0.6158}$$

$$\frac{3}{1.8474}$$

$$= \log 70.37. Ans.$$

13. Find by logarithms the value of $(\frac{1}{2})^5$.

$$\log 412 = 2.6149$$

$$\operatorname{colog} 617 = 7.2097 - 10$$

$$9.8246 - 10$$

$$\frac{5}{9.1230 - 10}$$

$$= \log 0.1327. \text{ Arg.}$$

14. Find by logarithms the value of $(\frac{3}{5})^8$.

$$\log 83 = 1.9191$$

$$\cos 97 = 8.0132 - 10$$

$$9.9323 - 10$$

$$\frac{8}{9.4584 - 10}$$

$$= \log 0.2873. Ans.$$

15. Find by logarithms the value of $(\frac{507}{522})^2$.

16. Find by logarithms the value of $(\frac{1741}{116})^8$.

$$\log 1741 = 3.2408$$

$$\operatorname{colog} 1816 = \frac{6.7409 - 10}{9.9817 - 10}$$

$$\frac{8}{9.8536 - 10}$$

$$= \log 0.7138. Ans.$$

17. Find by logarithms the value of

$$\frac{19.258 \times 3.1416 \times 812.72}{716.4 \times 8.002 \times 21.465}$$

$$\log 19.258 = 1.2846$$

$$\log 3.1416 = 0.4971$$

$$\log 812.72 = 2.9100$$

$$\operatorname{colog} 716.4 = 7.1449 - 10$$

$$\operatorname{colog} 8.002 = 9.0968 - 10$$

$$\operatorname{colog} 21.465 = 8.6683 - 10$$

$$9.6017 - 10$$

$$= \log 0.3996. Ans.$$

18. Find by logarithms the value of

$$\frac{2018 \times 0.00261 \times 1728}{1412 \times 0.0965 \times 0.08621}$$

$$\log 2018 = 3.3050$$

$$\log 0.00261 = 7.4166 - 10$$

$$\log 1728 = 3.2375$$

$$\operatorname{colog} 1412 = 6.8502 - 10$$

$$\operatorname{colog} 0.0965 = 1.0155$$

$$\operatorname{colog} 0.08621 = 1.0644$$

$$2.8892$$

$$= \log 774.8. Ans.$$

19. Find by logarithms the value of

$$\frac{44816 \times 17.265 \times 181}{28754 \times 1.2871 \times 206.45}$$

$$\log 44816 = 4.6514$$

$$\log 17.265 = 1.2371$$

$$\log 181 = 2.2577$$

$$\operatorname{colog} 28754 = 5.5413 - 10$$

$$\operatorname{colog} 1.2871 = 9.8904 - 10$$

$$\operatorname{colog} 206.45 = 7.6852 - 10$$

$$1.2631$$

$$= \log 18.33. Ans.$$

20. Find by logarithms the value of

$$\frac{216.1 \times 5280 \times 144.2}{187.42 \times 4622.6 \times 156.8}$$

$$\log 216.1 = 2.3347$$

$$\log 5280 = 3.7226$$

$$\log 144.2 = 2.1590$$

$$\operatorname{colog} 187.42 = 7.7271 - 10$$

$$\operatorname{colog} 4622.6 = 6.3351 - 10$$

$$\operatorname{colog} 156.8 = 7.8047 - 10$$

$$0.0832$$

$$= \log 1.211. Ans.$$

21. Find by logarithms the value of

22. Find by logarithms the value of

$$\frac{14.718 \times 48.67 \times 96.542}{2746.2 \times 0.0467 \times 2.1876}$$

$$\log 14.718 = 1.1678$$

$$\log 48.67 = 1.6872$$

$$\log 96.542 = 1.9847$$

$$\operatorname{colog} 2746.2 = 6.5613 - 10$$

$$\operatorname{colog} 0.0467 = 1.3307$$

$$\operatorname{colog} 2.1876 = 9.6601 - 10$$

$$2.3918$$

$$= \log 246.5. \text{ Ans.}$$

23. Find by logarithms the value of

$$\sqrt{\frac{83.25 \times 4267 \times 0.008576}{0.0327 \times 687.5 \times 0.005003}}$$

$$\log \quad 83.25 = 1.9204$$

$$\log \quad 4267 = 3.6301$$

$$\log \quad 0.008576 = 7.9333 - 10$$

$$\operatorname{colog} \quad 0.0327 = 1.4855$$

$$\operatorname{colog} \quad 687.5 = 7.1627 - 10$$

$$\operatorname{colog} \quad 0.005003 = 2.3008$$

$$2 \boxed{4.4328}$$

$$2.2164$$

$$= \log 164.6. Ans.$$

24. Find by logarithms the value of

$$\frac{4.163^{2} \times 17.74^{4} \times 0.7183^{\frac{1}{2}}}{\sqrt{3.013^{2} \times 34.34 \times 0.08137^{\frac{1}{2}}}}$$

$$\log \quad 4.163^{2} = 1.2388$$

$$\log \quad 17.74^{4} = 4.9960$$

$$\log \quad 0.7183^{\frac{1}{2}} = 9.9282 - 10$$

$$\operatorname{colog} \quad 3.013^{2} = 9.0420 - 10$$

$$\operatorname{colog} \quad 34.34 = 8.4642 - 10$$

$$\operatorname{colog} \quad 0.08137^{\frac{1}{2}} = 0.5447$$

$$3 \overline{4.2139}$$

$$1.4046$$

$$= \log 25.39. Ans.$$

25. Find by logarithms the value of

$$\sqrt[4]{0.7132 \times 9.245 \times 0.5477^{2}}$$

$$\sqrt[4]{76.93 \times 0.000173^{\frac{1}{3}} \times 0.01}$$

$$\log \quad 0.7132 = 9.8532 - 10$$

$$\log \quad 9.245 = 0.9659$$

$$\log \quad 0.5477^{2} = 9.4772 - 10$$

$$\cosh \quad 76.93 = 8.1139 - 10$$

$$\cosh \quad 0.00173^{\frac{1}{3}} = 1.2540$$

$$\cosh \quad 0.01 = 2.0000$$

$$4 \boxed{1.6642}$$

$$0.4161$$

$$= \log 2.607. Ans.$$

26. Find by logarithms the value of

$$\frac{85.02^{2} \times 0.002753 \times 97.98^{\frac{1}{2}}}{7.298 \times 0.04754 \times 8.156^{\frac{1}{2}}}$$

$$\log \quad 65.02^{2} = 3.6260$$

$$\log \quad 0.002753 = 7.4398 - 10$$

$$\log \quad 97.98^{\frac{1}{2}} = 0.9956$$

$$\operatorname{colog} \quad 7.298 = 9.1368 - 10$$

$$\operatorname{colog} \quad 0.04754 = 1.3229$$

$$\operatorname{colog} \quad 8.156^{2} = 8.1770 - 10$$

$$5 \boxed{0.6981}$$

$$0.1396$$

$$= \log 1.379. Ans.$$

27. Find by logarithms the value of

$$\frac{23.79^{2} \times 0.00756 \times 0.4648^{\frac{1}{3}}}{4723^{\frac{1}{2}} \times 0.6571 \times 0.8246^{\frac{1}{3}}}$$

$$\log 23.79^{2} = 2.7528$$

$$\log 0.00756 = 7.8785 - 10$$

$$\log 0.4648^{\frac{1}{3}} = 9.8891 - 10$$

$$\cosh 4723^{\frac{1}{2}} = 8.1629 - 10$$

$$\cosh 0.6571 = 0.1823$$

$$\cosh 0.8246^{\frac{1}{4}} = 0.0209$$

$$8.8865 - 10$$

$$50. -50$$

$$6 58.8865 - 60$$

$$9.8144 - 10$$

$$= \log 0.6523. Ans.$$

28. Find by logarithms the value of

$$\sqrt{\frac{0.6012 \times 0.6012^{\frac{1}{2}} \times 0.6012^{\frac{1}{3}}}{0.5926 \times 0.5926^{\frac{1}{2}} \times 0.5926^{\frac{1}{3}}}}$$

$$\log 0.6012 = 9.7790 - 10$$

$$\log 0.6012^{\frac{1}{2}} = 9.8895 - 10$$

$$\log 0.6012^{\frac{1}{3}} = 9.9263 - 10$$

$$\cosh 0.5926 = 0.2272$$

$$\cosh 0.5926^{\frac{1}{2}} = 0.1136$$

$$\cosh 0.5926^{\frac{1}{3}} = 0.0757$$

$$7 \boxed{0.0113}$$

$$0.0016$$

$$= \log 1.004. Ans.$$

29. Find by logarithms the value of

$$\begin{pmatrix}
0.03214 \times 3.718^{3} \times 0.07824^{\frac{1}{2}} \\
0.05142 \times 0.4728^{\frac{1}{2}} \times 1.239^{3}
\end{pmatrix}^{\frac{3}{4}}$$

$$\log 0.03214 = 8.5071 - 10$$

$$\log 3.718^{3} = 1.7109$$

$$\log 0.07824^{\frac{1}{2}} = 9.4467 - 10$$

$$\operatorname{colog} 0.05142 = 1.2888$$

$$\operatorname{colog} 0.4728^{\frac{1}{2}} = 0.1626$$

$$\operatorname{colog} 1.239^{3} = 9.7207 - 10$$

$$0.8368$$

$$\frac{3}{4} \underbrace{2.5104}_{0.6276}$$

$$= \log 4.242. Ans.$$

30. Find by logarithms the value of

$$\frac{0.07986 \times 0.7555^{\frac{1}{3}} \times 0.5557^{\frac{1}{3}}}{0.06897 \times 0.5777^{\frac{1}{3}} \times 0.05698^{2}})^{\frac{3}{7}}$$

$$\log 0.07986 = 8.9023 - 10$$

$$\log 0.7555^{\frac{1}{3}} = 9.9594 - 10$$

$$\log 0.5557^{\frac{1}{3}} = 9.9150 - 10$$

$$\operatorname{colog} 0.06897 = 1.1614$$

$$\operatorname{colog} 0.5777^{\frac{1}{3}} = 0.0794$$

$$\operatorname{colog} 0.05698^{2} = 2.4886$$

$$2.5061$$

$$\frac{3}{7.5183}$$

$$1.0740$$

$$= \log 11.86. Ans.$$

31. Find by logarithms the value of

$$\frac{(0.07543 \times 0.7689^{\frac{1}{2}} \times 0.8965^{2})^{\frac{1}{8}}}{(0.06987 \times 0.07986^{\frac{1}{2}} \times 0.9867^{\frac{3}{2}})}$$

$$\log 0.07543 = 8.8776 - 10$$

$$\log 0.7689^{\frac{1}{2}} = 9.9429 - 10$$

$$\log 0.8965^{2} = 9.9052 - 10$$

$$\cosh 0.06987 = 1.1557$$

$$\cosh 0.07986^{\frac{1}{2}} = 0.5488$$

$$\cosh 0.9867^{\frac{3}{8}} = 0.0039$$

$$0.4341$$

$$\frac{5}{0.3618}$$

$$= \log 2.301. \text{ Ans.}$$

Exercise 157. Page 360.

1. Find the compound interest on \$1280 for 7 years at 4½%.

$$A = 1280 \times 1.045^{7}$$
.
 $log 1280 = 3.1072$
 $log 1.045^{7} = \underbrace{0.1337}_{3.2409}$
 $= log 1742$.
\$ 1742 - \$ 1280 = \$ 462. Ans.

2. Find the compound interest on \$2645 for 5 years at 3½%.

$$A = 2645 \times 1.035^{5}$$
.
 $\log 2645 = 3.4224$
 $\log 1.035^{5} = \frac{0.0745}{3.4969}$
 $= \log 3140$.
\$ 3140 - \$ 2645 = \$ 495. Ans.

3. Find the amount of \$848 for 6 years at 5% compound interest.

$$A = 848 \times 1.05^6$$
.
 $\log 848 = 2.9284$
 $\log 1.05^6 = 0.1272$
 3.0556
 $= \log 1137$.
\$1137. Ans.

4. Find the amount of \$3600 for 5 years at $5\frac{1}{2}\%$ compound interest.

$$A = 3600 \times 1.055^{6}$$
.
 $\log 3600 = 3.5563$
 $\log 1.055^{6} = 0.1165$
 3.6728
 $= \log 4708$.
\$4708. Ans.

5. What principal will amount to \$720 in 4 years at 6% compound interest?

$$720 = P \times 1.04^{6}$$
.

$$\therefore P = \frac{720}{1.04^{6}}$$

$$\log 720 = 2.8573$$

$$\operatorname{colog} 1.04^{6} = \frac{9.8980}{2.7553} - 10$$

$$= \log 569.3$$
\$ 569.30. Ans.

6. What principal will amount to \$1640 in 6 years at 3% compound interest?

$$1640 = P \times 1.03^{6}.$$

$$\therefore P = \frac{1640}{1.03^{6}}.$$

$$\log 1640 = 3.2148$$

$$\operatorname{colog} 1.03^{6} = \frac{9.9232}{3.1380} - 10$$

$$= \log 1374.$$
\$ 1374. Ans.

7. At what rate of interest will \$648 amount to \$788.20 in 5 years at compound interest?

$$788.20 = 648 \times (1 + r)^{5}.$$

$$\therefore (1 + r)^{5} = \frac{788.20}{648},$$
and
$$1 + r = \sqrt[5]{\frac{788.20}{648}}.$$

$$\log 788.20 = 2.8966$$

$$\cosh 648 = 7.1884 - 10$$

$$5 \boxed{0.0850}$$

$$0.0170$$

$$= \log 1.04.$$

Therefore, the required rate of interest is 4%. Ans.

8. At what rate of interest will \$2415 amount to \$3237 in 6 years at compound interest?

$$3237 = 2415 \times (1 + r)^{6}.$$

$$\therefore (1 + r)^{6} = \frac{3237}{2415},$$
and
$$1 + r = \sqrt[6]{\frac{3237}{2415}}.$$

$$\log 3237 = 3.5101$$

$$\operatorname{colog} 2415 = 6.6171 - 10$$

$$6 \boxed{0.1272}$$

$$0.0212$$

Therefore, the required rate of interest is 5%. Ans.

 $= \log 1.05.$

9. In what time at 4½% compound interest will \$ 1265 amount to \$ 1576?

 $log 1576 = log 1265 + n \times log 1.045,$ $n \times log 1.045 = log 1576 + colog 1265.$

$$n = \frac{\log 1576 + \operatorname{colog} 1265}{\log 1.045}$$
$$= \frac{3.1976 + 6.8979 - 10}{0.0191}$$
$$= \frac{0.0955}{0.0191} = 5.$$

The required time is 5 years. Ans.

10. In what time at 5% compound interest will \$ 1845 amount to \$2413?

 $\log 2413 = \log 1845 + n \times \log 1.05,$ $n \times \log 1.05 = \log 2413 + \operatorname{colog} 1845.$

$$n = \frac{\log 2413 + \operatorname{colog} 1845}{\log 1.05}$$
$$= \frac{3.3825 + 6.7340 - 10}{0.0212}$$
$$= \frac{0.1165}{0.0212} = 5.4953.$$

5.4953 yr. = 5 yr. 5 mo. 28 dy. Ans.

Exercise 158. Page 363.

1. A man deposits \$60 in a savings bank, and draws out his whole account at the end of 8 years, with 4% compound interest. What amount does he receive?

The amount of \$1 for 8 yr. at 4% is \$1.36857.

\$82.11. Ans.

2. What will \$100 amount to in 7 years with interest at 8% per annum, compounded semi-annually?

The amount of \$1 for 14 yr. at 4% is \$1.73168.

\$ 173.17. Ans.

3. In how many years will a sum of money double itself at 6% compounded annually?

By the table, in a little less than 12 yr. Ans.

4. In how many years will a sum of money treble itself at 6%, compounded annually?

By the table, in a little less than 19 yr. Ans.

5. In how many years will \$87 amount to \$99 at 3%, compounded annually?

Since \$87 amounts to \$99, \$1 amounts to \$% = \$1.13793. By the table, \$1 will in 4 yr. at 3% amount to \$1.12551.

Hence, the required time is a little more than 4 yr. Ans.

6. In how many years will \$100 amount to \$175 at 4%, compounded annually?

Since \$100 amounts to \$175, \$1 amounts to $\frac{175}{100}$ = \$1.75000. By the table, \$1 will in 14 yr. at 4% amount to \$1.73168.

Hence, the required time is a little more than 14 yr. Ans.

- 7. At what rate per cent will a sum of money double itself in 12 years, compound interest?
- \$1 will in 12 yr. amount to \$2. By the table, \$1 will in 12 yr. at 6% amount to \$2.01220. Hence, the required rate is 6%, nearly. Ans.
- 8. At what rate will a sum of money treble itself in 19 years, compound interest?
- \$1 will in 19 yr. amount to \$3. By the table, \$1 will in 19 yr. at 6% amount to \$3.02560. Hence, the required rate is 6%, nearly. Ans.
- 9. At what rate will \$80 at compound interest amount to \$110 in 8 years?

Since \$80 amounts to \$110, \$1 amounts to \$ $\frac{110}{80}$ = \$1.37500. By the table, \$1 will in 8 yr. at 4% amount to \$1.36857. Hence, the required rate is 4%, nearly. Ans.

10. What sum must be invested at 5%, compound interest, to amount to \$1200 in 7 years?

The amount of \$1 for 7 yr. at 5% is \$1.40710. Since \$1.40710 is the amount of \$1, \$1200 is the amount of $\frac{1200}{1.40710} = 852.83 . Ans.

11. What sum must be invested at 4%, compound interest, to amount to \$2000 in 10 years? To amount to \$5000 in 8 years?

The amount of \$1 for 10 yr. at 4% is \$1.48024. Since \$1.48024 is the amount of \$1, \$2000 is the amount of $\frac{2000}{1.48024} = 1351.13 . Ans.

The amount of \$1 for 8 yr. at 4% is \$1.36857. Since \$1.36857 is the amount of \$1, \$5000 is the amount of $\frac{5000}{1.36857} = 3653.45 . Ans.

12. At what rate compound interest will \$462.50 yield \$277.98 interest in 12 years?

The amount of \$462.50 for 12 yr. is \$462.50 + \$277.98 = \$740.48. Since the amount of \$462.50 is \$740.48, the amount of \$1 is $\frac{740.48}{462.50}$ = \$1.60103. By the table, \$1 will in 12 yr. at 4% amount to \$1.60103. Hence, the required rate is 4%. Ans.

13. What principal will in 10 years at 6% amount to \$3612.22, interest being compounded semi-annually?

The amount of \$1 for 20 yr. at 3% is \$1.80611. Since \$1.80611 is the amount of \$1, \$3612.22 is the amount of $\frac{3612.22}{1.80611} = 2000 . Ans.

14. In what time at 5% will \$1250 amount to \$2000, interest being compounded semi-annually?

Since \$1250 amounts to \$2000, \$1 amounts to $\frac{1200}{1250} = 1.60000$. By the table, \$1 at $\frac{12}{2}$ % will in 19 yr. amount to \$1.59865. Hence, the required time is nearly 19 half years, or $\frac{12}{2}$ years, nearly. Ans.

15. At what rate per annum will \$500 amount to \$779.83 in 9 years, interest being compounded semi-annually?

Since \$500 amounts to \$779.83, \$1 amounts to $\frac{779.83}{500} = 1.55966$. By the table, \$1 will in 18 yr. at $2\frac{1}{4}$ % amount to \$1.55966. Hence, the required rate is $2\frac{1}{4}$ % semi-annually, or 6% annually. 6%. Ans.

Exercise 159. Page 366.

1. Find the present value of an annuity of \$300 for 6 years, if money is worth 5%

$$P = \frac{300}{0.05} \times \frac{1.05^6 - 1}{1.05^6}$$

$$\log 1.05 = 0.0212$$

$$\frac{6}{0.1272} = \log 1.34$$

$$\therefore P = \frac{300}{0.05} \times \frac{0.34}{1.34}$$

$$\log 300 = 2.4771$$

$$\log 0.34 = 9.5315 - 10$$

$$\operatorname{colog} 0.05 = 1.3010$$

$$\operatorname{colog} 1.34 = 9.8728 - 10$$

$$3.1824 = \log 1522$$

2. Find the present value of an annuity of \$600 for 4 years, if money is worth $5\frac{1}{2}$ %.

8 1522. Ans.

\$2104. Ans.

$$P = \frac{600}{0.055} \times \frac{1.055^4 - 1}{1.055^4}.$$

$$\log 1.055 = 0.0233$$

$$\frac{4}{0.0932} = \log 1.239.$$

$$\therefore P = \frac{600}{0.055} \times \frac{0.239}{1.239}.$$

$$\log 600 = 2.7782$$

$$\log 0.239 = 9.3784 - 10$$

$$\operatorname{colog} 0.055 = 1.2596$$

$$\operatorname{colog} 1.239 = 9.9068 - 10$$

$$3.3230 = \log 2104.$$

3. Find the present value of an annuity of \$800 for 5 years, if money is worth 6%.

$$P = \frac{800}{0.06} \times \frac{1.06^{5} - 1}{1.06^{5}}$$

$$\log 1.06 = 0.0253$$

$$\frac{5}{0.1265} = \log 1.338$$

$$\therefore P = \frac{800}{0.06} \times \frac{0.338}{1.338}$$

$$\log 800 = 2.9031$$

$$\log 0.338 = 9.5289 - 10$$

$$\cosh 0.06 = 1.2218$$

$$\cosh 0.338 = 9.8735 - 10$$

$$3.5273 = \log 3368$$

$$\$ 3368. Ans.$$

4. Find the present value of a perpetual scholarship of \$900, if money is worth 3½%.

$$P = \frac{900}{0.035}$$

$$\log 900 = 2.9542$$

$$\operatorname{colog} 0.035 = \underbrace{1.4559}_{4.4101} = \log 25,710.$$

$$\$ 25,710. Ans.$$

5. Find the present value of a perpetual fellowship of \$3200, if money is worth 41%.

$$P = \frac{3200}{0.0425}$$

$$\log 3200 = 3.5051$$

$$\operatorname{colog} 0.0425 = 1.3716$$

$$4.8767 = \log 75,280$$

$$\$ 75,280. Ans.$$

6. What is the value of a sinking fund, if \$25,000 is set apart yearly for 7 years at 4½% compound interest?

$$A = \frac{25000 \times (1.045^7 - 1)}{0.045}.$$

$$\log 1.045 = 0.0191$$

$$\frac{7}{0.1337} = \log 1.361.$$

$$\therefore A = \frac{25000 \times 0.361}{0.045}.$$

$$\log 25000 = 4.3979$$

$$\log 0.361 = 9.5575 - 10$$

$$\operatorname{colog} 0.045 = \frac{1.3468}{5.3022}$$

$$= \log 200,500.$$

7. What is the value of a sinking fund, if \$18,000 is set apart yearly for 5 years at 3½% compound interest?

$$A = \frac{18000 \times (1.035^{5} - 1)}{0.035}.$$

$$\log 1.035 = 0.0149$$

$$\frac{5}{0.0745} = \log 1.187.$$

$$\therefore A = \frac{18000 \times 0.187}{0.035}.$$

$$\log 18000 = 4.2553$$

$$\log 0.187 = 9.2718 - 10$$

$$\operatorname{colog} 0.035 = 1.4559$$

$$\frac{4.9830}{4.9830}$$

$$= \log 96,160.$$

$$\$ 96,160.$$

$$Ans.$$

Exercise 160. Page 369.

1. Find the present value of an annuity of \$900 for 15 years at 4%.

\$ 200,500. Ans.

2. Find the present value of an annuity of \$1500 for 12 years at 4%.

3. Find the present value of an annual pension of \$144 for 10 years at $3\frac{1}{2}$ %.

4. Find the present value of a scholarship of \$200 for 25 years at $3\frac{1}{2}$ %.

5. Find the present value of an annuity of \$2500 for 30 years at 4%.

\$17.29203

2500 864601500

3458406

\$43230.07500 **\$43,230.08**. Ans.

6. Find the present value of an annuity of \$250 for 12 years at 3½%.

\$ 9.66333

250 48316650 1932666

\$ 2415.83250

\$2415.83. Ans.

7. A person 22 years old has a life annuity of \$750. Find its present value at 4%.

The expectancy of life for a person 22 yr. old is about 40 yr.

8 19.79277

750 98963850 13854939 \$ 14844.57750

\$ 14,844.58. Ans.

8. A person 35 years old has a life annuity of \$1800. Find its present value at 4%.

The expectancy of life for a person 35 yr. old is about 31 yr.

\$ 17.58849

1800 1407079200 1758849 \$ 31659.28200

\$31,659.28. Ans.

9. A person 53 years old has a life annuity of \$500. Find its present value at 4%.

The expectancy of life for a person 53 yr. old is about 19 yr.

\$ 13.13394

500

8 6566.97000

\$6566.97. Ars.

10. A person 75 years old has a life annuity of \$2400. Find its present value at 3½%.

The expectancy of life for a person 75 yr. old is about 7 yr.

8 14674.89600

\$14,674.90. Ans.

11. A boy 15 years old has a life annuity of \$3250. Find its present value at 4%.

The expectancy of life for a person 15 yr. old is about 45 yr.

$$P = \frac{3250}{0.04} \times \frac{1.04^{45} - 1}{1.04^{45}}$$

$$P = \frac{3250}{0.04} \times \frac{4.821}{5.821}$$

$$\log 3250 = 3.5119$$

$$\log 4.821 = 0.6831$$

$$\operatorname{colog} 0.04 = 1.3979$$

$$\operatorname{colog} 5.821 = \frac{9.2350 - 10}{4.8279 = \log 67,280}$$

$$\$ 67,280. \ Ans.$$

12. A person 22 years old pays \$4948.19 for a life annuity. If interest is 4%, find the amount of the annuity.

The expectancy of life for a person 22 yr. old is about 40 yr. The present value of an annuity of \$1 per annum at 4% for 40 yr. is \$19.79277.

Therefore, \$4948.19 is the present value of an annuity of

$$\begin{array}{c} \$ \, \frac{4948.19}{19.79277} = \$ \, 250. \quad Ans. \\ \hline 250 \\ 1979277 \overline{\smash{\big)}494819000} \\ \underline{3958554} \\ \hline 9896360 \\ \underline{9896385} \\ 00 \\ \end{array}$$

13. A person 29 years old pays \$7465.84 for a life annuity. If interest is 4%, find the amount of the annuity.

The expectancy of life for a person 29 yr. old is about 35 yr.

The present value of an annuity of \$1 per annum at 4% for 35 yr. is \$18.66461.

Therefore, \$7465.84 is the present value of an annuity of

$$\frac{7465.84}{18.66461} = \$ 400$$
. Ans.

14. A person 35 years old pays \$9368.14 for a life annuity. If interest is 3½%, find the amount of the annuity.

The expectancy of life for a person 35 yr. old is about 31 yr.

The present value of an annuity of \$1 per annum at 3½% for 31 yr. is \$18.73628.

Therefore, \$9368.14 is the present value of an annuity of

$$\$ \frac{9368.14}{18.73628} = \$ 500. \ Ans.$$

$$500$$

$$1873628)936814000$$

$$9368140$$

$$00$$

15. A person 44 years old pays \$5933.35 for a life annuity. If interest is 3½%, find the amount of the annuity.

The expectancy of life for a person 44 yr. old is about 25 yr.

The present value of an annuity of \$1 per annum at $3\frac{1}{2}$ % for 25 yr. is \$16.48152.

Therefore, \$ 5933.35 is the present value of an annuity of

$$\$ \frac{5933.35}{16.48152} = \$ 360. \ Ans.$$

$$\frac{360}{1648152)593335000}$$

$$\frac{4944456}{9888940}$$

$$\frac{9888912}{280}$$

Exercise 161. Page 371.

1. Find the cost at compound interest of a coöperative bank share that matured in 10 years, when money was worth 4½%.

$$10 \text{ yr.} = 120 \text{ mo.}$$

The rate of interest was $4\frac{1}{2}$ % yearly or 0.375% monthly.

$$A = \frac{1 \times (1.00375^{120} - 1)}{1.00375 - 1}.$$

$$\log 1.00375 = 0.0016$$

$$\frac{120}{320}$$

$$\frac{16}{0.1920}$$

$$= \log 1.556.$$

$$A = \frac{0.556}{0.00375}$$

$$\log \quad 0.556 = 9.7451 - 10$$

$$colog \quad 0.00375 = \frac{2.4260}{2.1711}$$

$$= \log 148.3.$$
\$ 148.30. Ans.

2. Find the cost at compound interest of a coöperative bank share that matured in 11½ years, when money was worth 5%.

$$11\frac{1}{2}$$
 yr. = 138 mo.

The rate of interest was 5% yearly, or $\frac{5}{12}$ % monthly.

$$A = \frac{1 \times (1.00_{\frac{1}{12}}^{\frac{5}{188}} - 1)}{1.00_{\frac{5}{12}} - 1}.$$

3. How much more does it cost to borrow \$2000 from a coöperative bank, monthly interest being \$12, and the shares maturing in 10 years, than to borrow \$2000 at compound interest for 10 years, if money is worth 5% in both cases?

To borrow \$2000, the shareholder must own 10 shares; and he pays monthly \$10 + \$12, or \$22, for 10 yr., that is 120 mo.

The rate of interest is 5 % yearly or $\frac{5}{12}$ % monthly.

$$A = \frac{22 \times (1.00_{13}^{5})^{120} - 1}{1.00_{13}^{5} - 1}.$$

$$\log 1.00_{13}^{5} = 0.0018$$

$$\frac{120}{360}$$

$$\frac{18}{0.2160} = \log 1.644.$$

$$A = \frac{22 \times 0.644}{0.00\frac{5}{13}} = \frac{12 \times 22 \times 64.4}{5}$$

$$\log 12 = 1.0792$$

$$\log 22 = 1.3424$$

$$\log 64.4 = 1.8089$$

$$0 = 9.3010 - 10$$

Hence, the cost of borrowing \$2000 from the cooperative bank is \$3400.

 $3.5315 = \log 3400.$

$$A = 2000 \times 1.05^{10}$$
.
 $\log 2000 = 3.3010$
 $\log 1.05^{10} = 0.2120$
 $3.5130 = \log 3258$.

Hence, the cost of borrowing \$2000 at compound interest is \$3258.

$$$3400 - $3258 = $142$$
. Ans.

MISCELLANEOUS PROBLEMS.

1. Make six different numbers with the digits 1, 2, 3, and find their sum.

2. Make six different numbers with the digits 2, 3, 5, and find, by logarithms, their continued product.

$$235 \times 253 \times 325$$

 $\times 352 \times 523 \times 532$.
 $\log 235 = 2.3711$
 $\log 253 = 2.4031$
 $\log 325 = 2.5119$
 $\log 352 = 2.5465$
 $\log 523 = 2.7185$
 $\log 532 = 2.7259$
 15.2770

 $= \log 1,892,000,000,000,000.$

3. Make six different numbers with the digits 8, 7, 3, and find, by logarithms, their continued product.

- $= \log 61,770,000,000,000,000.$
- 4. Find, by logarithms, the missing term in each of the following proportions:

(i)

$$7.13:3.57::4.18:?.$$

$$\frac{3.57 \times 4.18}{7.13} = 2.093. \text{ Ans.}$$

$$\log 3.57 = 0.5527$$

$$\log 4.18 = 0.6212$$

$$\cosh 7.13 = \frac{9.1469}{0.3208} - 10$$

$$= \log 2.093.$$

(ii)
$$5.89:76.3::?:38.7.$$

$$\frac{5.89 \times 38.7}{76.3} = 2.987. \text{ Ans.}$$

$$\log 5.89 = 0.7701$$

$$\log 38.7 = 1.5877$$

$$\cosh 76.3 = 8.1175 - 10$$

$$0.4753$$

$$= \log 2.987.$$

$$(iv)$$

$$?:69.7::3.79:29.4.$$

$$\log 69.7 = 1.8432$$

$$\log 3.79 = 0.5786$$

$$\cosh 99.7 = 1.9432$$

$$\log 3.79 = 0.5786$$

$$\cosh 99.7 = 1.8432$$

$$\cosh 99.7 = 1.843$$

5. Find, by logarithms, the value of $0.08^{\frac{1}{3}}$; $2734^{\frac{1}{3}}$; $21.97^{\frac{1}{3}}$; $7^{3.6}$; $9.71^{\frac{7}{3}}$; $7.936^{\frac{5}{7}}$.

$$\frac{1}{3} \times \log 0.08 = \frac{1}{3} \times (8.9031 - 10) = 9.6344 - 10 = \log 0.4309.$$
 $\frac{1}{3} \times \log 2734 = \frac{1}{3} \times 3.4368 = 1.1456 = \log 13.98.$
 $\frac{1}{3} \times \log 21.97 = \frac{1}{3} \times 1.3418 = 0.4473 = \log 2.801.$
 $\frac{1}{3} \times \log 7 = 3.6 \times 0.8451 = 3.0424 = \log 1103.$
 $\frac{1}{3} \times \log 9.71 = \frac{1}{3} \times 0.9872 = 2.3035 = \log 201.1.$
 $\frac{1}{3} \times \log 7.936 = \frac{1}{3} \times 0.8996 = 0.6426 = \log 4.391.$

6. Find the value of

$$\sqrt[5]{\frac{4.79^2 \times 3.1416 \times 12.72}{0.5236 \times 14.28}}$$

$$\log 4.79^2 = 1.3606$$

$$\log 3.1416 = 0.4971$$

$$\log 12.72 = 1.1045$$

$$\operatorname{colog} 0.5236 = 0.2810$$

$$\operatorname{colog} 14.28 = 8.8453 - 10$$

$$5 2.0885$$

$$0.4177$$

$$= \log 2.616. Ans.$$

7. If the air-line distance between two points is 1534 ft., and the difference of level is 34 ft., what is the horizontal distance between the two points?

$$\sqrt{1534^2 - 34^2}$$
 ft.
= $\sqrt{2353156 - 1156}$ ft.
= $\sqrt{2352000}$ ft.
= 1533.623 ft. Ans.

8. If the road distance is 1 mi., and the rise 347 ft., find the horizontal distance.

$$\sqrt{5280^2 - 347^2} \text{ ft.}$$

$$= \sqrt{27878400 - 120409} \text{ ft.}$$

$$= \sqrt{27757991} \text{ ft.}$$

$$= 5268.585 \text{ ft.} \text{ Ans.}$$

$$27 75 79 91 (5268.585 \frac{25}{102)275} \frac{204}{204} \frac{1046)7179}{6276} \frac{6276}{10528)90391} \frac{84224}{10536)61670} \frac{52680}{89900} \frac{84288}{56120} \frac{52680}{52680}$$

9. If the road distance is half a mile, and the horizontal distance 2513 ft., find the difference of level.

$$\frac{1}{2} \text{ mi.} = 2640 \text{ ft.}$$

$$\sqrt{2640^2 - 2513^2} \text{ ft.}$$

$$= \sqrt{6969600} - 6315169 \text{ ft.}$$

$$= \sqrt{654431} \text{ ft.} = 808.97 \text{ ft.}$$
Ans.
$$654431(808.97)$$

$$64$$

$$1608)14431$$

$$12864$$

$$1616)15670$$

$$14544$$

$$11260$$

10. The diagonal of a rectangular floor is 34.6 ft., and the width is 17.8 ft. Find the length of the floor.

$$\sqrt{34.6^2 - 17.8^2} \text{ ft.}$$

$$= \sqrt{1197.16 - 316.84} \text{ ft.}$$

$$= \sqrt{880.32} \text{ ft.} = 29.67 \text{ ft.}$$
Ans.
$$880.32(29.67)$$

$$4$$

$$49)480$$

$$441$$

$$586)3932$$

$$3516$$

$$592)4160$$

$$4144$$

11. The height of a tower on the bank of a river is 55 ft., and the length of a line from the top of the tower to the opposite bank is 78 ft. Find the breadth of the river.

$$\sqrt{78^2 - 55^2}$$
 ft. $= \sqrt{6084 - 3025}$ ft. $= \sqrt{3059}$ ft. $= 55.31$ ft. Ans. $\frac{3069(55.31)}{25}$
 $\frac{25}{105)559}$
 $\frac{525}{1103)3400}$
 $\frac{3309}{1106)910}$

12. The number of seamen at Portsmouth is 800, at Charlestown 404, and at Brooklyn 756. A ship is commissioned whose complement is 490 seamen. Determine the number to be drafted from each place to obtain a proportionate number from each.

800 + 404 + 756 = 1960.
$$\frac{404}{1960} \times 490 = 101$$
, C. $\frac{756}{1960} \times 490 = 200$, P. $\frac{756}{1960} \times 490 = 189$, B.

13. Show, without division, that 36,432 contains 8, 9, 11 as factors.

$$432 = 54 \times 8.$$

 $3+6+4+3+2=18.$
 $3+4+2=6+3.$ (§ 181)

14. Find the smallest multiplier that will make 47,250 a perfect cube.

$$47,250 = 2 \times 3^8 \times 5^8 \times 7.$$

 $2^2 \times 7^2 = 4 \times 49 = 196.$ Ans.

15. Find the proper fraction that, when reduced to a continued fraction, has for quotients 1, 3, 5, 7, 2, 4.

$$\frac{1}{1+\frac{1}{3+\frac{1}{5+\frac{1}{1+\frac{1}{4}}}}} \frac{\frac{1}{2+\frac{1}{4}} = \frac{4}{9}; \qquad \frac{1}{7+\frac{4}{9}} = \frac{9}{67}; \qquad \frac{1}{5+\frac{9}{67}} = \frac{67}{344};$$

$$\frac{1}{7+\frac{1}{2+\frac{1}{4}}} \frac{1}{3+\frac{67}{344}} = \frac{344}{1099}; \qquad \frac{1}{1+\frac{344}{1099}} = \frac{1099}{1443}.$$
Ans.

16. If the meter is equal to 1.09362 yd., find a series of four fractions that will express more and more nearly the true ratio of the meter to the yard.

$$1.09362 = 1\frac{9362}{1000000} = 1\frac{4681}{500000}.$$

$$4681)50000(10$$

$$\frac{46810}{3190)4681(1)}$$

$$\frac{3190}{1491)3190(2)}$$

$$\frac{2982}{208)1491(7)}$$

$$\frac{1456}{35}$$

$$1 + \frac{1}{10} = \frac{11}{10}.$$

$$1 + \frac{1}{10} = \frac{11}{10}.$$

$$1 + \frac{1}{100} = \frac{11}{10}.$$

$$1 + \frac{1}{100} = \frac{11}{10}.$$

$$1 + \frac{1}{100} = \frac{257}{235}.$$

$$1 + \frac{1}{10} = \frac{11}{10}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{12}{235}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{35}{32}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{257}{235}.$$

$$1 + \frac{1}{10 + \frac{1}{1}} = \frac{257}{32}.$$

17. Find the square factors contained in 33,075.

$$33,075 = 3^8 \times 5^2 \times 7^2$$
.
 $3^2 = 9$,
 $5^2 = 25$,
 $7^2 = 49$,
 $3^2 \times 5^2 = 225$,
 $5^2 \times 7^2 = 1225$,
 $3^2 \times 5^2 \times 7^2 = 1225$,
 $3^2 \times 5^2 \times 7^2 = 11,025$.
 $3^2 \times 5^2 \times 7^2 = 1225$,
 $3^2 \times 5^2 \times 7^2 = 11,025$.
 $3^2 \times 5^2 \times 7^2 = 1225$,
 $3^2 \times 5^2 \times 7^2 = 11,025$.

18. The height of St. Peter's, Rome, is $\frac{9}{100}$ of a mile, and that of St. Paul's, London, is $\frac{17}{264}$ of a mile. How many feet higher is St. Peter's than St. Paul's?

$$\frac{9}{110}$$
 of \$280 ft. = 432 ft $\frac{17}{264}$ of \$280 ft. = 340 ft.
432 ft. - 340 ft. = 92 ft. Ans.

19. How many days elapsed between the annular eclipse of May 15, 1836, and that of March 15, 1858?

`yr.	mo.	dy.
1858	3	15
1836	5	15
21	10	0

During the interval there were five leap years, and in the ten months from May 15 to March 15 there are 304 days.

 $21 \times 365 \text{ days} = 7665 \text{ days}$. (7665 + 304 + 5) days = 7974 days. Are

20. In a gale, a flagstaff 60 ft. high snaps 28.8 ft. from the bottom; and, not being wholly broken off, the top touches the ground. If the ground is level, how far is the top from the bottom?

$$60 \text{ ft.} - 28.8 \text{ ft.} = 31.2 \text{ ft.}$$

$$\sqrt{31.2^2 - 28.8^2}$$
 ft. = $\sqrt{973.44 - 829.44}$ ft. = $\sqrt{144}$ ft. = 12 ft. Ans.

21. Seventeen trees are standing in a straight line, 20 yd. apart; a man walks from the first to the second and back, then to the third and back, and so on. How far does he walk?

The distance is the sum of the terms of an arithmetical progression in which the first term is 40 yd., the common difference 40 yd., and the number of terms 16.

The 16th term = 40 yd. + 15 × 40 yd. = 40 yd. + 600 yd. = 640 yd. The sum = $16 \times \frac{1}{2} (40 \text{ yd.} + 640 \text{ yd.}) = 5440 \text{ yd.}$ Ans.

22. A canal is 14½ mi. long and 48 ft. wide. At one end is a lock 80 ft. by 24 ft., with a fall of 8 ft. 6 in. How many barges can pass through the lock before the water in the canal is lowered 1 in.?

The amount of water that is drained off in lowering the level 1 in. is $(14\frac{3}{4} \times 5280 \times 48 \times \frac{1}{12})$ cu. ft.

The amount of water that is wasted each time a barge passes through the lock is $(80 \times 24 \times 8\frac{1}{2})$ cu. ft.

Hence, the number of barges is

$$\frac{11}{66} \frac{2}{2} = \frac{14\frac{3}{4} \times 5280 \times 48 \times \frac{1}{12}}{80 \times 24 \times 8\frac{1}{2}} = \frac{59 \times 3280 \times 48 \times 2}{4 \times 89 \times 24 \times 17 \times 12} = \frac{649}{34} = 19\frac{3}{19} = \frac{19\frac{3}{14}}{19} = \frac{19\frac{3}{14}}$$

23. Find the capacity, in liters and in bushels, of a box 1.7^m long, 87^{cm} wide, and 31^{cm} deep.

$$(170 \times 87 \times 31)^{\text{cem}} = 458,490^{\text{cem}} = 458.49^{\text{l}}$$
. Ans.

$$458.49^{1} = 458.49 \times 0.908 \text{ qt.} = \frac{458.49 \times 0.908}{32} \text{ bu.} = 13.01 \text{ bu.}$$
 Ans.

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24. Find the number of kilograms of olive oil, specific gravity 0.915, required to fill a rectangular vessel 2.3^m long, 1.8^m wide, and 74^{cm} deep.

$$(2.3 \times 1.8 \times 0.74)^{\text{cbm}} = 3.0636^{\text{cbm}}.$$

3.0636cbm of water weighs 3063.6kg.

$$0.915 \times 3063.6$$
kg = 2803.194 kg. Ans.

$$\begin{array}{c} 2.3 \\ \hline 1.8 \\ \hline 184 \\ \hline 23 \\ \hline 4.14 \\ \hline 0.74 \\ \hline 1656 \\ \hline \hline 2898 \\ \hline 3.0636 \\ \end{array}$$

25. How many tons in a block of marble 4 ft. long, 34 in. wide, 17.3 in. thick, specific gravity 2.73?

Volume =
$$(48 \times 34 \times 17.3)$$
 cu. in. = $\frac{48 \times 34 \times 17.3}{1728}$ cu. ft.
Weight = $\frac{48 \times 34 \times 17.3}{1728} \times 2.73 \times 62\frac{1}{2}$ lb.
= $\frac{17}{1728 \times 19} \times \frac{91}{199} \times \frac{5}{273} \times \frac{125}{2} \times \frac{1}{2000}$ t.
= $\frac{267631}{192000}$ t. = 1.394 t. Ans.

26. Find the surface of a sphere 18.3 in. in diameter.

$$3.1416 \times (18.3 \times 18.3)$$
 sq. in. = 1052.09 sq. in. Ans.

27. Find the number of acres in a circular field 213 yd. 2 ft. in diameter.

Diameter is 213 yd. 2 ft. = 641 ft.

Radius is
$$\frac{1}{2}$$
 of 641 ft. = 320.5 ft.

1 A. = 43,560 sq. ft.

Area = $\frac{3.1416 \times 320.5^2}{43560}$ A. = 7.407 A. Ans.

 $\log 3.1416 = 0.4971$
 $\log 320.5^2 = 5.0116$
 $\operatorname{colog} 43,560 = 5.3609 - 10$
 $0.8696 = \log 7.407$.

28. How many cubic inches in a 10-inch globe? in a 20-inch globe? What is the ratio of their volumes?

The ratio of their volumes is $10^3 : 20^8 = 1^3 : 2^8 = 1 : 8$. Ans. (0.5236×10^8) cu. in. = 523.6 cu. in. Ans. 8×523.6 cu. in. = 4188.8 cu. in. Ans.

29. How many balls 3 in. in diameter can be cast from a pig of iron 7 ft. long, 6.7 in. wide, 3.8 in. thick, if the waste in melting and casting is reckoned at 31%?

7 ft. = 84 in.
The number of balls =
$$\frac{84 \times 6.7 \times 3.8 \times 0.9675}{3^8 \times 0.5236}$$
.

$$log 84 = 1.9243
log 6.7 = 0.8261
log 3.8 = 0.5798
log 0.9675 = 9.9857 - 10
colog 27 = 8.5686 - 10
colog 0.5236 = 0.2810
2.1655 = log 146.4.$$

Hence, the number of balls is 146. Ans.

30. Find the difference in length, at 80° F., of a glass rod and a steel rod, each 3 ft. long at 0° C., if the expansion at 100° C. is 0.00085 for glass and 0.0012 for steel.

80° F. =
$$\frac{1}{6}(80^{\circ} - 32^{\circ})$$
C. = $26\frac{1}{6}$ ° C. 0.0012 - 0.00085 = 0.00035.

Difference in length = $\frac{26\frac{3}{2}}{100} \times 0.00035 \times 36$ in. = 0.00336 in. Ans.

36 in.	0.0126 in.
0.00035	$\cdot 0.26\frac{2}{3}$
180	84
108	758
0.01260 in.	252
	0.003360 in.

31. A grain of gold is beaten into leaf to cover 56 sq. in. What weight will be required to gild the faces of a cube whose edge is 3½ ft.?

$$6 \times (3\frac{1}{2} \times 3\frac{1}{2})$$
 sq. ft. = $6 \times \frac{7}{2} \times \frac{7}{2} \times 144$ sq. in.

Number of grains of gold required is

$$\frac{6 \times \frac{7}{4} \times \frac{7}{4} \times 144}{56} = \overset{3}{6} \times \frac{7}{2} \times \frac{7}{2} \times \cancel{144} \times \frac{1}{\cancel{56}} = 189.$$

189 gr. = 7 dwt. 21 gr. Ans.

32. What premium must be paid, at the rate of $4\frac{7}{8}\%$, for insuring a vessel worth \$100,000, in order that in the event of loss the owner may receive both the value of the ship and the premium?

100 % of policy = policy (vessel and premium).

$$4\frac{7}{8}$$
% of policy = premium.
 $95\frac{1}{8}$ % of policy = vessel.
 $$100,000 \div 0.95\frac{1}{8} = $105,124.84.$
 $$105,124.84 - $100,000 = $5124.84.$ Ans.

$$105124.83$$

$$95125)100000000000.$$

$$\frac{95125}{487500}$$

$$\frac{475625}{118750}$$

$$\frac{95125}{236250}$$

$$\frac{190250}{460000}$$

$$\frac{380500}{795000}$$

33. By selling goods at 60 cents a pound, 8% is lost. What advance must be made in the price to gain 15%?

761000

340000 285375

54625

Cost = 60 cents $\div \frac{92}{100} = \frac{100}{92}$ of 60 cents.

$$\frac{115}{199} \times \frac{199}{92} \times \frac{15}{99}$$
 cents = 75 cents. 75 cents - 60 cents = 15 cents. Ans.

34. The sharpest grade on Mt. Washington Ry. is 1980 ft. to the mile. What fraction of a foot is the rise for each foot? What is the per cent of grade?

$$\frac{1280}{5280}$$
 ft. = \frac{3}{5} ft. Ans. $\frac{3}{5} = 37\frac{1}{2}\%$ Ans.

35. Find the square root, to four decimal places, of the reciprocal of 0.0043.

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36. The population of a city in 1890 was 12,298, showing a decrease of 8\frac{1}{3}\text{\omega} on its population in 1880; in 1880 there was an increase of 7\frac{1}{3}\text{\omega} on the census of 1870. What was its population in 1870?

Population in $1880 = 12298 \div \frac{91\frac{3}{2}}{100}$.

Population in 187026

$$= \left(12298 \div \frac{91\frac{2}{3}}{100}\right) \div \frac{107\frac{1}{2}}{100} = 1229\% \times \frac{12}{300} \times \frac{40}{215} = 12,480. \ Ans.$$

37. Find the increase of income obtained by transferring 25 shares of 3 % stock at 94 to 4 % stock at 104 to 5, brokerage 1 on each transaction.

 $25 \times $3 = 75 , income from the 3 % stock.

 $25 \times $94.50 = 2362.50 , proceeds from the 3 % stock.

\$1.05 is paid for \$1 worth of 4% stock.

Hence, \$2362.50 is paid for $$2362.50 \div 1.05 = 2250 stock.

4% of \$2250 = \$90, income from 4% stock.

\$90 - \$75 = \$15, increase of income. Ans.

38. Each person in breathing spoils the air of a closed room at the rate of about 8 cu. ft. a minute. An audience of 400 persons enter a closed hall 70 ft. by 40 ft., and 20 ft. high. How long will it take them to spoil the air?

$$\frac{35}{\cancel{70} \times \cancel{40} \times \cancel{20}} = \frac{35}{2} = 17\frac{1}{2}.$$

171 min. Ans.

39. How long can the windows and doors of a schoolroom be safely kept closed when occupied by 50 children, if the room is 25 ft. by 20 ft., and 10 ft. high?

$$\frac{23 \times 20 \times 10}{50 \times 8} = \frac{25}{2} = 12\frac{1}{2}.$$

121 min. Ans.

40. A pays B \$230 as the present value of \$300 due in 5 years. Which gains by the payment, and how much, if interest is reckoned at 5% compound interest?

The present value of \$300 due in 5 yr. at 5 % is

$$\frac{1}{1.27628} \text{ of } \$300 = \$ \frac{300}{1.27628} = \$235.06.$$

$$\frac{235.05}{127628)300000000.}$$

$$\frac{255256}{447440}$$

$$\frac{382884}{645560}$$

$$\frac{638140}{742000}$$

$$\frac{638140}{103860}$$

Therefore, A gains \$235.06 - \$230 = \$5.06. Ans.

41. Find the quantity of coal required by a steamer for a voyage of 4043 mi., if her rate per hour is 14.04 knots, and her consumption of coal 87 long tons per day.

The rate of the ship per day = 24×14.04 knots = $24 \times 14.04 \times 6086$ ft. 4043 mi. = 4043×5280 ft.

Therefore, the number of days is $\frac{4043 \times 5280}{24 \times 14.04 \times 6086}$.

The number of long tons of coal is $\frac{4043 \times 5280 \times 87}{24 \times 14.04 \times 6086}$

$$\begin{array}{c} \log \ 4043 = 3.6067 \\ \log \ 5280 = 3.7226 \\ \log \ 87 = 1.9395 \\ \operatorname{colog} \ 24 = 8.6198 - 10 \\ \operatorname{colog} \ 14.04 = 8.8527 - 10 \\ \operatorname{colog} \ 6086 = 6.2157 - 10 \\ \hline 2.9570 = \log 905.8. \end{array}$$

905.8 l. t. Ans.

42. Find the area of a circular ring whose inner and outer diameters are 7.36 in. and 10.64 in., respectively.

Area =
$$0.7854 \times (10.64^2 - 7.36^2)$$
 sq. in.
= $0.7854 \times (113.2096 - 54.1696)$ sq. in.
= 0.7854×59.04 sq. in. = 46.37 sq. in. Ans.

10.64	7.36	0.7854
10.64	7.36	59.04
4256	4416	31416
6384	2208	70686
1064	5 152	39270
113.2096	54.1696	46.370016

43. A and B can do a piece of work in 13\frac{1}{2} days; A and C in 10\frac{1}{2} days; A, B, and C in 7\frac{1}{2} days. In how many days can A do the work alone?

If A and B can do the work in $13\frac{1}{3}$ days, in 1 day they can do $\frac{1}{13\frac{1}{4}} = \frac{3}{40}$ of it.

If A and C can do the work in $10\frac{2}{3}$ days, in 1 day they can do $\frac{1}{10\frac{2}{3}} = \frac{3}{32}$ of it.

If A, B, and C can do the work in $7\frac{1}{2}$ days, in 1 day they can do $\frac{1}{7\frac{1}{2}} = \frac{2}{15}$ of it.

Hence, in 1 day B can do $\frac{2}{15} - \frac{3}{32} = \frac{19}{480}$ of the work. Hence, in 1 day A can do $\frac{3}{40} - \frac{19}{480} = \frac{17}{480}$ of the work. Therefore, it will take A $\frac{480}{17}$ days = $28\frac{4}{17}$ days. Ans. 44. If 3 men working 11 hours a day can reap 20 A. in 11 days, how many men working 12 hours a day can reap a field 360 yd. long and 320 yd. broad in 4 days?

$$\frac{11 \times 11 \times 360 \times 320 \times 3 \text{ men}}{12 \times 4 \times 20 \times 160 \times 30\frac{1}{4}} = \frac{11 \times 11 \times 369 \times 329 \times 4 \times 3 \text{ men}}{12 \times 4 \times 29 \times 169 \times 121}$$
= 9 men. Ans.

45. Find the area of a triangle whose sides are 12 in., 5 in., and 13 in., respectively.

Since $13^2 = 12^2 + 5^2$, the triangle is a right triangle.

Hence, area = $\frac{1}{4} \times (12 \times 5)$ sq. in. = 30 sq. in. Ans.

46. The four sides of a field measured in succession are 237 ft., 253 ft., 244 ft., and 261 ft., and the diagonal measured from the end of the first side to the end of the third side is 351 ft. Find the area of the field.

$$\frac{237 + 261 + 351}{2} = 424.5.$$

Area of 1st triangle = $\sqrt{424.5 \times 187.5 \times 163.5 \times 73.5}$ sq. ft.

$$\frac{253 + 244 + 351}{2} = 424.$$

Area of 2d triangle = $\sqrt{424 \times 171 \times 180 \times 73}$ sq. ft.

$$\begin{array}{lll} \log 424.5 = 2.6279 & \log 424 = 2.6274 \\ \log 187.5 = 2.2730 & \log 171 = 2.2330 \\ \log 163.5 = 2.2135 & \log 180 = 2.2553 \\ \log 73.5 = 1.8663 & \log 73 = 1.8633 \\ 28.9807 & 28.9790 \\ \hline 4.4904 & 4.4895 \\ = \log 30,930. & = \log 30,860. \end{array}$$

30,930 sq. ft. + 30,860 sq. ft. = 61,790 sq. ft. Ans.

47. The four sides of a field measured in succession are 361 ft., 561 ft., 443 ft., and 357 ft., and the distance from the beginning of the first side to the end of the second side is 682 ft. Find the area of the field.

$$\frac{361+561+682}{2} = 802.$$
 Area of triangle = $\sqrt{802 \times 441 \times 241 \times 120}$ sq. ft.
$$\log 802 = 2.9042$$

$$\log 441 = 2.6444$$

$$\log 241 = 2.3820$$

$$\log 120 = 2.0792$$

$$2 \boxed{10.0098}$$

$$5.0049 = \log 101,100.$$

$$\frac{443+357+682}{2} = 741.$$
 Area of triangle = $\sqrt{741 \times 298 \times 384 \times 59}$ sq. ft.

Area of triangle = $\sqrt{741 \times 298 \times 384 \times 59}$ sq. ft. $\log 741 = 2.8698$ $\log 298 = 2.4742$ $\log 384 = 2.5843$ $\log 59 = 1.7709$ $2 \boxed{9.6992}$ $4.8496 = \log 70,730$.

101,100 sq. ft. + 70,730 sq. ft. = 171,830 sq. ft. Ans.

48. Find the altitude of a triangle, if each side is 1000 ft.

$$\sqrt{1000^2-500^2}$$
 ft. = $\sqrt{1000000-250000}$ ft. = $\sqrt{750000}$ ft. = 866.025 ft.

Ans.

75 00 00(866.025 64 166)1100 996 1726)10400 10356 173202)440000 346404 1732045)9359600 8660225 49. Find the three altitudes of a triangle, if its sides are 17.8^{mm}, 23.6^{mm}, and 31.5^{mm}, respectively.

$$\frac{17.8 + 23.6 + 31.5}{2} = 36.45.$$

Area = $\sqrt{36.45 \times 18.65 \times 12.85 \times 4.95^{\text{qmm}}}$.

50. How many square inches in the surface of a sphere that has a radius of 12.37 in.?

Area =
$$3.1416 \times 4 \times 12.37^2$$
.
 $\log 3.1416 = 0.4971$
 $\log 4 = 0.6021$
 $\log 12.37^2 = 2.1848$
 $3.2840 = \log 1923$.
1923 sq. in. Ans.

51. Find the area of the surface of the largest globe that can be turned out from a joist 4 in. by 6 in.

52. How many cubic inches in a globe that has a diameter of 10 in.? Volume = 0.5236×10^8 cu. in. = 523.6 cu. in. Ans.

53. If a tree is round, and its girth is 17 ft. 6 in., find its diameter. Find the area of a cross section, and also the number of cubic feet in the largest sphere that can be cut from it.

Diameter =
$$\frac{17.5}{3.1416}$$
 ft. = 5.57 ft. Ans.

Area = 0.7854×5.57^2 sq. ft. = 24.37 sq. ft. Ans. Volume = 0.5236×5.57^8 cu. ft. = 90.52 cu. ft. Ans.

$$\log 17.5 = 1.2430$$

$$\operatorname{colog} 3.1416 = 9.5029 - 10$$

$$0.7459 = \log 5.57.$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log 5.57^2 = 1.4918$$

$$1.3869 = \log 24.37.$$

$$\log 0.5236 = 9.7190 - 10$$

$$\log 5.57^3 = 2.2377$$

$$1.9567 = \log 90.52.$$

54. Find the weight in kilograms and in pounds of an iron ball 21.5^{cm} in diameter, specific gravity 7.47; of a tin ball 13^{cm} in diameter, specific gravity 7.29; of a lead ball 17.3^{cm} in diameter, specific gravity 11.35; of a silver ball 1.31^{cm} in diameter, specific gravity 10.47.

Iron.

Weight =
$$7.47 \times 0.5236 \times (2.15^8)^{kg} = 38.86^{kg}$$
. Ans.
 $38.86^{kg} = 38.86 \times 2.205 \text{ lb.} = 85.68 \text{ lb.}$ Ans.
 $\log 7.47 = 0.8733$
 $\log 0.5236 = 9.7190 - 10$
 $\log 2.15^8 = 0.9972$
 $1.5895 = \log 38.86$.
 $\log 38.86 = 1.5895$
 $\log 2.205 = 0.3434$
 $1.9329 = \log 85.68$.

122 = 1 Ave = 127 M

. . . .

 $(x,y,1), \quad (x,y) = \frac{1}{2}, \quad$

55. A slab of cast iron 4 ft. 2½ in. long. 17 in. wide, and 8½ in. thick, specific gravity 7.31, is cast into 2-lb. balls. If there is a loss of 5% in melting, how many balls are obtained, and what is the diameter of each?

The slab will make $\frac{50.5 \times 17 \times 25 \times 0.95 \times 62.5 \times 7.31}{2 \times 3 \times 1728} = 898$ balls.

The diameter will be $\sqrt[3]{\frac{50.5 \times 17 \times 25 \times 0.95}{0.5236 \times 3 \times 898}}$ in. = 2.436 in. Ans.

898 balls. Ans.

56. How many pounds will a ball of iron 30 in. in diameter weigh, if the specific gravity of the iron is 7.31?

$$\frac{0.5236 \times 30^3 \times 7.31 \times 62.5}{1728} \text{ lb.} = 3738 \text{ lb.} \quad Ans.$$

$$\log 0.5236 = 9.7190 - 10$$

$$\log \quad 30^3 = 4.4313$$

$$\log \quad 7.31 = 0.8639$$

$$\log \quad 62.5 = 1.7959$$

$$\text{colog} \quad 1728 = 6.7625 - 10$$

$$3.5726 = \log 3738.$$

57. If the specific gravity of ice is 0.930, find the weight and the surface of each of three spheres of ice whose diameters are 1^{cm}, 10^{cm}, and 1^m.

$$0.5236 \times (1^8)^{\text{ccm}} = 0.5236^{\text{ccm}}.$$
 $0.930 \times 523.6^{\text{mg}} = 486.948^{\text{mg}}.$ Ans.
 $0.5236 \times (10^3)^{\text{ccm}} = 523.6^{\text{ccm}}.$
 $0.930 \times 523.6^{\text{g}} = 486.948^{\text{g}}.$ Ans.

$$0.5236 \times (1^8)^{\text{cbm}} = 0.5236^{\text{cbm}}.$$
 $0.930 \times 523.6^{\text{kg}} = 486.948^{\text{kg}}.$ Ans.
$$\begin{array}{c} 523.6 \\ 0.93 \\ \hline 15708 \\ 47124 \\ \hline 486.948 \end{array}$$

$$3.1416 \times (1^2)^{\text{qcm}} = 3.1416^{\text{qcm}}$$
. Ans. $3.1416 \times (10^2)^{\text{qcm}} = 314.16^{\text{qcm}}$. Ans. $3.1416 \times (100^2)^{\text{qcm}} = 31,416^{\text{qcm}}$. Ans.

58. Find the capacity in gallons of a round cistern 13 ft. in diameter and 9 ft. deep.

$$V = \frac{9 \times 3.1416 \times 6.5^2 \times 1728}{231} \text{ gal.} = 8933 \text{ gal.} \text{ Ans.}$$

$$\log \quad 9 = 0.9542$$

$$\log 3.1416 = 0.4971$$

$$\log \quad 6.5^2 = 1.6258$$

$$\log \quad 1728 = 3.2375$$

$$\cosh \quad 231 = 7.6364 - 10$$

$$3.9510 = \log 8933.$$

59. A cylinder is 10 in. in diameter and 12 in. long. Find the area of each end, the lateral surface, the total surface, and the contents in gallons.

Area of end = $0.7854 \times (10^2)$ sq. in. = 78.54 sq. in. Ans. Lateral surface = $3.1416 \times (10 \times 12)$ sq. in. = 3.1416×120 sq. in. = 376.99 sq. in. Ans.

Total surface = 376.99 sq. in. + 2×78.54 sq. in. = 534.07 sq. in. Ans.

Volume =
$$\frac{4}{12 \times 78.34} \frac{1.02}{231}$$
 gal. = 4.08 gal. Ans.

60. What must be the diameter of a cylinder 10 in. deep that it may hold 1 gallon?

231 =
$$10 \times 0.7854 \times D^2$$
.

$$D = \sqrt{\frac{231}{7.854}} \text{ in.} = 5.424 \text{ in.} \text{ Ans.}$$

$$\log 231 = 2.3636$$

$$\operatorname{colog} 7.854 = 9.1049 - 10$$

$$2 \overline{1.4685}$$

$$0.7343 = \log 5.424.$$

61. Find the volume of a cylinder 8 in. in diameter and 11 in. high. Volume = $(11 \times 0.7854 \times 8^2)$ cu. in. = 552.92 cu. in. Ans.

8	0.7854
8	704
64	31416
11	549 78
64	552.9216
64	
 704	

62. Find the dimensions of three cylinders that have the diameters equal to the heights, and hold 1 gallon, 1 quart, and 1 liter, respectively.

$$V = 0.7854 \times D^{2} \times H = 0.7854 \times D^{3}.$$

$$\therefore D = \sqrt[3]{\frac{V}{0.7854}}$$

$$D = \sqrt[3]{\frac{231}{0.7854}} \text{ in.} = 6.65 \text{ in.} \text{ Ans.}$$

$$\log \quad 231 = 2.3636$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$3 \boxed{2.4685}$$

$$0.8228 = \log 6.65.$$

$$D = \sqrt[3]{\frac{57.75}{0.7854}} \text{ in.} = 4.19 \text{ in.} \text{ Ans.}$$

$$\log \quad 57.75 = 1.7616$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$3 \boxed{1.8665}$$

$$0.6222 = \log 4.19.$$

$$D = \sqrt{\frac{1.09}{.7554}} = 1.4544. \text{ Ans.}$$

$$\log 1999 = 3.9999$$

$$\operatorname{coug} ? 7554 = 9.1949$$

$$3.1149$$

$$1.9550 = \log 19.54.$$

63. How many said: yards in a pyramid 123 ft. high, with a square base 210 ft. on a said?

64. Find the capacity of a cup, whose mouth is 4 in. square, and whose sides are four equilateral triangles.

Diagonal of base =
$$\sqrt{4^2 + 4^2}$$
 in. = $\sqrt{16 + 16}$ in. = $\sqrt{32}$ in.

Altitude of pyramid =
$$\sqrt{4^2 - (\frac{1}{2}\sqrt{32})^2}$$
 in. = $\sqrt{16 - 8}$ in. = $\sqrt{8}$ in.

Volume = $\frac{1}{4} \times (4^2 \times \sqrt{8})$ cu. in. = 15.09 cu. in. Ans.

$$\log 16 = 1.2041$$

$$\log \sqrt{8} = 0.4516$$

$$\operatorname{colog} 3 = \underbrace{9.5229}_{1.1786} - 10$$

$$= \log 15.09.$$

65. The largest of the Egyptian pyramids is 147^m high, with a base 231^m square. Find its volume in cubic meters.

Volume =
$$\frac{1}{4} \times (147 \times 231^2)^{\text{cbm}} = 2,614,689^{\text{cbm}}$$
. Ans.

2 31	3 147	53361
231	49	49
231		480249
693		213444
462		2614689
53361		

66. The slant depth of a conical cup is 93^{mm}, and the diameter at the top 8^{cm}. What is its capacity?

Height =
$$\sqrt{9.3^2 - 4^{2}}$$
 = $\sqrt{86.49 - 16}$ = $\sqrt{70.49}$ cm.

Volume = $\frac{1}{4} \times (\sqrt{70.49} \times 0.7854 \times 8^2)^{\text{ccm}} = 140.7^{\text{ccm}} = 0.1407^1$. Ans.

$$\log \sqrt{70.49} = 0.9241$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log 64 = 1.8062$$

$$\cosh 3 = 9.5229 - 10$$

$$2.1483 = \log 140.7$$

67. The volume of a cone is 1^{cbm}; its height is equal to the radius of its base. Find the dimensions of the cone.

$$V = \frac{1}{3} \times 3.1416 \times R^2 \times H = \frac{1}{3} \times 3.1416 \times R^3$$
.

$$\therefore R = \sqrt[3]{\frac{V}{1 \times 3.1416}} = \sqrt[3]{\frac{V}{1.0472}}$$

$$R = \sqrt[3]{\frac{1000000}{1.0472}}^{\text{em}} = 98.48^{\text{em}}$$
. Ans.

68. Find the capacity in pints of a cylinder, diameter 1.9375 in., height 2.4375 in.; of a cylinder, diameter $3\frac{1}{16}$ in., height $5\frac{1}{16}$ in. height $5\frac{1}{16}$ in.

1 pt. =
$$\frac{1}{4}$$
 of 231 cu. in. = 28.875 cu. in.

Volume =
$$\frac{0.7854 \times 1.9375^2 \times 2.4375}{28.875}$$
 pt. = 0.2489 pt. Ans.

$$\log 0.7854 = 9.8951 - 10$$

$$\log 1.9375^2 = 0.5746$$

$$\log 2.4375 = 0.3869$$

$$\operatorname{colog} 28.875 = 8.5395 - 10$$

$$9.3961 - 10 = \log 0.2489.$$

Volume =
$$\frac{0.7854 \times 3.125^2 \times 3.625}{26.875}$$
 pt. = 0.9632 pt. Ans.
 $\log 0.7854 = 9.8951 - 10$
 $\log 3.125^2 = 0.9898$
 $\log 3.625 = 0.5593$
 $\operatorname{colog} 28.875 = 8.5395 - 10$
 $9.9837 - 10 = \log 0.9632$.
Volume = $\frac{0.7854 \times 3.8125^2 \times 5.0625}{28.875}$ pt. = 2.002 pt. Ans.
 $\log 0.7854 = 9.8951 - 10$
 $\log 3.8125^3 = 1.1624$
 $\log 5.0625 = 0.7044$
 $\operatorname{colog} 28.875 = 8.5395 - 10$

69. Find the capacity, in pecks, of a cylinder, diameter 15.865 in., height 12.5 in.; of a cylinder, diameter 9.25 in., height 4.25 in.; of a cylinder, diameter 18.5 in., height 8 in.

 $0.3014 = \log 2.002.$

$$1 \text{ pk.} = \frac{1}{4} \text{ of } 2150.42 \text{ cu. in.} = 537.605 \text{ cu. in.}$$

$$Volume = \frac{0.7854 \times 15.865^2 \times 12.5}{537.605} \text{ pk.} = 4.597 \text{ pk.} \text{ Ans.}$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log 15.865^2 = 2.4010$$

$$\log 12.5 = 1.0969$$

$$\cosh 537.605 = 7.2695 - 10$$

$$0.6625 = \log 4.597.$$

Volume =
$$\frac{0.7854 \times 9.25^2 \times 4.25}{537.605}$$
 pk. = 0.5311 pk. Ans.

$$\log 0.7854 = 9.8951 - 10$$

$$\log 9.25^2 = 1.9322$$

$$\log 4.25 = 0.6284$$

$$\operatorname{colog} 537.605 = 7.2695 - 10$$

$$9.7252 - 10 = \log 0.5311$$

Volume =
$$\frac{0.7854 \times 18.5^2 \times 8}{537.605}$$
 pk. = 4 pk. Ans.
 $\log 0.7854 = 9.8951 - 10$
 $\log 18.5^2 = 2.5344$
 $\log 8 = 0.9031$
 $\operatorname{colog} 537.605 = 7.2695 - 10$
 $0.6021 = \log 4$.

70. What must be the diameter of a circle to contain 78.54 sq. ft.? to contain 314.16 sq. ft.?

Area =
$$0.7854 \times D^2$$
.Area = $0.7854 \times D^2$. $78.54 = 0.7854 \times D^2$. $314.16 = 0.7854 \times D^2$. $\therefore D^2 = 100$. $\therefore D^2 = 400$. $D = 10$. $D = 20$.10 ft. Ans. 20 ft. Ans.

71. What must be the diameter of a circle to contain 1 A.? to contain 9 A.?

1 A. = 43,560 sq. ft.
Area = 0.7854 ×
$$D^2$$
.

$$\log 43,560 = 4.6391$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$2 \overline{4.7440}$$

$$2.3720 = \log 235.5$$

$$3 \times 235.5 \text{ ft.} = 706.5 \text{ ft.} Ans.$$

$$3 \times 235.5 \text{ ft.} = 706.5 \text{ ft.} Ans.$$

72. What must be the diameter of a circle to contain 1^{ha}? to contain 25^{ha}?

$$1^{\text{ha}} = 10,000^{\text{qm}}. \qquad \therefore D = \sqrt{\frac{10000}{0.7854}}.$$

$$\log 10000 = 4.0000$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$2 \boxed{4.1049}$$

$$2.0525 = \log 112.8. \qquad 112.8^{\text{m}}. \quad Ans.$$

$$\sqrt{25} = 5. \qquad 5 \times 112.8^{\text{m}} = 564^{\text{m}}. \quad Ans.$$

73. Divide \$ 1270 into parts proportional to 41, 51, 63.

$$42 \times (4\frac{1}{3}, 5\frac{1}{6}, 6\frac{3}{7}) = 182, 217, 264.$$

 $182 + 217 + 264 = 663.$

$$\frac{14}{182}$$

$$\frac{182}{663}$$
 of \$ 1270 = \$ $\frac{17780}{51}$ = \$ 348.63.
$$\frac{217}{663}$$
 of \$ 1270 = \$ $\frac{275590}{663}$ = \$ 415.67.
$$\frac{88}{264}$$

$$\frac{264}{663}$$
 of \$ 1270 = \$ $\frac{111760}{221}$ = \$ 505.70.

74. How much water will a hemispherical bowl hold that is 10 in. in diameter?

 $\frac{1}{2}$ of $0.5236 \times (10^3)$ cu. in. = 0.5236×500 cu. in. = 261.8 cu. in. Ans.

75. At 50 cents a square foot, what will it cost to gild a hemispherical dome 10 ft. in diameter?

$$\frac{1}{2} \times 3.1416 \times 10^{2} \times \$\frac{1}{2} = \frac{1}{2} \times 3.1416 \times 100 \times \$\frac{1}{2} = \$78.54. \text{ Ans.}$$

76. If the moon is a sphere 2170 miles in diameter, how many million bushels would it hold if hollow?

Volume =
$$\frac{0.5236 \times (2170 \times 5280 \times 12)^8}{2150.42}$$
 bu.
= $633,000,000,000,000,000,000$ bu. Ans.
log $0.5236 = 9.7190 - 10$
log $2170^3 = 10.0095$
log $5280^3 = 11.1678$
log $12^3 = 3.2376$
colog $2150.42 = 6.6675 - 10$
 20.8014
= $\log 633,000,000,000,000,000,000$

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77. If the earth is 7920 miles in diameter, and the air is 40 miles deep, how many cubic miles of air are there?

$$7920 + 80 = 8000.$$

$$\log 8000^8 = 11.7093$$

$$\log 0.5236 = 9.7190 - 10$$

$$11.4283$$

$$= \log 268,100,000,000$$

$$268,100,000,000 - 260,100,000,000 = 8,000,000,000$$

$$Ans.$$

- 78. What is the difference between 2 feet square and 2 square feet? between a foot square and a square foot? between half a foot square and 6 in. square?
- "2 feet square" means a square 2 ft. on a side; "2 square feet," any surface equivalent in area to two squares each 1 foot on a side. A "foot square" is a square 1 ft. on a side; while a square foot is an equivalent area in any shape. "Half a foot square" is ambiguous. Half "a foot square" is half a square foot, while "half a foot" square is 6 inches square; that is, one-fourth a square foot. "6 in. square" is a square 6 in. on a side.
- 79. Find the volume of a frustum of a right pyramid whose lower base is a square 3 ft. on a side, upper base a square 2 ft. on a side, and height 4 ft.

$$\frac{1}{8} \times 4 \times (3^2 + 2^2 + \sqrt{3^2 \times 2^2}) = \frac{1}{8} \times 4 \times (9 + 4 + 6) = \frac{1}{8} \times 4 \times 19 = 25\frac{1}{3}.$$
25\frac{1}{3} \text{ cu. ft. } Ans.

80. Find the capacity in liquid quarts of a tin pan 10 in. in diameter at the top, 8 in. in diameter at the bottom, and 4 in. deep.

$$\frac{1}{8} \times 4 \times (0.7854 \times 10^{2} + 0.7854 \times 8^{2} + \sqrt{0.7854 \times 10^{2} \times 0.7854 \times 8^{2}})$$

$$= \frac{1}{8} \times 4 \times 0.7854 \times (100 + 64 + 80)$$

$$= \frac{1}{3} \times 4 \times \cancel{9.7854} \times 244 = 255.5168.$$

$$255.5168 \text{ cu. in.} = \frac{255.5168}{57.75} \text{ qt.} = 4.42 \text{ qt. } Ans.$$

81. How many hektoliters will a circular vat hold 5^m in diameter at the top, 4.57^m in diameter at the bottom, and 1.17^m deep?

 $21.0539^{\text{cbm}} = 210.539^{\text{hl}}$. Ans.

82. If 4 cu. in. of iron weigh 1 lb. avoirdupois, what is the weight in grains of 1 cu. in. of iron? What is the specific gravity of the iron?

1 cu. in. of iron weighs $\frac{1}{4}$ lb. = $\frac{1}{4}$ of 7000 gr. = 1750 gr. Ans. 1 cu. ft. of iron weighs $1728 \times \frac{1}{4}$ lb. = 432 lb. $432 \div 62\frac{1}{2} = 432 \times \frac{2}{125} = \frac{364}{125} = 6.912$. Ans. $\frac{6.912}{125)864}$ 750

83. If 4 cu. in. of iron weigh 1 lb., what is the diameter of a 6-lb. ball? of a 32-lb. ball?

$$V = (6 \times 4) \text{ cu. in.} = 24 \text{ cu. in.}$$

$$V = 0.5236 \ D^{8}.$$

$$24 = 0.5236 \ D^{8}.$$

$$D = \sqrt[3]{\frac{24}{0.5236}} \text{ in.} = 3.578 \text{ in.} \quad Ans.$$

$$V = (32 \times 4) \text{ cu. in.} = 128 \text{ cu. in.}$$

$$V = 0.5236 \ D^{8}.$$

$$128 = 0.5236 \ D^{8}.$$

$$D = \sqrt[3]{\frac{128}{0.5236}} \text{ in.} = 6.253 \text{ in.} \quad Ans.$$

$$D = \sqrt[3]{\frac{128}{0.5236}} \text{ in.} = 6.253 \text{ in.} \quad Ans.$$

$$0 = \sqrt[3]{\frac{128}{0.5236}} \text{ in.} = 6.253 \text{ in.} \quad Ans.$$

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$$0 = \sqrt[3]{\frac{128}{0.5236}} \text{ in.} = 6.253 \text{ in.} \quad Ans.$$

84. At \(\frac{1}{4}\) lb. to the cubic inch, what is the weight of a rectangular block of iron 17.36 in. by 8.7 in. by 1.76 in.? What would be its diameter if cast into a ball, if 11% is allowed for waste?

85. At \{\}\] lb. to the cubic inch, what is the weight of a rectangular block of iron 71.4 in. by 8\{\}\] in. by 3\{\}\] in.? What would be its diameter if cast into a ball, if 11% is allowed for waste?

713 × 83 × 33 × 4 lb. =
$$\frac{337}{5}$$
 × $\frac{26}{3}$ × $\frac{10}{3}$ × $\frac{1}{4}$ lb. = $\frac{1547}{3}$ lb. = 5153 lb. Ans.

Diameter = $\sqrt[3]{\frac{0.89 \times 4 \times 5153}{0.5236}}$ in. = 15.19 in. Ans.

86. What is the diameter of a cylinder 11 in. long that will hold 2 gallons?

2 gal. = 2 × 231 cu. in. = 462 cu. in.

$$462 = 0.7854 \times D^{2} \times 11.$$

$$D = \sqrt{\frac{462}{0.7854 \times 11}} \text{ in.} = \sqrt{\frac{42}{0.7854}} \text{ in.} = 7.313 \text{ in.} \quad Ans.$$

$$\log \quad 42 = 1.6232$$

$$\cosh 0.7854 = 0.1049$$

$$2 \boxed{1.7281}$$

$$0.8641 = \log 7.313.$$

87. What is the diameter of a cylinder 9 in. long that will hold 2 gallons?

$$462 = 0.7854 \times D^2 \times 9.$$
 $D = \sqrt{\frac{462}{0.7854 \times 9}} \text{ in.} = 8.086 \text{ in.} Ans.$
 $\log 462 = 2.6646$
 $\operatorname{colog} 0.7854 = 0.1049$
 $\operatorname{colog} 9 = 9.0458 - 10$
 $2 \overline{1.8153}$
 $0.9077 = \log 8.086.$

88. What is the diameter of a cylinder 30cm long that will hold 10 liters?

$$10^{1} = 10,000^{\text{ccm}}.$$
 $10,000 = 0.7854 \times D^{2} \times 30.$

$$D = \sqrt{\frac{1000}{0.7854 \times 3}}^{\text{cm}} = 20.6^{\text{cm}}. \text{ Ans.}$$

$$\log 1000 = 3.0000$$

$$\operatorname{colog} 0.7854 = 0.1049$$

$$\operatorname{colog} 3 = 9.5229 - 10$$

$$2 \boxed{2.6278}$$

$$1.3139 = \log 20.6.$$

89. Find the circumference of a globe, if the number of square centimeters in its surface is three times the number of cubic centimeters in its volume.

$$V = 0.5236 \times D^3$$
; $S = 3.1416 \times D^2$.
 $3 \times 0.5236 \times D^3 = 3.1416 \times D^2$.

Divide both sides by $3 \times 0.5236 \times D^2$, D = 2.

Hence, the circumference is $3.1416 \times 2^{cm} = 6.2832^{cm}$. Ans.

90. Find the diameter of a circle, if the number of inches in its circumference is equal to the number of square feet in its area.

Area = $0.7854 \times D^2$ sq. ft.

Circumference = $3.1416 \times D$ ft. = $12 \times 3.1416 \times D$ in.

$$0.7854 \times D^2 = 12 \times 3.1416 \times D.$$

Divide both sides by $0.7854 \times D$, D = 48.

48 ft. Ans.

91. How many times does a carriage wheel 3 ft. 2 in. in diameter turn in going a mile on a smooth road?

$$\frac{5280}{3.1416 \times 3\frac{1}{6}} = 530.7. \text{ Ans.}$$

$$\frac{31}{5236} = 99484)52800000.$$

$$\frac{497420}{305800}$$

$$\frac{99484}{9.9484} = \frac{298452}{734800}$$

$$\frac{696388}{38412}$$

92. A point in the tire moves, while the wheel turns once, just four times the diameter of the wheel. How far does a spike head in the tire travel while a wheel, 3 ft. 2 in. in diameter, travels 1 mi.?

From Example 91, the wheel turns 530.7 times while the wheel goes 1 mi.

530.7 × 4 × 3\frac{1769}{5} ft. =
$$\frac{33611}{5}$$
 ft. = 6722.2 ft. Ans.

93. An oil can is formed of two cylinders connected by a frustum of a cone. The upper cylinder, or neck, is 6^{cm} in diameter, and 75^{mm} high; the lower cylinder is 13^{cm} in diameter, and 153^{mm} high; the total length of the can is 30^{cm}. Find the capacity of the can in liters.

A square shaft to contain the neck would contain

$$(6 \times 6 \times 7.5)^{\text{ccm}} = 270^{\text{ccm}}$$
.

A square shaft to contain the body would contain

$$(13 \times 13 \times 15.3)^{\text{ccm}} = 2585.7^{\text{ccm}}$$
.

The frustum of a square pyramid to enclose the remainder would contain

94. A common tunnel is formed of a frustum of a cone terminated with a cylinder. The height of the frustum is 14cm, and the diameters of the two bases are 175mm and 16mm, respectively. The cylinder is 8cm long. Find the capacity of the tunnel in liters.

2776.31046

The volume of the cylinder

$$= 0.7854 \times (8 \times 1.6^{2})^{\text{ccm}} = 0.7854 \times 20.48^{\text{ccm}}$$

The volume of the frustum of the cone

$$= \frac{14}{3} \times 0.7854 \times (17.5^{2} + 1.6^{2} + \sqrt{17.5^{2} \times 1.6^{2}})^{\text{ccm}}$$

$$= \frac{14}{3} \times 0.7854 \times (306.25 + 2.56 + 28)^{\text{ccm}}$$

$$= \frac{14}{3} \times 0.7854 \times 336.81^{\text{ccm}} = 0.7854 \times 1571.78^{\text{ccm}}.$$

Therefore, the tunnel holds

$$0.7854 \times 20.48^{\text{cem}} + 0.7854 \times 1571.78^{\text{cem}}$$
 $= 0.7854 \times 1592.26^{\text{cem}} = 1250^{\text{cem}} = 1.25^{\text{l}}$. Ans.

 1592.26
 0.7854
 636904
 796130
 1273808
 1114582

95. A pan in the form of a frustum of a cone is 10^{cm} deep, 12^{cm} across the bottom, and 23^{cm} across the top. Find the capacity of the pan in liters.

1250.561004

$$\frac{1}{3} \times 10 \times 0.7854 \times (23^{2} + 12^{2} + \sqrt{23^{2} \times 12^{2}})$$

$$= \frac{1}{3} \times 10 \times 0.7854 \times (529 + 144 + 276)$$

$$= \frac{1}{3} \times 10 \times 0.7854 \times 949 = 2484.5.$$

 $2484.5^{\text{cem}} = 2.4845^{\text{l}}$. Ans.

96. Find the number of square centimeters of sheet iron in a stovepipe 4^m long, 26^{cm} in diameter, and 1^{mm} thick, if the edges lap one centimeter. Find the weight of the pipe, if the specific gravity of the sheet iron is 7.8.

 $4^{m} = 400^{cm}$; $1^{mm} = 0.1^{cm}$. Surface = $400 \times (3.1416 \times 26 + 1)^{qcm} = 33,072.64^{qcm}$. Ans.

Weight = $7.8 \times (0.1 \times 33,072.64)^{8} = 25,797^{8} = 25.797^{8}$. Ans.

3.1416 26	. 3307.264 7.8
188 496	26458 112
62832	23150848
81. 6 81 6 1.	25796.6592
82.6816	
92070 6400	
33072.6400	

97. A steam boiler is formed of a cylinder terminated at each end by a hemispherical cap of the same diameter. The length of the cylinder is 3.4^m, interior diameter 0.8^m. Find the number of hektoliters of water required to fill the boiler half full.

Volume of the cylinder

$$= 0.7854 \times (3.4 \times 0.8^2)^{\text{cbm}} = 1.709^{\text{cbm}} = 17.09^{\text{hl}}.$$

The two caps form a sphere, whose volume

$$= 0.5236 \times (0.8^8)^{\text{cbm}} = 0.268^{\text{cbm}} = 2.68^{\text{hl}}.$$

 $\frac{1}{4} \times (17.09^{\text{hl}} + 2.68^{\text{hl}}) = 9.89^{\text{hl}}$. Ans.

0.	7854
_2	2.176
4	7124
54	978
78	54
1570	8
1.709	0304
0.	5236
_0).512
1	0472
5	236
261	80
0.268	เกยรอ

98. A spherical bomb is 32cm in diameter, and the sides 38mm thick. If the specific gravity of the metal is 7.2, what is the weight of the bomb and its capacity?

Inside diameter =
$$32^{\text{cm}} - 2 \times 3.8^{\text{cm}} = 24.4^{\text{cm}}$$
.
Inside volume = $0.5236 \times (24.4^8)^{\text{ccm}} = 7607^{\text{ccm}} = 7.607^{\text{l}}$. Ans.
$$\log 0.5236 = 9.7190 - 10$$

$$\log 24.4^8 = \underbrace{4.1622}_{3.8812} = \log 7607$$
.

Total volume = $0.5236 \times (32^8)^{\text{ccm}} = 17,150^{\text{ccm}}$.
$$\log 0.5236 = 9.7190 - 10$$

$$\log 32^8 = \underbrace{4.5153}_{4.2343} = \log 17,150$$
.
$$17,150^{\text{ccm}} - 7607^{\text{ccm}} = 9543^{\text{ccm}} = 9.543^{\text{cdm}}$$
.
$$7.2 \times 9.543^{\text{kg}} = 68.71^{\text{kg}}$$
. Ans.
$$9.543 - \frac{7.2}{19086}$$

$$66801$$

99. The diameters of a lampshade are 25cm and 7cm, and its slant height is 134mm. Find its curved surface in square centimeters.

68.7096

$$\frac{1}{2} \times (25^{\text{cm}} + 7^{\text{cm}}) = 16^{\text{cm}}.$$

$$134^{\text{mm}} = 13.4^{\text{cm}}.$$

$$(13.4 \times 3.1416 \times 16)^{\text{qcm}} = 673.6^{\text{qcm}}. \text{ Ans.}$$

$$\frac{3.1416}{13.4}$$

$$\frac{16}{804}$$

$$\frac{16}{804}$$

$$\frac{125664}{134}$$

$$\frac{31416}{62832}$$

214.4

673.55904

100. A niche is formed like a half-cylinder surmounted by a quarter of a sphere. The height of the cylinder is 1.2^m, the diameter 0.8^m. Find the volume of the niche, and the area of its interior surface.

Volume of half-cylinder = $\frac{1}{2} \times (1.2 \times 0.7854 \times 0.8^2)^{\text{chan}}$ $= 0.30159^{\text{cbm}} = 301.59^{\text{l}}$. Volume of quarter-sphere = $\frac{1}{4} \times (0.5236 \times 0.8^{\circ})^{\text{cbm}}$ $= 0.06702^{\text{cbm}} = 67.02!$ $301.59^{1} + 67.02^{1} = 368.61^{1}$. Ans. 0.8 0.8 0.8 0.8 0.64 0.64 0.6 0.8 0.3840.512 0.5236 0.7854

 $\begin{array}{ccc} 0.7854 & 0.5236 \\ \underline{0.384} & \underline{0.512} \\ \overline{31416} & 10472 \\ \underline{62832} & \underline{5236} \\ \underline{23562} & \underline{26180} \\ \overline{0.3015936} & 4 & \underline{0.2680832} \end{array}$

0.0670208

Surface of half-cylinder $= \frac{1}{2}(1.2 \times 3.1416 \times 0.8)^{qm} = 1.5080^{qm}$. Surface of quarter-sphere $= \frac{1}{4} \times (3.1416 \times 0.8^2)^{qm} = 0.5027^{qm}$. Surface of the floor $= \frac{1}{4} \times (0.7854 \times 0.8^2)^{qm} = 0.2513^{qm}$.

 $1.5080^{qm} + 0.5027^{qm} + 0.2513^{qm} = 2.262^{qm}$. Ans.

0.8	3.1416	0.8	3.1416	0.7854
0.6	0.48	0.8	0.16	0.32
$\frac{0.6}{0.48}$	$\overline{251328}$	$4\overline{0.64}$	188496	15708
	125664	0.16	31416	23562
	$\overline{1.507968}$		0.502656	0.251328

101. What is the expense, at 30 cents a square yard, of painting the walls and ceiling of a room 22 ft. 6 in. long, 13 ft. 6 in. wide, and 10 ft. high?

Perimeter = $2 \times (22\frac{1}{2} \text{ ft.} + 13\frac{1}{2} \text{ ft.}) = 72 \text{ ft.}$

Area of walls = (10×72) sq. ft. = 720 sq. ft.

Area of ceiling = $(22\frac{1}{2} \times 13\frac{1}{2})$ sq. ft. = 303.75 sq. ft.

Total area = 720 sq. ft. + 303.75 sq. ft. = 1023.75 sq. ft. = 113.75 sq. yd. 114 sq. yd. at \$0.30 a sq. yd. will cost $114 \times $0.30 = 34.20 . Ans.

102. In what time will an empty cistern be filled by three pipes whose diameters are ½ in., ½ in., and 1 in., if the largest alone would fill it in 40 min.? The rates of flow are proportional to the squares of the diameters.

The smallest alone would fill it in $(\frac{2}{4})^2$ of 40 min. = 160 min. The other alone would fill it in $(\frac{4}{4})^2$ of 40 min. = 71 $\frac{1}{4}$ min. Hence, in 1 min. the largest fills $\frac{1}{40}$ of the cistern, the smallest fills $\frac{1}{160}$ of the cistern, the other fills $\frac{2}{640}$ of the cistern, and all three together fill $\frac{1}{40} + \frac{2}{160} + \frac{29}{640}$ of it.

Hence, it will take $\frac{440}{35}$ min. = $22\frac{2}{29}$ min. Ans.

103. How many gallons of water are contained in a length of 50 yd. of a canal, if its width at the top is 8 yd. and at the bottom 7 yd., and its depth 5 ft.?

The average width is
$$\frac{8+7}{2}$$
 yd. = $7\frac{1}{2}$ yd. = $22\frac{1}{2}$ ft.
50 yd. = 150 ft.

$$\frac{150 \times 22\frac{1}{2} \times 5 \times 1728}{231} = \frac{\cancel{150} \times 45 \times 5 \times \cancel{1728}}{\cancel{2} \times \cancel{231}} = \frac{9720000}{77} = 126,233.8.$$

$$\frac{150 \times 22\frac{1}{2} \times 5 \times 1728}{77} = \frac{126,233.8 \text{ gal. } Ans.}{126,233.8 \text{ gal. } Ans.}$$

864	126233.8	
5	77)9720000.	
4320	77	
50	202	
216000	154	
45	480	
1080000	462	
864	180	
9720000	154	
	260	
	231	
	290	
	231	
	590	

104. A man who rows 4 miles an hour in still water takes 1 hr.
12 min. to row 4 miles up a river. How long will it take him to row down again?

$$1 \text{ hr. } 12 \text{ min.} = 1.2 \text{ hr.}$$

In still water the man could row 1.2×4 mi.=4.8 mi. in 1 hr. 12 min. Hence, the stream carries him down 0.8 mi. in 1.2 hr., or flows at the rate of $\frac{0.8}{1.2}$ mi. = $\frac{2}{3}$ mi. per hour. When he rows with the stream he will row $4\frac{1}{4}$ mi. per hour, and will row 4 mi. in $\frac{4}{4\frac{1}{4}}$ hr. = $\frac{4}{4}$ hr. = $\frac{4}{4}$ hr. = $\frac{4}{4}$ hr. = $\frac{4}{4}$ min. Ans.

105. How long must a ladder be to reach a window 40 ft. from the ground, if the distance of the foot of the ladder from the wall is 9 ft.?

The length of the ladder

$$= \sqrt{40^2 + 9^2} \text{ ft.} = \sqrt{1600 + 81} \text{ ft.} = \sqrt{1681} \text{ ft.} = 41 \text{ ft.} \text{ Ans.}$$

$$\frac{1681(41)}{8181}$$
81

106. If 3 oz. of gold 15 carats fine are mixed with 7 oz. 12 carats fine, what will be the fineness of the compound? What must be the fineness of 11 oz. that, when added to this compound, the whole may be 14 carats fine?

$$3 \times 15 = 45$$
 $10 \text{ oz.} + 11 \text{ oz.} = 21 \text{ oz.}$
 $7 \times 12 = 84$ $21 \times 14 = 294$.
 $10 \times 129 = 165$.
 $12.9 \times 165 \div 11 = 15$.

12.9 carats. Ans. 15 carats. Ans.

107. Find the surface of each face of a cube whose volume is 14 cu. ft. 705.088 cu. in.

14 cu. ft. 705.088 cu. in. = 24,897.088 cu. in.

108. Determine the depth of conical wineglasses $2\frac{1}{2}$ in across the top that 60 of them may hold a gallon.

Volume =
$$\frac{1}{60}$$
 of 231 cu. in. = $\frac{77}{20}$ cu. in.
Volume = $\frac{1}{3} \times (2.5 \times 2.5 \times 0.7854 \times h)$ cu. in.
= $\frac{1}{3} \times (6.25 \times 0.7854 \times h)$ cu. in.

$$\therefore \frac{77}{20} = \frac{1}{3} \times 6.25 \times 0.7854 \times h.$$

$$\therefore h = \frac{\frac{77}{20}}{\frac{1}{3} \times 6.25 \times 0.7854}$$
 in.

$$\frac{8}{16}$$
= $\left(\frac{77}{20} \times 3 \times \frac{100}{623} \times \frac{10000}{7834}\right)$ in. = $\frac{40}{17}$ in. = 2.353 in. Ans.

$$\frac{102}{34}$$

$$\frac{34}{17}$$

109. What must be the length of spermaceti candles $\frac{7}{4}$ of an inch in diameter that six of them may weigh a pound, if the specific gravity of spermaceti is 0.943?

$$V = 0.7854 \times \left(\frac{7^2}{8^2} \times h\right)$$
 cu. in.

1 lb. is the weight of $\frac{1728}{0.943 \times 62.5}$ cu. in. of spermaceti.

Hence,
$$0.7854 \times \frac{7^2}{8^2} \times h = \frac{1728}{6 \times 0.943 \times 62.5}$$

$$h = \frac{1728 \times 8^2}{0.7854 \times 7^2 \times 6 \times 0.943 \times 62.5}$$
 in. = 8.124 in. Ans.

110. A cylinder 10 in. across and 10 in. high contains 0.3927 cu. ft. of water. How many shot 0.1 in. in diameter must be poured in to raise the water to the top?

Volume of cylinder = $0.7854 \times (10^{3} \times 10)$ cu. in. = 785.4 cu. in. 0.3927 cu. ft. = 0.3927×1728 cu. in. = 678.5856 cu. in. 785.4 cu. in. - 678.5856 cu. in. = 106.8144 cu. in.

Volume of each shot = $0.5236 \times (0.1^8)$ cu. in. = 0.0005236 cu. in. $106.8144 \div 0.0005236 = 204,000$. Ans.

0.3927	204000
<u>1728</u>	5236)1068144000
31416	10472
7854 ·	20944
27489	20944
3927	
378 5856	000

111. How deep must a round cistern 4 ft. in diameter be made to be lined with the same amount of lead as a cubical cistern 4 ft. on an edge? Compare their capacities.

Amount of lead to line cubical cistern

$$= 5 \times (4 \times 4)$$
 sq. ft. = 80 sq. ft.

Area of bottom of round cistern

$$= 0.7854 \times 16 \text{ sq. ft.} = 12.5664 \text{ sq. ft.}$$

80 sq. ft.
$$-12.5664$$
 sq. ft. $=67.4336$ sq. ft.

.. depth =
$$\frac{67.4336}{4 \times 3.1416}$$
 ft. = 5.366 ft. Ans.

TEACHERS' EDITION.

$$\begin{array}{r}
 3.1416 \\
 \underline{4} \\
 \hline
 12.5664 \\
 \hline
 12.5664 \\
 \hline
 125664 \\$$

Cubical cistern: round cistern

=
$$(4^8)$$
 cu. ft. : $(5.366 \times 0.7854 \times 16)$ cu. ft. = $64 : 67.43$. Ans.

0.7854	12.5664
16	5.366
47124	753984
7854	753984
12.5664	376992
	628320
	67.4313024

112. The material for lining a cubical cistern cost \$10. Find the cost of the material for lining two similar cisterns which shall each hold one half as much.

The cost is proportional to

$$(\sqrt[4]{1})^2 : 2 \times (\sqrt[4]{\frac{1}{2}})^2 = 1^2 : 2 \times 0.7937^2 = 1 : 2 \times 0.63 = 1 : 1.26.$$

1:1.26::\$10:?. 1.26 \times\$10 = \$12.60. Ans.

113. If 5 excavators sink a circular shaft 8 ft. in diameter and 125 fathoms deep in 100 days of 10 hr. each, how many nights of 7 hr. each will 4 excavators be in sinking a shaft 6 ft. in diameter and 75 fathoms deep, if the difficulty of working by night is one seventh greater than by day, and the hardness of the ground in the smaller shaft is to that in the larger shaft as 7 is to 5?

$$4:5$$
 9
 3
 2
 25
 $8^2:6^2$
 $5 \times 36 \times 75 \times 19 \times 8 \times 7 \times 199$ nights

 $125:75::100$ nights:?.
 $4 \times 64 \times 125 \times 7 \times 7 \times 7 \times 5$
 $7:10$
 8
 5
 $7:8$
 4
 $5:7$
 $6:7$ nights = 96 nights. Ans.

114. Find the number of dry quarts a tub will hold that is 22 in. across the top, 20 in. across the bottom, and 18 in. deep.

Area of upper base = $3.1416 \times 11^2 = 380.1336$. Area of lower base = $3.1416 \times 10^2 = 314.16$. $\sqrt{380.1336 \times 314.16} = \sqrt{3.1416^2 \times 11^2 \times 10^2} = 3.1416 \times 11 \times 10 = 345.576$. $V = \frac{1}{4} \times 18 \times (380.1336 + 314.16 + 345.576)$ $= 6 \times 1039.8696 = 6239.2176$. 6239.2176 cu. in. = $\frac{6239.2176}{67.2}$ dry qt. = 92.8455 dry qt. Ans.

115. Find the number of dry quarts a cylinder will hold that is 28 in. long and has a diameter of 18 in.

$$V = \frac{28 \times 3.1416 \times 9^{2}}{67.2} \text{dry qt.} \qquad \begin{cases} \log & 28 = 1.4472 \\ \log 3.1416 = 0.4971 \end{cases}$$
$$= 106 \text{ dry qt. } Ans. \qquad \begin{cases} \log & 81 = 1.9085 \\ \cos & 67.2 = 8.1726 - 10 \\ \hline 2.0254 & = \log 106.0. \end{cases}$$

116. How high will 2 quarts of milk stand in a cylindrical pail 7 in. in diameter? How high will 2 quarts of oats stand in the same pail?

2 liquid qt. =
$$2 \times 57\frac{3}{4}$$
 cu. in.
= $115\frac{1}{2}$ cu. in.
 $V = 3.1416 \times 3.5^2 \times h$.
115.5 = $3.1416 \times 3.5^2 \times h$.

$$\therefore h = \frac{115.5}{3.1416 \times 3.5^2}$$

$$\log 115.5 = 2.0626$$

$$\cosh 3.1416 = 9.5029 - 10$$

$$\cosh 3.5^2 = 8.9118 - 10$$

$$0.4773$$

$$= \log 3.001$$

$$3.001 \text{ in. } Ans.$$
2 dry qt. = $2 \times 67\frac{1}{3}$ cu. in.

$$V = 3.1416 \times 3.5^2 \times h$$
.

$$V = 3.1416 \times 3.5^2 \times h$$
.

$$\therefore h = \frac{134.4}{3.1416 \times 3.5^2}$$

$$\cosh 3.1416 = 9.5029 - 10$$

$$\cosh 3.5^2 = 8.9118 - 10$$

$$0.5431$$

$$= \log 3.492$$
3.492 in. Ans.

117. Find the capacity in gallons of a cylindrical boiler 1 ft. in diameter and 4 ft. 10 in. long; of a cylindrical boiler 1 ft. 6 in. in diameter and 3 ft. 6 in. long; of a cylindrical boiler 2 ft. 8 in. in diameter and 5 ft. 6 in. long.

1 ft. = 12 in.; 4 ft. 10 in. = 58 in.

$$V = \frac{3.1416 \times 6^2 \times 58}{231}$$

$$\log 3.1416 = 0.4971$$

$$\log 36 = 1.5563$$

$$\log 58 = 1.7634$$

$$\cosh 231 = \frac{7.6364}{1.4532}$$

$$= \log 28.39$$

$$28.39 \text{ gal. } Ans.$$

1 ft. 6 in. = 18 in.; 3 ft. 6 in.
$$= 42 \text{ in.}$$

$$V = \frac{3.1416 \times 9^2 \times 42}{231}$$

$$\log 3.1416 = 0.4971$$

$$\log 3.1416 = 0.4971$$

$$\log 3.1416 = 0.4971$$

$$\log 42 = 1.9085$$

$$\log 42 = 1.6232$$

$$\cosh 231 = \frac{7.6364}{1.6652}$$

$$= \log 46.26$$

$$46.26 \text{ gal. } Ans.$$

2 ft. 8 in. = 32 in.; 5 ft. 6 in. = 66 in.

$$V = \frac{3.1416 \times 16^2 \times 66}{231}$$

$$\log 3.1416 = 0.4971$$

$$\log 16^2 = 2.4082$$

$$\log 66 = 1.8195$$

$$\operatorname{colog} 231 = \frac{7.6364}{2.3612} - 10$$

$$= \log 229.7$$

$$229.7 \text{ gal. } Ans.$$

118. Find the capacity of a tumbler $3\frac{1}{4}$ in. across the bottom, $3\frac{1}{2}$ in. across the top, and $3\frac{1}{4}$ in. deep; of a cylindrical tumbler $3\frac{1}{4}$ in. in diameter and $3\frac{1}{4}$ in. deep.

Area of upper base = $0.7854 \times (3.5^2)$ sq. in. = 9.62115 sq. in.

Area of lower base = $0.7854 \times (3.25^2)$ sq. in. = 8.29579 sq. in.

$$\sqrt{9.62115 \times 8.29579} = \sqrt{3.5^2 \times 3.25^2 \times 0.7854^2}
= 3.5 \times 3.25 \times 0.7854 = 8.93392.$$

Volume = $\frac{1}{3} \times 3.5 \times (9.62115 + 8.29579 + 8.93392)$ cu. in. = $\frac{1}{3} \times 3.5 \times 26.85086$ cu. in. = 31.326 cu. in. Ans.

3.5	0.7854	3.25	10.5625
3.5	12.25	3.25	0.7854
175	39270	1625	422500
105	15708	650	52 8125
12.25	15708	975	845000
12.20	7854	10.5625	739375
	9.621150		8.29578750

119. Find the area of an ellipse whose longest and shortest diameters are 11 in. and 8 in., respectively.

134.6961

$$0.7854 \times (11 \times 8)$$
 sq. in. = 69.115 sq. in. Ans.
$$0.7854$$

$$- 88$$

$$- 62832$$

$$- 62832$$

$$- 69.1152$$

120. The ends of a rope 100 ft. long are fastened to stakes placed 80 ft. apart on level ground. A ring, to which a kid is tied, plays freely on the rope. How far from a straight line joining the stakes can the ring be pulled?

$$\sqrt{50^2-40^2}$$
 ft. = $\sqrt{2500-1600}$ ft. = $\sqrt{900}$ ft. = 30 ft. Ans.

121. If the stakes of Ex. 120 are placed 25 ft. apart, by how many per cent is the kid's pasturage increased, provided he can graze 18 in. beyond the rope when stretched?

$$\sqrt{50^2 - 12.5^2}$$
 ft. = $\sqrt{2500 - 156.25}$ ft. = $\sqrt{2343.75}$ ft. = 48.4 ft.
 $23 \ 43.75 (48.4)$

$$\frac{16}{88)743}$$

$$\frac{704}{964)3975}$$

$$3856$$

The diameters of the ellipse are 100 ft. $+2 \times 1\frac{1}{2}$ ft. and 2×48.4 ft. $+2 \times 1\frac{1}{2}$ ft.; that is, 103 ft. and 99.8 ft.

Area = $0.7854 \times (103 \times 99.8)$ sq. ft.

Diameters of ellipse of Ex. 120 are 103 ft. and 63 ft.

Area =
$$0.7854 \times (103 \times 63)$$
 sq. ft.

$$\frac{0.7854 \times 103 \times 99.8}{0.7854 \times 103 \times 63} = \frac{99.8}{63} = 1.584.$$

Hence, the increase is 58.4%. Ans.

122. A cylindrical log, 11 in. in diameter, is sawed off at such a slant that the pieces are 8 in. longer on the longest than on the shortest side. Find the diameters of the ellipse thus made, and its area.

The shortest diameter is evidently the diameter of the log, or 11 in. The longest diameter is

$$\sqrt{11^2 + 8^2}$$
 in. $= \sqrt{121 + 64}$ in. $= \sqrt{185}$ in. $= 13.6$ in.
Area $= (13.6 \times 11 \times 0.7854)$ sq. in. $= 117.5$ sq. in. Ans.
 $\log 13.6 = 1.1335$
 $\log 11 = 1.0414$
 $\log 0.7854 = \frac{9.8951}{2.0700} = \log 117.5$.

123. Find the area of an ellipse, if its longest diameter is 12 in. and its shortest diameter 9 in.

Area =
$$0.7854 \times (12 \times 9)$$
 sq. in. = 84.8232 sq. in. Ans.
$$0.7854$$

$$\frac{108}{62832}$$

$$\frac{7854}{84.8232}$$

124. Find the number of quarts a conical vessel will hold if it is 9 in. across the top and 8 in. deep.

$$V = \frac{1 \times 0.7854 \times 9^2 \times 8}{57.75} \text{ qt.} = 2.938 \text{ qt.} \quad Ans.$$

$$colog \quad 3 = 9.5229 - 10$$

$$log \quad 0.7854 = 9.8951 - 10$$

$$log \quad 81 = 1.9085$$

$$log \quad 8 = 0.9031$$

$$colog \quad 57.75 = 8.2384 - 10$$

$$0.4680 \quad = log 2.938.$$

125. Find the number of pints a spherical bowl will hold if it is 5 in. across the top and 2½ in. deep.

$$V = \frac{\frac{2}{3} \times 2.25 \times 5^{2} \times 0.7854}{\frac{1}{4} \times 57.75} \text{ pt.} = \frac{1.5 \times 5^{2} \times 0.7854}{28.875} \text{ pt.} = 1.02 \text{ pt. Ars.}$$

$$\log \quad 1.5 = 0.1761$$

$$\log \quad 25 = 1.3979$$

$$\log 0.7854 = 9.8951 - 10$$

$$\cosh 28.875 = \frac{8.5395}{0.0086} - 10$$

126. Find the number of pints a spherical bowl will hold if it is 4 in. across the top and 3½ in. deep.

$$V = \frac{\frac{3}{4} \times 3\frac{1}{2} \times 4^{2} \times 0.7854}{28.875} \text{ pt.} = 1.016 \text{ pt.} \quad Ans.$$

$$\log \quad 2 = 0.3010$$

$$\cosh \quad 3 = 9.5229 - 10$$

$$\log \quad 3.5 = 0.5441$$

$$\log \quad 16 = 1.2041$$

$$\log \quad 0.7854 = 9.8951 - 10$$

$$\cosh \quad 28.875 = 8.5395 - 10$$

$$0.0067 = \log 1.016.$$

127. Find the capacity in pints of a coffee cup 3 in. across the top and 3 in. deep.

$$V = \frac{\frac{1}{2} \times 3 \times 3^{2} \times 0.7854}{\frac{1}{2} \times 57.75} \text{ pt.} = \frac{27 \times 0.7854}{57.75} \text{ pt.} = 0.3672 \text{ pt.}$$
 Ans.
$$\log 27 = 1.4314$$

$$\log 0.7854 = 9.8951 - 10$$

$$\cosh 57.75 = \frac{8.2384 - 10}{9.5649 - 10} = \log 0.3672.$$

128. Find the capacity in liters of a spherical wash bowl 80cm in diameter and 5cm deep.

$$V = \frac{2}{8} \times (5 \times 3.1416 \times 15^{2})^{\text{ccm}} = \left(\frac{2}{3} \times 5 \times 3.1416 \times 225\right)^{\text{ccm}}$$

$$= 2356.2^{\text{ccm}} = 2.356^{1}. \text{ Ans.}$$

$$\frac{3.1416}{1570800}$$

$$\frac{219912}{2356.2000}$$

129. Find the capacity in liters of the basin of a fountain 89cm in diameter and 31cm deep.

$$V = \frac{2}{3} \times (31 \times 0.7854 \times 89^2)^{\text{ccm}} = 128,600^{\text{ccm}} = 128.6^1$$
. Ans.
$$\log \quad 2 = 0.3010$$

$$\cosh \quad 3 = 9.5229 - 10$$

$$\log \quad 31 = 1.4914$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log \quad 89^2 = \frac{3.8988}{5.1092} = \log 128,600$$
.

130. Find the capacity in quarts of a bowl 10 in. in diameter and 4 in. deep.

$$V = \frac{\frac{3}{5} \times 4 \times 0.7854 \times 10^{2}}{57.75} \text{ qt.} = 3.627 \text{ qt.} \quad Ans.$$

$$\log \quad 2 = 0.3010$$

$$\cosh \quad 3 = 9.5229 - 10$$

$$\log \quad 4 = 0.6021$$

$$\log \quad 0.7854 = 9.8951 - 10$$

$$\log \quad 100 = 2.0000$$

$$\cosh \quad 57.75 = \frac{8.2384}{0.5595} - 10$$

$$= \log 3.627.$$

132. How many gallons will a spherical b 2 ft. deep hold?

$$V = \frac{\frac{2}{3} \times 2 \times 0.7854 \times 5^{2} \times 1728}{231} \text{ gal.}:$$

$$\log \quad 2 = 0.3010$$

$$\cosh \quad 3 = 9.5229 - 10$$

$$\log \quad 2 = 0.3010$$

$$\log \quad 0.7854 = 9.8951 - 10$$

$$\log \quad 25 = 1.3979$$

$$\log \quad 1728 = 3.2375$$

$$\cosh \quad 231 = \frac{7.6364}{2.2918} - 10$$

133. How many gallons will a spherical bov 1 ft. deep hold?

. 134. Find the capacity in pints of a saucer 5 in. across and 2 in. deep.

$$V = \frac{\frac{2}{3} \times 2 \times 0.7854 \times 5^{2}}{28.875} \text{ pt.} = \frac{100 \times 0.7854}{3 \times 28.875} \text{ pt.} = 0.9068 \text{ pt.} \quad Ans.$$

$$\log \quad 100 = 2.0000$$

$$\log 0.7854 = 9.8951 - 10$$

$$\cosh \quad 3 = 9.5229 - 10$$

$$\cosh \quad 28.875 = \frac{8.5395 - 10}{9.9575 - 10} = \log 0.9068.$$

135. Find the capacity in gallons of a paraboloid (shaped like a coffee cup) boiler 25 in. across and 14 in. deep.

$$V = \frac{\frac{1}{4} \times 14 \times 0.7854 \times 25^{2}}{231} \text{ gal.} = \frac{7 \times 0.7854 \times 625}{231} \text{ gal.} = 14.88 \text{ gal.} \text{ Ans.}$$

$$\log \quad 7 = 0.8451$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log \quad 625 = 2.7959$$

$$\cosh \quad 231 = \frac{7.6364}{1.1725} = \log 14.88.$$

136. Find the capacity in quarts of a conical vessel 9 in. across and 7 in. deep.

$$V = \frac{\frac{1}{8} \times 7 \times 0.7854 \times 9^{2}}{57.75} \text{qt.} = \frac{7 \times 0.7854 \times 27}{57.75} \text{qt.} = 2.571 \text{ qt.}$$

$$\log \quad 7 = 0.8451$$

$$\log 0.7854 = 9.8951 - 10$$

$$\log \quad 27 = 1.4314$$

$$\cosh \quad 57.75 = \frac{8.2384}{0.4100} - 10$$

$$= \log 2.571.$$

137. Find the number of gallons contained in a full cask whose bung diameter is 24 inches, head diameter 22 inches, and length 30 inches.

$$24 \text{ in.} - 22 \text{ in.} = 2 \text{ in.}$$

Mean diameter = 22 in. + 0.65×2 in. = 22 in. + 1.3 in. = 23.3 in.

$$V = \frac{30 \times 23.3^2}{294} \text{ gal.} = 55.41 \text{ gal.} \quad Ans.$$

$$\log 30 = 1.4771$$

$$\log 23.3^2 = 2.7348$$

$$\operatorname{colog} 294 = \frac{7.5317}{1.7436} - 10$$

$$= \log 55.41.$$

138. Find the number of gallons contained in a full cask whose bung diameter is 22 inches, head diameter 20 inches, and length 28 inches.

$$22 \text{ in.} - 20 \text{ in.} = 2 \text{ in.}$$

Mean diameter = 20 in. + 0.65 \times 2 in. = 20 in. + 1.3 in. = 21.3 in.

$$V = \frac{28 \times 21.3^{2}}{294} \text{ gal.} = 43.22 \text{ gal. Ans.}$$

$$\log 28 = 1.4472$$

$$\log 21.3^{2} = 2.6568$$

$$\operatorname{colog} 294 = \frac{7.5317}{1.6357} = \log 43.22.$$

139. Find the number of gallons contained in a full cask whose bung diameter is 20 inches, head diameter 18 inches, and length 28 inches.

20 in.
$$-18$$
 in. $=2$ in.

Mean diameter = $18 \text{ in.} + 0.65 \times 2 \text{ in.} = 18 \text{ in.} + 1.3 \text{ in.} = 19.3 \text{ in.}$

$$V = \frac{28 \times 19.3^2}{294}$$
 gal. = 35.49 gal. Ans.
 $\log 28 = 1.4472$
 $\log 19.3^2 = 2.5712$
 $\cosh 294 = 7.5317 - 10$
 $1.5501 = \log 35.49$.

140. The flash of a gun is seen 7½ sec. before the report of the gun is heard; there is no wind, and the temperature is 73° F. How far off is the gun?

$$73^{\circ} - 32^{\circ} = 51^{\circ}$$
. 51×1.1 ft. = 56.1 ft. 1090 ft. + 56.1 ft. = 1146.1 ft. $\frac{7.5}{57305}$ $\frac{80227}{8595.75}$ ft. Ans.

141. A meteor was seen to burst; the report followed in 4 min. 17 sec. What was its distance, if the average temperature of the intervening air was 50° F.?

4 min. 17 sec. = 257 sec.
$$50^{\circ} - 32^{\circ} = 18^{\circ}$$
. 18×1.1 ft. = 19.8 ft.

1090 ft. + 19.8 ft. = 1109.8 ft.

	54.01
1109.8	5280)285218.6
257	<u>26400</u>
776 86	21218
55490	21120
22196	9860
285218.6	5280
	4580
	54.02 mi. Ans

142. How long will it take for an explosion at the equator to be heard at the antipodes of the place, if the circumference of the earth at the equator is reckoned at 40,000km, and the average temperature at the equator at 23° C.?

$$23 \times 0.609^{m} = 14.007^{m}.$$
 $332^{m} + 14.007^{m} = 346.007^{m}.$
 $20,000^{km} = 20,000,000^{m}.$
 $20,000,000 \div 346.007 = 57,802.$

57,802 sec. = 16 hr. 3 min. 22 sec. Ans.

0.609	57802
23	346007)20000000000
1827	1730035
1218	2699650
14.007	2422049
332.	2776010
346.007	2768056
	795400
	692014
	103386

143. If an explosion at the equator occurs at sunset and the average temperature east of the spot is 22° C., and that to the west 24° C., how far from the antipodes will the sound waves meet?

$$22 \times 0.609^{m} = 13.398^{m}.$$
 $332^{m} + 13.398^{m} = 345.398^{m}.$
 $24 \times 0.609^{m} = 14.616^{m}.$
 $332^{m} + 14.616^{m} = 346.616^{m}.$
 $345.398^{m} + 346.616^{m} = 692.014^{m},$

the velocity per second with which the two sound waves are approaching each other.

692.014:346.616::40,000km:?.

$$\begin{array}{c} 0.609 \\ \underline{22} \\ 1218 \\ 1218 \\ \hline 13.388 \\ \hline 0.609 \\ \underline{24} \\ \underline{2436} \\ 14.616 \\ \hline \end{array}$$

$$\begin{array}{c} 346616 \times 40000^{km} = 20,035.2^{km}. \\ 20,035.2^{km} - 20,000^{km} = 35.2^{km}. \\ Ans. \\ \underline{40000} \\ 13864640000 \\ \hline \end{array}$$

144. How far off is the lightning when the thunder follows in 13 sec., the temperature being 76° F.?

$$76^{\circ} - 32^{\circ} = 44^{\circ}$$
.
 $44 \times 1.1 \text{ ft.} = 48.4 \text{ ft.}$
 $1000 \text{ ft.} + 48.4 \text{ ft.} = 1138.4 \text{ ft.}$

1138.4 ft.	2.8
13	5280)14799.2
34152	10560
11:34	42392
11:4	42240
14799.2 ft.	153

2.8 mi. Ars.

145. How long would it take sound to go through a whispering tube 3 mi. long, temperature 61° F.?

$$61^{\circ} - 32^{\circ} = 29^{\circ}$$
.
 29×1.1 ft. = 31.9 ft.
 1090 ft. + 31.9 ft. = 1121.9 ft.
 $3 \text{ mi.} = 3 \times 5280$ ft. = 15,840 ft.
 $15,840 \div 1121.9 = 14.1$.

14.1 sec. Ans.

$$\begin{array}{r}
14.1\\
11219)158400.\\
\underline{11219}\\
46210\\
\underline{44876}\\
13340\\
\underline{11219}\\
2121
\end{array}$$

146. Sound travels in iron about 10½ times as fast as in air. How long, then, after seeing the blow of a sledge hammer given on the other end of an iron pipe 1½ mi. long, may I expect to hear the sound by the iron; and how long after, to hear the sound through the air in the pipe; thermometer 63° F.?

63° - 32° = 31°.
31 × 1.1 ft. = 34.1 ft.
1090 ft. + 34.1 ft. = 1124.1 ft.
10½ × 1124.1 ft. = 11,803.05 ft.
1½ mi. =
$$\frac{3}{2}$$
 × 5289 ft. = 7920 ft.
7920 ÷ 11,803.05 = 0.671.
9½ × 0.671 sec. = 6.375 sec.

$$\begin{array}{c} 0.671 \\ \hline 1180305)792000. \\ \hline \underline{7081830} \\ \hline 8381700 \\ \underline{8262135} \\ \hline 1195650 \\ \underline{1180305} \\ \hline 15345 \\ \end{array}$$

By the iron in 0.671 sec.; through the air 6.375 sec. after. Ans.

147. Two guiders fire at each other simultaneously from forts limit apart; the wind, at 70° Fi. blows steadily from one fort to the other, at 11 mi, an hour. How soon will each hear the report of the other's guil? Suppose one ball flies on the average 987 ft. a second, the other 515 ft. a second; when will each receive the other's shot?

The velocity of the sound with the wind = 1131.8 ft. + 16.1 ft. = 1147.9 ft. per second.

The velocity of the sound against the wind = 1131.8 ft. -16.1 ft. = 1115.7 ft. per second.

6.89	7.09	
11479)79200.	11157)79200.	
68874	78099	
103260	110100	
91832	100413	
114280	9687	
103311		
10969		

Therefore, it will take the first sound 6.9 sec. and the second 7.1 sec.

Ans.

 $\begin{array}{r}
8.02 \\
987)7920. \\
7896 \\
\hline
2400 \\
1974 \\
\hline
426 \\
\hline
6720 \\
6544 \\
\hline
176
\end{array}$

Therefore, it will take the first ball 8.02 sec., and the second 9.68 sec.

Ans.

148. Sound travels in water about 4.26 times as fast as in air. How many seconds sooner would the sound of a torpedo exploded under water 2 mi. off reach you by water than by air, at 68° F.?

$$68^{\circ} - 32^{\circ} = 36^{\circ}$$
.
 36×1.1 ft. = 39.6 ft.
 1090 ft. + 39.6 ft. = 1129.6 ft.

The velocity by water is 4.26×1129.6 ft. = 4812.096.

1129.6	5280
4.26	2
67776	10560
22592	
45184	
4812.096	

9.35	2.19
11296)105600. 101664	4812096)10560000. 9624192
39360 33888	9358080 4812096
5472	45459840 43308864
	2150976

9.35 sec. - 2.19 sec. = 7.16 sec. Ans.

149. A hill 482 ft. high is 8 mi. from the shore. How many miles out at sea is it visible?

$$\frac{1}{2} \log 482 = 1.3415$$

$$\frac{0.1215}{1.4630 = \log 29.04}$$

$$29.04 \text{ mi.} - 8 \text{ mi.} = 21.04 \text{ mi.} Ans.$$

150. A sailor at the topmast 80 ft. above the sea can just see a sailor at the topmast of a similar ship. How many miles apart are the vessels?

$$\frac{1}{2} \log 80 = 0.9516$$

$$\frac{0.1215}{1.0731} = \log 11.83.$$
 $2 \times 11.83 \text{ mi.} = 23.66 \text{ mi.} Ans.$

151. How far is a mountain 1000^m high visible? a mountain 2000^m high?

$$\frac{1}{2} \log 1000 = 1.5000$$
 $\frac{0.5880}{2.0880} = \log 122.5.$
 $\frac{1}{2} \log 2000 = 1.6505$
 $\frac{0.5880}{2.2385} = \log 173.2.$
 122.5km ; 173.2 km. Ans.

152. If a man stands on a bluff that raises his eyes 11^m above the sea, how far can he see from the shore?

$$\frac{1}{2} \log 11 = 0.5207$$

$$\frac{0.5880}{1.1087} = \log 12.84.$$
12.84km. Ans.

153. A sailor at sea is at a distance of 171km from a mountain when the top of the mountain is just visible. How high is the mountain?

$$H = \left(\frac{171^2}{15}\right)^{\text{m}} = 1950^{\text{m}}$$
. Ans.
 $\log 171^2 = 4.4660$
 $\operatorname{colog} \quad 15 = \underbrace{8.8239}_{3.2899} - 10$
 $= \log 1950$.

154. A vessel approaching Valparaiso at daybreak just makes out the peak of Aconcagua, 22,427 ft. high and 140 mi. back from the coast. How far is the vessel from land if the eye of the observer is 30 ft. above the water?

$$\frac{1}{2} \log 30 = 0.7386$$
 $\frac{0.1215}{0.8601} = \log 7.247.$
 $\frac{0.1215}{2.2969} = \log 198.1.$
 $\frac{1}{2} \log 22427 = 2.1754$
 $\frac{0.1215}{2.2969} = \log 198.1.$

155. If Mount Washington is 6293 ft. high and 76 mi. in an air line from Cape Elizabeth, how far out from the Cape will its peak be visible in the ordinary state of the atmosphere?

$$\frac{1}{2} \log 6293 = 1.8994$$

$$\frac{0.1215}{2.0209} = \log 104.9.$$

$$104.9 \text{ mi.} - 76 \text{ mi.} = 28.9 \text{ mi.} Ans.$$

58.1 mi. + 7.25 mi. = 65.35 mi. Ans.

156. How many acres of water can a man see if he stands on a raft with his eyes just 6 ft. above the water, and no land is in sight?

$$\frac{1}{3} \log 6 = 0.3891$$

$$\frac{0.1215}{0.5106}$$

$$\frac{2}{1.0212}$$

$$\log 3.1416 = 0.4971$$

$$\log 640 = \frac{2.8062}{4.3245} = \log 21,110.$$
21,110 A. Ans.

157. How far would a mountain 29,000 ft. high be visible? one of 5000 ft. high? one of 1000 ft. high?

$$\frac{1}{2} \log 29000 = 2.2312$$
 $\frac{0.1215}{2.3527} = \log 225.3.$ 225.3 mi. Ans.
 $\frac{1}{2} \log 5000 = 1.8495$
 $\frac{0.1215}{1.9710} = \log 93.54.$ 93.54 mi. Ans.
 $\frac{1}{2} \log 1000 = 1.5000$
 $\frac{0.1215}{1.6215} = \log 41.83.$ 41.83 mi. Ans.

158. How high must a mountain be in order to be visible at sea level 50 miles? 100 miles? 150 miles?

\$ of
$$50^2 = $ \times 2500 = 1429$$
.
\$ of $100^2 = $ \times 10,000 = 5714$.
\$ of $150^2 = $ \times 22,500 = 12,857$.

1429 ft.; 5714 ft.; 12,857 ft. Ans.

159. What distance can be seen from the top of a mountain 4 miles high?

4 mi. = 21,120 ft.

$$\frac{1}{1} \log 21120 = 2.1624$$

 $\frac{0.1215}{2.2839} = \log 192.3$. 192.3 mi. Ans.

160. Find the length of a pendulum that beats half-seconds; of a pendulum that beats quarter-seconds.

```
2^2: 1^2: 39.138 \text{ in.} : ?.
4:1::39.138 \text{ in.} : ?.
4:1::39.138 \text{ in.} : ?.
16:1::39.138 \text{ in.} : ?.
16:1::39.138 \text{ in.} : ?.
16:1::39.138 \text{ in.} : ?.
```

161. How many centimeters long is a pendulum that swings 80 times a minute? a pendulum that swings 30 times a minute?

$$1 \text{ in.} = 2.53998e^{\text{cm}}.$$

$$80^2 : 60^2 :: 39.138 \times 2.53998e^{\text{cm}} : ?.$$

$$\frac{3600 \times 39.138 \times 2.53998}{6400} = 55.91e^{\text{m}}. \text{ Ans.}$$

$$30^2 : 60^2 :: 39.138 \times 2.53998e^{\text{cm}} : ?.$$

$$\frac{3600 \times 39.138 \times 2.53998}{900} = 397.6e^{\text{m}}. \text{ Ans.}$$

$$\log \quad 3600 = 3.5563 \qquad \log \quad 3600 = 3.5563$$

$$\log \quad 39.138 = 1.5926 \qquad \log \quad 39.138 = 1.5926$$

$$\log \quad 2.53998 = 0.4048 \qquad \log \quad 2.53998 = 0.4048$$

$$\cosh \quad 6400 = 6.1938 - 10 \qquad \cosh \quad 900 = 7.0458 - 10$$

$$1.7475 \qquad 2.5995$$

$$= \log 55.91. \qquad = \log 397.6.$$

162. If a cannon ball is suspended by a fine wire 176 ft. long in the central well of the Bunker Hill Monument, how many times a minute will it swing?

176 ft. = 2112 in.
$$\log \sqrt{39.138} = 0.7963$$

 $\sqrt{2112} : \sqrt{39.138} = 60 : ?$ $\log 60 = 1.7782$
 $\frac{\sqrt{39.138} \times 60}{\sqrt{2112}} = 8.17$. Ans. $\frac{\cos \sqrt{2112} = 8.3376 - 10}{0.9121 = \log 8.168}$

163. How long is a pendulum that swings three times in two seconds? that swings five times in two seconds?

$$3^{2}: 2^{2} = 39.138 \text{ in.} : ?.$$
 $9: 4 = 39.138 \text{ in.} : ?.$
 $25: 4 = 39.138 \text{ in.} : ?.$
 $\frac{13.046}{4 \times 39.138 \text{ in.}} = \frac{52.184}{3} \text{ in.}$
 $= 14.061 \text{ in.}$ Ans.
$$\frac{39.138}{25} = 6.262 \text{ in.}$$
 Ans.
$$\frac{39.138}{234828} = 39138$$

6.26208

677

164. What velocity in meters a second will a cannon ball acquire in falling three quarters of a second? in falling three and a quarter seconds?

165. How long will it take a leaden ball, rolling off a table 29 in. high, to reach the floor?

$$16\frac{1}{13} \text{ ft.} = 193 \text{ in.}$$

$$193:29:1^2:(?)^2.$$

$$\sqrt{\frac{29}{193}} \text{ sec.} = 0.3876 \text{ sec.} \quad Ans.$$

$$\log 29 = 1.4624$$

$$\operatorname{colog} 193 = 7.7144 - 10$$

$$9.1768 - 10$$

$$10. \quad -10$$

$$2 \boxed{19.1768 - 20}$$

$$9.5884 - 10$$

$$= \log 0.3876.$$

166. What velocity will a crowbar attain in falling endwise from a balloon 2000^m high? How long will it be in coming down?

$$4.903 : 2000 : : 1^{2} : (?)^{2}.$$

$$\sqrt{\frac{2000}{4.903}} \text{ sec.} = 20.2 \text{ sec.} \quad Ans.$$

$$\log 2000 = 3.3010$$

$$\operatorname{colog} 4.903 = 9.3095 - 10$$

$$2 \boxed{2.6105}$$

$$1.3053 = \log 20.2.$$

$$9.806^{m}$$

$$20.2$$

$$\boxed{19612}$$

$$\boxed{198.0812^{m}} \quad Ans.$$

167. What velocity will a crowbar attain in falling endwise from a balloon one mile and a quarter high? How long will it be in coming down?

$$1_{2} = \frac{1}{4} / 5299 = 900. = 900. = 9000. = 10. =$$

651.64 651.7 ft. Ans.

166. How long will it take a ball, rolling off a table, to drop 1⁻²? 1 in.? 10⁻²? 6 in.?

4.96% = 490.3 cm.
490.3 :
$$1 = 1^2 : (?)^2$$
.
 $\sqrt{\frac{1}{490.3}}$ sec. = 0.04517 sec. Ans.
 $\log 1 = 0.0000$ colog 490.3 = 7.3095 - 10
 $10. - 10$ $2 = 10.000$

169. If Carisbrook Well is 210 ft. deep, how long after a pebble is dropped will it be heard to strike the bottom, if the velocity of sound is 1120 ft. a second?

$$16\frac{1}{13}: 210 = 1^2: (?)^2.$$

$$193: 2520 = 1^2: (?)^2.$$

$$\sqrt{\frac{2520}{193}} \text{ sec.} = 3.613 \text{ sec.}$$

$$\log 2520 = 3.4014$$

$$\operatorname{colog} 193 = 7.7144 - 10$$

$$2 1.1158 \over 0.5579 = \log 3.613.$$

The sound requires $\frac{210}{1120}$ sec. = $\frac{3}{16}$ sec. = 0.188 sec.

 $3.613 \sec. + 0.188 \sec. = 3.801 \sec. Ans.$

170. How long after a pebble is dropped will it be heard to strike the bottom of a ventilating shaft 1600 ft. deep, if the temperature is 68° F.?

$$16\frac{1}{13}:1600 = 1^2:(?)^2.$$

$$\sqrt{\frac{19200}{193}} \sec. = 9.975 \sec.$$

$$\log 19200 = 4.2833$$

$$\operatorname{colog} 193 = 7.7144 - 10$$

$$2\frac{1.9977}{0.9989} = \log 9.975.$$

 $68^{\circ} - 32^{\circ} = 36^{\circ}$. 36×1.1 ft. = 39.6 ft. 1090 ft. + 39.6 ft. = 1129.6 ft.

The sound requires $\frac{1600}{1129.6}$ sec. = 1.416 sec.

$$\log 1600 = 3.2041$$

$$\operatorname{colog} 1129.6 = 6.9471 - 10$$

$$0.1512 = \log 1.416.$$

$$9.975 \operatorname{sec.} + 1.416 \operatorname{sec.} = 11.391 \operatorname{sec.} Ans.$$

171. If a rock dropped over a precipice strikes the bottom in 7½ sec., how high is the precipice?

$$1^{2}: (7\frac{1}{2})^{2} = 16\frac{1}{12} \text{ ft.} : ?.$$

$$1: \frac{24^{5}}{4} = 16\frac{1}{12} \text{ ft.} : ?.$$

$$\frac{75}{4} \times 16\frac{1}{12} \text{ ft.} = \frac{225}{4} \times \frac{193}{12} \text{ ft.} = \frac{14475}{16} \text{ ft.} = 904.7 \text{ ft.} Ans.$$

172. E.w. mag nites a pedicile dropped down a shaft 133 ft. deep will a be heart 3, strike the bottom. If the temperature is 59° F.?

が一世三世 ダ (11九三野7九 1940九 - 29.7九 = 1119.7九

The sound requires
$$\frac{100}{1000}$$
 sec. = 0.11% sec.

Fig. 132 = 2.1239
color 11127 =
$$\frac{6.3009 - 10}{9.0749 - 10} = \log 0.1188$$
.
2.571 sec. = 0.119 sec. = 2.994 sec. Ans.

173. Find the lifting power of a hydraulic press, the plunger being limit in immension with a force of 100%, if the lifting piston is limit managers.

$$1^{2} = 100^{20}$$
.
 $1^{2} = 100^{2} = 1000 \times 100^{2} = 1000,000^{2} = 1000$. Ans.

174. If the planger is § in. in diameter, and is driven with a force of 1300 lb. h. w math can it lift with a lifting piston 4 ft. in diameter?

$$4 \text{ fi.} = 48 \text{ in.}; 1000 \text{ lb.} = \frac{1}{4} \text{ t.}$$

$$\frac{(4^{5})^{2}}{1} \times \frac{1}{2} \text{ t.} = 48 \times 48 \times 2 \times 2 \times \frac{1}{2} \text{ t.} = 4608 \text{ t. Ans.}$$

175. If the plunger is 2 in, in diameter, and is driven with a force of 1000 lb, h, w much can it lift with a lifting piston 2 ft, in diameter?

$$2 \text{ ft.} = 24 \text{ in.}$$
; $1000 \text{ lb.} = \frac{1}{2} \text{ L}$
 $\frac{1}{2}^{4} \times \frac{1}{2} \text{ L} = 12^{2} \times \frac{1}{2} \text{ L} = 144 \times \frac{1}{2} \text{ L} = 72 \text{ L.}$ Ans.

176. The water stands in a fissure in a rock 10^m high and 12^m long. What pressure is exerted to split the rock on the lowest meter's width? on the highest meter's width? in the whole fissure?

$$(1 \times 12 \times 9.5)^{cbm} = 114^{cbm}$$
. $(10 \times 12 \times 5)^{cbm} = 600^{cbm}$. $1 \times 12 \times 0.5)^{cbm} = 600^{cbm}$. 114° .; 6°.; 600°. Ans.

177. A dam is 100 ft. long and 10 ft. deep, and the water is just flowing over it. What pressure is exerted on the lowest two feet of the dam?

$$(100 \times 9 \times 2)$$
 cu. ft. = 1800 cu. ft.

$$1800 \times 62\frac{1}{2}$$
 lb. = $1899 \times \frac{125}{2}$ lb. = $112,500$ lb. = $56\frac{1}{4}$ t. Ans.

178. Water is running 2 ft. over a dam that is 180 ft. long and 12 ft. deep. Find the pressure on the dam.

$$(180 \times 12 \times 7)$$
 cu. ft. = 15,120 cu. ft.

 $15,120 \times 62.5$ lb. = 945,000 lb. = 472.5 t. Ans.

12	15120	
7	62.5	
84	75600	
180	30240	
6720	90720	
84	945000.0	
15120		

179. Water is running 9 in. deep over a dam that is 78 ft. long and 8 ft. deep. Find the pressure on the dam.

$$(78 \times 8 \times 4\frac{3}{4})$$
 cu. ft. = 2730 cu. ft.

 2730×62.5 lb. = 170,625 lb. = 85 t. 625 lb. Ans.

48	62.5
8	2730
35	18750
78	4375
	1250
245	170625.0
2730	

180. With what velocity will water flow through a hole 9 ft. below the surface?

$$\sqrt{9}: \sqrt{16} = 3:4.$$
 and a function of the first answer of the fi

181. With what velocity will water leave a fountain having free play, and a head of 25 ft.? a head of 100 ft.?

$$\sqrt{25}: \sqrt{16} = 5:4.$$
 $\sqrt{100}: \sqrt{16} = 10:4 = 5:2.$ § of 32 ft. = 40 ft. Ans.

182. If a hole in the side of a cistern 4 ft. below the surface of the water is delivering 10 gal. an hour, how many gallons would it deliver with 5 ft. more head?

$$\sqrt{4}$$
: $\sqrt{9} = 10$ gal. :?. $\frac{3 \times 19 \text{ gal.}}{2} = 15$ gal. Ans.

183. If a pipe 2 in. in diameter, and 1 ft. long, inserted in a dam, the head of water being kept constant, delivers 4 gallons of water a minute, how many gallons a minute may be expected when another pipe of the same length, but 2½ in. in diameter, is substituted for the two-inch pipe?

$$\frac{2^2 : (2\frac{1}{4})^2 = 4 \text{ gal.} : ?.}{4 : 6\frac{1}{4} = 4 \text{ gal.} : ?.} \qquad \frac{6\frac{1}{4} \times 4 \text{ gal.}}{4} = 6\frac{1}{4} \text{ gal.} \text{ Ans.}$$

184. If a one-inch pipe, 20 in. long, is substituted for the two-inch pape, I the long, in Example 183, and the flow is found to be 5 pints a number, what part of the decrease of flow is due to the smaller area of the orifice, and what part to the increased friction on the sides of the longer pipe?

$$4:1=4 \text{ gal.}:?.$$
 $\frac{1\times 4 \text{ gal.}}{4}=1 \text{ gal.}$
 $4 \text{ gal.}-1 \text{ gal.}=3 \text{ gal.}$ Ans.
 $1 \text{ gal.}-5 \text{ pt.}=8 \text{ pt.}-5 \text{ pt.}=3 \text{ pt.}$ Ans.

185 A miller is using water flowing through the gateway under 4 it head. How much more work could be do if the head was raised to 11 it how much more if the head was raised to 25 ft.?

186. A cross section of a stream of water is a rectangle 6 ft. by 2½ ft.; the velocity is 40 ft. per minute. There is a fall of 10 ft. where a water wheel is erected that utilizes 70% of the work. Find the horse power of the wheel.

The volume of water going over the fall per minute is

$$(6 \times 2\frac{1}{4} \times 40)$$
 cu. ft. = 600 cu. ft.

The weight of the water per minute = 600×62.5 lb.

The work of the wheel per minute = $(10 \times 600 \times 62.5)$ ft.-lb.

The horse power of the wheel = $\frac{10 \times 600 \times 62.5}{33000}$.

The utilized horse power of the wheel = $\frac{0.70 \times 10 \times 600 \times 62.5}{33000}$

= 7.955. Ans.

187. Find the horse power of the wheel of Ex. 186, if the fall of the water is 14 ft.

The horse power =
$$\frac{0.70 \times 14 \times 600 \times 62.5}{33000} = 11.136$$
. Ans.

188. A cross section of a stream of water is a rectangle 5 ft. by 4 ft.; the velocity is 50 ft. per minute. There is a fall of 12 ft. where a water wheel is erected that utilizes 65% of the work. Find the horse power of the wheel.

The volume of water per minute

$$= (5 \times 4 \times 50)$$
 cu. ft. $= 1000$ cu. ft.

The horse power of the wheel

$$=\frac{0.65\times12\times1000\times62.5}{33000}=14.773. Ans.$$

189. Find the horse power of the wheel of Ex. 188, if the fall of the water is 16 ft.

The horse power =
$$\frac{0.65 \times 16 \times 1000 \times 62.5}{33000}$$
 = 19.697. Ans.

190. A cross section of a stream of water is a trapezoid whose altitude is 3½ ft., and parallel sides 6 ft. and 5 ft., respectively; the velocity is 150 ft. per minute. There is a fall of 9 ft. where a water wheel is erected that utilizes 75% of the work. Find the horse power of the wheel.

Area of cross section = $[3\frac{1}{2} \times \frac{1}{2}(6+5)]$ sq. ft. = 19 $\frac{1}{2}$ sq. ft.

Volume of water per minute = $(150 \times 19\frac{1}{4})$ cu. ft. = 2887.5 cu. ft.

The horse power =
$$\frac{0.75 \times 9 \times 2887.5 \times 62.5}{33000}$$
 = 36.914. Ans.

191. If a top i in in commerce is making 300 revicinious a second.

with what force force the other dependent away from the centre?

61.55 times the weight of the material. Aus.

192. If a sling of in long contains a some that weighs \(\frac{1}{2}\) lb., and is whiried round \(\text{0}\) times a minute, what is the force pulling on the string?

Radius = 30 in. = 2 $\frac{1}{2}$ ft. 80 times a minute = $\frac{1}{4}$ times a second. 1.227 × 2 $\frac{1}{4}$ × $\frac{1}{4}$, $\frac{1}{2}$ × $\frac{1}{4}$ lb. = 1.227 × $\frac{5}{2}$ × $\frac{4}{3}$ × $\frac{1}{4}$ lb. = $\frac{8.18}{3}$ lb. = 2.727 lb. Ans.

193. With what force does a locomotive that weighs 60 tons running 30 mi. an hour, on a curve of 800 ft. radius, bear against the outer rail? If the locomotive is running 60 mi. an hour, with what force does it bear on the outer rail?

30 ml. per hr. = $\frac{1}{2}$ ml. per min. = 2640 ft. per min. = 44 ft. per sec. The circumference of the curve = $2 \times 3.1416 \times 800$ ft. = 5026.56 ft.

Hence, the locomotive makes $\frac{44}{5026.56}$ revolutions per second.

Force =
$$1.227 \times 800 \times \left(\frac{44}{5026.56}\right)^2 \times 120,000 \text{ lb.} = 9028 \text{ lb.}$$
 Ans.

$$\log \quad 1.227 = 0.0889$$

$$\log \quad 800 = 2.9031$$

$$\log \quad 44^2 = 3.2870$$

$$\cosh 5026.56^2 = 2.5974 - 10$$

$$\log \quad 120,000 = 5.0792$$

$$3.9556 = \log 9028$$

If the locomotive is running 60 mi. an hour, it makes twice as many revolutions a second. Hence, since the force contains as a factor the square of the number of revolutions a second, the force is four times as great as at 30 mi. per hour.

$$4 \times 9028$$
 lb. = 36,112 lb. Ans.

194. If washed wool is put wet into a wire basket 1.2^m in diameter, and the basket is set to spinning at the rate of 180 revolutions a second, with what force is water wrung out of the wool?

Radius =
$$\frac{1}{2}$$
 of $1.2^{m} = 0.6^{m}$.
 $4.025 \times 0.6 \times 180^{2} = 78,246$.

180	4.025
180	0.6
14400	2.4150
180	32400
32400	966000
	4830
	7245
	78246.000

78,246 times its weight. Ans.

195. If steel pens are revolved in a basket 32cm in diameter, 17 revolutions a second, with what force is the oil drained from them?

Radius = $\frac{1}{2}$ of $32^{cm} = 16^{cm} = 0.16^{m}$.

$$4.025 \times 0.16 \times 17^2 = 186.116$$
.

4.025	0.644	10.948
0.16	17	17
24150	4508	76636
4025	644	1094 8
0.64400	10.948	186.116

186.116 times its weight. Ans.

196. The top of a wheel is at each instant moving with twice the velocity of the carriage, and is moving in a curve whose centre, at the instant, is as far below ground as the point is above ground. What, then, is the force exerted to separate the mud from the top of a wheel 3 ft. 2 in. in diameter, when the carriage is moving at the rate of 10 miles an hour?

When the carriage is going at the rate of 10 mi. an hour, the top of the wheel is going at the rate of 20 mi. an hour, or 29½ ft. a second. The radius of the curve = $2 \times 3½$ ft. = 6½ ft. The circumference of the curve is $2 \times 3.1416 \times 6½$ ft. = 39.7936 ft. The force = $1.227 \times 6½$ $\times \left(\frac{29.3333}{39.7936}\right)^2 = 4.224$ times the weight of the mud. Ans.

197 E w string a normalization of a charm, weighing half a plant of the names part curve with an look made in which was part curve with an look made in which it

150 A pair rope. Verming a line is the yard, is fastened at one and it. A statement that the issues such a the same level, runs over a court. And the 12 - h Vermit him; is it. What is the radius of its and the line is the line of its and the line is the line of the line is the line of the line is the line of the line

The horse a witness with the which represents 100 yd. of rope than which will be a state.

198 Ash ver were the rope of Example 198, and increases its weight # , what i es to miles now become?

The weight of the rige being $\frac{1}{1+1} = \frac{1}{2}$ of what it was, it takes only $\frac{1}{2}$ of $\frac{1}{2}$

200. A steam that in a trengenty to move a ship, straightened the harvest mood the roll as of the 3 west point was 1980 ft. The rope was well and we give by it to the yard. With what force was it stretched?

$$1.80 \text{ fb.} = 600 \text{ yd.}$$

 $600 \text{ yd.} 15. = 2145 \text{ fb. Ass.}$

201 A that Si finding hands between points on a level, and sags 4 fin. What is the radius at the 1 west point?

Radius =
$$\frac{1}{2} \frac{\sinh \ln - \sin^2 h}{2 \times \sin^2 h}$$
 ft.
= $\frac{15.5 - 4}{2 \times 4} \times \frac{11.5 - 4}{4}$ ft. = $\frac{19.5 \times 11.5}{8}$ ft. = 28.031 ft. Ans.
 $\frac{19.5}{975}$
 $\frac{19.5}{195}$
 $\frac{19.5}{8 \times 224.25}$
 $\frac{224.25}{28.031}$

202. The whole chain, in Example 201, weighs 18 lb. What is the horizontal tension? What is the distance between the points? What is the slant, or batter, of the end of the chain?

Tension = weight of radius =
$$28.031 \times \frac{14}{15}$$
 lb. = 16.28 lb. Ans. | $10g \ 28.031 = 1.4477$ | $1.2900 - 1.0607 = 0.2293$. | $10g \ 18 = 1.2553$ | $10g \ 18 = 1.2553$ | $10g \ 19.5 = 1.2900$ | $10g \ 11.5 = 1.0607$ | $10g \ 0.2293 = 9.3604 - 10$ | $10g \ 0.3293 = 1.4477$ | $10g$

203. A chain weighing 1^{kg} to the meter is suspended from points on a level; the length of chain is 31^m, and it sags 1.3^m. Find all the conditions, and find how much it falls below a level at 10^{cm} from each end.

Radius=
$$\frac{(15.5+1.3) \times (15.5-1.3)^m}{2 \times 1.3}$$
 Tension = 91.75kg. Ans.
 $=\frac{16.8 \times 14.2^m}{2.6}$ Span = 15.42m.
 $=91.75$ m. Ans.
 $\log 16.8 = 1.2253$ $\log 16.8 = 1.2253$ $\log 14.2 = 1.1523$ $\log 0.0730 = 8.8633 - 10$ $\cos 1.3 = 9.8861 - 10$ $\cos 1.9626$ $\cos 1.3 = 9.8861 - 10$ 200 File out to Andrew 200 a single for the sage of th

= 10g 38.75.

206. How heavy a rock placed 6 in. from the fulcrum can a man, who weighs 180 lb., raise with a crowbar 5 ft. 6 in. long?

180 lb.: W = 6 in.: 5 ft. 180 lb.: W = 1:10. $W = 10 \times 180$ lb. = 1800 lb. Ans.

207. Two weights of 30 lb. and 20 lb., respectively, at the ends of a horizontal lever 5 ft. long, balance. Find how far and in which direction the fulcrum must be moved for the weights to balance when each is increased by 5 lb.

30: 20 = 20-lb. arm: 30-lb. arm. ∴ 20-lb. arm = $\frac{2}{3}$ of 5 ft. = 3 ft. 35: 25 = 25-lb. arm: 35-lb. arm. ∴ 25-lb. arm = $\frac{7}{12}$ of 5 ft. = $2\frac{1}{12}$ ft. = 2 ft. 11 in.

Therefore, the fulcrum must be moved 1 in. toward the lighter weight. Ans.

208. A man who weighs 160 lb., wishing to raise a rock, leans with his whole weight on a horizontal crowbar 5 ft. long, which is propped at the distance of 4 in. from the end in contact with the rock. Find the force he exerts on the rock, and the pressure the prop has to sustain, if the weight of the crowbar is not reckoned.

4:56 = 160 lb.:?. $\frac{40}{4}$ $\frac{56 \times \cancel{160} \text{ lb.}}{\cancel{4}} = 2240 \text{ lb. } Ans.$ 2240 lb. + 160 lb. = 2400 lb. Ans.

209. A child weighing 56 lb. is scated at one end of a plank 16 ft. long, and a child weighing 72 lb. is at the other end. Find the distance of each child from the fulcrum when the plank is used for a seesaw.

$$56:72=7:9.$$

Therefore, the 56-lb. child is 9 ft. from the fulcrum, and the 72-lb. child is 7 ft. Ans.

210. In a pair of nutcrackers if the nut is placed at a distance of 1 in. from the hinge, and the hand presses at a distance of 8 in. from the hinge, find the pressure upon the nut for every ounce of pressure exerted by the hand.

1:8=1 oz.:?. $8\times 1 \text{ oz.}=8 \text{ oz.}$ Ans.

211. A body is welched in both arms of a false balance, and its agreet weights are 2.56 lb, and 2.25 lb. Find its true weight.

2.56: true weight = true weight: 2.25.

True weight = $\sqrt{2.56} \times 2.25$ lb. = (1.6 × 1.5) lb. = 2.4 lb. Ans.

212. In a steelyard the weight of the beam is 15 lb., and the distance of its centre of gravity from the fulcrum is 3 in. Find the distance from the fulcrum a weight of 6 lb. must be placed to balance the beam.

6:15 = 3 in.:?.
$$\frac{15 \times 3 \text{ in.}}{6} = 7\frac{1}{2} \text{ in. Ans.}$$

213. A cask weighing 160% is attached to a rope wound on an axle 190% in diameter; at one end of the axle is a wheel 1750m in diameter. With what force must a man pull down on a rope passing over the wheel to raise the cask?

$$\frac{175:19=160^{kg}:?.}{\frac{19\times160^{kg}}{175}=17\frac{1}{3}^{kg}=17.37^{kg}. \text{ Ans.}}$$

214. A rope passes over a single pulley. How much force is required to raise 180 lb. attached to one end of a rope if 1% of the force is required to overcome friction?

$$\frac{100}{99}$$
 of 180 lb. = $\frac{2000}{11}$ lb. = 181.82 lb. Ans.

215. If the radius of the wheel is four times that of the axle, and the string round the wheel can support a weight of 50 lb. only, find the greatest weight that can be lifted.

$$1:4=50$$
 lb. : ?. 4×50 lb. = 200 lb. Ans.

216. Find the ratio of the radii of a wheel and axle that a force of 100 lb. may just support a weight of 1 ton.

1 t.
$$= 2000$$
 lb.

Radius of wheel: radius of axle = 2000:100 = 20:1. Ans.

217. The radius of a wheel is 80^{cm} and the radius of the axle is 12^{cm} . What weight can be supported by a force of 30^{kg} ? Find the work done if the weight is raised 60^{cm} .

12:80 =
$$30^{\text{kg}}$$
:?.
$$\frac{30 \times 30^{\text{kg}}}{12} = 200^{\text{kg}}$$
. Ans.
$$\frac{40 \times 30^{\text{kg}}}{12} = 200^{\text{kg}}$$
. $60^{\text{cm}} = 0.6^{\text{m}}$.

Work = (200×0.6) kilogram-meters = 120 kilogram-meters. Ans.

218. The power arm of a screw is 16 in. long, and by one turn of the screw the head advances one eighth of an inch. If the power is 3 lb., find the weight lifted.

The circumference described by the end of the power arm is

$$(2 \times 16 \times 3.1416)$$
 in. = 100.5312 in.
 $\frac{1}{8}$: 100.5312 = 3 lb. : ?.
 $8 \times 100.5312 \times 3$ lb. = 2412.75 lb. Ans.

219. In a screw used to raise a load of 10 tons, the power is 50 lb., acting by an arm 4 ft. long. Find the distance between two consecutive threads.

The circumference described by the end of the power arm is

$$(2 \times 48 \times 3.1416)$$
 in. = 301.5936 in.
 $20,000:50 = 301.6$ in. :?.
 $\frac{59 \times 301.6}{29999}$ in. $\frac{299999}{400}$ = 0.754 in. Ans.

220. The lever of a screw is 1 ft. 9 in. long, and the power applied at the end is 100 lb. What must be the distance between the threads that a pressure of 5000 lb. may act on the press board?

The circumference described by the end of the power arm is

$$2 \times 3.1416 \times 21$$
 in. = 131.9472 in.
 $5000 : 100 = 131.95$ in. : ?.

$$\frac{190 \times 131.95 \text{ in.}}{5000} = 2.639 \text{ in. } Ans.$$

221. The lever of a screw is 3 ft. 6 in. long, and the distance between the threads is \{\frac{1}{2}\) in. What power must be applied at the end of the lever to produce a pressure of 10 tons on the press board?

The circumference described by the end of the power arm is

$$2 \times 3.1416 \times 42$$
 in. = 263.8944 in.
 $263.8944 : \frac{1}{2} = 20,000$ lb. : ?.
 $\frac{1}{2} \times 20000$ lb. = 15.158 lb. Ans.
 263.8944
 15.157
 263.8944
 13610560
 13194720
 4158400
 2638944
 15194560
 13194720
 19998400
 18473508
 1524892

222 What per cent of water is oxygen? what per cent hydrogen?

$$(2 \times 1) + 16 = 2 + 16 = 18.$$

 $1\frac{1}{2}$ of $100\% = 11\frac{1}{2}\%$ H. Ans.
 $100\% - 11\frac{1}{2}\% = 88\frac{1}{2}\%$ O. Ans.

223. What per cent of quicklime, CaO, is oxygen?

$$40 + 16 = 56$$
. 38 of $100\% = 284\%$. Ans.

224. What per cent of water in slacked lime, CaO₂H₂?

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225 What per cent of pure marble, CaCO₃, is oxygen?

$$40 + 12 + 48 = 100$$
. $150 \text{ of } 100\% = 48\%$. Ans.

226. What per cent of gypsum, called plaster of Paris, CaSO₄ + 2 H₃O, is sulphur?

$$40 + 32 + 64 + 2(2 + 16) = 136 + 36 = 172.$$
Ans.

227. What per cent of washing soda, Na₂CO₈ + 10 H₂O, is carbon? 46 + 12 + 48 + 10(2 + 16) = 106 + 180 = 286.

$$\frac{12}{286}$$
 of $100\% = 4\frac{28}{143}\%$. Ans.

228. In 118 lb. of Glauber salts, $Na_2SO_4 + 10 H_2O$, how many ounces of sulphur?

$$46 + 32 + 64 + 10(2 + 16) = 142 + 180 = 322.$$

 $\frac{32}{322}$ of 118×16 oz. = 187.6 oz. Ans.

229. How many ounces of soda, $Na_2O + H_2O$, in 7 lb. of borax, $Na_2B_4O_7 + 10 H_2O$?

$$46 + 16 + (2 + 16) = 80.$$
 $46 + 44 + 112 + 10(2 + 16) = 202 + 180 = 382.$
 $7 \text{ lb.} = 112 \text{ oz.}$
 $100 \times 112 \text{ oz.} = 23.46 \text{ oz.} \text{ Ans.}$

230. What per cent of pure alcohol, C₂H₆O, is carbon? What per cent of pure white marble, CaCO₃, is carbon?

$$24 + 6 + 16 = 46.$$
 $40 + 12 + 48 = 100.$ $\frac{14}{100}$ of $100\% = 52\frac{4}{18}\%$. Ans. $\frac{12}{100}$ of $100\% = 12\%$. Ans.

231. What per cent of pure acetic acid (the acid of vinegar) is carbon, the formula being $C_2H_4O_2$?

$$24 + 4 + 32 = 60$$
. $\frac{24}{60}$ of $100\% = 40\%$. Ans.

232. How much acetic acid can be obtained from 12 lb. of alcohol, C₂H₆O, if there is no waste?

$$C_2H_4O_2 = 60$$
, acid. $24 + 6 + 16 = 46$, alcohol.

Alcohol contains $\frac{18}{18}$ of O, and acid $\frac{82}{80}$ $\frac{82}{80}: \frac{18}{18}: 12:$?.

$$\frac{16}{48} \times \frac{60}{32} \times 12$$
 lb. = 7.83 lb. Ans.

233. How many grains of carbon in 1 oz. avoirdupois of oxalic acid, $C_2H_2O_4 + 2 H_2O$?

$$24 + 2 + 64 + 2(2 + 16) = 90 + 36 = 126.$$

$$\frac{3}{3} = \frac{360}{300}$$

$$\frac{24}{126} \text{ of } \frac{7000}{16} \text{ gr.} = \frac{250}{3} \text{ gr.} = 83\frac{1}{3} \text{ gr. } Ans.$$

234. How many milligrams of earbon in 3 of tartaric acid, $C_4H_6O_6$?

$$48 + 6 + 96 = 150.$$
 $\frac{48}{150} \times \frac{20}{2000} = 950^{-1}$. Are.

235. How many kilograms of carbon in 95 of white sugar, $C_{12}H_{22}(t_{11})$?

$$\frac{8}{144 + 22 + 176} = 342. \qquad \frac{144}{342} \times 95^{48} = 40^{48}. \text{ Ans.}$$

236. The formula of camphor is $C_{10}H_{16}O$. How many grams of carbon in 14^{kg} of camphor?

$$\frac{15}{120 + 16 + 16} = 152. \qquad \frac{\frac{15}{120}}{\frac{132}{19}} \times 14000s = \frac{210000s}{19} = 11,052.6s. \text{ Ars.}$$

237. In 20kg of oil of vitriol, H₂SO₄, how many grams of sulphur?

$$\frac{16}{\frac{32}{98}} \times 20000^{\circ} = \frac{320000^{\circ}}{49} = 6530.6^{\circ}. \text{ Ans.}$$

238. What per cent of oil of vitriol is water? what per cent sulphuric acid, SO₈?

$$H_2S()_4 = 98.$$
 $\frac{18}{98}$ of $100\% = 18.37\%$, water. $H_3() = 18.$ $100\% - 18.37\% = 81.63\%$, sulphuric acid.

239. In 8.5% of black oxide of iron, FeO, how many milligrams of iron?

3.5g = 3500mg. 56 + 16 = 72.

$$\frac{56}{72}$$
 of 3500mg = $\frac{24500$ mg}{9} = 2722 $\frac{2}{5}$ mg. Ans.

240. Red iron-rust consists of 70% iron and 30% oxygen. Find its

Fo = 56 and O = 16.
$$56:16=7:2$$
. $70:30=7:3$.

First seek multiples of 56 and 16 in the ratio of 70 to 30; that is, of 7 to 3. \therefore Fe: O = 2:3.

Formula = Fe₂O₈. Ans.

241. The choking vapor of burning sulphur is sulphur and oxygen in equal parts. Find its formula.

$$S = 32.$$
 $O = 16.$ $O_2 = 32.$

Formula = SO_2 . Ans.

242. Copperas is 28.9% sulphuric acid, 25.7% oxide of iron, 45.4% water. Find its formula.

Water being 18, oxide of iron 72, and sulphuric acid 80, first seek multiples of 72 and 80, in the ratio of 25.7 to 28.9; that is, of 0.8893 to 1. But 72 and 80 are in almost exactly that ratio. This gives $FeSO_4 + water$; and it remains to find a multiple of 18 which is to 152 as 45.4 is to 54.6; that is, which is 0.8315 of 152, or 126.4. But $7 \times 18 = 126$; and the addition of 7 parts of water gives as the complete formula, $FeSO_4 + 7 H_2O$. Ans.

243. Spirits of turpentine is 11.76% hydrogen and 88.24% carbon. Find its formula. What per cent of oxygen combined with spirits of turpentine are required to make camphor, $C_{10}H_{16}O$?

Hydrogen being 1 and carbon 12, and 88.24 being almost exactly 7.5 times 11.76, we seek the smallest multiple of 12 that is 7.5 times a whole number. This is evidently 5 times 12, equal to 7.5 times 8. Therefore the formula is C_5H_8 , or as chemistry gives it $C_{10}H_{16}$. Ans.

Add O, and we have $C_{10}H_{16}()$, the formula of camphor; containing $\frac{16}{136} = 11.76\%$ of oxygen added to spirits of turpentine. Ans.

244. If the resistance of 1 mile of wire 2^{mm} in diameter is 4.72 ohms, what is the resistance of 3 miles of wire of the same material 3^{mm} in diameter?

$$\frac{1:3}{3^2:2^2}::4.72$$
 ohms: resistance.

Resistance =
$$\frac{3 \times 2 \times 2 \times 4.72 \text{ ohms}}{1 \times 3 \times 3} = 6.29 \text{ ohms. } Ans.$$

245. What length of copper wire 1^{mm} in diameter has the same resistance as 720^m of copper wire 4^{mm} in diameter?

$$(\frac{1}{4})^2$$
 of $720^m = \frac{1}{16}$ of $720^m = 45^m$. Ans.

246. The conductivity of iron is $\frac{1}{2}$ that of copper. If the resistance of a copper wire 1 mile long and $\frac{1}{2}$ in. in diameter is 6.8 ohms, what is the resistance of an iron wire $\frac{1}{16}$ in. in diameter and 5 miles long?

1:7 1:5::6.8 ohms: resistance. $(\frac{1}{16})^2:(\frac{1}{8})^2$

Resistance =
$$\frac{7 \times 5 \times \frac{1}{1} \times \frac{1}{18} \times 6.8 \text{ ohms}}{\frac{1}{18} \times \frac{1}{18}} = 7 \times 5 \times 4 \times 6.8 \text{ ohms}$$

= 952 ohms. Ans.

247. If 50 volts force 54.8 ampères of electrical current through a lamp, what is the resistance?

Ampères =
$$\frac{\text{volts}}{\text{ohms}}$$
. $54.8 = \frac{50}{\text{ohms}}$.

Resistance = $\frac{50}{54.8}$ ohms = 0.912 ohm. Ans.

248. If the resistance of an electric lamp is 2.8 ohms when a current of 10 ampères is passing through it, what is the voltage?

$$10 = \frac{\text{volts}}{2.8}$$
 Voltage = 10×2.8 volts = 28 volts. Ans.

249. Five arc lamps on a circuit have each a resistance of 2.35 ohms. The resistance of the wires is 1.2 ohms and of the dynamo is 0.75 ohm. What voltage is required to send a current of 15 ampères through the circuit?

$$5 \times 2.35 \text{ ohms} = 11.75 \text{ ohms.}$$

Total resistance = 11.75 ohms + 1.2 ohms + 0.75 ohm = 13.7 ohms. Voltage = 15×13.7 volts = 205.5 volts. Ans.

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